

## Tutorial 5

### 1. Difference b/w BFS and DFS.

#### BFS

- Stands for breadth first search.
- uses queue data structure for finding path.
- gives shortest path from source to destination.
- Considers all the neighbours of source node and then their neighbours.
- Time Complexity - list :  $O(V+E)$   
Matrix:  $O(V^2)$
- No Concept of back tracking as it do not uses recursion.

- Application:
1. Shortest path
  2. MST for unweighted graph
  3. Peer to peer networks
  4. Social Networking Sites



5. GPS navigation

6. Cycle detection indication.

### DFS :

- Stands for depth first search.
- Uses stack data structure.
- Gives one of the possible paths from source node to destination node.
- Considers a source node, then considers its source node till the end.
- Time Complexity: List:  $O(V+E)$   
Matrix:  $O(V^2)$
- has concept of backtracking.

### Application:

1. Topological Sorting
2. Finding Strongly connected components of graph.
3. Path finding



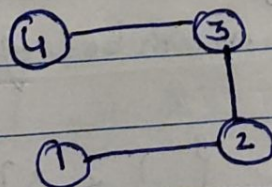
2. Which data structures are used to implement BFS & DFS.

Data structures used in case of BFS & DFS are queue & stack respectively.

→ BFS requires ~~just~~ queue data structure because it traverses the graph in breadthward motion and uses a queue to remember to get the next vertex to start a search when a dead end occurs in any iteration.

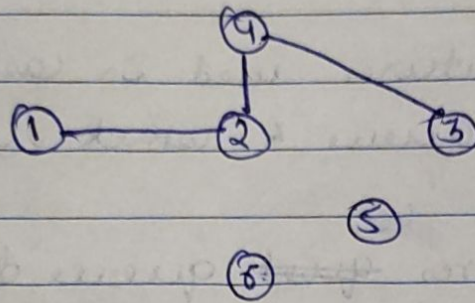
→ DFS requires stack data structure because it traverse ~~as~~ a graph in a depthward motion & uses a stack to remember it to get to the next vertex to start a search, when a dead end occurs in iteration.

3. Dense graph is a graph in which number of edges is close to maximal no. of edges.





Sparse graph is a graph in which no. of edges is close to minimal no. of edges.



→ It is ideal to use sparse graph by adjacency list and dense graph by adjacency matrix.

#### 4. Disjoint Set Data Structure:

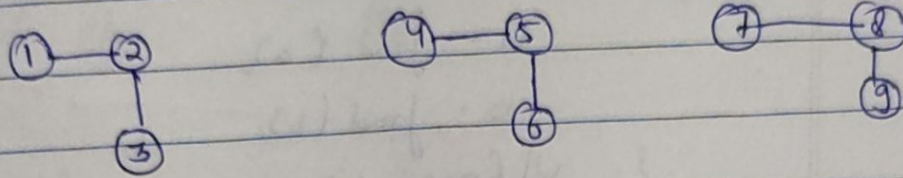
A disjoint set data structure also called as union find data structure or merge. Find data structure is a data structure that stores a partition of set into disjoint subsets.

It provides operations for adding sets, merging sets and finding a representative member of a set.

Eg.  $S_1 = \{1, 2, 3\}$   
 $S_2 = \{4, 5, 6\}$



$$S3 = \{7, 8, 9\}$$



### Operations Performed:

- (i) Find: It can be implemented recursively by traversing the parent array until we hit a node who is parent to itself. Here, path compression can be achieved by keeping track or size of node.

```
int find (int i)
{
```

```
    if (parent[i] == i)
```

```
        return i;
```

```
    return parent[i] = find (parent[i]);
}
```

- (ii) Union: It takes two elements as input and finds the parent of the inputs using find operation and performs merging of the one child to the parent node.



```
void union (inta, intb)
{
```

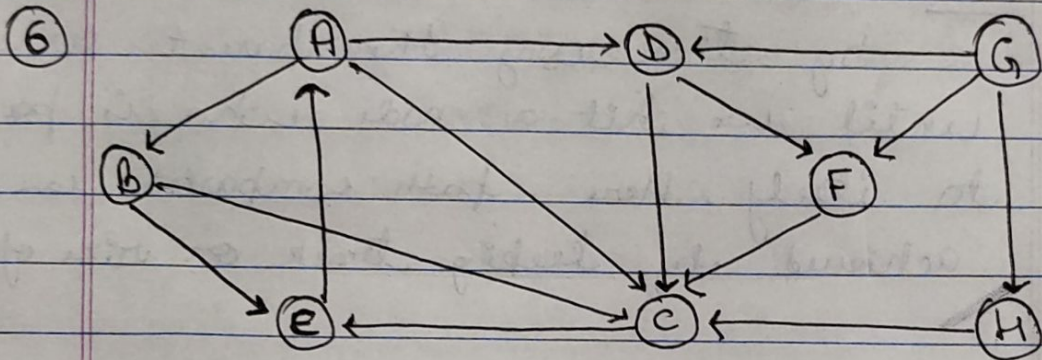
```
    a = find(a);
```

```
    b = find(b);
```

```
    if (a == b)
```

```
        parent[a] = b;
```

```
}
```



BFS

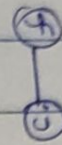
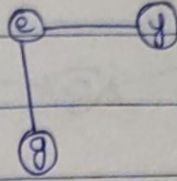
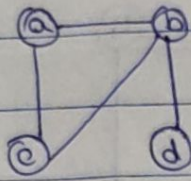
Node	B	E	C	A	D	F
Parent	-	B	B	E	A	D

DFS

B	E	A	D	F	C
---	---	---	---	---	---



7.



$$U = \{ a, b, c, d, e, f, g, h, i, j \}$$

Here, make, find and union operations will be performed.

→ First each vertex will be parent of itself

→ If an edge exists between vertices, then we perform find operation & check if their parent is same and perform union operation on them.

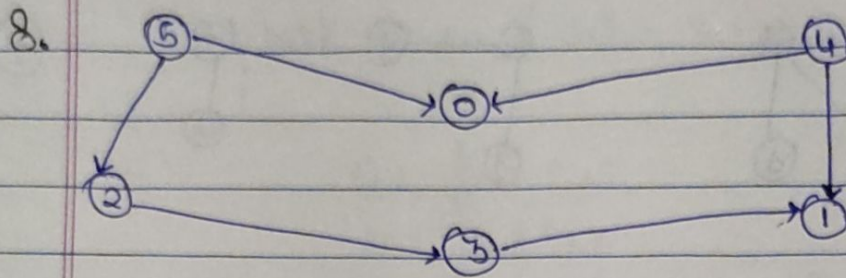
$$S_1 = \{ a, b, c, d \}$$

$$S_2 = \{ e, f, g \}$$

$$S_3 = \{ h, i \}$$

$$S_4 = \{ j \}$$





toposort (0) : push (0)

toposort (1) : push (1)

toposort (2) : toposort (3)

~~then~~ first push (3), then push 2

toposort (4) : push (4)

toposort (5) : push (5)

∴ 

5	4	2	3	1	0
---	---	---	---	---	---

9. We can use heaps to implement the priority queue. It will take  $O(\log N)$  time to insert & delete each element in priority queue.

→ Based on heap structure, priority queue ~~has~~ also two types - Max & min priority.



Some algorithm's where we need to use priority queue :

i) Dijkstra's :

→ used for calculating shortest path in algorithm.

→ When the graph is stored in the form of adjacency list or matrix, priority queue can be used to extract efficiently.

ii) Prim's : used to implement prim's algo to store keys of nodes and extract minimum key node at every step.

iii) Data Compression :

→ Used in Huffman's coding which is used to compress data.



## 10. Min heap

- In a min heap the key present at root must be less than or equal to the children.
- Min key element is at root of heap.
- Used ascending priority.
- Smallest element has a priority.
- Smallest element is to be popped from heap.

## Max heap

- In max heap, key at root must be greater than the key at the children.
- Max key element is at root of heap.
- Uses descending priority.
- Largest element has a priority.
- Largest element is to be popped from heap.