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import numpy as np
import torch
def fun(x):
  return x[0]**2 + (x[1]-3)**2
def g1(x):
  return x[1]**2 - 2*x[0]
def g2(x):
  return (x[1]-1)**2 + 5*x[0] -15
def dfdx(x):
  return torch.tensor([[2*x[0],2*(x[1]-3)]])
def dfdq1(x):
  return torch.tensor([[-2,2*x[1]]])
def dfdg2(x):
  return torch.tensor([[5,2*(x[1]-1)]])
def ch weights(mu, weights,k):
  if k > 0:
    weights = torch.max(abs(mu), 0.5 * (weights + abs(mu)))
  else:
    weights = abs(mu)
  return weights
def marit fun(x,weights,alpha,s):
  G1=max(0, g1(x + alpha*s)) # constrain 1
 G2=max(0, g2(x + alpha*s)) # constrain 2
  return fun(x + alpha*s) + weights[0,:] * G1 + weights[1,:]* G2
def dFdalpha(x,weights,s):
  if g1(x) \ll 0:
       dg1 da = 0
  else:
      dg1 da= torch.matmul(dfdg1(x), s)
  if g2(x) <= 0:
      dg2 da = 0
  else:
    dg2 da = torch.matmul(dfdg2(x), s)
  dF da = torch.matmul(dfdx(x), s) + (weights[0, :] * dg1 da +
weights[1, :] * dg2 da)
  return dF da
def lineSearch(x,mu,weights,s,k):
    t = 0.25
    alpha = 1
    weights = ch_weights(mu, weights,k)
    phi = lambda x, weights, alpha, t, dFdalpha: marit fun(x, weights,
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0, 0) + alpha * t * dFdalpha(x,weights,s)
    while phi(x, weights, alpha, t, dFdalpha) < marit fun(x, weights,</pre>
alpha, s):
        alpha = 0.5 * alpha
    return alpha, weights
def BFGS(x,W, s, mu, alpha):
  lx k = dfdx(x) + torch.matmul(mu.T, torch.tensor([g1(x),g2(x)]))
  lx k 1 = dfdx(x + alpha*s) + torch.matmul(mu.T, torch.tensor([g1(x +
alpha*s), q2(x + alpha*s)))
  delta l = lx k 1 - lx k
  Q = torch.matmul((alpha*s).T, W), (alpha*s))
  if torch.matmul((alpha*s).T, delta l.T) >= 0.2 *
torch.matmul(torch.matmul((alpha*s).T, W), (alpha*s)):
        theta = 1
  else:
        theta = 0.8 * Q / (Q - torch.matmul((alpha*s).T, delta_l.T))
  y = theta * delta l.T + (1 - theta) * torch.matmul(W, (alpha*s))
  W = W + torch.matmul(y, y.T) / torch.matmul(y.T, s) -
torch.matmul(torch.matmul(W, s), torch.matmul(s.T, W)) /
torch.matmul(torch.matmul(s.T, W), s)
  return W
def LangMulticheck(mu,active):
    mu check = 0
    if len(mu) == 0 or min(mu) > 0:
        mu check = 1
        mu idx = np.argmin(np.array(mu))
        mu = mu[mu!=min(mu)]
        active.pop(mu idx)
    return active, mu check ,mu
def solve sqp(x, W):
    active = []
    A initial = torch.cat((dfdg1(x), dfdg2(x)),0)
    B initial=torch.tensor([[g1(x), g2(x)]]).T
    mu initial = torch.zeros((B initial.shape[0], 1))
    mu = []
    while True:
      if len(active) == 0:
            s mu = torch.matmul(torch.linalg.inv(W), -dfdx(x).T)
            s = s mu[:2, :]
      if len(active) > 0:
        if len(active) == 1:
                A = A initial[active[0], :].reshape(1, -1)
                B = B initial[active[0], :].reshape(1,1)
        if len(active) == 2:
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A = A initial
                B = B initial
        Z = torch.zeros((A.shape[0], A.shape[0]))
        matrix=torch.cat((torch.cat((W,A.T),1),torch.cat((A,Z),1)),0)
        j=torch.cat((-dfdx(x).T,-B),0)
        s mu = torch.matmul(torch.linalg.inv(matrix), j)
        s = s mu[:2, :]
        mu = s mu[2:, :]
      if len(mu) == 1:
          mu initial[0] = s mu[2:3, :]
      if len(mu) == 2:
          mu initial[0] = s mu[2:3, :]
          mu initial[1] = s mu[3:, :]
      sqp constraint = torch.round((torch.matmul(A initial,
s.reshape(-1, 1)) + B initial))
      active, mu check,mu = LangMulticheck(mu,active)
      if torch.max(sqp_constraint) <= 0 and mu check == 1:</pre>
            return s, mu initial
      else:
          index = np.argmax(sqp constraint)
          active.append(index)
          active = np.unique(np.array(active)).tolist()
x = torch.tensor([[1,1.]]).T
x initial = x
\overline{mu} = torch.zeros((x.shape[0], 1))
weights = torch.zeros((x.shape[0], 1))+2
W = torch.eye(x.shape[0])
eps = 1e-3
k = 0
delta L norm = np.linalg.norm(dfdx(x) + np.matmul(mu.T,
torch.cat((dfdg1(x), dfdg2(x)),0)))
while delta L norm > eps:
    s, mu = solve sqp(x, W)
    a, weights = \overline{lineSearch}(x,mu,weights,s,k)
    weights old = weights
    W = BFGS(x,W, s, mu, a)
    x += a*s
    k += 1
    delta L norm = np.linalg.norm(dfdx(x) + np.matmul(mu.T,
torch.cat((dfdg1(x),dfdg2(x)),0)))
X reults = x.T
print("The value of x1 and x2 is:\nx1={}\nx2={}".format(x[0][0],x[1]
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