

Project : 1

Name: Geethav Lavadiya

ASUID: 1222768924

- for the given conditions

- Gravity acceleration = 0.12

- Boost acceleration = 0.18

-
$$\text{drag} = C_D \cdot A \cdot \rho \times \frac{1}{2} \times V^2$$

- Assumed values for drag calculation

- $C_D = 0.25$

- $A = 10$ (Crosssection area of rocket)

- $\rho = \text{density} = 0.00179$

- $V = \text{velocity in } y \text{ direction}$

⇒ rocket Parameters

→ mass = 549054 kg

→ diameter = 3.7 m

→ Area = 10.75 ≈ 10 taken for simplicity

→ Volume = 752.64706

- $\rho = \text{mass} / \text{volume}$

→ $x \Rightarrow x$ -coordinates

$y \Rightarrow y$ -coordinates

$v_x \Rightarrow$ velocity in x direction

$v_y \Rightarrow$ velocity in y direction

→ objective function:

$$\min_{\theta} \|S(\tau)\|^2$$

where $S(\tau) = (x(\tau), v_x(\tau), y(\tau), v_y(\tau), \theta)$

→ constraints

$$x(t+1) = x(t) + v_x(t) \cdot \Delta t$$

$$y(t+1) = y(t) + v_y(t) \cdot \Delta t$$

$$\rightarrow v_x(t+1) = v_x(t) + \Delta t \cdot (-g \cos \theta(t))$$

$$v_y(t+1) = v_y(t) + \Delta t \cdot \sin \theta(t)$$

$$\Rightarrow \text{drag} = -\frac{1}{2} \cdot C_d \cdot A \cdot \rho \cdot V_j^2$$

$$\Rightarrow \text{state} = \text{state} + \text{delta_state} \cdot \text{gravity} + \text{delta_state} \cdot \text{thrust} - \text{drag}$$

$$\text{Step.mat} = \begin{bmatrix} 1 & \Delta t & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \Delta t & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha \\ \gamma \\ v_x \\ v_y \\ \theta \end{bmatrix}$$

→ the optimizer is set to run 30 iterations for $T=100s$.

⇒ conclusions

→ from value of loss and graph of convergence we can say that at the end of 30 iteration loss converges to zero.

→ also, for α at the iteration 30 by it also approaches to zero.