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import numpy as np
import matplotlib.pyplot as plt

def mean_squared_error(y_true, y_predicted):
    cost = np.sum((y_true-y_predicted)**2) / len(y_true)
    return cost

def gradient_descent(x, y, iterations = 1000, learning_rate = 0.009, stopping_threshold = 1e-6):
    current_weight = 0.1
    current_bias = 0.01
    iterations = iterations
    learning_rate = learning_rate
    n = float(len(x))

    costs = []
    weights = []
    previous_cost = None

    for i in range(iterations):

        y_predicted = (current_weight * x) + current_bias

        current_cost = mean_squared_error(y, y_predicted)
        if previous_cost and abs(previous_cost-current_cost)<=stopping_threshold:
            break

        previous_cost = current_cost

        costs.append(current_cost)
        weights.append(current_weight)

        weight_derivative = -(2/n) * sum(x * (y-y_predicted))
        bias_derivative = -(2/n) * sum(y-y_predicted)

        current_weight = current_weight - (learning_rate * weight_derivative)
        current_bias = current_bias - (learning_rate * bias_derivative)

    print("Iteration",i+1, "Cost: ",current_cost, "Weight: ",current_weight,"Bias: ",current_bias)

    return current_weight, current_bias

X = np.array([1,3.5,6])
Y = np.array([4,5.5,9])

estimated_weight, estimated_bias = gradient_descent(X, Y, iterations=1000)
print(f"\nEstimated Weight: {estimated_weight}\nEstimated Bias: {estimated_bias}")

Y_pred = estimated_weight*X + estimated_bias

plt.figure(figsize = (8,6))
plt.scatter(X, Y, marker='o', color='red')
plt.plot([min(X), max(X)], [min(Y_pred), max(Y_pred)], color='blue',markerfacecolor='red', markersize=10,)
plt.xlabel("X")
plt.ylabel("Y")
plt.show()

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Iteration 974 Cost: 0.2225007978226865 Weight: 1.0071355015027494 Bias: 2.63369
Iteration 975 Cost: 0.22249837002655445 Weight: 1.007104340388653 Bias: 2.63383
Iteration 976 Cost: 0.2224959633887503 Weight: 1.0070733153567972 Bias: 2.63397
Iteration 977 Cost: 0.2224935777248799 Weight: 1.0070424258129034 Bias: 2.63412
Iteration 978 Cost: 0.22249121285215367 Weight: 1.0070116711652888 Bias: 2.6342
Iteration 979 Cost: 0.22248886858937586 Weight: 1.0069810508248538 Bias: 2.6344
Iteration 980 Cost: 0.22248654475693083 Weight: 1.006950564205072 Bias: 2.63454
Iteration 981 Cost: 0.22248424117676635 Weight: 1.0069202107219783 Bias: 2.6346
Iteration 982 Cost: 0.22248195767238468 Weight: 1.0068899897941577 Bias: 2.6347
Iteration 983 Cost: 0.2224796940688235 Weight: 1.0068599008427341 Bias: 2.6349
Iteration 984 Cost: 0.2224774501926464 Weight: 1.0068299432913597 Bias: 2.6351
Iteration 985 Cost: 0.22247522587192936 Weight: 1.0068001165662035 Bias: 2.6352
Iteration 986 Cost: 0.2224730209362449 Weight: 1.0067704200959404 Bias: 2.63537
Iteration 987 Cost: 0.22247083521665287 Weight: 1.0067408533117406 Bias: 2.6355
Iteration 988 Cost: 0.2224686685456836 Weight: 1.0067114156472576 Bias: 2.63565
Iteration 989 Cost: 0.2224665207573281 Weight: 1.0066821065386193 Bias: 2.63578
Iteration 990 Cost: 0.22246439168702314 Weight: 1.0066529254244154 Bias: 2.6359
Iteration 991 Cost: 0.22246228117164066 Weight: 1.0066238717456872 Bias: 2.6360
Iteration 992 Cost: 0.22246018904947376 Weight: 1.0065949449459173 Bias: 2.6361
Iteration 993 Cost: 0.22245811516022532 Weight: 1.0065661444710186 Bias: 2.6363
Iteration 994 Cost: 0.22245605934499366 Weight: 1.0065374697693237 Bias: 2.6364
Iteration 995 Cost: 0.2224540214462644 Weight: 1.0065089202915742 Bias: 2.63658
Iteration 996 Cost: 0.22245200130789397 Weight: 1.0064804954909106 Bias: 2.6367
Iteration 997 Cost: 0.2224499987751001 Weight: 1.0064521948228615 Bias: 2.63685
Iteration 998 Cost: 0.22244801369445022 Weight: 1.006424017745333 Bias: 2.63698
Iteration 999 Cost: 0.22244604591384787 Weight: 1.0063959637185989 Bias: 2.637
Iteration 1000 Cost: 0.222444064591384787 Weight: 1.0063959637185989 Bias: 2.637
```

Estimated Weight: 1.0063959637185989
Estimated Bias: 2.637109908483543

