

Q4. Given two arrays of equal size n and an integer k . The task is to permute both arrays such that the sum of their corresponding element is greater than or equal to k i.e $a[i] + b[i] \geq k$. The task is to print “Yes” if any such permutation exists, otherwise print “No”.

Input :

$a[] = \{2, 1, 3\}$, $b[] = \{7, 8, 9\}$, $k = 10$.

Output : Yes

Input :

$a[] = \{1, 2, 2, 1\}$, $b[] = \{3, 3, 3, 4\}$, $k = 5$.

Output : No

$$\begin{array}{rcl}
 \downarrow & \begin{array}{c} \underline{6} + \underline{4} \\ 7 + 3 \\ 8 + 2 \\ \underline{9} + \underline{1} \end{array} & \begin{array}{c} = 10 \\ = 10 \\ = 10 \\ = 10 \end{array} \\
 & & \downarrow
 \end{array}$$

$$\underline{9 + 4 = 13} \quad \checkmark$$

$$\underline{6 + 1 = 7} \quad \times$$

$$\begin{array}{lcl}
 a = \{2, 1, 3\} \rightarrow \{ \textcircled{1}, \textcircled{2}, \textcircled{3} \} & & \{ \underline{1}, \underline{2}, \underline{3} \} \\
 \text{---} \text{---} K=10 & & \{ \underline{9}, \underline{8}, \underline{7} \} \\
 b = \{7, 8, 9\} \rightarrow \{ \textcircled{7}, \textcircled{8}, \textcircled{9} \} & & \\
 & & \text{Yes} \\
 & & \text{---} \text{---}
 \end{array}$$

$\text{---} \text{---} 10 \quad \text{---} \text{---} 10 \quad \text{---} \text{---} 10$

Sum $\geq K$

① Sort → Ascending

② Sort → Descending

① Sort a in ascending order

② Sort b in descending order

③ Iterate and check check condition

$$\underline{a[i] + b[i] \geq K} \rightarrow \text{Yes}$$

$$a[i] + b[i] < K \rightarrow \text{No}$$

$$a = \{1, 2, 2, 1\}$$

$$b = \{3, 3, 3, 4\}$$

$$K = 5$$

$$\rightarrow \underline{\text{sort } a \text{ asc}} \rightarrow \{1, 1, 2, 2\} \quad \underline{\text{asc}}$$

$$\rightarrow \underline{\text{sort } b \text{ desc}} \rightarrow \{4, 3, 3, 3\} \quad \underline{\text{desc}}$$

$$\underline{\underline{a[i] + b[i] \geq K}}$$

5	4	5	5
✓	x	✓	✓

No

$$a = \{1, 3, 5, 2\}$$

$$b = \{4, 3, 6, 8\}$$

$$k = 6$$

① sort a asc $\rightarrow \{1, 2, 3, 5\}$

② sort b desc $\rightarrow \{8, 6, 4, 3\}$

③ check the condition

yes

$\begin{array}{cccc} 0 & 1 & 2 & 3 \\ \underline{1} & \underline{8} & \underline{7} & \underline{8} \\ \checkmark & \checkmark & \checkmark & \checkmark \end{array}$

$$\underline{a[i] + b[i]} \times k$$

Time Complexity : $O(n \log n)$

Sorting $\rightarrow O(n \log n)$

Space Complexity : Auxiliary space : $O(1)$
Total space complexity : $O(n)$