

1.1

Test Case	Current State	Next State	Inputs				Expected Outputs			
			D	G	P	Z	B	I	T	X
1	Start	OFF	0	0	0	0	0	0	0	0
2	OFF	OFF	1	0	0	0	0	0	0	0
3	OFF	L	0	1	0	0	1	0	1	0
4	OFF	U	0	0	1	0	1	0	0	1
5	OFF	OFF	0	0	0	1	0	0	0	0
6	U	U	1	0	0	0	1	0	0	1
7	U	U	0	1	0	0	1	0	0	1
8	U	OFF	0	0	1	0	0	0	0	0
9	U	X5	0	0	0	1	1	0	0	2
10	X5	N	1	0	0	0	1	1	0	2
11	X5	X5	0	1	0	0	1	0	0	2
12	X5	X5	0	0	1	0	1	0	0	2
13	X5	X10	0	0	0	1	1	0	0	3
14	N	X5	1	0	0	0	1	0	0	2
15	N	N	0	1	0	0	1	1	0	2
16	N	N	0	0	1	0	1	1	0	2
17	N	N	0	0	0	1	1	1	0	2
18	X10	X10	1	0	0	0	1	0	0	3
19	X10	X10	0	1	0	0	1	0	0	3
20	X10	X10	0	0	1	0	1	0	0	3
21	X10	U	0	0	0	1	1	0	0	2
22	L	L	1	0	0	0	1	0	1	0
23	L	L	0	1	0	0	1	0	1	0
24	L	OFF	0	0	1	0	0	0	0	0
25	L	L	0	0	0	1	1	0	1	0

1.2

Length	Sequence	Response	Equivalence	Carry to next level
0	Idle	$B = 0, I = 0, T = 0, X = 0$	idle	
1	D	$B = 0, I = 0, T = 0, X = 0$	idle	
	G	$B = 1, I = 0, T = 1, X = 0$	-	Yes
	P	$B = 1, I = 0, T = 0, X = 1$	-	Yes
	Z	$B = 0, I = 0, T = 0, X = 0$	idle	
2	PD	$B = 1, I = 0, T = 0, X = 1$	P	
	PG	$B = 1, I = 0, T = 0, X = 1$	P	
	PP	$B = 0, I = 0, T = 0, X = 0$	idle	
	PZ	$B = 1, I = 0, T = 0, X = 2$	-	Yes
	GD	$B = 1, I = 0, T = 1, X = 0$	G	
	GG	$B = 1, I = 0, T = 1, X = 0$	G	
	GP	$B = 0, I = 0, T = 0, X = 0$	idle	
	GZ	$B = 1, I = 0, T = 1, X = 0$	G	
3	PZD	$B = 1, I = 1, T = 0, X = 2$	-	Yes
	PZG	$B = 1, I = 0, T = 0, X = 2$	PZ	
	PZP	$B = 1, I = 0, T = 0, X = 2$	PZ	
	PZZ	$B = 1, I = 0, T = 0, X = 3$	-	Yes
4	PZDD	$B = 1, I = 0, T = 0, X = 2$	PZ	
	PZDG	$B = 1, I = 1, T = 0, X = 2$	PZD	
	PZDP	$B = 1, I = 1, T = 0, X = 2$	PZD	
	PZDZ	$B = 1, I = 1, T = 0, X = 2$	PZD	
	PZZD	$B = 1, I = 0, T = 0, X = 3$	PZZ	
	PZZG	$B = 1, I = 0, T = 0, X = 3$	PZZ	
	PZZP	$B = 1, I = 0, T = 0, X = 3$	PZZ	
	PZZZ	$B = 1, I = 0, T = 0, X = 1$	P	

Canonical sequence: **G, P, PZ, PZD, PZZ**

Test Case No	Inputs			Exp. Outputs
	Time Of Day	Call Length	Call Type	Cost
1	12:00:00 AM	1	International	\$0.24
2	12:00:00 AM	5	Domestic	\$0.40
3	12:00:00 AM	10	Conference	\$4.00
4	7:59:59 AM	1	Domestic	\$0.08
5	7:59:59 AM	5	International	\$1.20
6	7:59:59 AM	10	International	\$2.40
7	7:59:59 AM	15	Conference	\$6.00
8	8:00:00 AM	1	Conference	\$1.25
9	8:00:00 AM	5	International	\$3.75
10	8:00:00 AM	10	Domestic	\$2.50
11	7:00:00 PM	5	Conference	\$6.25
12	7:00:00 PM	15	International	\$11.25
13	7:00:00 PM	61	Domestic	\$15.25
14	7:00:01 PM	15	Domestic	\$2.25
15	7:00:01 PM	61	International	\$27.45
16	7:00:01 PM	1	Conference	\$0.75
17	9:59:59 PM	61	Conference	\$45.75
18	9:59:59 PM	1	International	\$0.45
19	9:59:59 PM	5	Domestic	\$0.75
20	10:00:00 PM	1	Domestic	\$0.10
21	10:00:00 PM	5	Conference	\$2.50
22	10:00:00 PM	10	International	\$3.00
23	11:59:59 PM	10	Domestic	\$1.00
24	11:59:59 PM	15	International	\$4.50
25	11:59:59 PM	61	Conference	\$30.50
26	12:00:00 AM	15	Domestic	\$1.20
27	12:00:00 AM	61	International	\$14.64
28	7:59:59 AM	61	Domestic	\$4.88
29	8:00:00 AM	15	Conference	\$18.75
30	8:00:00 AM	61	International	\$45.75
31	7:00:00 PM	10	Conference	\$12.50
32	7:00:00 PM	1	International	\$0.75
33	7:00:01 PM	5	International	\$2.25
34	7:00:01 PM	10	Domestic	\$1.50
35	9:59:59 PM	10	International	\$4.50
36	9:59:59 PM	15	Domestic	\$2.25
37	10:00:00 PM	15	International	\$4.50
38	10:00:00 PM	61	Domestic	\$6.10
39	11:59:59 PM	1	Domestic	\$0.10
40	11:59:59 PM	5	Conference	\$2.50

3.a)

$$a'b'c' + abc + abc'd' + a'b'cd' + a'bc'd + a'bcd + ab'c'd$$

		CD			
		00	01	11	10
AB	00	1	1		1
	01		1	1	
	11	1		1	1
	10		1		

$$\text{Output} - a'b'd' + b'c'd + a'c'd + abd' + bcd$$

3.b)

$$a'b'c' + a'cd' + ac'd' + ab'c + a'b'cd + abcd' + ab'c'd + a'bc'd'$$

		CD			
		00	01	11	10
AB	00	1	1	1	1
	01	1			1
	11	1			1
	10	1	1	1	1

$$\text{Output} - c'd + a'b' + ab' + cd' = b' + d'$$

3.c)

$$cd + a'b'c'd' + a'b'c'd + ab'cd + a'bcd + a'b'cd' + ab'c'd' + a'bc'd' + ab$$

		CD			
		00	01	11	10
AB	00	1	1	1	1
	01	1		1	
	11	1	1	1	1
	10	1		1	

$$\text{Output} - a'b' + ab + c'd' + cd$$

3.d)

$$a'b'c'd + abcd + a'b'cd + abc'd + a'bc'd + ab'cd + a'bcd + ab'c'd$$

		CD			
		00	01	11	10
AB	00		1	1	
	01		1	1	
	11		1	1	
	10		1	1	

$$\text{Output} - d$$

4.a)	Condition			Decision
	a	b	c	$a+b'c'$
	F	F	F	T
	F	F	T	F
	F	T	F	F
	F	T	T	F
	T	F	F	T
	T	F	T	T
	T	T	F	T
	T	T	T	T
	C/D	(FFT, TTF)		
	C	(FFF, TTT)		
	D	(FFF, FFT)		
	TOF	a, b'c		
	TNF	$(a)' + b'c' = a' + b'c'$, $a + (b'c')' = a + b + c$		

4.b)	Condition			Decision
	a	c	d	$a(c + d)$
				$ac + ad$
	F	F	F	F
	F	F	T	F
	F	T	F	F
	F	T	T	F
	T	F	F	F
	T	F	T	T
	T	T	F	T
	T	T	T	T
	C/D	(FFF, TTT)		
	C	(FTT, TFF)		
	D	(FFF, TFT)		
	TOF	ac, dc		
	TNF	$(ac)' + ad = a' + c' + ad$, $ac + (ad)' = ac + a' + d'$		

4.c)	Condition				Decision
	a	b	c	d	$ab + c' + d$
	F	F	F	F	T
	F	F	F	T	T
	F	F	T	F	F
	F	F	T	T	T
	F	T	F	F	T
	F	T	F	T	T
	F	T	T	F	F
	F	T	T	T	T
	T	F	F	F	T
	T	F	F	T	T
	T	F	T	F	F
	T	F	T	T	T
	T	T	F	F	T
	T	T	F	T	T
	T	T	T	F	T
	T	T	T	T	T
	C/D	(FFTF, TTFT)			
	C	(FFFF, TTTT)			
	D	(FFFF, FFTF)			
	TOF	$c' + d, ab + d, ab + c'$			
	TNF	$(ab)' + c' + d = a' + b' + c' + d$, $ab + (c')' + d = ab + c + d$, $ab + c' + (d)' = ab + c' + d'$			

4.d)	Condition		Decision
	a	b	$ab \text{ XOR } (a + b)$
	F	F	F
	F	T	T
	T	F	T
	T	T	F
	C/D	-	
	C	(FF, TT)	
	D	(FF, FT)	
	TOF	$a'b, ab'$	
	TNF	$(ab')' + a'b = a' + b$, $ab' + (a'b)' = a + b'$	

5.1.a)	$ab' + c$
	COI a: XFF
	COI b: TXF
	COI c: FFX, FTX, TTX
	base set: FFF, TFF, TTF
	UC: FFF, TFF, TTF, FFT

5.1.b)	$a' + b + c$
	COI a: XFF
	COI b: TXF
	COI c: TFX
	base set: TFF
	UC: TFF, FFF, TTF, TFT

5.1.c)	$a + bc + d'$
	COI a: XFFT, XFTT, XTFT
	COI b: FXTT
	COI c: FTXT
	COI d: FFFX, FFTX, FTFX
	base set: FT TT, FFTT, FTFT
	UC: FT TT, FFTT, FTFT, TFFT, FFTF

5.2.a)	$abc \text{ XOR } (ab'c')' = a' + b'c + bc'$			
	Condition			Decision
	a	b	c	$abc \text{ XOR } (ab'c')'$
				$a' + b'c + bc'$
	F	F	F	T
	F	F	T	T
	F	T	F	T
	F	T	T	T
	T	F	F	F
	T	F	T	T
	T	T	F	T
	T	T	T	F
	C/D	(FFF, TTT)		
	C	(FFT, TTF)		
	D	(FFF, TFF)		
	TOF	$b'c + bc', a' + bc', a + b'c$		
	TNF	$(a')' + b'c + bc' = a + b'c + bc'$ $a' + (b'c)' + bc' = a' + b + c'$ $a' + b'c + (bc')' = a' + b' + c$		

5.2.b)	$((a+b)(b'+c))' = a'b' + a'c' + bc'$			
	Condition			Decision
	a	b	c	$((a+b)(b'+c))'$
				$a'b' + bc'$
	F	F	F	T
	F	F	T	T
	F	T	F	T
	F	T	T	F
	T	F	F	F
	T	F	T	F
	T	T	F	T
	T	T	T	F
	C/D			(FFF, TTT)
	C			(FFT, TTF)
	D			(FFF, FTT)
	TOF			$a'b', bc'$
	TNF			$(a'b')' + bc' = a+b$ $a'b' + (bc')' = b'+c$

5.2.c)	$(ab' + ac + c'd)' = a'c + a'd' + bc'd'$				
	Condition				Decision
	a	b	c	d	$(ab' + ac + c'd)'$
					$a'c + a'd' + bc'd'$
	F	F	F	F	T
	F	F	F	T	F
	F	F	T	F	T
	F	F	T	T	T
	F	T	F	F	T
	F	T	F	T	F
	F	T	T	F	T
	F	T	T	T	T
	T	F	F	F	F
	T	F	F	T	F
	T	F	T	F	F
	T	F	T	T	F
	T	T	F	F	T
	T	T	F	T	F
	T	T	T	F	F
	T	T	T	T	F
	C/D				(FFFF, TTTT)
	C				(FFFT, TTTF)
	D				(FFFF, FFFT)
	TOF				$a'd' + bc'd', a'c + bc'd', a'c + a'd'$
	TNF				$(a'c)' + a'd' + bc'd' = a + c' + a'd'$ $a'c + (a'd')' + bc'd' = a'c + a + d + bc'd'$ $a'c + a'd' + (bc'd')' = a'd' + b' + c + d$

5.3.a)	$(a'b'c' + a'b'd')' = a + b + cd$
COI a:	XFFF, XFFT , XFTF
COI b:	FXFF, FXFT , FXTF
COI c:	FFXT
COI d:	FFTX
base set:	FFFT , FFTT , FFTF
UC1:	FFFT , FFTT , FFTF , TFFT, FTFT
UC2:	FFFT , FFTT , FFTF , TFFT, FTTF
UC3:	FFFT , FFTT , FFTF , TFTF, FTFT
UC4:	FFFT , FFTT , FFTF , TFTF, FTTF

5.3.b)	$(a'c' + a'd' + a'b)' = a + b'cd$
COI a:	XFFF, XFFT , XFTF , XTFT, XTTF, XTTT , XTFF
COI b:	FXTT
COI c:	FFXT
COI d:	FFTX
base set:	FFTT , FTTT , FFFT , FFTF
UC1:	FFTT , FTTT , FFFT , FFTF , TFFT
UC2:	FFTT , FTTT , FFFT , FFTF , TFTF
UC3:	FFTT , FTTT , FFFT , FFTF , TTTT

5.3.c)	$(abd + acd)' = a' + b'c' + d'$
COI a:	XTTT, XTFT , XFTT
COI b:	TXFT
COI c:	TFXT
COI d:	TTTX, TTFX , TFTX
base set:	TFFT , TTFT , TFTT
UC1:	TFFT , TTFT , TFTT , FTFT, TTFF
UC2:	TFFT , TTFT , TFTT , FTFT, TFTF
UC3:	TFFT , TTFT , TFTT , FFFT, TTFF
UC4:	TFFT , TTFT , TFTT , FFFT, TFTF

Bonus Questions	
b.1.a)	$ab' + c' + d'$
	COI a: XFTT
	COI b: TXTT
	COI c: FFXT , FTXT, TTXT
	COI d: FFTX , FTTX, TTTX
	base set: FFTT , TFTT , TTTT
	UC1: FFTT , TFTT , TTTT , FFFT, FFTF
	UC2: FFTT , TFTT , TTTT , FFFT, TTTF
	M: FFTT , TFTT , TTTT , FTFT, FTTF

b.1.b)	$a + bc + d'$
	COI a: XFFT, XFTT , XTFT
	COI b: FXTT
	COI c: FTXT
	COI d: FFFX, FFTX , FTFX
	base set: FFTT , FTTT , FTFT
	UC1: FFTT , FTTT , FTFT , TFTT, FFTF
	UC2: FFTT , FTTT , FTFT , TFTT, FTFF
	M: FFTT , FTTT , FTFT , TFFT, FFFF

b.2.a)	$a = (b < 0) \parallel c$			
	Test Case	Inputs		Expected Outputs
		b	c	a
	1	0	F	F
	2	0	T	T
	3	-1	F	T

b.2.b)	$a = b \ \&\& \ (c < 5)$			
	Test Case	Inputs		Expected Outputs
		b	c	a
	1	T	4	T
	2	T	5	F
	3	F	4	F

b.2.c)	a = (b >5) && (c<8)			
	Test Case	Inputs		Expected Outputs
		b	c	a
	1	6	7	T
	2	5	7	F
	3	6	8	F

b.2.d)	a = (b>5) && (b<10)			
	Test Case	Inputs		Expected Outputs
		b	c	a
	1	6	9	T
	2	6	10	F
	3	5	9	F