

Module 10: CS31003: Compilers

Global Register Allocation

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Module Objectives

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Objectives &
Outline

Issues in Register
Allocation

The Problem

GRA by Usage
Count

Bubble Sort

Chaitin's
Algorithm: GRA
by Graph
Coloring

Graph Coloring

Framework

Example

Register Spill

- Issues in Global Register Allocation
- The Problem
- Register Allocation based on Usage Counts
- Chaitin's graph coloring based algorithm

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 - Graph Coloring
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 - Example
 - Register Spill

Some Issues in Register Allocation

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- Which values in a program reside in registers? ([Register Allocation](#))
- In which register? ([Register Assignment](#))
 - The two together are usually loosely referred to as **Register Allocation (RA)**
- What is the unit at the level of which register allocation is done?
 - Typical units are *basic blocks*, *functions*, and *regions*
 - RA within *basic blocks* is called **local RA**
 - RA within *functions* and *regions* are known as **global RA**
 - Global RA requires lot more time than local RA



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- Phase ordering between *register allocation* and *instruction scheduling*
- In which register? (*register assignment*)
 - Performing RA first restricts movement of code during scheduling – *not recommended*
 - Scheduling instructions first cannot handle spill code introduced during RA
 - ▷ Requires another pass of scheduling
- Tradeoff between *speed* and *quality of allocation*
 - In some cases, for example, in Just-In-Time compilation, cannot afford to spend too much time in register allocation
 - Only local or both local and global allocation?

The Problem

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- Global Register Allocation assumes that allocation is done beyond basic blocks and **usually at function level**
- Decision problem related to register allocation
 - Given an intermediate language program represented as a control flow graph and a number k , is there an assignment of registers to program variables such that
 - ▷ *no conflicting variables* are assigned the same register,
 - ▷ *no extra loads or stores* are introduced, and
 - ▷ *at most k* registers are used
- This problem has been shown to be NP-hard (Sethi 1970)
- **Graph colouring** is the most popular heuristic used
- However, there are simpler algorithms as well

Conflicting Variables

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- Two variables interfere or conflict if their **live ranges** intersect
 - A variable is **live** at a point p in the flow graph, if there is a **use** of that variable in the path from p to the end of the flow graph
 - The **live range** of a variable is the *smallest set of program points* at which it is live
 - The representation for a point is:
 - ▷ basic block number
 - ▷ instruction number in the basic block

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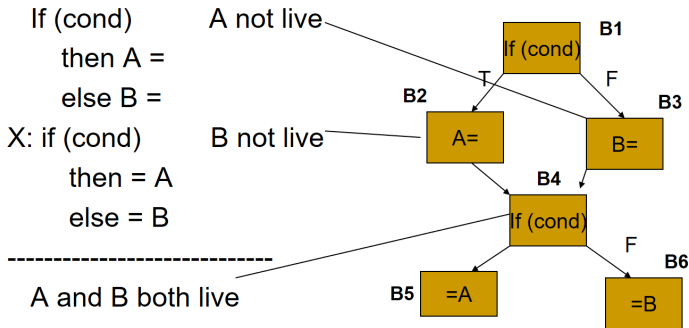
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Register Spill

- **Live range of A: B2, B4, B5**
- **Live range of B: B3, B4, B6**



Global Register Allocation via Usage Counts (for Single Loops)

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- Allocate registers for variables used within loops
- Requires information about liveness of variables at the entry and exit of each basic block (BB) of a loop
- Once a variable is computed into a register, it stays in that register until the end of the BB (subject to existence of next-uses)
- Load/Store instructions cost 2 units (because they occupy two words)

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[1] For every **usage** of a variable **v** in a BB, **until it is first defined**, do:

- $\text{savings}(v) = \text{savings}(v) + 1$
- after **v** is defined, it stays in the register any way, and all further references are to that register

[2] For every variable **v computed** in a BB, if it is **live on exit** from the BB,

- count a **savings of 2**, since it is not necessary to store it at the end of the BB

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- Total savings per variable v are

$$\sum_{B \in \text{Loop}} (\text{savings}(v, B)) + 2 * \text{liveandcomputed}(v, B)$$

- $\text{liveandcomputed}(v, B)$ in the second term is 1 or 0
- On entry to (exit from) the loop, we load (store) a variable live on entry (exit), and lose 2 units for each
 - But, these are *one time* costs and are neglected
- Variables, whose savings are the highest will reside in registers

Global Register Allocation via Usage Counts (for Single Loops)

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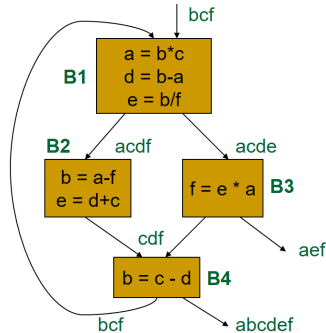
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Savings for the variables

	B1	B2	B3	B4	
a:	(0+2)+	(1+0)+	(1+0)+	(0+0)=	4
b:	(3+0)+	(0+0)+	(0+0)+	(0+2)=	5
c:	(1+0)+	(1+0)+	(0+0)+	(1+0)=	3
d:	(0+2)+	(1+0)+	(0+0)+	(1+0)=	4
e:	(0+2)+	(0+0)+	(1+0)+	(0+0)=	3
f:	(1+0)+	(1+0)+	(0+2)+	(0+0)=	4

If there are 3 registers, they will be allocated to the variables, a, b, and d (or f)

Global Register Allocation via Usage Counts (for Nested Loops)

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- We first assign registers for inner loops and then consider outer loops. Let **L1** nest **L2**
- For variables assigned registers in L2, but not in L1
 - load these variables on entry to L2 and store them on exit from L2
- For variables assigned registers in L1, but not in L2
 - store these variables on entry to L2 and load them on exit from L2
- All costs are calculated keeping the above rules

Global Register Allocation via Usage Counts (for Nested Loops)

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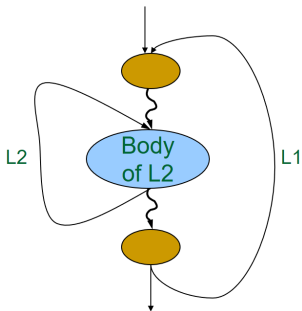
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- **Case 1:** Variables x, y, z assigned registers in L2, but not in L1
 - Load x, y, z on entry to L2
 - Store x, y, z on exit from L2
- **Case 2:** Variables a, b, c assigned registers in L1, but not in L2
 - Store a, b, c on entry to L2
 - Load a, b, c on exit from L2
- **Case 3:** Variables p, q assigned registers in both L1 and L2
 - No special action

Sample Code Generation: Bubble Sort

Three Address Code

- Three Address Code for Bubble Sort as generated by syntax directed translation

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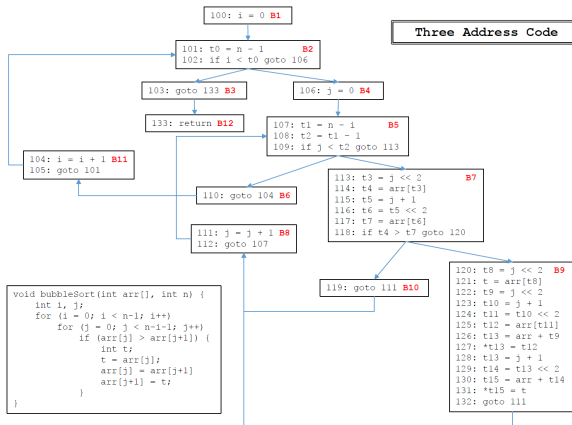
Register Spill

```

100*: i = 0
101*: t0 = n - 1
102 : if i < t0 goto 106
103*: goto 133
104*: i = i + 1
105 : goto 101
106*: j = 0
107*: t1 = n - i
108 : t2 = t1 - 1
109 : if j < t2 goto 113
110*: goto 104
111*: j = j + 1
112 : goto 107
113*: t3 = j << 2
114 : t4 = arr[t3]
115 : t5 = j + 1
116 : t6 = t5 << 2
117 : t7 = arr[t6]
118 : if t4 > t7 goto 120
119*: goto 111
120*: t8 = j << 2
121 : t = arr[t8]
122 : t9 = j << 2
123 : t10 = j + 1
124 : t11 = t10 << 2
125 : t12 = arr[t11]
126 : t13 = arr + t9
127 : *t13 = t12
128 : t13 = j + 1
129 : t14 = t13 << 2
130 : t15 = arr + t14
131 : *t15 = t
132 : goto 111
133*: return
    
```

```

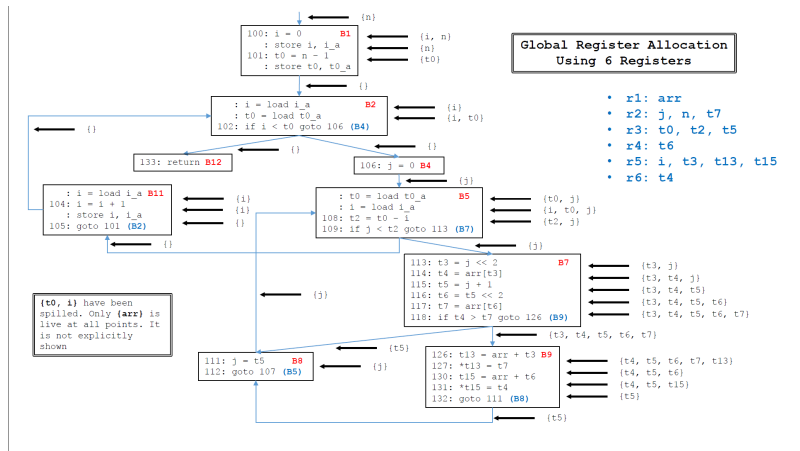
void bubbleSort(int arr[], int n) {
    int i, j;
    for (i = 0; i < n-1; i++)
        for (j = 0; j < n-i-1; j++)
            if (arr[j] > arr[j+1]) {
                int t;
                t = arr[j];
                arr[j] = arr[j+1];
                arr[j+1] = t;
            }
}
    
```



Sample Code Generation: Bubble Sort

Liveness after LCSE, GCSE Optimization

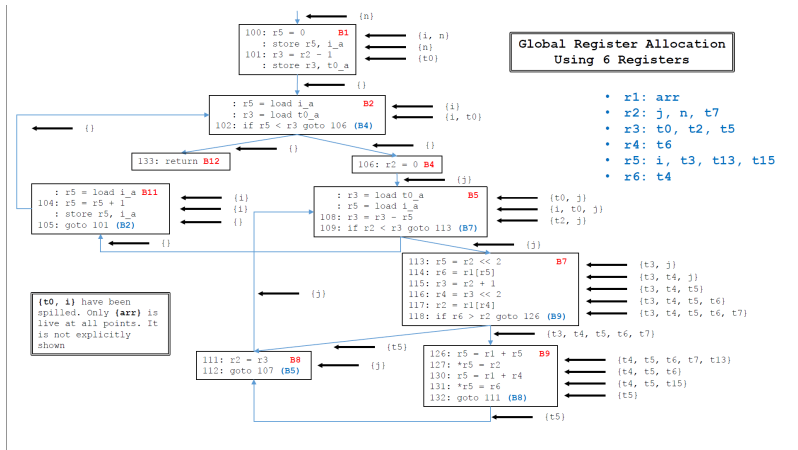
- Three Address Code Optimized by peephole, LCSE by VN and GCSE by DFA. Finally, live variables are computed by DFA



Sample Code Generation: Bubble Sort

Global Register Allocation

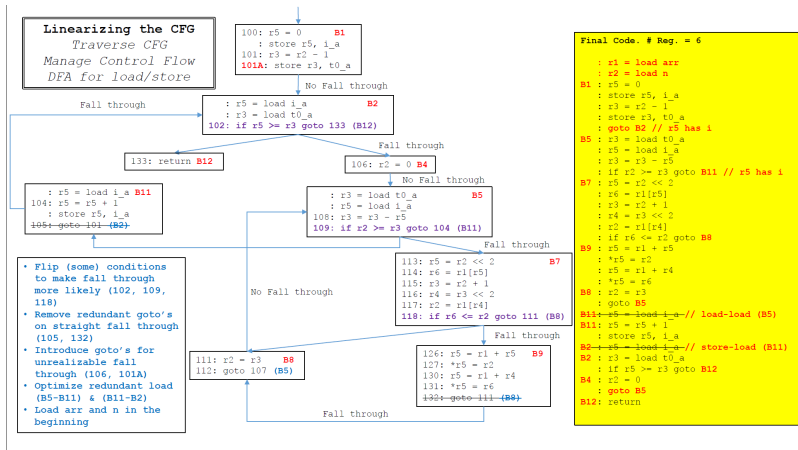
- Registers are allocated globally using graph coloring based on the liveness information
- Variables are replaced by respective registers



Sample Code Generation: Bubble Sort

Linearized and Optimized Target Code

- The CFG is linearized and further optimized to get the final target code



Chaitin's Formulation of the Register Allocation Problem

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- A graph colouring formulation on the interference graph
- Nodes in the graph represent either live ranges of variables or entities called webs
- An edge connects two live ranges that interfere or conflict with one another
- Usually both adjacency matrix and adjacency lists are used to represent the graph.
- Assign colours to the nodes such that two nodes connected by an edge are not assigned the same colour
 - The number of colours available is the number of registers available on the machine
 - A k-colouring of the interference graph is mapped onto an allocation with k registers



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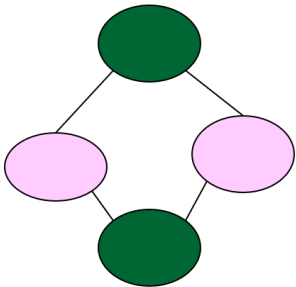
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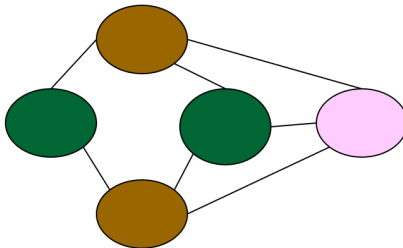
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Register Spill

Two Colorable



Three Colorable



Idea behind Chaitin's Algorithm

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- Choose an arbitrary node of degree less than k and put it on the stack
- Remove that vertex and all its edges from the graph
 - This may decrease the degree of some other nodes and cause some more nodes to have degree less than k
- At some point, if all vertices have degree greater than or equal to k , some node has to be spilled
- If no vertex needs to be spilled, successively pop vertices off stack and colour them in a colour not used by neighbours (reuse colours as far as possible)

Simple example – Given Graph

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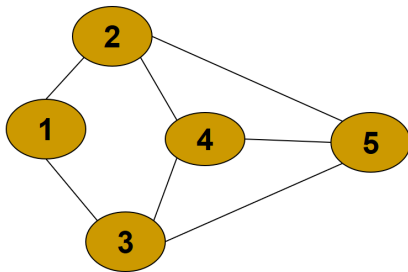
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Example

Register Spill



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3 REGISTERS

Simple example – Delete Node 1

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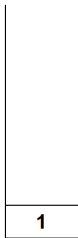
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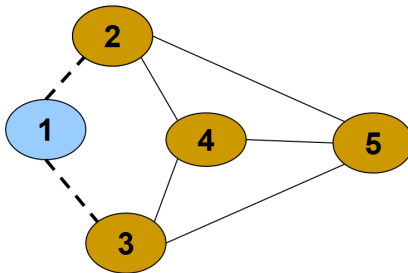
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Simple example – Delete Node 2

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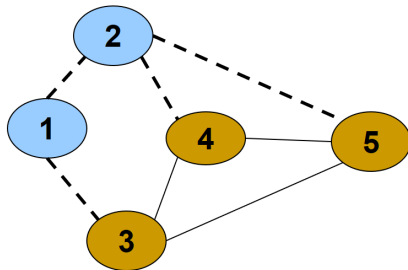
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Simple example – Delete Node 4

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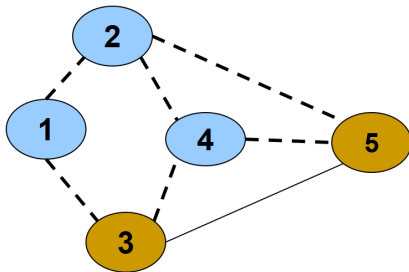
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Register Spill

4
2
1

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Simple example – Delete Node 3

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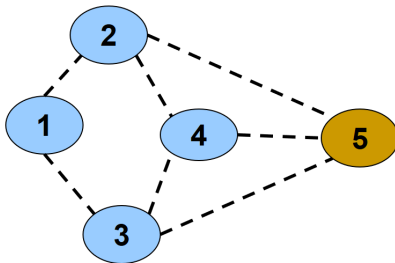
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Register Spill

3
4
2
1

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Simple example – Delete Node 5

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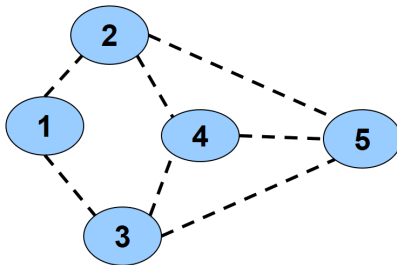
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Register Spill

5
3
4
2
1

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Simple example – Colour Node 5

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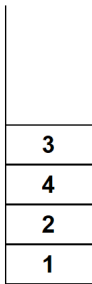
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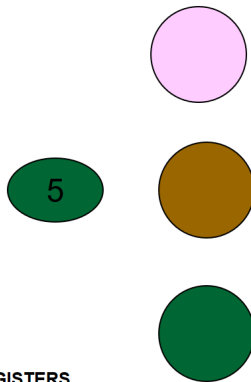
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Simple example – Colour Node 3

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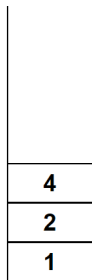
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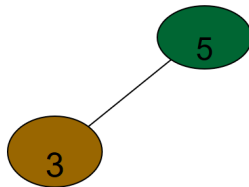
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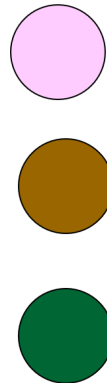
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Simple example – Colour Node 4

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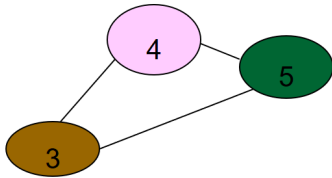
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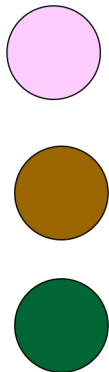
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Simple example – Colour Node 2

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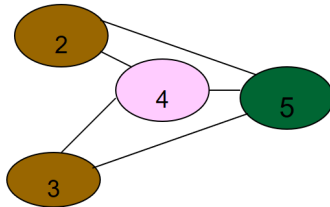
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Simple example – Colour Node 1

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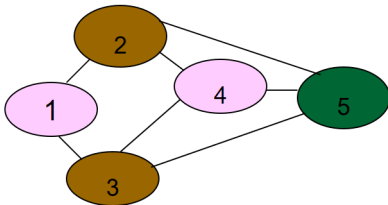
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Steps in Chaitin's Algorithm

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- Identify units for allocation
 - Renames variables/symbolic registers in the IR such that each live range has a unique name (number)
- Build the interference graph
- Coalesce by removing unnecessary move or copy instructions
- Colour the graph, thereby selecting registers
- Compute spill costs, simplify and add spill code till graph is colourable

The Chaitin Framework

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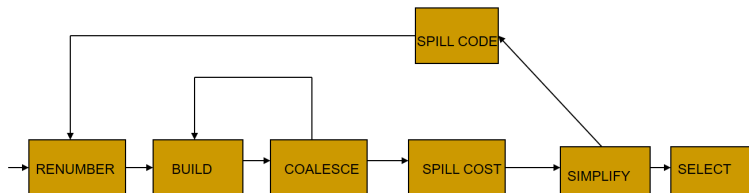
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Example of Renaming

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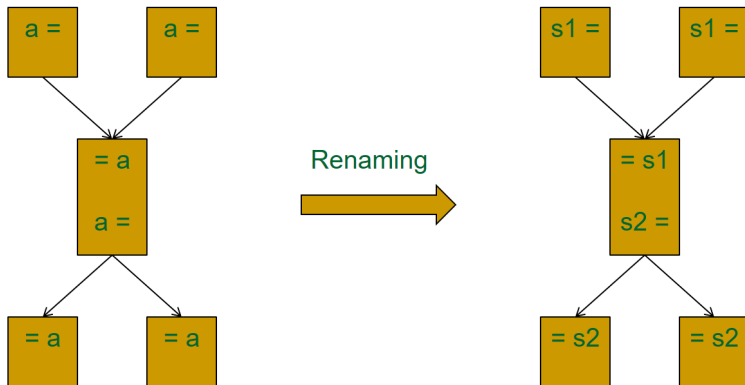
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Register Spill

Original code

1. $x = 2$
2. $y = 4$
3. $w = x + y$
4. $z = x + 1$
5. $u = x * y$
6. $x = z * 2$

Code with symbolic registers

1. $s1 = 2;$ (lv of $s1$: 1-5)
2. $s2 = 4;$ (lv of $s2$: 2-5)
3. $s3 = s1 + s2;$ (lv of $s3$: 3-3)
4. $s4 = s1 + 1;$ (lv of $s4$: 4-6)
5. $s5 = s1 * s2;$ (lv of $s5$: 5-5)
6. $s6 = s4 * 2;$ (lv of $s6$: 6-...)

An Example: Interference Graph

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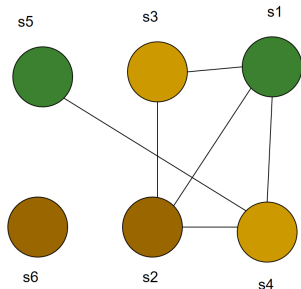
Graph Coloring

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Register Spill

Interference Graph



Stack Order for Colouring & Register Allocation (Number of Registers = 3)

s1 → r1
s2 → r2
s3 → r3
s4 → r3
s5 → r1
s6 → r2

1. x = 2
2. y = 4
3. w = x + y
4. z = x + 1
5. u = x * y
6. x = z * 2

1. s1 = 2; (lv of s1: 1-5)
2. s2 = 4; (lv of s2: 2-5)
3. s3 = s1 + s2; (lv of s3: 3-3)
4. s4 = s1 + 1; (lv of s4: 4-6)
5. s5 = s1 * s2; (lv of s5: 5-5)
6. s6 = s4 * 2; (lv of s6: 6- ...)

An Example: Interference Graph

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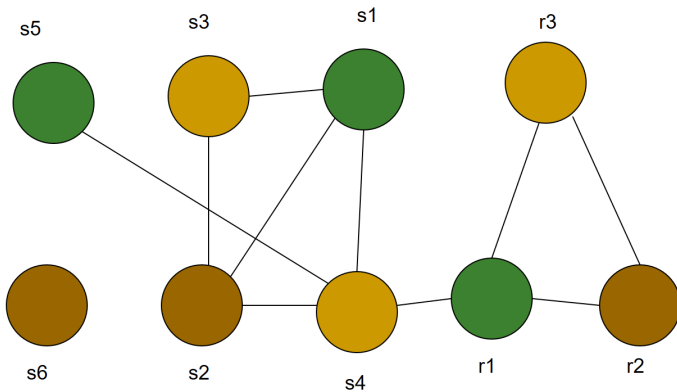
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Interference Graph

Here assume variable Z (s4) cannot occupy r1

An Example: Interference Graph

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Register Spill

s1 → r1
s2 → r2
s3 → r3
s4 → r3
s5 → r1
s6 → r2

1. x = 2
2. y = 4
3. w = x + y
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5. u = x * y
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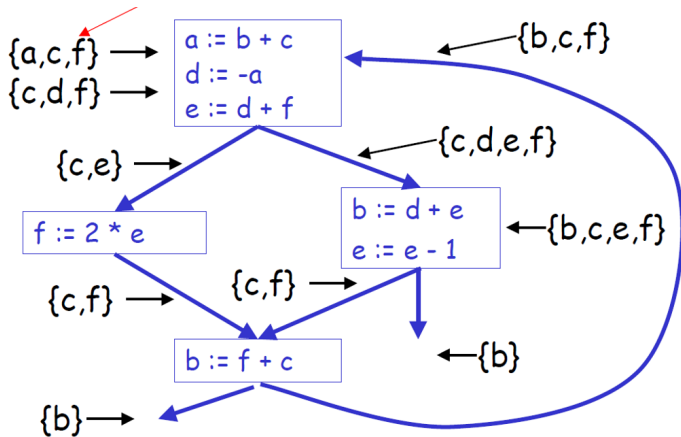
Final Code:

3 reg. are sufficient for no spills

r1 = 2
r2 = 4
r3 = r1 + r2
r3 = r1 + 1
r1 = r1 * r2
r2 = r3 * 2

Another Example

Compute live variables at each point



Register Interference Graph

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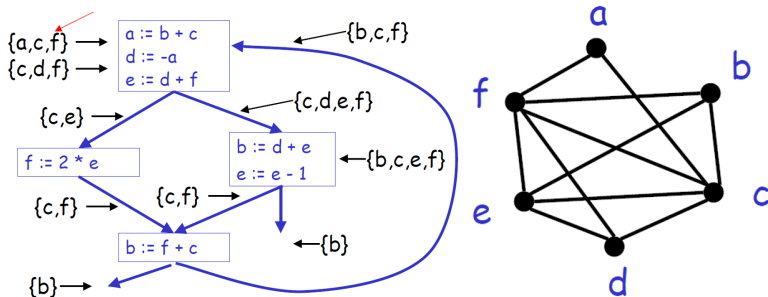
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Example

Register Spill

- b and c cannot be in the same register
- b and d can be in the same register





Graph Coloring: Example

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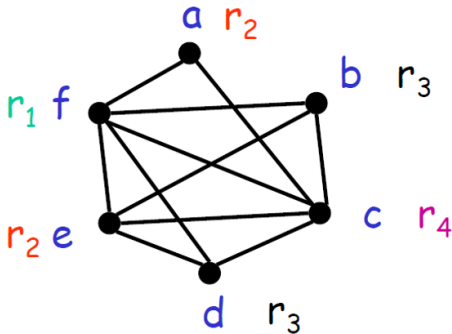
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Register Spill

- There is no coloring with less than 4 colors (has two 4-cliques)
- There are 4 colorings of the graph



Graph Coloring: Example

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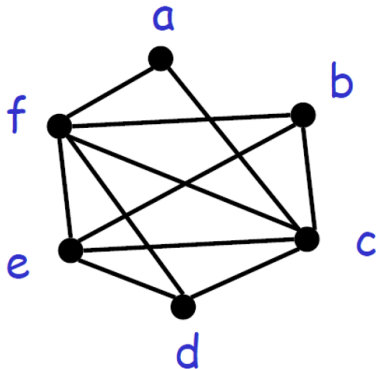
Graph Coloring

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Example

Register Spill

- Start with the RIG and with $k = 4$. $\text{Stack} = \{\}$



- Remove a and then d : $\text{Stack} = \{d, a\}$



Graph Coloring: Example

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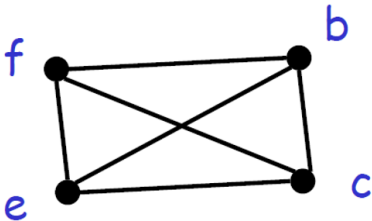
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Example

Register Spill

- Now all nodes have less than 4 neighbors and can be removed. Say, as: c, b, e, f



- $\text{Stack} = \{f, e, b, c, d, a\}$

Graph Coloring: Example

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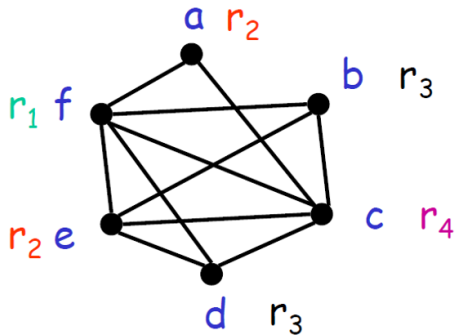
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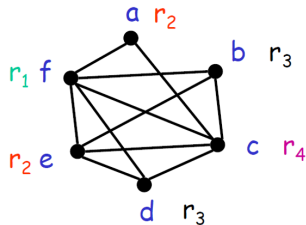
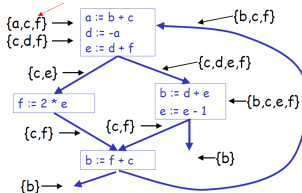
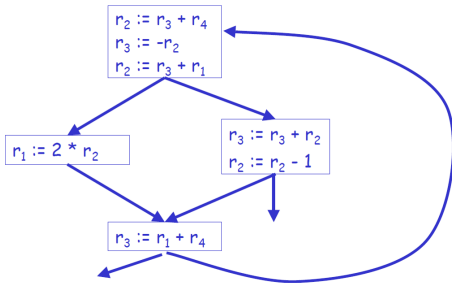
- Start assigning colors to: f, e, b, c, d, a





Code with Registers Allocated

- With the coloring the code becomes





What if the Heuristic Fails?

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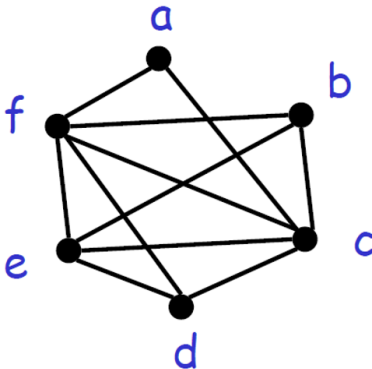
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Example

Register Spill

- What if during simplification we get to a state where all nodes have k or more neighbors?
- Let us try a 3-coloring





What if the Heuristic Fails?

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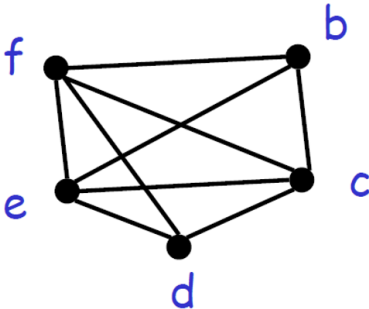
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Example

Register Spill

- Remove a and get stuck
- Pick a node as a candidate for spilling
 - A spilled temporary “lives” in memory
- Assume that f is picked as a candidate



What if the Heuristic Fails?

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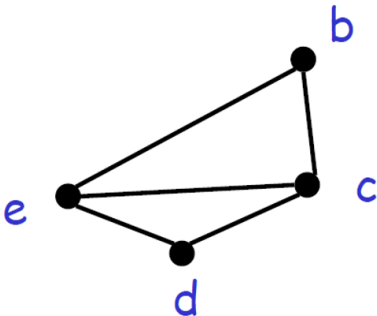
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Example

Register Spill

- Remove f and continue the simplification
 - Simplification now succeeds: b, d, e, c





What if the Heuristic Fails?

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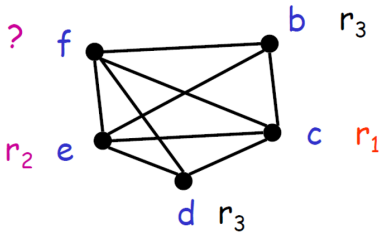
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Example

Register Spill

- On the assignment phase we get to the point when we have to assign a color to f
- We hope that among the 4 neighbors of f we use less than 3 colors \Rightarrow **optimistic coloring**



- We fail and we must spill temporary f
- We must allocate a memory location as the home of f
 - Typically this is in the current stack frame
 - Call this address fa
- Before each operation that uses f , insert
 - $f := \text{load } fa$
- After each operation that defines f , insert
 - $\text{store } f, fa$



Code with Spilling

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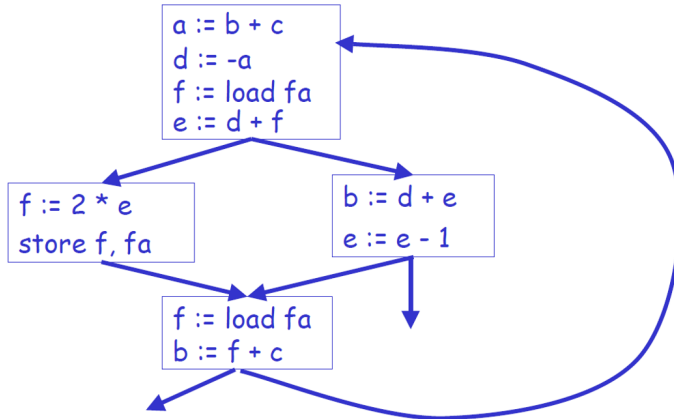
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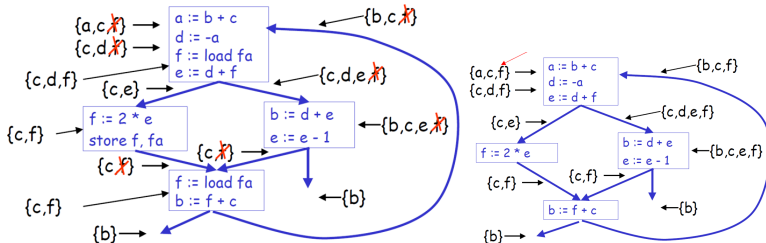
Register Spill

- The new code after spilling f



Recomputing Liveness Information

- The new liveness information after spilling





Recomputing Liveness Information

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Register Spill

- The new liveness information is almost as before
- f is live only
 - Between a $f := \text{load } fa$ and the next instruction
 - Between a $\text{store } f, fa$ and the preceding instruction
- Spilling reduces the live range of f
- And thus reduces its interferences
- Which results in fewer neighbors in RIG for f



Recompute RIG after Spilling

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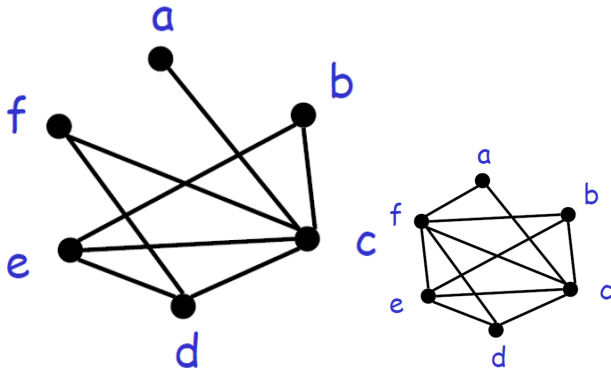
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Example

Register Spill

- The only changes are in removing some of the edges of the spilled node
- In our case f still interferes only with c and d
- And the resulting RIG is 3-colorable





Spilling

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Register Spill

- Additional spills might be required before a coloring is found
- The tricky part is deciding what to spill
- Possible heuristics:
 - Spill temporaries with most conflicts
 - Spill temporaries with few definitions and uses
 - Avoid spilling in inner loops
- Any heuristic is correct