# (a)

## i) P= SHE\_SELLS\_SEASHELLS

j	P[0j]	P[1j]	F[j]
0	S	-	0
1	SH	Н	0
2	SHE	HE	0
3	SHE_	HE_	0
4	SHE_S	HE_S	1
5	SHE_SE	HE_SE	0
6	SHE_SEL	HE_SEL	0
7	SHE_SELL	HE_SELL	0
8	SHE_SELLS	HE_SELLS	1
9	SHE_SELLS_	HE_SELLS_	0
10	SHE_SELLS_S	HE_SELLS_S	1
11	SHE_SELLS_SE	HE_SELLS_SE	0
12	SHE_SELLS_SEA	HE_SELLS_SEA	0
13	SHE_SELLS_SEAS	HE_SELLS_SEAS	1
14	SHE_SELLS_SEASH	HE_SELLS_SEASH	2
15	SHE_SELLS_SEASHE	HE_SELLS_SEASHE	3
16	SHE_SELLS_SEASHEL	HE_SELLS_SEASHEL	0
17	SHE_SELLS_SEASHELL	HE_SELLS_SEASHELL	0
18	SHE_SELLS_SEASHELL	HE_SELLS_SEASHELLS	1

### ii) P= ABRACADABRACADABRA

j	P[0j]	P[1j]	F[j]
0	А	-	0
1	АВ	В	0
2	ABR	BR	0
3	ABRA	BRA	1
4	ABRAC	BRAC	0
5	ABRACA	BRACA	1
6	ABRACAD	BRACAD	0
7	ABRACADA	BRACADA	1
8	ABRACADAB	BRACADAB	2
9	ABRACADABR	BRACADABR	3
10	ABRACADABRA	BRACADABRA	4
11	ABRACADABRAC	BRACADABRAC	5
12	ABRACADABRACA	BRACADABRACA	6
13	ABRACADABRACAD	BRACADABRACAD	7
14	ABRACADABRACADA	BRACADABRACADA	8

15	ABRACADABRACADAB	BRACADABRACADAB	9
16	ABRACADABRACADABR	BRACADABRACADABR	10
17	ABRACADABRACADABRA	BRACADABRACADABRA	11

### iii) P= ABRACADABRACAPABRA

j	P[0j]	P[1j]	F[j]
0	А	-	0
1	AB	В	0
2	ABR	BR	0
3	ABRA	BRA	1
4	ABRAC	BRAC	0
5	ABRACA	BRACA	1
6	ABRACAD	BRACAD	0
7	ABRACADA	BRACADA	1
8	ABRACADAB	BRACADAB	2
9	ABRACADABR	BRACADABR	3
10	ABRACADABRA	BRACADABRA	4
11	ABRACADABRAC	BRACADABRAC	5
12	ABRACADABRACA	BRACADABRACA	6
13	ABRACADABRACAP	BRACADABRACAP	0
14	ABRACADABRACAPA	BRACADABRACAPA	1
15	ABRACADABRACAPAB	BRACADABRACAPAB	2
16	ABRACADABRACAPABR	BRACADABRACAPABR	3
17	ABRACADABRACAPABRA	BRACADABRACAPABRA	4

### iv) P= ABRACADABRACABABRA

j	P[0j]	P[1j]	F[j]
0	A	-	0
1	AB	В	0
2	ABR	BR	0
3	ABRA	BRA	1
4	ABRAC	BRAC	0
5	ABRACA	BRACA	1
6	ABRACAD	BRACAD	0
7	ABRACADA	BRACADA	1
8	ABRACADAB	BRACADAB	2
9	ABRACADABR	BRACADABR	3
10	ABRACADABRA	BRACADABRA	4
11	ABRACADABRAC	BRACADABRAC	5
12	ABRACADABRACA	BRACADABRACA	6
13	ABRACADABRACAB	BRACADABRACAB	2

14	ABRACADABRACABA	BRACADABRACABA	1
15	ABRACADABRACABAB	BRACADABRACABAB	2
16	ABRACADABRACABABR	BRACADABRACABABR	3
17	ABRACADABRACABABRA	BRACADABRACABABRA	4

```
(b)
i)
failureArray(P):
P: String (pattern)
returns failure array
                         // F is our failure array
1. F[0] \leftarrow 0
2. i \leftarrow 1
3. j \leftarrow 0
4. while i < len(P) do
// Continue to match suffix
// Keep matching if we encounter wildcard character ?
5.
        if P[i] = P[j] or P[i] = '?' or P[j] = '?' then
6.
            j++
7.
            F[i] \leftarrow j
8.
            i++
9.
        else if j > 0 then
             j \leftarrow F[j-1]
10.
11.
         else
              F[i] \leftarrow 0
12.
13.
             i++
   14
15. return F
KMP(T, P):
T: Text
P: Pattern
returns the first match
1. F ← failureArray(P)
2. i \leftarrow 0
3. j \leftarrow 0
4. while i < len(T) do
// Keep matching if we encounter wildcard character ?
        if T[i] = P[j] or P[j] = '?' then
5.
            if j = len(P) - 1 then
6.
                 return i - j // matc
7.
            else
8.
9.
                 i++
10.
                  j++
```

j	P[0j]	P[1j]	F[j]
0	S	-	0
1	S?	}	1
2	S?E	?E	0
3	S?E_	?E_	0
4	S?E_S	?E_S	1
5	S?E_SE	?E_SE	2
6	S?E_SE?	?E_SE?	3
7	S?E_SE?L	?E_SE?L	0
8	S?E_SE?LS	?E_SE?LS	1
9	S?E_SE?LS_	?E_SE?LS_	2
10	S?E_SE?LS_S	?E_SE?LS_S	1
11	S?E_SE?LS_SE	?E_SE?LS_SE	2
12	S?E_SE?LS_SEA	?E_SE?LS_SEA	0
13	S?E_SE?LS_SEAS	?E_SE?LS_SEAS	1
14	S?E_SE?LS_SEASH	?E_SE?LS_SEASH	2
15	S?E_SE?LS_SEASHE	?E_SE?LS_SEASHE	3
16	S?E_SE?LS_SEASHEL	?E_SE?LS_SEASHEL	0
17	S?E_SE?LS_SEASHELL	?E_SE?LS_SEASHELL	0
18	S?E_SE?LS_SEASHELL	?E_SE?LS_SEASHELLS	1

#### P= ABRACADABRAC???BRA

j	P[0j]	P[1j]	F[j]
0	А	-	0
1	AB	В	0
2	ABR	BR	0
3	ABRA	BRA	1
4	ABRAC	BRAC	0
5	ABRACA	BRACA	1
6	ABRACAD	BRACAD	0
7	ABRACADA	BRACADA	1
8	ABRACADAB	BRACADAB	2

9	ABRACADABR	BRACADABR	3
10	ABRACADABRA	BRACADABRA	4
11	ABRACADABRAC	BRACADABRAC	5
12	ABRACADABRAC?	BRACADABRAC?	6
13	ABRACADABRAC??	BRACADABRAC??	7
14	ABRACADABRAC???	BRACADABRAC???	8
15	ABRACADABRAC???B	BRACADABRAC???B	9
16	ABRACADABRAC???BR	BRACADABRAC???BR	10
17	ABRACADABRAC???BRA	BRACADABRAC???BRA	11