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1 Electron Modelling

$V_{th} = 1.87 \text{ e5 m/s}$

The mean free path is $3.74 \text{ e }^{-9} \text{ nm}$

```
%properties
m0 = 9.10938215e-31;%resting mass
m = 9.10938215e-31*0.26;
q = 1.60217653e-19;
kb = 1.38064852e-23;
T = 300;
tmn = 0.2e-12; %time between collisions
%part 1
%plot parameters
x = 200e-9;
y = 100e-9;
natoms = 3000;
iteration = 10;
pc = 10; %population displayed on plot;

%thermal velocity
vth = sqrt((2*kb*T)/m); %thermal velocity
dt = y/vth/50; %time step
fprintf('The thermal velocity at 300 K is %d m/s\n',vth)

mfp = vth*tmn; %meanfree path

fprintf('The mean free path is %d nm\n',mfp)

%initialize the position and atoms
atomp = rand(natoms,2); %array for position
atomp(:,1) = atomp(:,1)*x; atomp(:,2) = atomp(:,2)*y;
atomv = vth*cos(2*pi*rand(natoms,2));
atom = [atomp atomv];
SCT = zeros(iteration,1); %semiconductor temperature
temp = zeros(iteration,1);
trajectory = zeros(iteration,pc*2);

for i = 1:iteration
    atom(:,1:2) = atom(:,1:2) + dt*atom(:,3:4);

    %use logical index to rearrange electrons hitting boundaries
    l = atom(:,1) > x;
    atom(l,1) = atom(l,1) - x;

    l = atom(:,1) < 0;
```

```

atom(1,1) = atom(1,1) + x;

l = atom(:,2) > y;
atom(1,4) = -1*atom(1,4);

l = atom(:,2) < 0;
atom(1,4) = -1*atom(1,4);

temp(i) = (sum(atom(:,3).^2) + sum(atom(:,4).^2))*m/kb/2/natoms;

for j = 1:pc
    trajectory(i, (2*j):(2*j+1)) = atom(j,1:2);

end
figure(1)
subplot(2,1,1);
%hold off

plot(atom(1:pc,1), atom(1:pc,2), 'o')
xlim([ 0 x])
ylim([0 y])

title(sprintf('Trajectories of %d electrons(Part 1)', pc));
xlabel('x')
ylabel('y')

subplot(2,1,2)
%hold off;
if i>1
plot(dt*(0:i-1), temp(1:i));
axis([0 dt*iteration min(temp)*0.98 max(temp)*1.02]);
title('Semiconductor Temperature');
xlabel('Time (s)')
ylabel('Temperature (K)')
end
%pause(0.05);
end

```

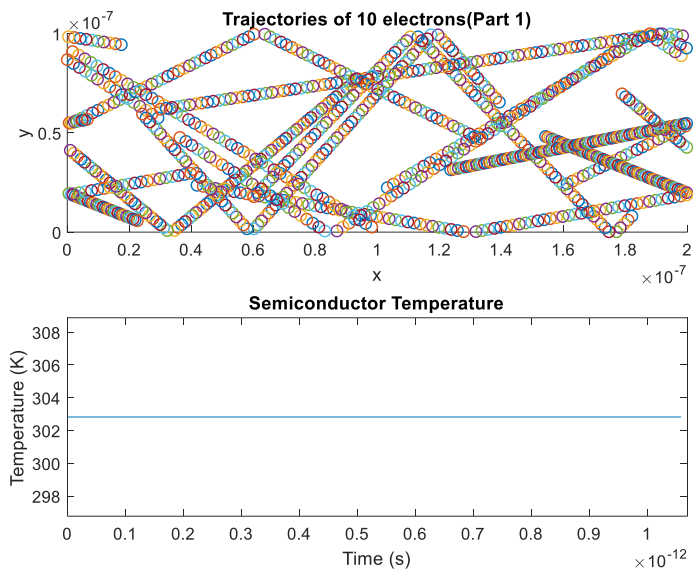


Figure 1: Trajectory of 10 electrons (100 iterations)

Part 2 Collisions with Mean Free Path

1. %Collisions with Mean Free Path

```
%velocity of maxwell distribution is gaussian so makedist() can be used
%(slide 43 of atomicandMD powerpoint
pscat = 1 - exp(-dt/tmn);
vpdf = makedist('Normal','mu',0,'sigma',sqrt((kb*T)/m)); %gaussian centered
on zero with a deviation of sqrt(kb*T/m)
```

```
atomp = rand(natoms,2); %array for position
atomp(:,1) = atomp(:,1)*x; atomp(:,2) = atomp(:,2)*y;
atomv = ones(natoms,2);
for i = 1:natoms
    atomv(i,1) = random(vpdf);
    atomv(i,2) = random(vpdf);
end
atom = [atomp atomv];
vavg = sqrt(sum(atom(:,3).^2)/natoms + sum(atom(:,4).^2)/natoms);
```

```
%Boltzmann Distrubion in histogram
vhist = sqrt(atom(:,3).^2 + atom(:,4).^2);
```

```
figure(2)
histogram(vhist)
xlabel('Speed m/s')
ylabel('Number of electrons')
fprintf('The average speed is %d m/s\n',vavg)
```

```
for i = 1 : iteration
    atom(:,1:2) = atom(:,1:2) + dt.*atom(:,3:4);

    %use logical index to rearrange electrons hitting boundaries
    l = atom(:,1) > x;
    atom(l,1) = atom(l,1) - x;

    l = atom(:,1) < 0;
    atom(l,1) = atom(l,1) + x;

    l = atom(:,2) > y;
    atom(l,4) = -1*atom(l,4);

    l = atom(:,2) < 0;
    atom(l,4) = -1*atom(l,4);

    j = pscat>rand(natoms,1);
    atom(j,3:4) = random(vpdf, [sum(j),2]);

    temp(i) = (sum(atom(:,3).^2) + sum(atom(:,4).^2))*m/kb/2/natoms;

    for j = 1:pc
        trajectory(i,(2*j):(2*j+1)) = atom(j,1:2);
    end
```

```

figure(3)
subplot(2,1,1);
%hold on;
plot(atom(1:pc,1),atom(1:pc,2),'O')

xlim([ 0 x])
ylim([0 y])

title(sprintf('Trajectories of %d electrons with scater(Part w)', pc));
xlabel('x')
ylabel('y')
subplot(2,1,2)

%hold off;
if i>1
plot(dt*(0:i-1), temp(1:i));
axis([0 dt*iteration min(temp)*0.98 max(temp)*1.02]);
title('Semiconductor Temperature');
xlabel('Time (s)')
ylabel('Temperature (K)')
end
%pause(0.05);
end

```

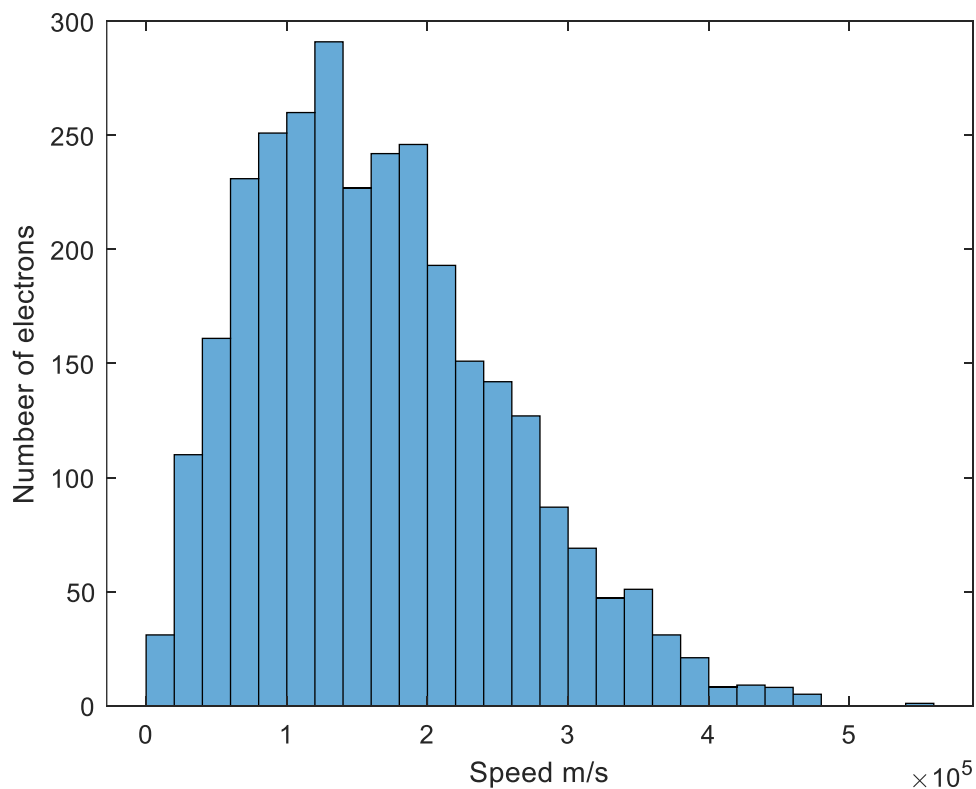


Figure 2:Histogram of the Boltzman distribution of each electron

Trajectory

1.

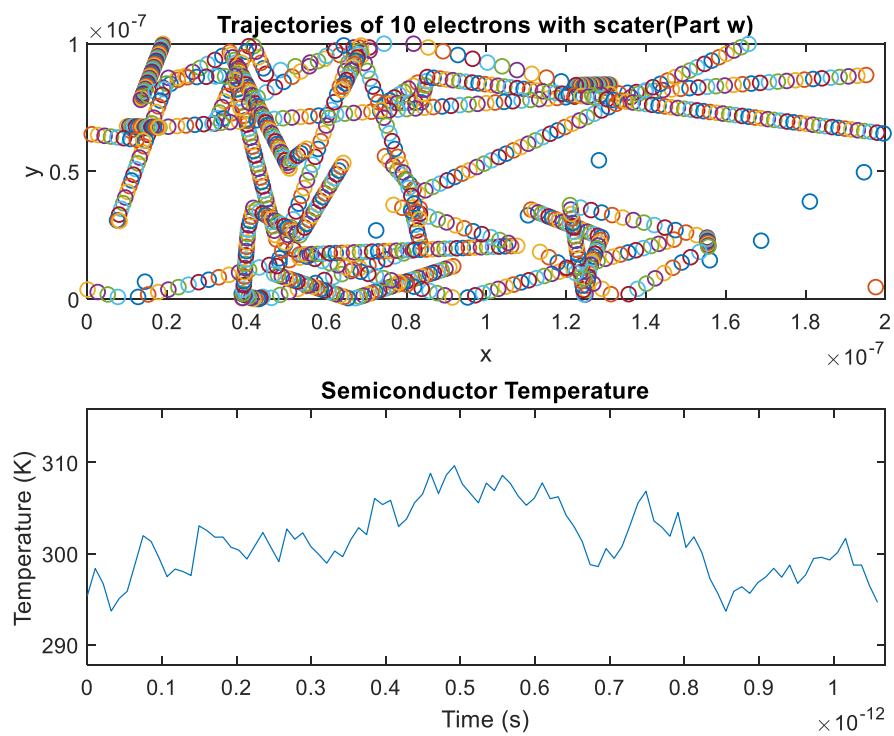


Figure 3: Trajectory with collisions

3, Average temperature raises up and down correlating to the thermal velocity, but overall it is near 300K.