

Auction-based and Distributed Optimization Approaches for Scheduling Observations in Satellite Constellations with Exclusive Orbit Portions

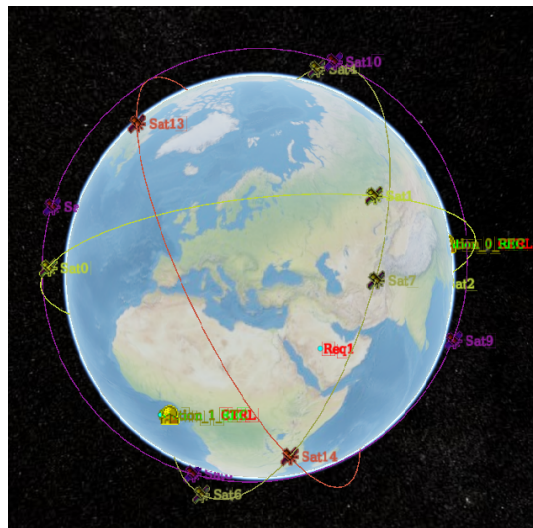
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ONERA, DTIS-SYD, Université de Toulouse

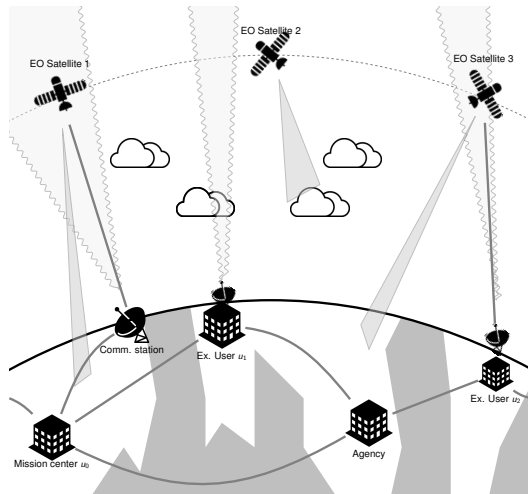
Context and Motivations

- Increasing size of deployed EOS constellations
- ⇒ Observe any point on Earth at higher frequency, e.g. Planet [SHAH et al., 2019]
- **but**, requires to **improve coordination and cooperation** between assets and stakeholders



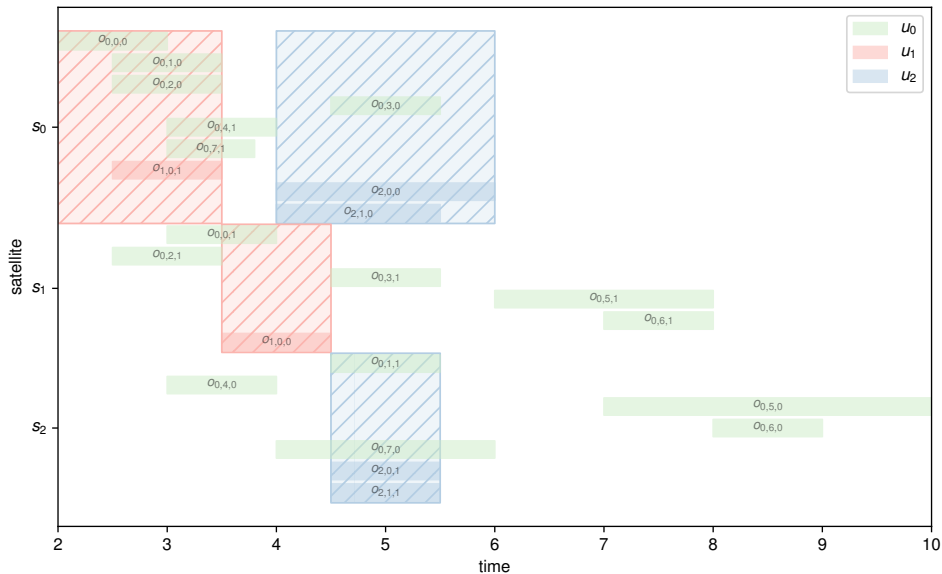
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- **but**, requires to **improve coordination and cooperation** between assets and stakeholders
- We focus here on **collective observation scheduling** on a constellation where some users have **exclusive access to some orbit portions**
- ⇒ Answer to strong user expectations to benefit both from a shared system (to reduce costs) and a proprietary system (total control and confidentiality)



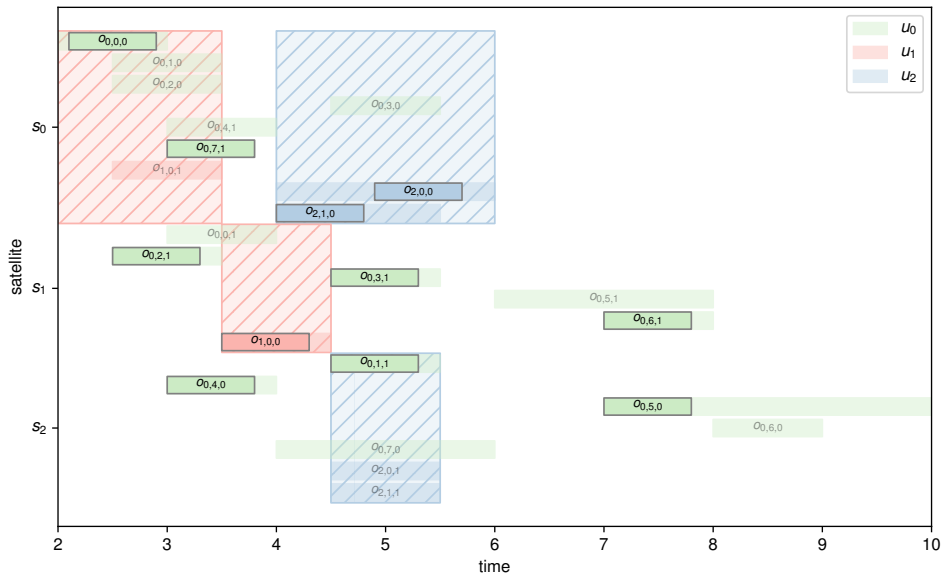
Scheduling Observations with Multiple Exclusive Orbit Portions

Illustrative Example



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Illustrative Example



Earth Observation Satellite Constellation Scheduling with Exclusives Problem is a tuple

$$P = \langle \mathcal{S}, \mathcal{U}, \mathcal{R}, \mathcal{O} \rangle$$

- $\mathcal{S} = \{s = \langle t_s^{\text{start}}, t_s^{\text{end}}, \kappa_s, \tau_s \rangle\}$ is a set of satellites
- $\mathcal{U} = \{u = \langle e_u, p_u \rangle\}$ is a set of users
- $\mathcal{R} = \{r = \langle t_r^{\text{start}}, t_r^{\text{end}}, \Delta_r, \rho_r, p_r, u_r, \theta_r \rangle\}$ is a set of requests
- $\mathcal{O} = \{o = \langle t_o^{\text{start}}, t_o^{\text{end}}, \Delta_o, r_o, \rho_o, s_o, u_o, p_o \rangle\}$ is a set of observation opportunities

A *solution* to an EOSCSP is a mapping $\mathcal{M} = \{(o, t) \mid o \in \mathcal{O}, t \in [t_o^{\text{start}}, t_o^{\text{end}}]\}$
s.t. the overall reward is maximized (sum of the rewards of the scheduled observations):
 $\arg \max_{\mathcal{M}} \sum_{(o,t) \in \mathcal{M}} \rho_o$

How to Solve EOSCSPs?

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- Centralized allocation

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$$\begin{aligned}
 & \underset{x_{s,o}}{\text{maximize}} && \sum_{o \in O, p \in P} p_o x_{s,o} && (1) \\
 & \text{s.t.} && && \\
 & && 2 - \beta_{s,o,p} - \beta_{s,p,o} \geq x_{s,o} && \forall s \in S, \forall o, p \in O, o \neq p \quad (2) \\
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 & && \beta_{s,o,p} + \beta_{s,p,o} \leq 3 - x_{s,o} - x_{s,p} && \forall s \in S, \forall o, p \in O, o \neq p \quad (4) \\
 & && \beta_{s,o,p} + \beta_{s,p,o} \leq 1 && \forall s \in S, \forall o, p \in O, o \neq p \quad (5) \\
 & && t_{s,p} - t_{s,o} \geq \tau_s(\alpha, p) + \Delta_o - \Delta_{s,o,p}^{\max} \beta_{s,o,p} && \forall s \in S, \forall o, p \in O, o \neq p, \text{s.t. } \Delta_{s,o,p}^{\max} > 0 \quad (6) \\
 & && t_{s,o} - t_{s,p} \geq \tau_s(\beta, o) + \Delta_p - \Delta_{s,p,o}^{\max} \beta_{s,p,o} && \forall s \in S, \forall o, p \in O, o \neq p, \text{s.t. } \Delta_{s,p,o}^{\max} > 0 \quad (7) \\
 & && \sum_{o \in O} x_{s,o} \leq \kappa_s && \forall s \in S \quad (8) \\
 & && \sum_{o \in R(s)} x_{s,o} \leq 1 && \forall s \in R \quad (9) \\
 & && x_{s,o} \in \{0, 1\} && \forall s \in S, \forall o \in O \quad (10) \\
 & && t_{s,o} \in [\tau_s^{\min}, \tau_s^{\max}] \subset \mathbb{R} && \forall s \in S, \forall o \in O \quad (11) \\
 & && \beta_{s,o,p} \in \{0, 1\} && \forall s \in S, \forall o, p \in O, o \neq p \quad (12) \\
 & \text{with} && \Delta_{s,o,p}^{\max} = \tau_o^{\max} - \tau_p^{\min} + \Delta_o + \tau^2(\alpha, p)
 \end{aligned}$$

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Algorithm 1: Greedy EOSCSP solver

Data: An EOSCSP $P = \langle S, \mathcal{U}, \mathcal{R}, O \rangle$

Result: An assignment \mathcal{M}

with $\mathcal{M} \leftarrow \{\}$

$O^{\text{sorted}} \leftarrow \text{sort}(O)$

$R \leftarrow \{(s, []) \mid s \in S\}$

for $o \in O^{\text{sorted}}$ **do**

$t \leftarrow \text{first.slot}(o, P, R)$

if $t \neq \emptyset$ **then**

$\mathcal{M} \leftarrow \mathcal{M} \cup \{(o, t)\}$

$O^{\text{sorted}} \leftarrow O^{\text{sorted}} \setminus \theta(r_o)$

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return  $S$ 
    
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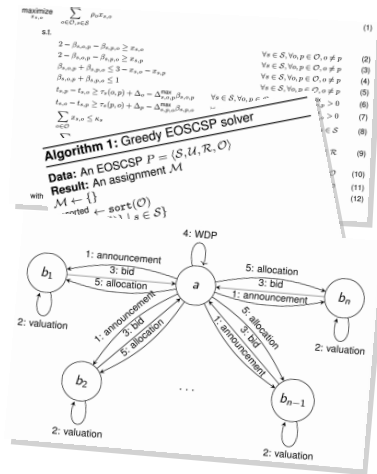
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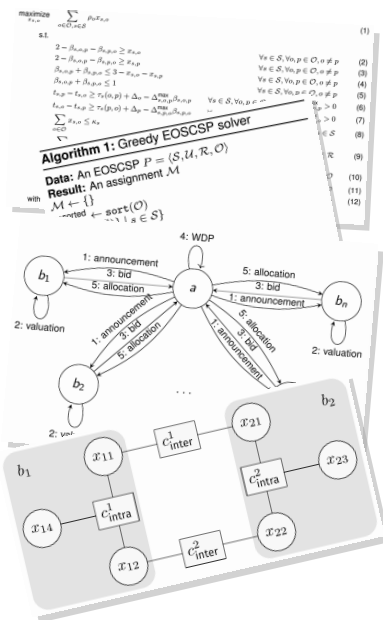
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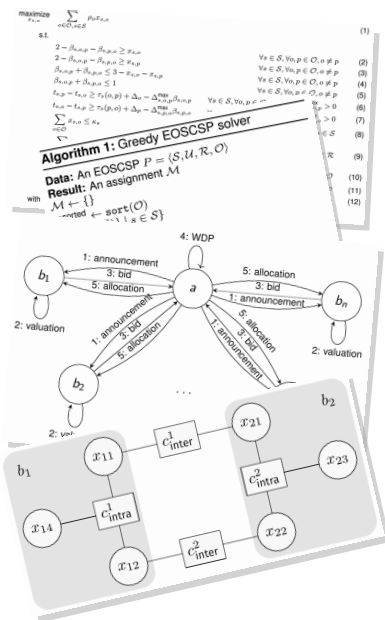
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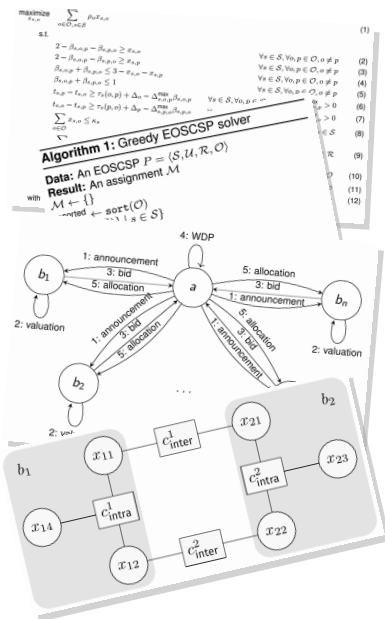
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 - ⚠ requires some coordination/communication



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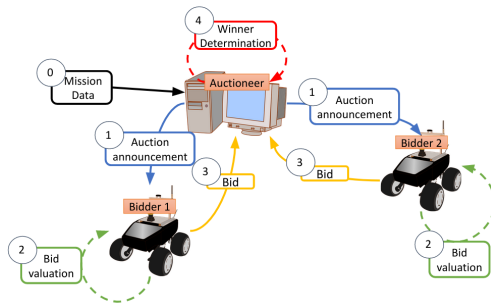
Auction-based Coordination for EOSCSP

Focus on Resource/Task Allocation

Many application fields, as Collective Robotics, make use of market-based approach to allocate tasks/resources to robots

- A set of **resources** (robots, satellites, etc.), $R = \{r_1, \dots, r_{|R|}\}$
- A set of **tasks**, $T = \{t_1, \dots, t_{|T|}\}$, each having a time-related and operation constraints
- Find an allocation of tasks to resources, wrt. some consistency constraints

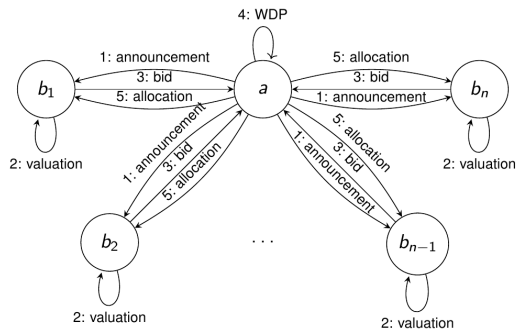
≈ **multi-item allocation**: each resource is allocated several tasks (bundle)



Auction-based Coordination for EOSCSP

Allocating non exclusive observations to best exclusive portions

Auction-based approaches are relevant for satellite task allocation [PHILLIPS and PARRA, 2021]

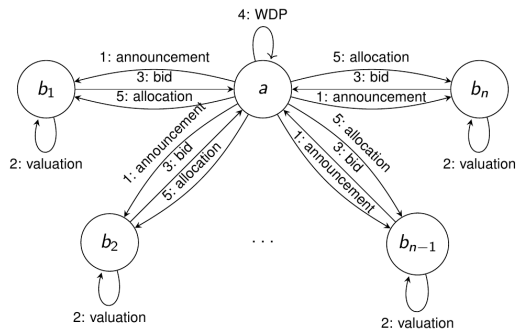


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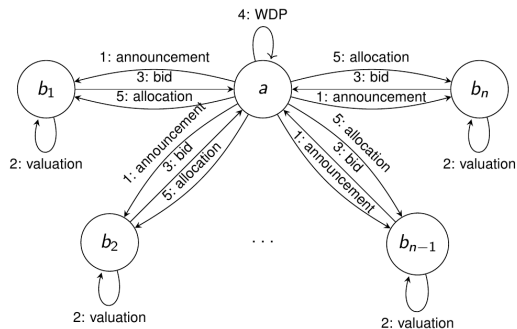
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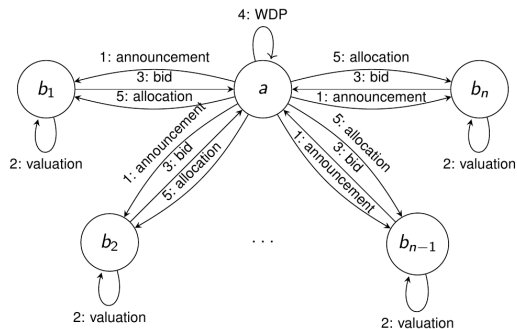


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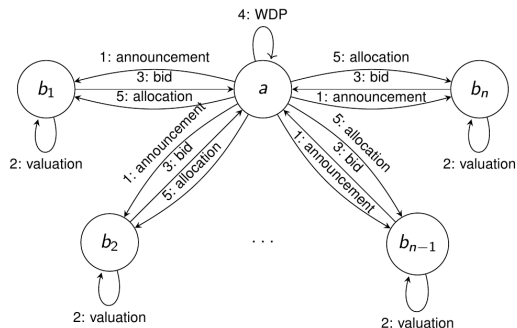


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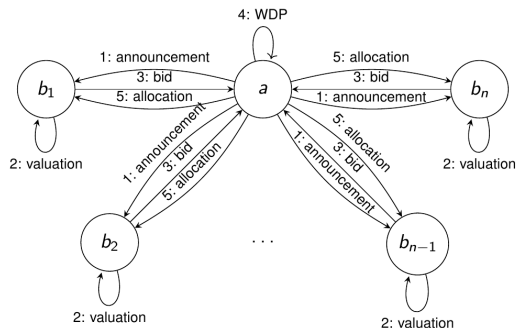


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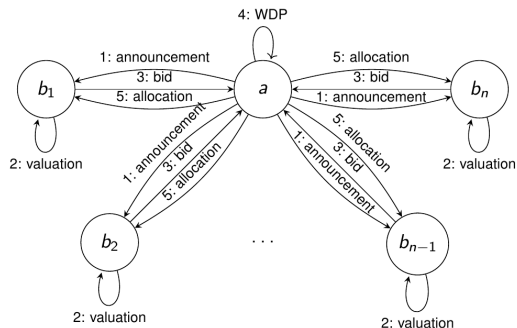


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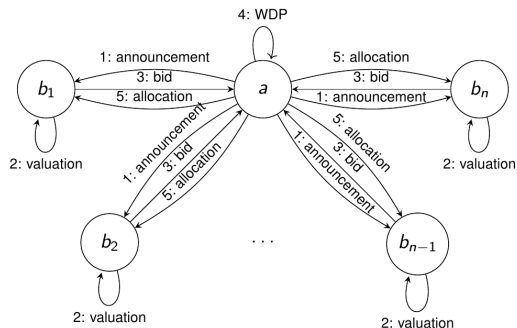


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 - Each agent bids on some *bundle of tasks* and *converge to a consensus* with other agents

General Scheme

-

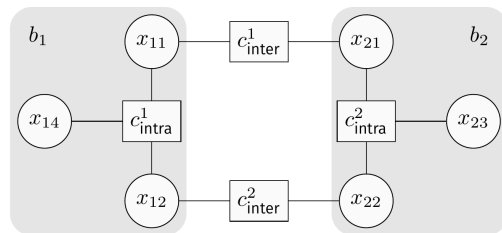
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DCOP-based Coordination for EOSCSP

Allocating non exclusive observations to best exclusive portions

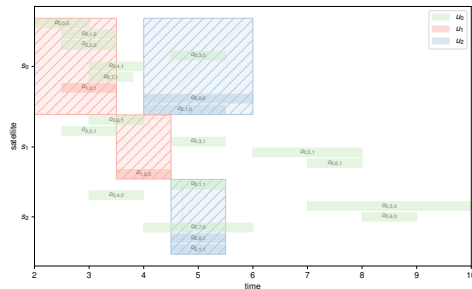
- Consider the **collective decision** for allocating non exclusive tasks to exclusive windows
- Collective decision to coordinate exclusive users' decisions modeled as a **distributed constraint optimization problem** (DCOP)
- As for auctions, exclusive users aim to **minimizing the marginal cost** of integrating non exclusive tasks in their schedule, while meeting some operational constraints



DCOP-based Coordination for EOSCSP

General Scheme

- 1 Identify non exclusive requests possibly fulfilled in exclusive windows
- 2 Send each identified request r to exclusives users, one by one
- 3 Solve the problem of r using a DCOP solution method (e.g. DPOP [PETCU and FALTINGS, 2005])
 - Costs are computed as the **best marginal cost** of integrating requests in their current plan (which amounts to solve a scheduling problem...)
- 4 Allocate as many remaining requests outside exclusive windows



DCOP-based Coordination for EOSCSP

DCOP Model

A DCOP $\langle \mathcal{A}, \mathcal{X}, \mathcal{D}, \mathcal{C}, \mu \rangle$ is defined for a given request r , and a current scheduling

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- The agents are the exclusive users which can potentially schedule r :

$$\mathcal{A} = \{u \in \mathcal{U}^{\text{ex}} | \exists (s, (t_u^{\text{start}}, t_u^{\text{end}})) \in e_u, \exists o \in \theta_r \text{ s.t. } s_o = s, [t_u^{\text{start}}, t_u^{\text{end}}] \cap [t_o^{\text{start}}, t_o^{\text{end}}] \neq \emptyset\} \quad (1)$$

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- Each agent u owns binary decision variables, one for each observation $o \in \mathcal{O}[u]^r$ and exclusive e in its exclusives e_u , stating whether it schedules o in e or not:

$$\mathcal{X} = \{x_{e,o} | e \in \bigcup_{u \in \mathcal{A}} e_u, o \in \mathcal{O}[u]^r\} \quad (2)$$

$$\mathcal{D} = \{\mathcal{D}_{x_{e,o}} = \{0, 1\} | x_{e,o} \in \mathcal{X}\} \quad (3)$$

A DCOP $\langle \mathcal{A}, \mathcal{X}, \mathcal{D}, \mathcal{C}, \mu \rangle$ is defined for a given request r , and a current scheduling

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- μ associates each variable $x_{e,o}$ to e 's owner

DCOP-based Coordination for EOSCSP (cont.)

DCOP Model

- Constraints should check that at most one observation is scheduled per request (4), that satellites are not overloaded (5), that at most one agent serves the same observation (6)

$$\sum_{e \in \bigcup_{u \in \mathcal{A}} e_u} x_{e,o} \leq 1, \quad \forall u \in \mathcal{X}, \forall o \in \mathcal{O}[u]^r \quad (4)$$

$$\sum_{o \in \{o \in \mathcal{O}[u]^r \mid u \in \mathcal{A}, s_o = s\}, e \in \bigcup_{u \in \mathcal{A}} e_u} x_{e,o} \leq \kappa_s^*, \quad \forall s \in \mathcal{S} \quad (5)$$

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DCOP-based Coordination for EOSCSP (cont.)

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- The cost to integrate an observation in the current user's schedule should be assessed to guide the optimization process

$$c(x_{e,o}) = \pi(o, \mathcal{M}_{u_o}), \quad \forall x_{e,o} \in \mathcal{X} \quad (7)$$

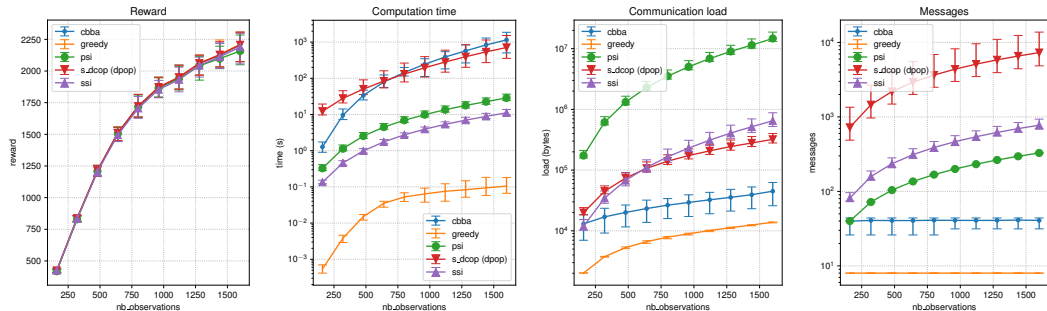
where π evaluates the best cost obtained when scheduling o and any combination of observations from \mathcal{M}_{u_o} , as to consider all possible revisions of u_o 's current schedule

$$\mathcal{C} = \{(4), (5), (6), (7)\} \quad (8)$$

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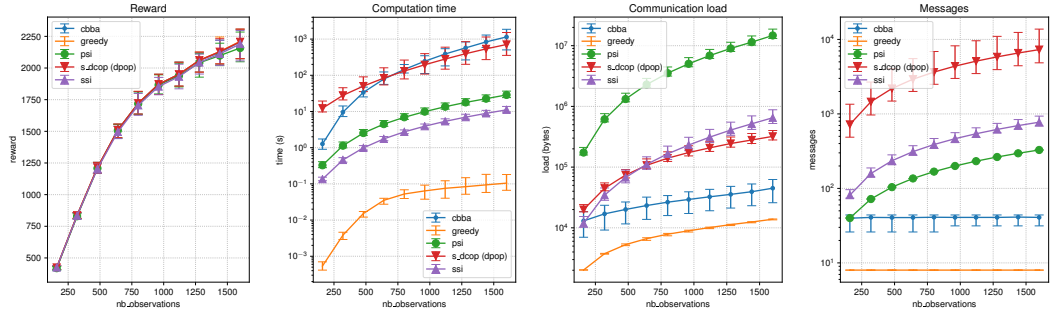
Highly conflicting randomly generated problems

5-min horizon with overlapping requests and limited capacity



Highly conflicting randomly generated problems

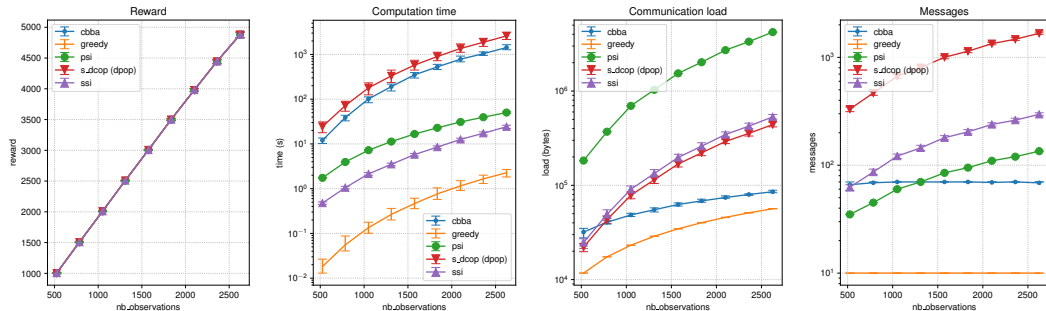
5-min horizon with overlapping requests and limited capacity



- ✗ cbba and s_dcop requires extra-computation time ($\approx 1000s$)
- ✓ cbba and s_dcop provide the best solutions wrt. reward
- ✓ cbba exchanges fewer messages of small size
- ✓ ssi remains the best compromise wrt. solution quality, computation time and communication load

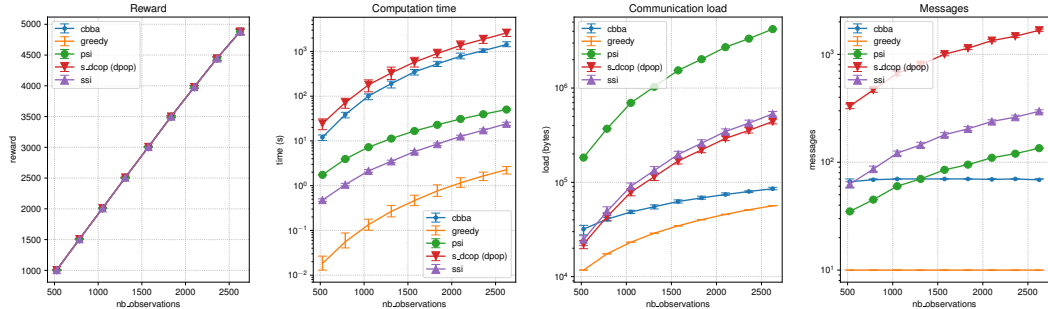
Realistic randomly generated problems

6-hour horizon with numerous requests and large capacity



Realistic randomly generated problems

6-hour horizon with numerous requests and large capacity

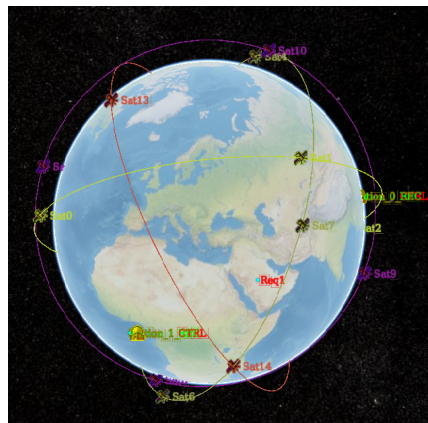


- ✓ cbba does require less time to compute than s_dcop
- ✓ s_dcop and cbba can perform many computation concurrently
- ⇒ There is room for computation speedup in real distributed settings

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Conclusions and Perspectives

- We proposed the **EOSCSP model** for allocating observation tasks in private orbit portions
 - We proposed several distributed allocation methods based on **auctions and DCOPs**
 - We evaluated the performance of these techniques on **randomly generated (but realistic) instances**
- ⇒ **SSI** is a good compromise with good performance with faster computation but slightly higher communication load
- Ideas for future developments
 - Investigate **exclusive windows allocation** (prior to EOSCSP) [MAQROT et al., 2022]
 - Approximate marginal cost instead of computing bundle marginal costs
 - Evaluate on larger realistic EOSCSP instances



Acknowledgements

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Auction-based and Distributed Optimization Approaches for Scheduling Observations in Satellite Constellations with Exclusive Orbit Portions

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ONERA, DTIS-SYD, Université de Toulouse

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