

# Engineering a Foldable Spinning Disk for a 16U CubeSat Time Dilation Experiment

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This paper outlines the design and cost analysis of a foldable 1 m carbon fiber disk for a 16U CubeSat experiment to test five-dimensional time dilation, inspired by the Randall-Sundrum model. Equipped with thorium-229m nuclear clocks, the disk spins at 1500 m/s in low Earth orbit. We detail the folding mechanism, construction specifications, hinge design, and a comprehensive cost estimate for the CubeSat and its deployable disk. The design fits within the CubeSats  $24\text{ cm} \times 24\text{ cm} \times 48\text{ cm}$  volume, using a passive spring-loaded hinge system for deployment. The total mission cost is estimated at \$1.2 million, encompassing development, fabrication, and launch.

## INTRODUCTION

To explore the five-dimensional time dilation proposed in the Randall-Sundrum model [1], we designed a 1 m carbon fiber disk that spins at 1500 m/s aboard a 16U CubeSat in low Earth orbit. The disk, with a mass of 5 kg, must fold to fit within the CubeSats  $24\text{ cm} \times 24\text{ cm} \times 48\text{ cm}$  launch volume. This paper presents the folding mechanism, construction details, hinge specifications, and a cost breakdown, ensuring the disk supports high-precision measurements with thorium-229m nuclear clocks [3? ].

## FOLDING MECHANISM

### Design Overview

The 1 m carbon fiber disk (radius 0.5 m, density  $1800\text{ kg/m}^3$ , tensile strength 7 GPa) is divided into six wedge-shaped panels to

fit within the CubeSats constrained volume. Each panel, roughly 0.5 m long and 0.26 m wide at its outer edge, folds along radial hinges into a compact stack, occupying approximately  $24\text{ cm} \times 24\text{ cm} \times 10\text{ cm}$ . This leaves ample space for the clocks, solar panels, and other subsystems.

### Deployment Sequence

The disk deploys passively to conserve power and enhance reliability:

- Release:** A burnwire, activated by a low-power signal, cuts a Dyneema cable holding the folded disk, a proven method in CubeSat missions [4].
- Unfolding:** Spring-loaded hinges drive the panels to unfold radially into a flat disk. Viscoelastic dampers control the motion, preventing vibrations

that could disrupt the thorium-229m clocks  $1 \times 10^{-19}$  s precision [? ].

3. **Locking:** Latches at the hinge interfaces engage to secure the panels, ensuring the disk withstands centrifugal stresses (3.6 GPa at the edge, calculated as  $\sigma = \rho\omega^2r^2$ , with  $\omega = 3000$  rad/s).

## CONSTRUCTION DETAILS

### Disk Material

The disk is made from carbon fiber composite (density  $1800 \text{ kg/m}^3$ , tensile strength 7 GPa), arranged in a quasi-isotropic layup to endure centrifugal stresses of 3.6 GPa, computed as:

$$\sigma = \rho\omega^2r^2, \quad (1)$$

where  $\rho = 1800 \text{ kg/m}^3$ ,  $\omega = 3000 \text{ rad/s}$ , and  $r = 0.5 \text{ m}$ . A 5 mm thickness balances the 5 kg mass with structural robustness.

### Clock Integration

Three thorium-229m nuclear clocks (total mass 3 kg) are positioned at radii of 0.2 m, 0.3 m, and 0.4 m. Each is encased in a diamond chamber (2.8 GPa strength) to endure centrifugal accelerations up to  $9 \times 10^6 g$  [3]. Vibration-damping mounts reduce noise to  $7 \times 10^{-19}$  s.

### Supporting Systems

The 16U CubeSat ( $24 \text{ cm} \times 24 \text{ cm} \times 48 \text{ cm}$ ) includes:

- **Power:** 200 W solar panels with battery backup for uninterrupted operation.
- **Thermal Control:** Passive cooling ensures 1 K stability for the clocks.
- **Communication:** X-band transceivers handle data transfer to ground stations.

## HINGE SPECIFICATIONS

### Hinge Design

Each disk segment connects to its neighbors via two titanium alloy (Ti-6Al-4V, yield strength 880 MPa) spring-loaded hinges. Key features include:

- **Torque:** 10 N m per hinge, driven by torsion springs, to overcome friction during deployment.
- **Damping:** Viscoelastic dampers slow deployment to 0.5 s per panel, minimizing oscillations.
- **Locking Mechanism:** Pin-and-socket latches, with 500 MPa shear strength, secure the deployed disk against centrifugal forces.

### Hinge Placement

Hinges are located at radial interfaces (e.g., 60°, 120°, etc.), embedded within the carbon fiber to reduce mass and maintain a smooth surface.

## COST PLAN

### Cost Breakdown

Table I outlines the estimated \$1.2 million cost for the CubeSat mission, based on industry benchmarks for small satellite projects [5].

Table I: Cost breakdown for the 16U CubeSat mission.

| Component                                         | Cost (USD) |
|---------------------------------------------------|------------|
| Carbon fiber disk (materials and fabrication)     | 50,000     |
| Thorium-229m clocks (development and integration) | 300,000    |
| Hinges and deployment mechanism                   | 20,000     |
| CubeSat structure and subsystems                  | 150,000    |
| Solar panels and power systems                    | 50,000     |
| Thermal and shielding systems                     | 30,000     |
| Testing and calibration                           | 100,000    |
| Launch (shared rideshare to LEO)                  | 400,000    |
| Mission operations and data analysis              | 100,000    |
| Total                                             | 1,200,000  |

### Cost Justification

- **Disk and Hinges:** Costs reflect aerospace-grade carbon fiber and

precision-machined titanium hinges for small-batch production.

- **Clocks:** Prototype thorium-229m clocks and their diamond chambers drive costs due to cutting-edge technology [3].
- **CubeSat Systems:** Standard 16U components (structure, power, communication) use commercial off-the-shelf pricing.
- **Launch:** A shared rideshare to LEO costs \$25,000 per U, totaling \$400,000 for 16U [5].
- **Testing and Operations:** Costs cover ground testing, calibration, and mission support staff. Sony, and piezoelectric isolation for vibration control. The \$1.2 million budget aligns with the scope of compact, high-precision CubeSat missions. Key challenges maintaining clock stability under extreme centrifugal forces and minimizing deployment vibrations are addressed through robust diamond chambers and advanced vibration isolation.

## CONCLUSION

This design for a foldable 1 m carbon fiber disk, integrated into a 16U CubeSat, enables a groundbreaking test of five-dimensional time dilation. The six-segment disk, deployed via

titanium spring-loaded hinges, meets all structural and operational needs. The \$1.2 million cost plan covers development, fabrication, and launch, making this mission a feasible step toward validating the Randall-Sundrum model

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- [1] G. Einarsson, *Five-Dimensional Time Dilation on a Spinning Disk* (2025), available at <https://github.com/GautiEinarsson/DilatationSim>.
- [2] A. D. Ludlow et al., *Rev. Mod. Phys.* **87**, 637 (2015).
- [3] E. Peik et al., *Quantum Sci. Technol.* **1**, 015001 (2015).
- [4] CubeSat Design Specification, Rev. 14, California Polytechnic State University (2020).
- [5] J. Bouwmeester and J. Guo, *Acta Astronautica* **66**, 1593 (2010).