

# Cross-Sectional Household Heterogeneity in Responses to Macroeconomic Shocks

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## **Abstract**

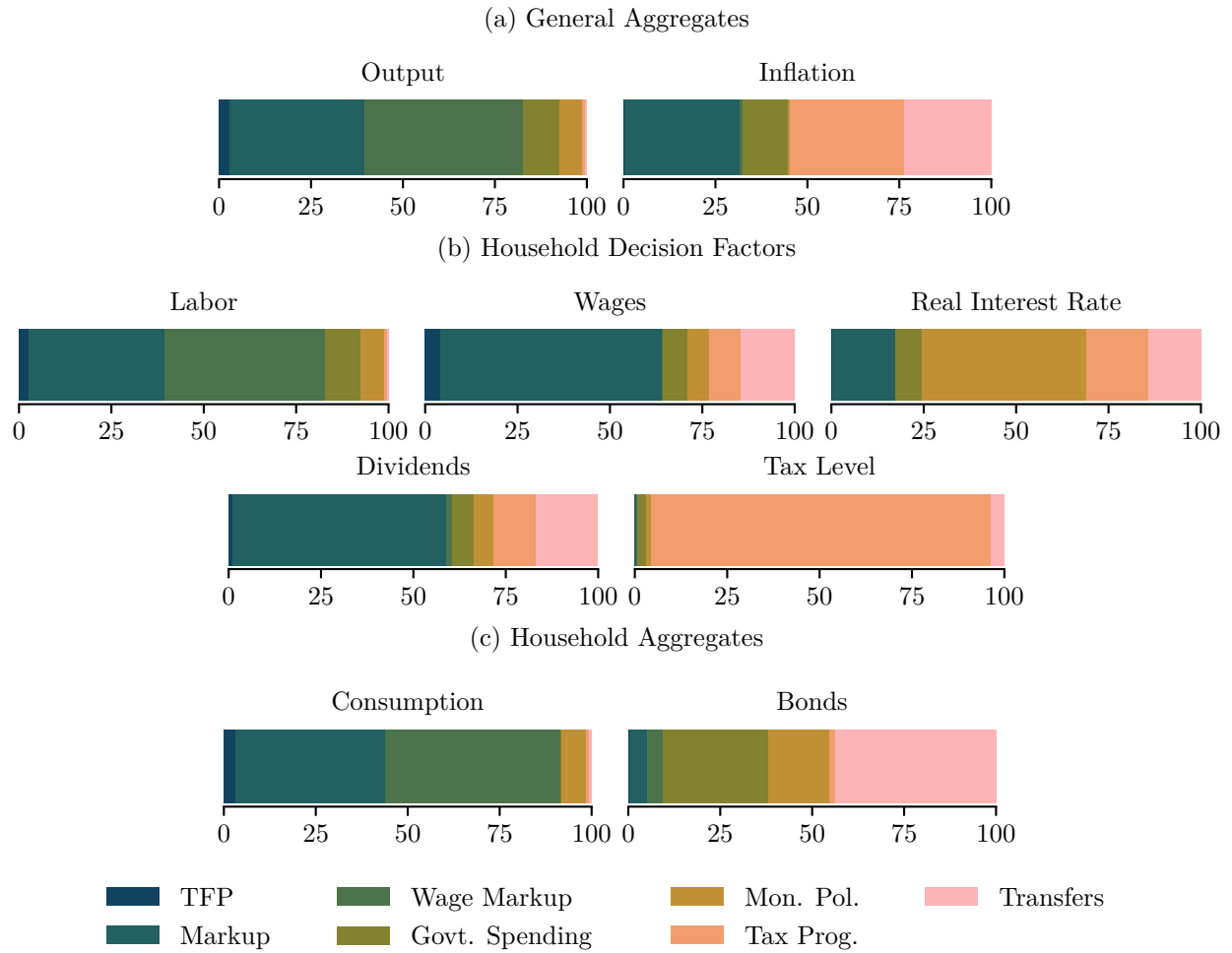
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\*Replication code available at <https://github.com/GavinEngelstad/HANK-Honors>.

Table 3.1: Computational Parameters

Parameter	Value	Description
$n_b$	501	Number of asset gridpoints
$\underline{b}$	0	Borrowing constraint
$\bar{b}$	50	Maximum asset gridpoint
$n_z$	7	Number of productivity gridpoints
$T$	300	Sequence space perturbation time horizon

Figure 5.1: Variance Decomposition: Aggregates



*Notes:* Forecast error variance decomposition calculated at a 4 quarter time horizon.

## 1 Introduction

## 2 Literature Review

## 3 Model

### 3.1 Households

### 3.2 Unions

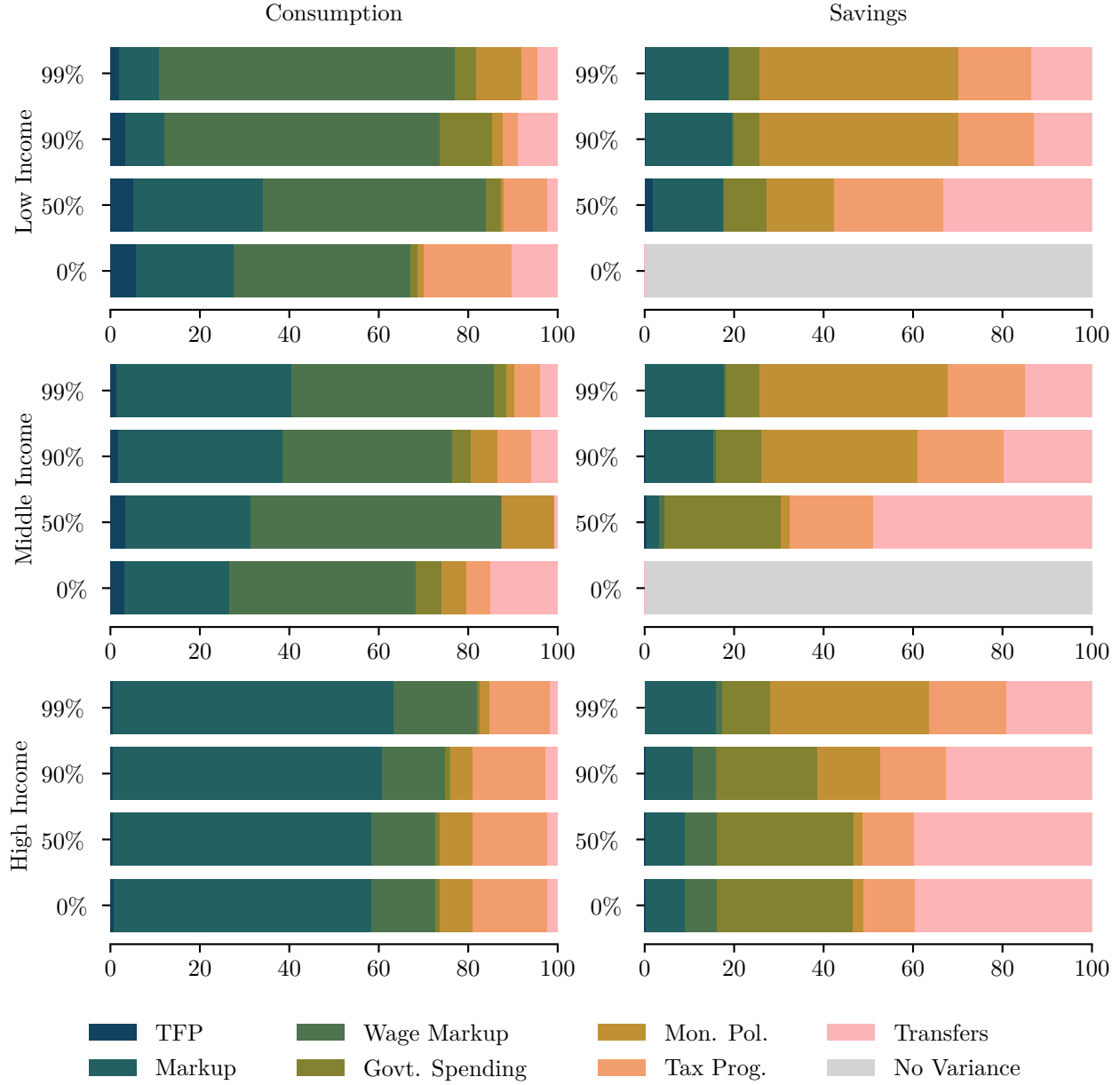
### 3.3 Firms

### 3.4 Government

### 3.5 Equilibrium

### 3.6 Computational Methods

Figure 5.2: Variance Decomposition: Household Decision Rules

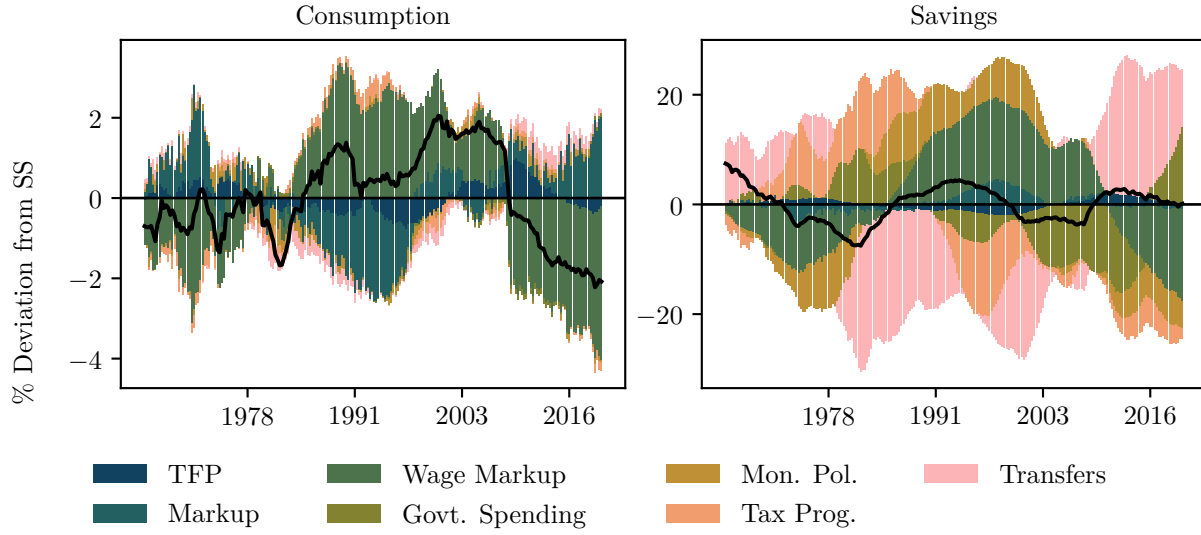


Notes: Forecast error variance decomposition calculated at a 4 quarter time horizon. Subplot y-axis is the household position on the wealth distribution.

## References

Auclert, Adrien, Matthew Rognlie, and Ludwig Straub. 2024. “The intertemporal keynesian cross.” *Journal of Political Economy* 132 (12): 4068–4121.

Figure 7.1: Historical Decomposition: Household Aggregates



Chetty, Raj. 2012. “Bounds on elasticities with optimization frictions: A synthesis of micro and macro evidence on labor supply.” *Econometrica* 80 (3): 969–1018.

Heathcote, Jonathan, Kjetil Storesletten, and Giovanni L Violante. 2017. “Optimal tax progressivity: An analytical framework.” *The Quarterly Journal of Economics* 132 (4): 1693–1754.

Kaplan, Greg, Benjamin Moll, and Giovanni L Violante. 2018. “Monetary policy according to HANK.” *American Economic Review* 108 (3): 697–743.

Storesletten, Kjetil, Chris I Telmer, and Amir Yaron. 2004. “Cyclical dynamics in idiosyncratic labor market risk.” *Journal of political Economy* 112 (3): 695–717.

Table 4.1: Model Parameters

Parameter	Value	Description	Target
<i>Preferences</i>			
$\beta$	0.945	Discount rate	2% annual interest rate
$\gamma$	4	Risk aversion	Kaplan, Moll, and Violante (2018)
$1/\chi$	1/2	Frisch elasticity	Chetty (2012)
$\phi$	3.16	Disutility of labor	$\bar{N} = 1$
$\underline{b}$	0	Borrowing constraint	
<i>Productivity</i>			
$\rho_z$	0.963	Productivity persistence	Storesletten, Telmer, and Yaron (2004)
$\sigma_z$	0.134	Productivity STD	Cross-sectional STD of 0.5
<i>Unions</i>			
$\kappa_W$	0.1	Wage Philips Curve	
<i>Firms</i>			
$\kappa$	0.1	Philips Curve	
<i>Government</i>			
$\rho_B$	0.93	Debt persistence	Auclert, Rognlie, and Straub (2024)
$\bar{B}$	0.577	Govt. debt target	57.7% debt to GDP steady state
$\omega_\pi$	1.5	Taylor inflation	
$\omega_Y$	0	Taylor output	
$\bar{\pi}$	1	Inflation target	0% inflation steady state
<i>Shock SS</i>			
$\bar{A}$	1	TFP	
$\bar{\psi}$	1.2	Markup	20% markup
$\bar{\psi}_W$	1.2	Wage markup	20% markup
$\bar{g}$	0.202	Govt. spending	20.1% govt. spending
$\bar{\eta}$	0.081	Transfers	8.1% transfers
$\bar{\tau}^P$	1.18	Tax progressivity	Heathcote, Storesletten, and Violante (2017)
$\bar{\xi}$	1	Monetary shock	

Table 4.2: Estimation Results

Parameter		Prior			Posterior			
Shock	Statistic	Distribution	Mean	Std. Dev.	Mode	Mean	5%	95%
TFP	$\rho$	Beta	0.50	0.15	0.952	0.952	0.934	0.969
	$\sigma$	Inv. Gamma	0.20	2.00	0.152	0.154	0.142	0.166
Markup	$\rho$	Beta	0.50	0.15	0.987	0.983	0.970	0.991
	$\sigma$	Inv. Gamma	0.20	2.00	0.549	0.558	0.511	0.611
Wage Markup	$\rho$	Beta	0.50	0.15	0.997	0.997	0.996	0.997
	$\sigma$	Inv. Gamma	0.20	2.00	1.761	1.765	1.621	1.921
Govt. Spend	$\rho$	Beta	0.50	0.15	0.850	0.856	0.807	0.906
	$\sigma$	Inv. Gamma	0.20	2.00	0.648	0.856	0.807	0.906
Mon. Pol.	$\rho$	Beta	0.50	0.15	0.634	0.627	0.574	0.678
	$\sigma$	Inv. Gamma	0.20	2.00	0.440	0.444	0.409	0.481
Tax Prog.	$\rho$	Beta	0.50	0.15	0.914	0.905	0.874	0.934
	$\sigma$	Inv. Gamma	0.20	2.00	1.707	1.852	1.512	2.242
Transfers	$\rho$	Beta	0.50	0.15	0.834	0.851	0.791	0.918
	$\sigma$	Inv. Gamma	0.20	2.00	2.460	2.409	2.050	2.784

Table 5.1: Household Steady State Behavior

	Low Income (10%)				Middle Income (50%)				High Income (90%)			
	0%	50%	90%	99%	0%	50%	90%	99%	0%	50%	90%	99%
<i>States</i>												
Productivity	0.444	0.444	0.444	0.444	1.000	1.000	1.000	1.000	2.252	2.252	2.252	2.252
Assets	0.000	0.040	1.874	5.896	0.000	0.040	1.874	5.896	0.000	0.040	1.874	5.896
<i>Decisions</i>												
Consumption	0.483	0.507	0.696	0.896	0.744	0.754	0.898	1.079	1.109	1.111	1.200	1.352
Savings	0.000	0.016	1.670	5.512	0.000	0.030	1.730	5.591	0.173	0.211	1.965	5.855
<i>Income</i>												
Wages	0.327 (67.79)	0.327 (62.60)	0.327 (13.83)	0.327 (5.11)	0.737 (99.00)	0.737 (93.95)	0.737 (28.05)	0.737 (11.05)	1.660 (129.54)	1.660 (125.62)	1.660 (52.45)	1.660 (23.03)
Interest	0.000 (0.00)	0.040 (7.66)	1.883 (79.60)	5.926 (92.47)	0.000 (0.00)	0.040 (5.10)	1.883 (71.67)	5.926 (88.83)	0.000 (0.00)	0.040 (3.03)	1.883 (59.51)	5.926 (82.22)
Transfers	0.248 (51.30)	0.248 (47.37)	0.248 (10.47)	0.248 (3.86)	0.248 (33.27)	0.248 (31.57)	0.248 (9.42)	0.248 (3.71)	0.248 (19.33)	0.248 (18.74)	0.248 (7.83)	0.248 (3.44)
Taxes	-0.092 (19.09)	-0.092 (17.63)	-0.092 (3.89)	-0.092 (1.44)	-0.240 (32.27)	-0.240 (30.62)	-0.240 (9.14)	-0.240 (3.60)	-0.626 (48.86)	-0.626 (47.38)	-0.626 (19.79)	-0.626 (8.69)
Total	0.483 (100.00)	0.523 (100.00)	2.366 (100.00)	6.408 (100.00)	0.744 (100.00)	0.785 (100.00)	2.628 (100.00)	6.670 (100.00)	1.282 (100.00)	1.326 (100.00)	3.165 (100.00)	7.207 (100.00)

Notes: Income share in parenthesis. Column percentiles correspond to the 0th, 50th, 90th, and 99th wealth percentiles.

Table 6.1: Direct Effects Decomposition: Consumption

	Total	Low Income				Middle Income				High Income			
		0th	50th	90th	99th	0th	50th	90th	99th	0th	50th	90th	99th
<i>Variance Components</i>													
Var( $L$ )	0.57 (70.8)	0.14 (130.0)	0.13 (1,048.1)	0.14 (66.8)	0.17 (135.2)	0.71 (912.6)	0.52 (77.4)	0.43 (24.8)	0.45 (39.2)	1.25 (13.5)	1.24 (13.4)	1.15 (13.8)	1.12 (19.6)
Var( $W$ )	0.00 (0.0)	0.00 (2.6)	0.00 (22.8)	0.00 (1.7)	0.02 (12.4)	0.01 (18.2)	0.00 (0.7)	0.01 (0.8)	0.03 (3.1)	0.02 (0.3)	0.02 (0.3)	0.05 (0.6)	0.07 (1.3)
Var( $R$ )	0.25 (31.6)	0.00 (0.0)	0.02 (150.7)	0.20 (94.3)	0.10 (78.6)	0.00 (0.0)	0.24 (36.2)	0.75 (43.0)	0.35 (30.5)	2.62 (28.3)	2.63 (28.4)	2.30 (27.6)	1.13 (19.7)
Var( $T$ )	0.09 (11.3)	0.08 (77.6)	0.06 (460.0)	0.09 (41.9)	0.13 (98.2)	0.08 (107.3)	0.06 (8.2)	0.11 (6.3)	0.14 (12.2)	0.12 (1.3)	0.12 (1.3)	0.15 (1.7)	0.15 (2.7)
Var( $\tau$ )	0.00 (0.6)	0.13 (120.7)	0.10 (769.9)	0.01 (6.0)	0.00 (2.7)	0.04 (54.7)	0.01 (1.7)	0.00 (0.1)	0.00 (0.3)	0.26 (2.9)	0.26 (2.8)	0.22 (2.7)	0.19 (3.2)
<i>Covariance Components</i>													
Cov( $L, W$ )	0.00 (0.1)	-0.02 (-17.5)	-0.02 (-153.8)	0.02 (10.2)	0.05 (40.8)	-0.10 (-123.0)	-0.05 (-6.8)	0.08 (4.3)	0.12 (10.9)	0.17 (1.8)	0.17 (1.9)	0.24 (2.8)	0.29 (5.0)
Cov( $L, R$ )	0.36 (44.9)	0.00 (0.0)	0.05 (382.5)	0.15 (71.5)	0.03 (25.1)	0.00 (0.0)	0.35 (52.3)	0.55 (31.6)	0.33 (28.8)	1.80 (19.4)	1.80 (19.4)	1.61 (19.2)	1.06 (18.6)
Cov( $L, T$ )	-0.23 (-28.2)	-0.11 (-98.3)	-0.08 (-686.4)	-0.11 (-52.9)	-0.15 (-115.2)	-0.24 (-306.4)	-0.17 (-25.2)	-0.22 (-12.5)	-0.25 (-21.9)	-0.39 (-4.2)	-0.39 (-4.2)	-0.41 (-4.9)	-0.42 (-7.3)
Cov( $L, \tau$ )	-0.03 (-3.8)	-0.13 (-124.5)	-0.11 (-890.2)	-0.04 (-19.5)	-0.02 (-18.4)	-0.16 (-204.8)	-0.07 (-9.7)	0.02 (1.1)	0.03 (3.0)	0.57 (6.2)	0.57 (6.2)	0.51 (6.0)	0.46 (8.0)
Cov( $W, R$ )	0.00 (0.1)	0.00 (0.0)	-0.01 (-55.1)	0.02 (9.9)	0.01 (5.8)	0.00 (0.0)	-0.03 (-4.8)	0.09 (5.3)	0.09 (7.6)	0.24 (2.5)	0.24 (2.6)	0.32 (3.9)	0.26 (4.6)
Cov( $W, T$ )	-0.00 (-0.1)	0.01 (12.4)	0.01 (99.9)	-0.02 (-8.1)	-0.04 (-34.8)	0.03 (38.7)	0.02 (2.2)	-0.04 (-2.2)	-0.07 (-6.1)	-0.05 (-0.6)	-0.05 (-0.6)	-0.08 (-1.0)	-0.11 (-1.9)
Cov( $W, \tau$ )	-0.00 (-0.0)	0.02 (16.3)	0.02 (130.2)	-0.01 (-2.8)	-0.01 (-5.4)	0.02 (24.1)	0.01 (1.0)	0.00 (0.2)	0.01 (0.9)	0.08 (0.8)	0.08 (0.9)	0.10 (1.2)	0.12 (2.0)
Cov( $R, T$ )	-0.15 (-18.4)	0.00 (0.0)	-0.03 (-261.1)	-0.12 (-56.2)	-0.03 (-20.9)	0.00 (0.0)	-0.11 (-17.2)	-0.28 (-15.9)	-0.18 (-16.0)	-0.56 (-6.1)	-0.56 (-6.1)	-0.57 (-6.8)	-0.39 (-6.9)
Cov( $R, \tau$ )	-0.03 (-3.5)	0.00 (0.0)	-0.04 (-336.2)	-0.05 (-22.7)	-0.01 (-6.2)	0.00 (0.0)	-0.05 (-7.2)	0.02 (1.1)	0.02 (1.9)	0.82 (8.9)	0.82 (8.9)	0.70 (8.4)	0.43 (7.6)
Cov( $T, \tau$ )	0.01 (1.7)	0.10 (96.2)	0.07 (594.4)	0.03 (15.3)	0.02 (15.7)	0.06 (74.9)	0.02 (3.3)	-0.01 (-0.6)	-0.02 (-1.7)	-0.18 (-1.9)	-0.18 (-1.9)	-0.18 (-2.1)	-0.17 (-3.0)
<i>Total</i>													
Var( $c$ )	0.80 (100.0)	0.11 (100.0)	0.01 (100.0)	0.21 (100.0)	0.13 (100.0)	0.08 (100.0)	0.67 (100.0)	1.74 (100.0)	1.14 (100.0)	9.27 (100.0)	9.27 (100.0)	8.35 (100.0)	5.72 (100.0)

*Notes:* Forecast error variance decomposition calculated at a 4 quarter time horizon. Variance percent share in parenthesis. Column percentiles correspond to the 0th, 50th, 90th, and 99th wealth percentiles.

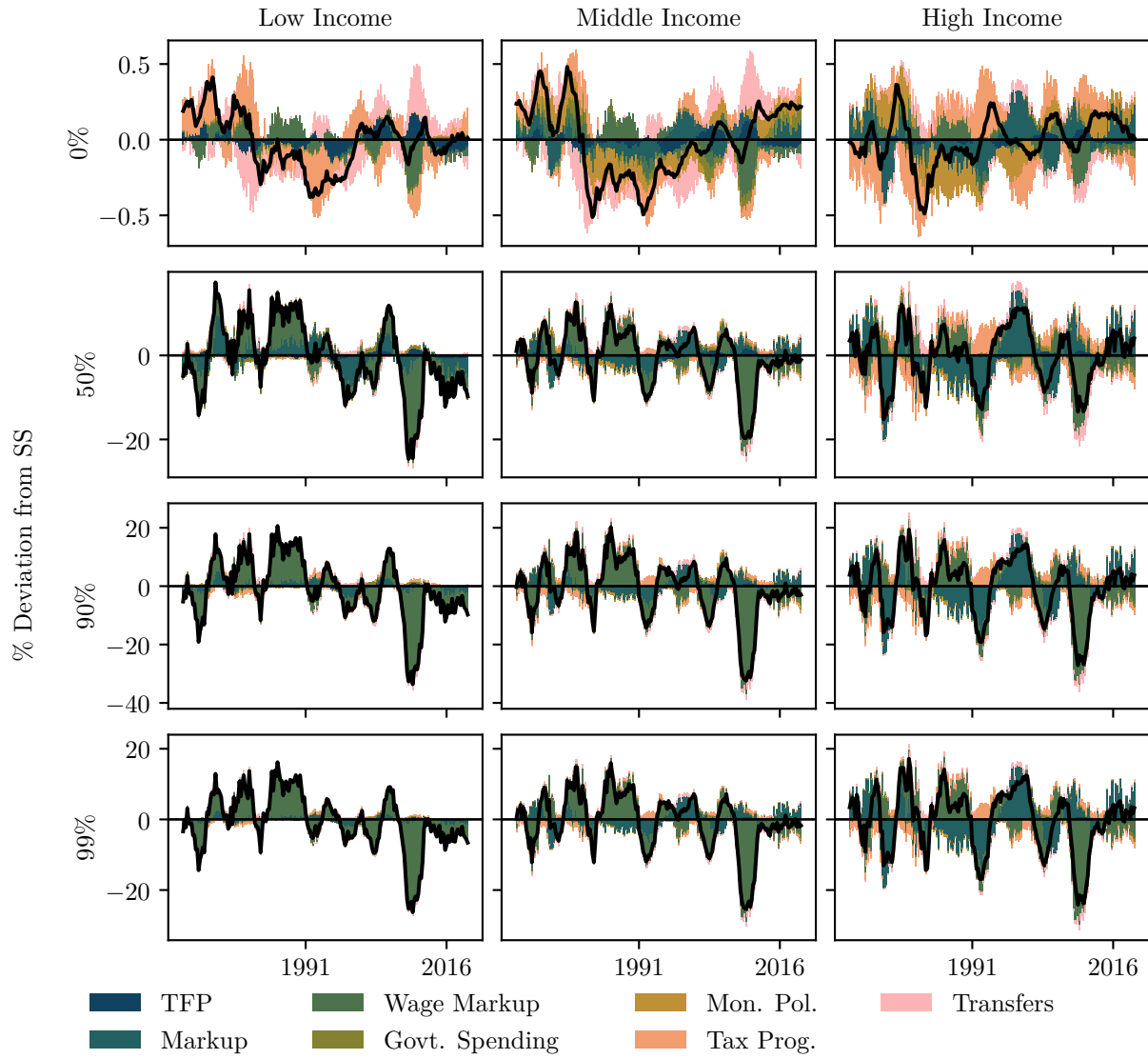


Table 6.2: Direct Effects Decomposition: Savings

	<b>Total</b>	<b>Low Income</b>				<b>Middle Income</b>				<b>High Income</b>			
		0th	50th	90th	99th	0th	50th	90th	99th	0th	50th	90th	99th
<i>Variance Components</i>													
Var( $L$ )	0.34 (12.2)	0.00 (0.0)	0.00 (0.4)	0.00 (0.0)	0.00 (0.0)	0.00 (0.0)	0.02 (4.6)	0.04 (0.4)	0.03 (0.0)	0.61 (837.3)	0.61 (772.3)	0.68 (10.8)	0.71 (1.2)
Var( $W$ )	0.12 (4.4)	0.00 (0.0)	0.00 (0.3)	0.01 (0.2)	0.03 (0.0)	0.00 (0.0)	0.00 (1.3)	0.06 (0.6)	0.09 (0.1)	0.18 (243.5)	0.18 (226.6)	0.24 (3.8)	0.29 (0.5)
Var( $R$ )	5.05 (182.6)	0.00 (0.0)	0.02 (43.7)	7.16 (87.9)	64.35 (95.8)	0.00 (0.0)	0.26 (76.9)	8.69 (92.0)	67.51 (97.3)	2.62 (3,599.0)	2.70 (3,398.3)	11.72 (185.9)	71.98 (118.0)
Var( $T$ )	0.00 (0.1)	0.00 (0.0)	0.00 (5.2)	0.01 (0.1)	0.01 (0.0)	0.00 (0.0)	0.01 (1.6)	0.01 (0.1)	0.02 (0.0)	0.01 (16.5)	0.01 (15.4)	0.02 (0.3)	0.02 (0.0)
Var( $\tau$ )	0.12 (4.4)	0.00 (0.0)	0.00 (4.6)	0.06 (0.8)	0.09 (0.1)	0.00 (0.0)	0.01 (2.9)	0.05 (0.5)	0.06 (0.1)	0.89 (1,215.6)	0.89 (1,118.6)	0.97 (15.4)	1.05 (1.7)
<i>Covariance Components</i>													
Cov( $L, W$ )	-0.20 (-7.2)	0.00 (0.0)	0.00 (0.2)	0.00 (0.0)	0.01 (0.0)	0.00 (0.0)	-0.00 (-1.3)	-0.04 (-0.4)	-0.05 (-0.1)	-0.31 (-419.6)	-0.31 (-389.0)	-0.38 (-6.0)	-0.43 (-0.7)
Cov( $L, R$ )	-1.24 (-45.0)	0.00 (0.0)	-0.00 (-3.5)	0.05 (0.6)	0.32 (0.5)	0.00 (0.0)	-0.06 (-18.3)	-0.28 (-3.0)	-0.41 (-0.6)	-1.26 (-1,735.0)	-1.29 (-1,616.9)	-2.00 (-31.7)	-3.28 (-5.4)
Cov( $L, T$ )	0.01 (0.5)	0.00 (0.0)	-0.00 (-1.5)	-0.00 (-0.0)	-0.01 (-0.0)	0.00 (0.0)	-0.01 (-2.2)	0.01 (0.1)	0.01 (0.0)	0.05 (63.1)	0.05 (59.5)	0.07 (1.2)	0.09 (0.1)
Cov( $L, \tau$ )	0.20 (7.2)	0.00 (0.0)	-0.00 (-1.3)	0.00 (0.0)	0.01 (0.0)	0.00 (0.0)	-0.01 (-3.7)	-0.04 (-0.4)	-0.04 (-0.1)	0.72 (985.0)	0.72 (907.5)	0.79 (12.6)	0.84 (1.4)
Cov( $W, R$ )	0.77 (28.0)	0.00 (0.0)	-0.00 (-0.5)	0.22 (2.7)	0.82 (1.2)	0.00 (0.0)	0.02 (7.1)	0.55 (5.9)	1.56 (2.2)	0.64 (879.8)	0.66 (832.5)	1.46 (23.2)	3.08 (5.1)
Cov( $W, T$ )	-0.01 (-0.4)	0.00 (0.0)	-0.00 (-0.8)	-0.00 (-0.1)	-0.02 (-0.0)	0.00 (0.0)	-0.00 (-0.1)	-0.02 (-0.2)	-0.03 (-0.0)	-0.04 (-51.3)	-0.04 (-48.1)	-0.06 (-0.9)	-0.07 (-0.1)
Cov( $W, \tau$ )	-0.12 (-4.4)	0.00 (0.0)	-0.00 (-0.3)	0.03 (0.3)	0.05 (0.1)	0.00 (0.0)	0.00 (1.0)	0.05 (0.5)	0.07 (0.1)	-0.39 (-537.0)	-0.40 (-497.1)	-0.48 (-7.6)	-0.55 (-0.9)
Cov( $R, T$ )	-0.08 (-3.0)	0.00 (0.0)	0.01 (12.3)	-0.17 (-2.1)	-0.76 (-1.1)	0.00 (0.0)	0.03 (7.4)	-0.24 (-2.6)	-0.86 (-1.2)	-0.10 (-136.6)	-0.11 (-134.6)	-0.41 (-6.5)	-1.00 (-1.6)
Cov( $R, \tau$ )	-0.77 (-28.0)	0.00 (0.0)	0.01 (14.0)	0.34 (4.1)	0.92 (1.4)	0.00 (0.0)	0.05 (14.5)	0.33 (3.5)	0.60 (0.9)	-1.50 (-2,054.4)	-1.53 (-1,922.9)	-2.77 (-43.9)	-5.32 (-8.7)
Cov( $T, \tau$ )	0.01 (0.4)	0.00 (0.0)	0.00 (4.4)	-0.00 (-0.0)	-0.02 (-0.0)	0.00 (0.0)	0.01 (1.8)	-0.01 (-0.1)	-0.02 (-0.0)	0.07 (100.0)	0.07 (93.7)	0.11 (1.7)	0.12 (0.2)
<i>Total</i>													
Var( $a$ )	2.76 (100.0)	0.00 (0.0)	0.06 (100.0)	8.15 (100.0)	67.17 (100.0)	0.00 (0.0)	0.34 (100.0)	9.45 (100.0)	69.36 (100.0)	0.07 (100.0)	0.08 (100.0)	6.31 (100.0)	61.02 (100.0)

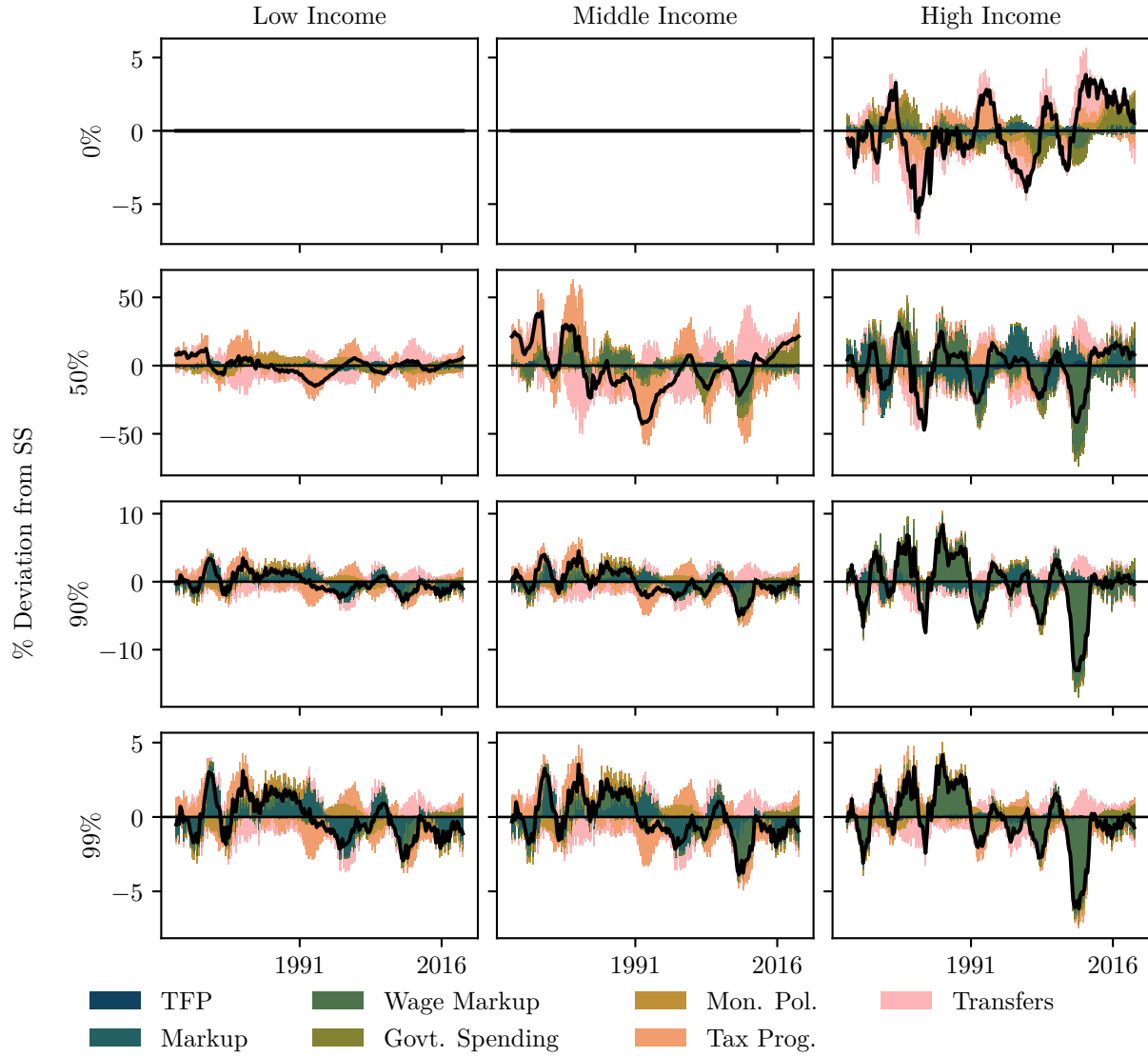
Notes: Forecast error variance decomposition calculated at a 4 quarter time horizon. Variance percent share in parenthesis. Column percentiles correspond to the 0th, 50th, 90th, and 99th wealth percentiles.

Figure 7.2: Historical Decomposition: Household Consumption



Notes: Row labeled by wealth percentile. 12 quarter moving average applied.

Figure 7.3: Historical Decomposition: Household Savings



Notes: Row labeled by wealth percentile. 12 quarter moving average applied.

Figure 7.4: Historical Endogenous Decomposition: Household Aggregates

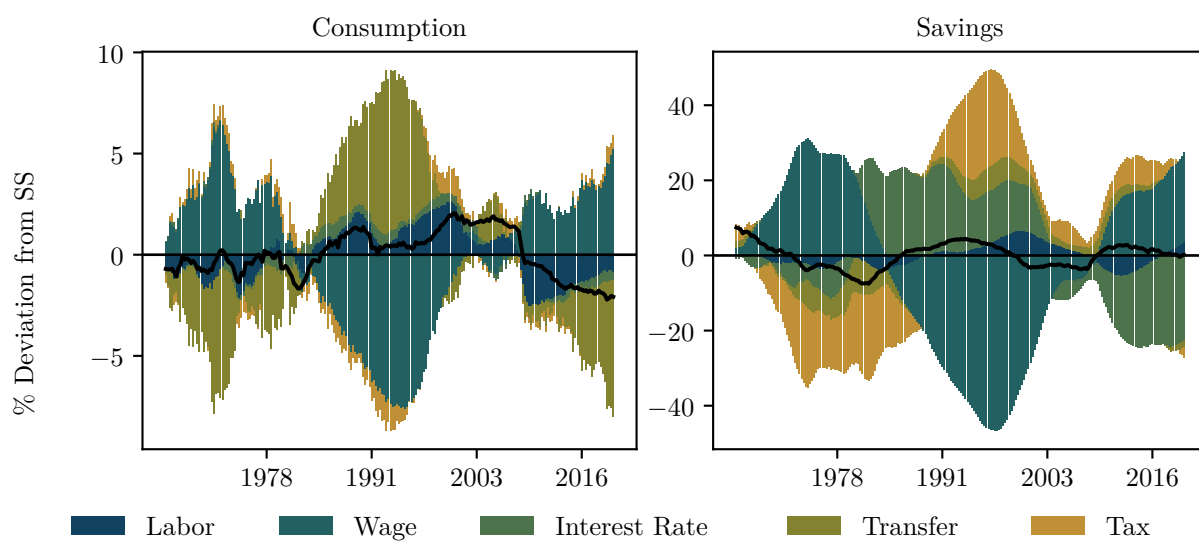


Figure 7.5: Historical Endogenous Decomposition: Household Consumption

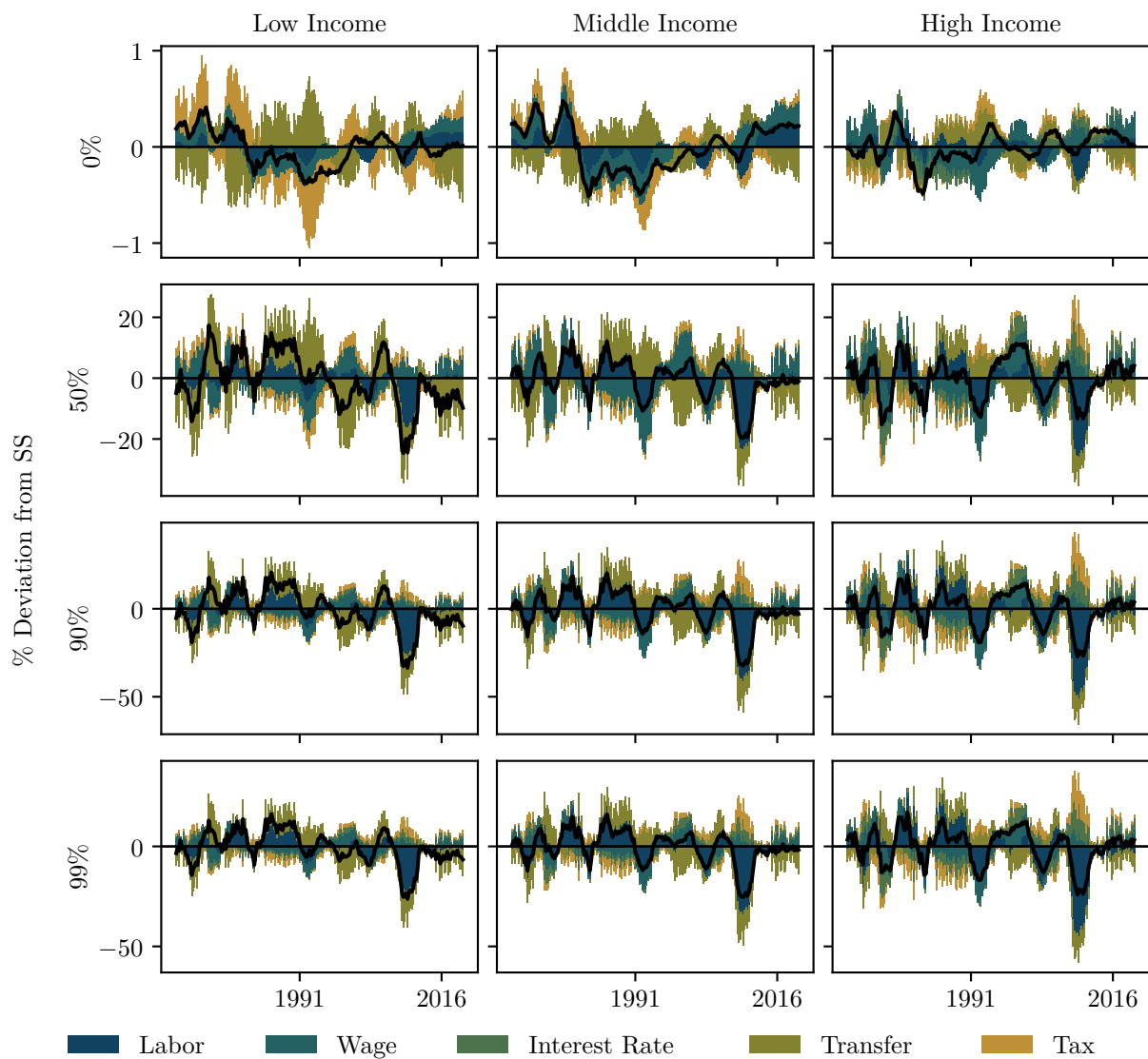
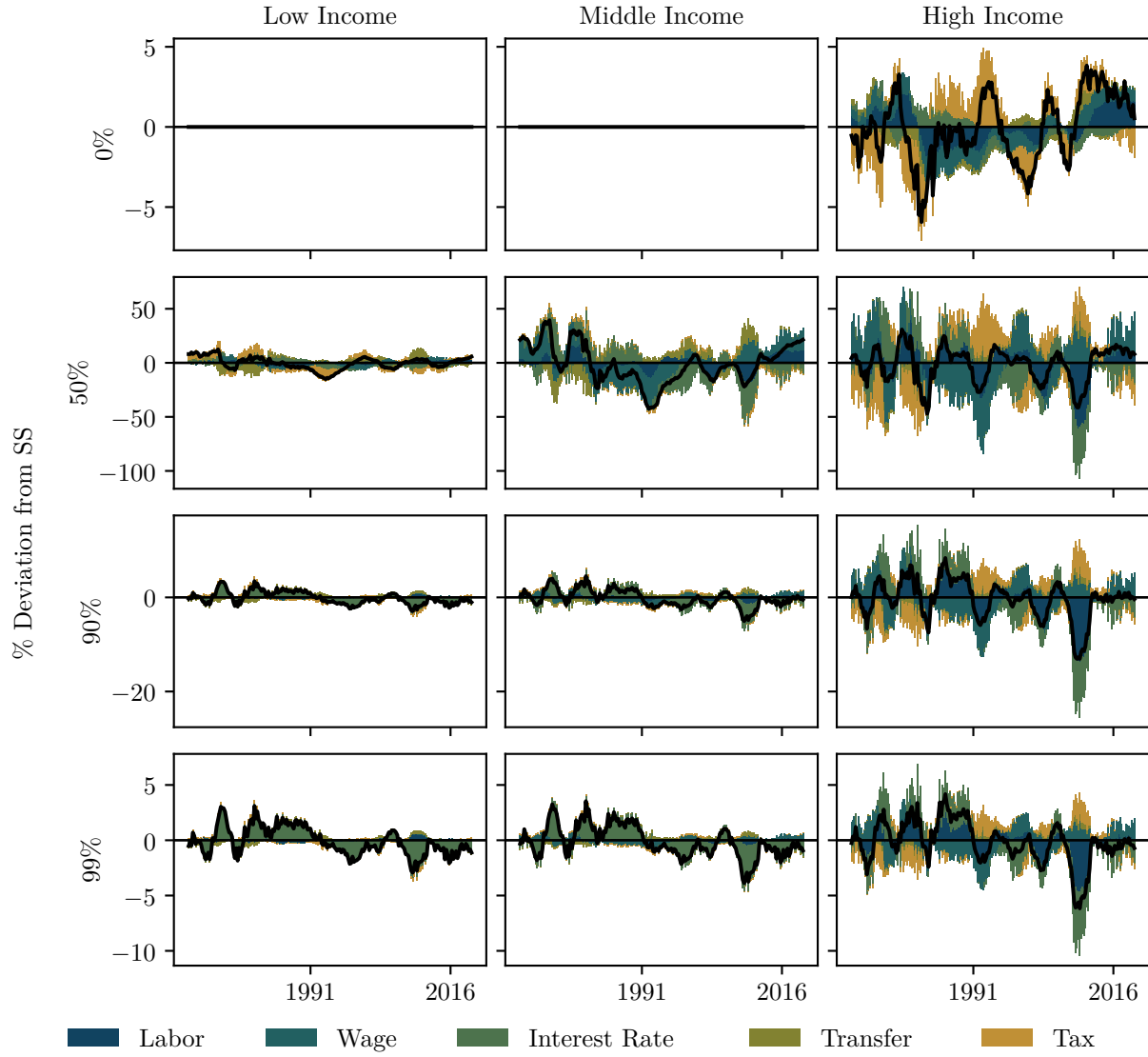


Figure 7.6: Historical Endogenous Decomposition: Household Savings



## **A Data**

## **B Additional Model Details**

### **B.1 Household Decision Rules**

### **B.2 Labor Packer Demand Function**

### **B.3 Wage Philips Curve**

### **B.4 Final Goods Firm Conditions**

### **B.5 Philips Curve**

### **B.6 Aggregation**

### **B.7 Characterization**

## **C Computational Error**

TBD

## **D Estimation Results**

Figure D.1: Recursive Means

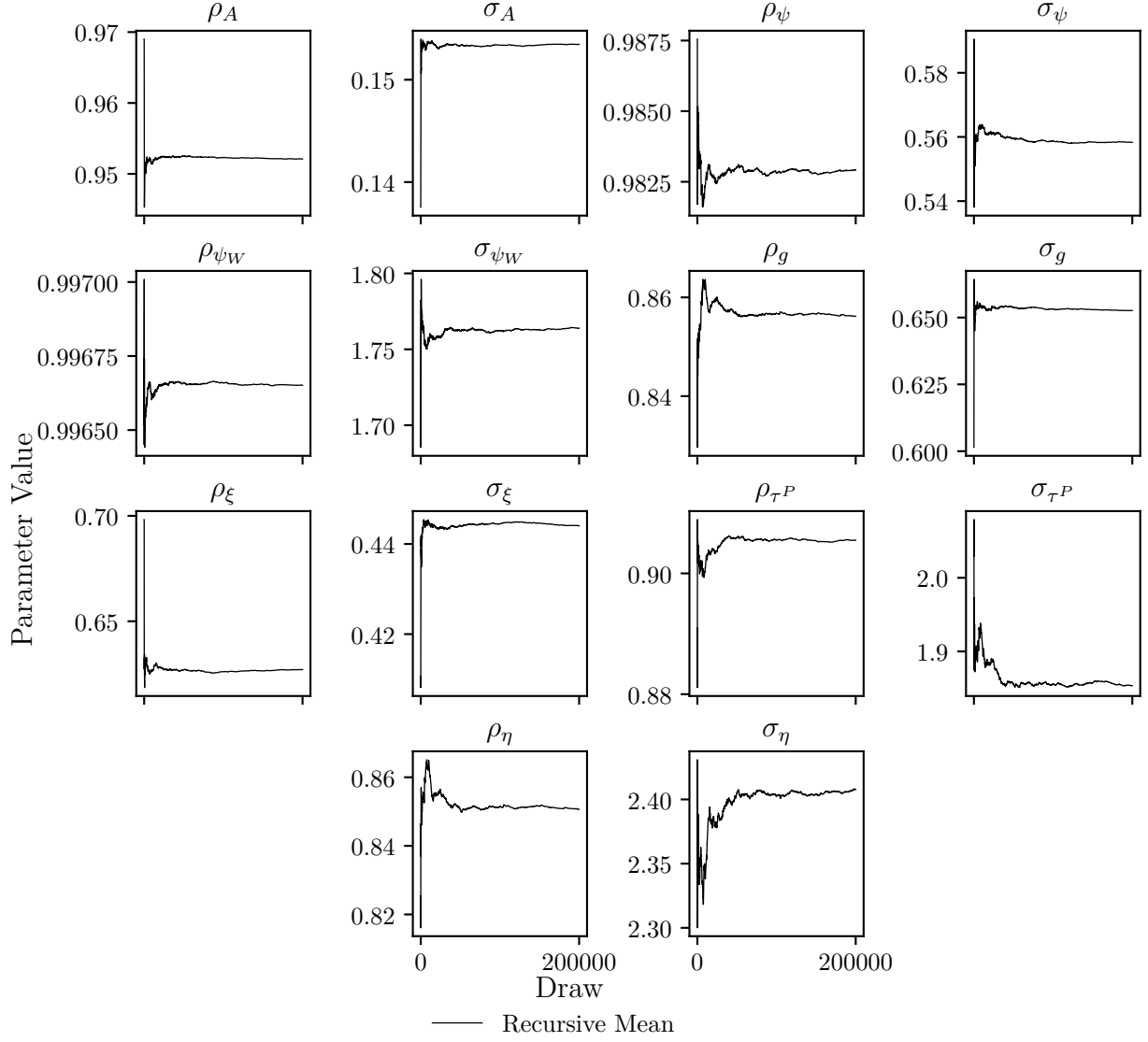




Figure D.2: Posterior Distributions

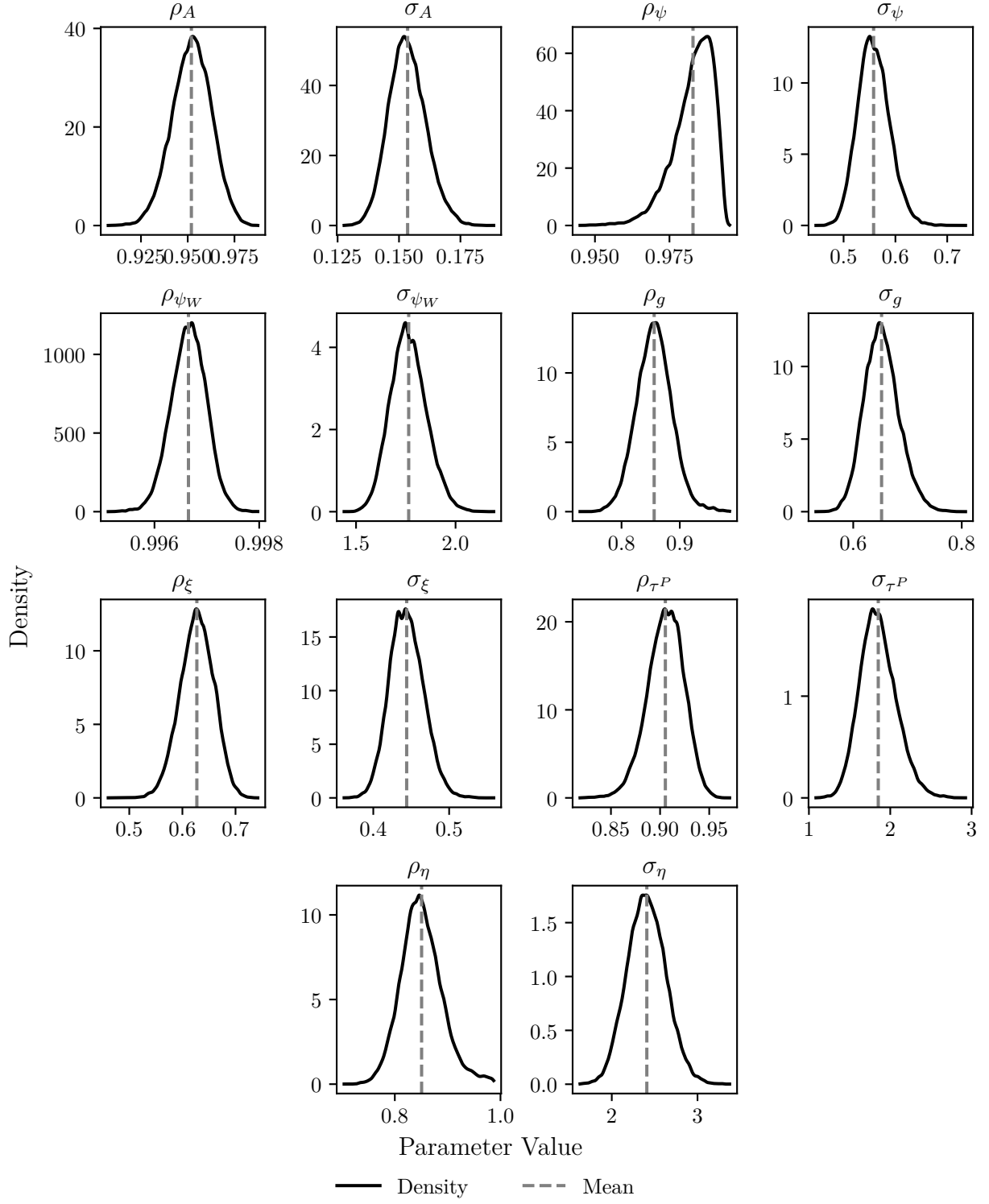
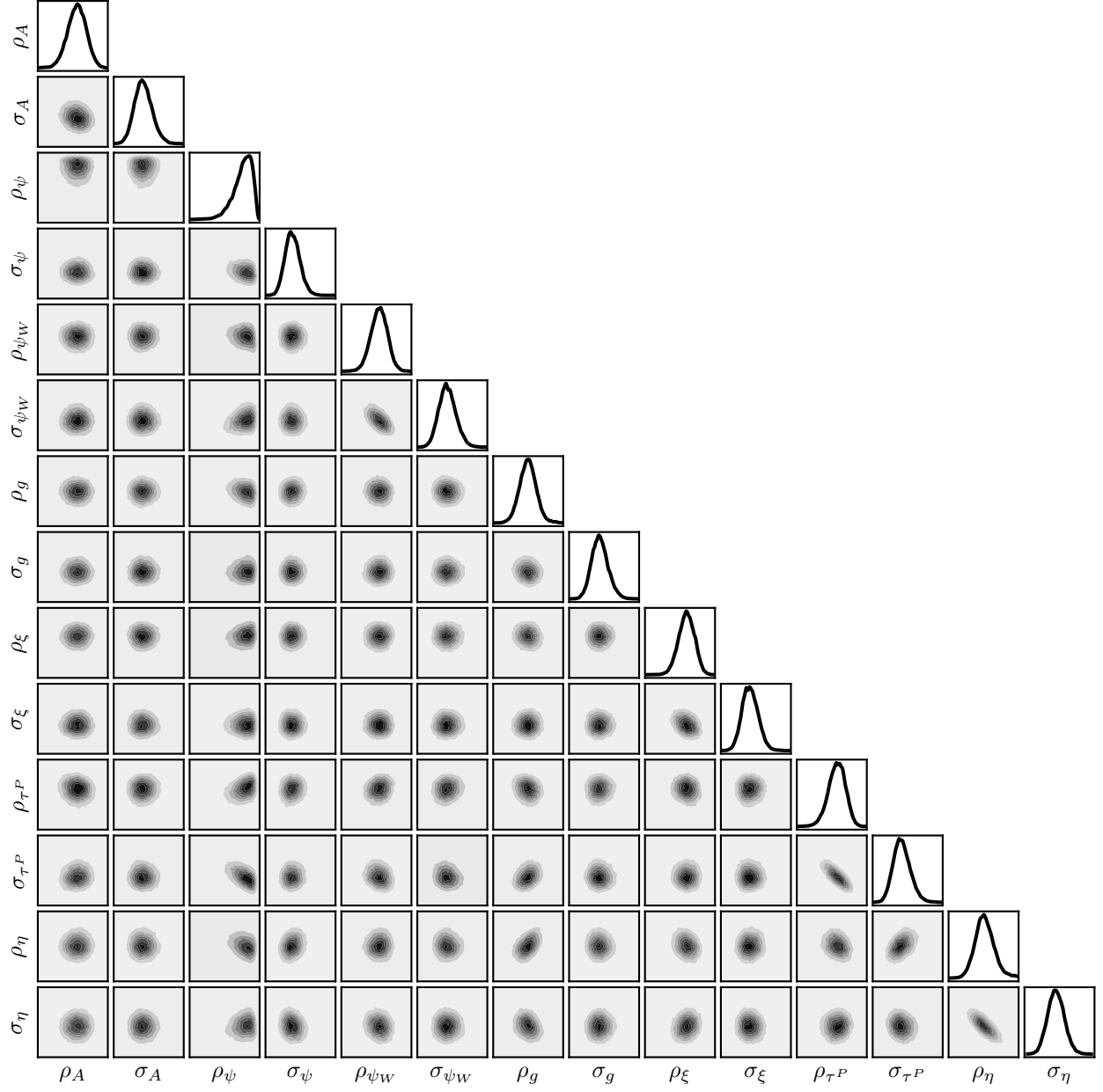


Figure D.3: Posterior Covariences



## E Aggregate IRFs

Figure E.1: TFP ( $A$ ) Shock Impulse Response Functions

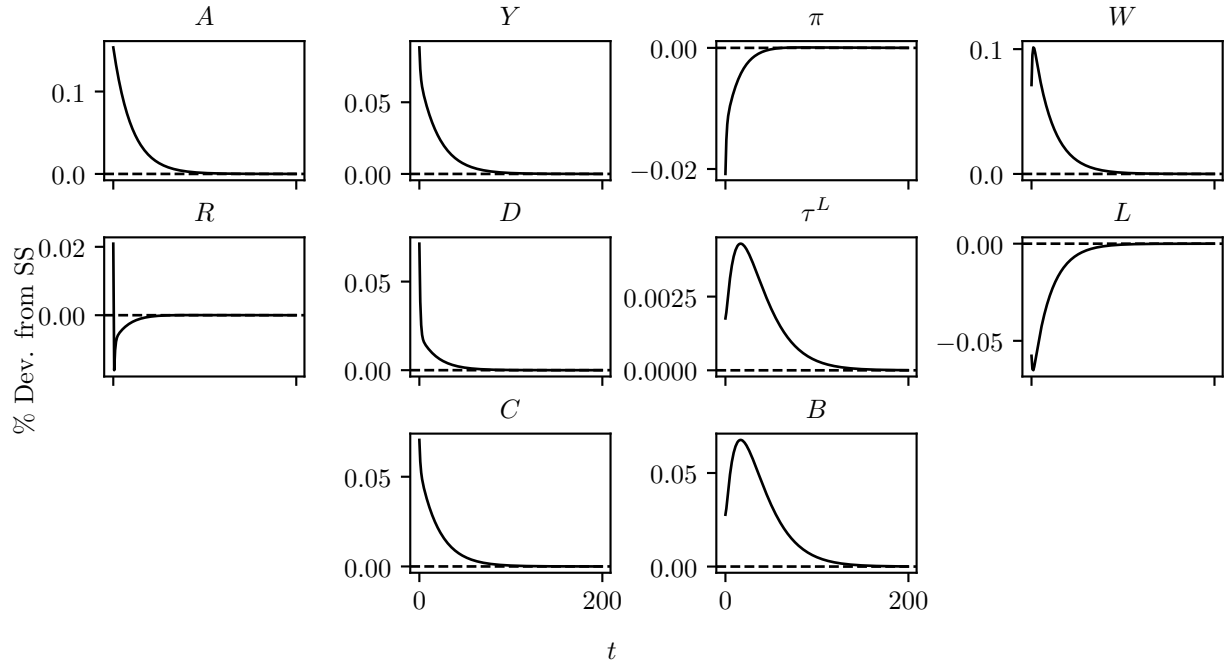


Figure E.2: Price Markup ( $\psi$ ) Shock Impulse Response Functions

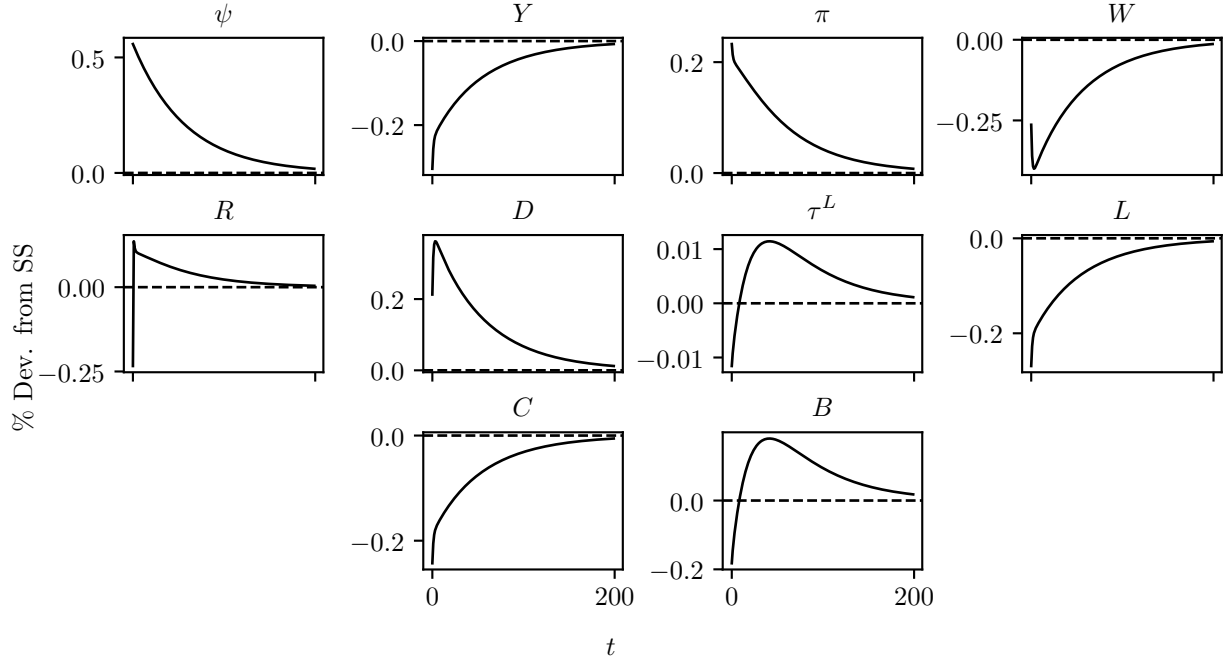


Figure E.3: Wage Markup ( $\psi_W$ ) Shock Impulse Response Functions

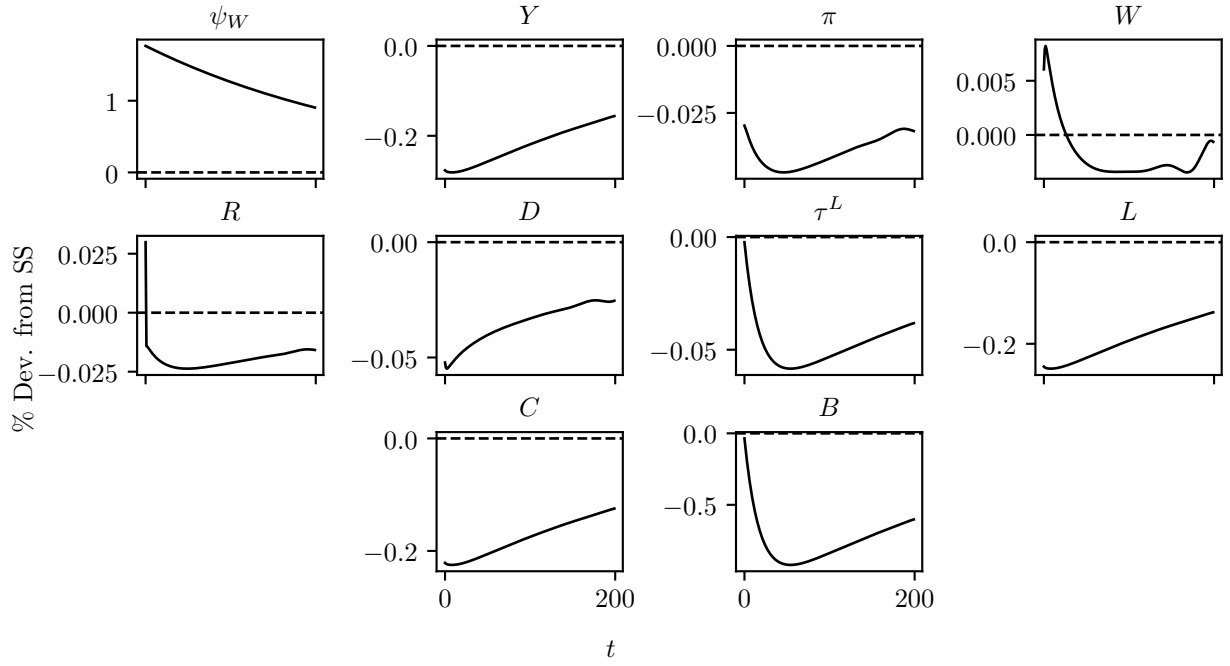


Figure E.4: Govt. Spending ( $g$ ) Shock Impulse Response Functions

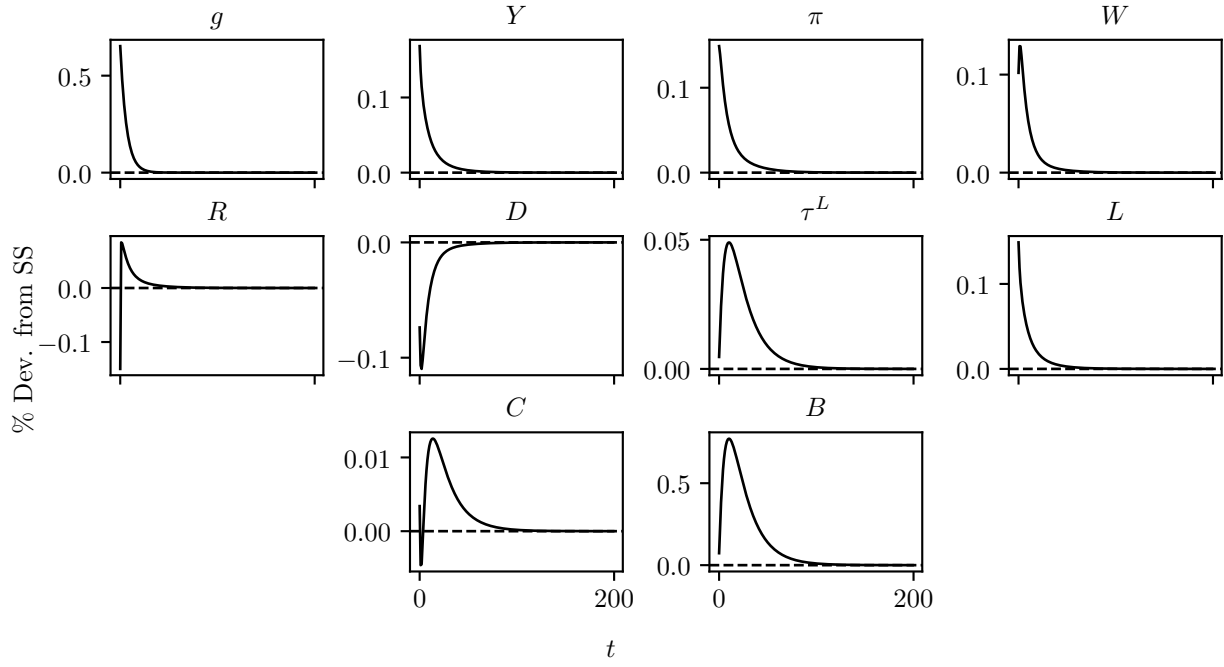


Figure E.5: Monetary Policy ( $\xi$ ) Shock Impulse Response Functions

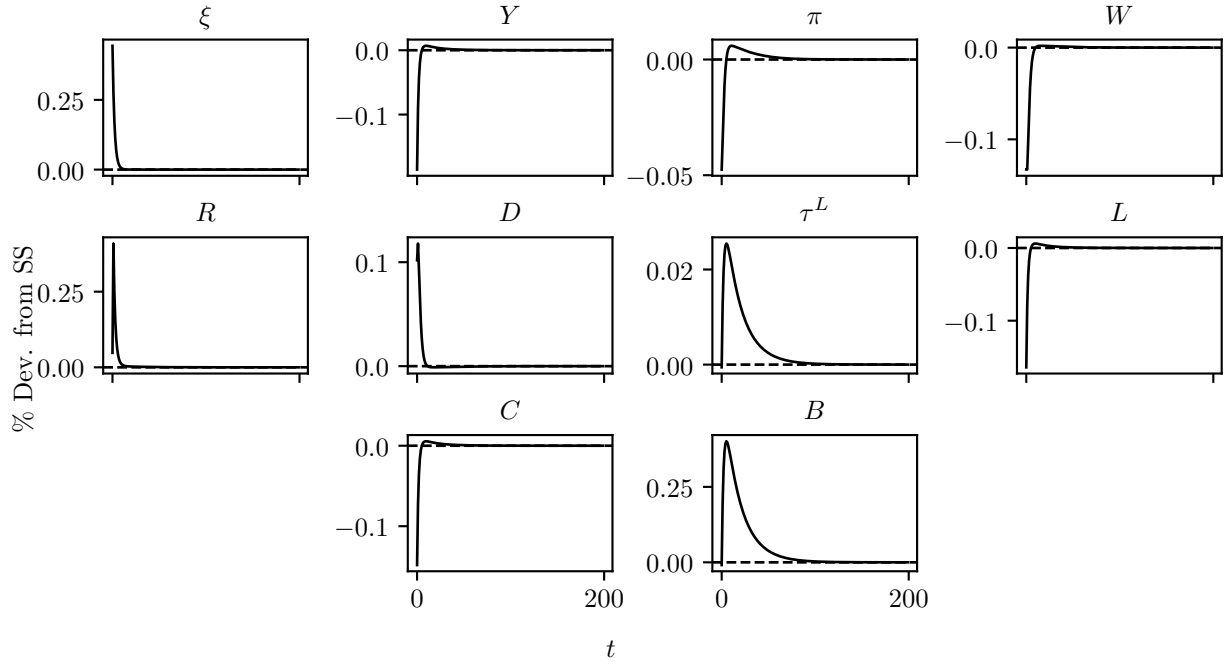


Figure E.6: Tax Progressivity ( $\tau^P$ ) Shock Impulse Response Functions

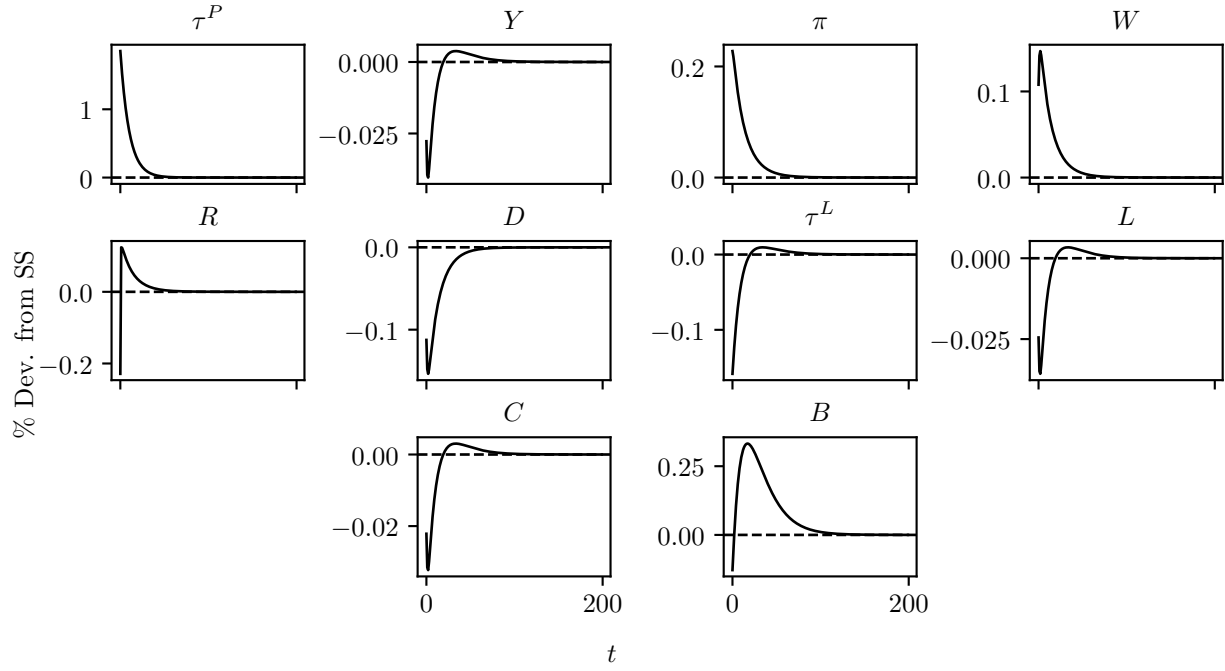
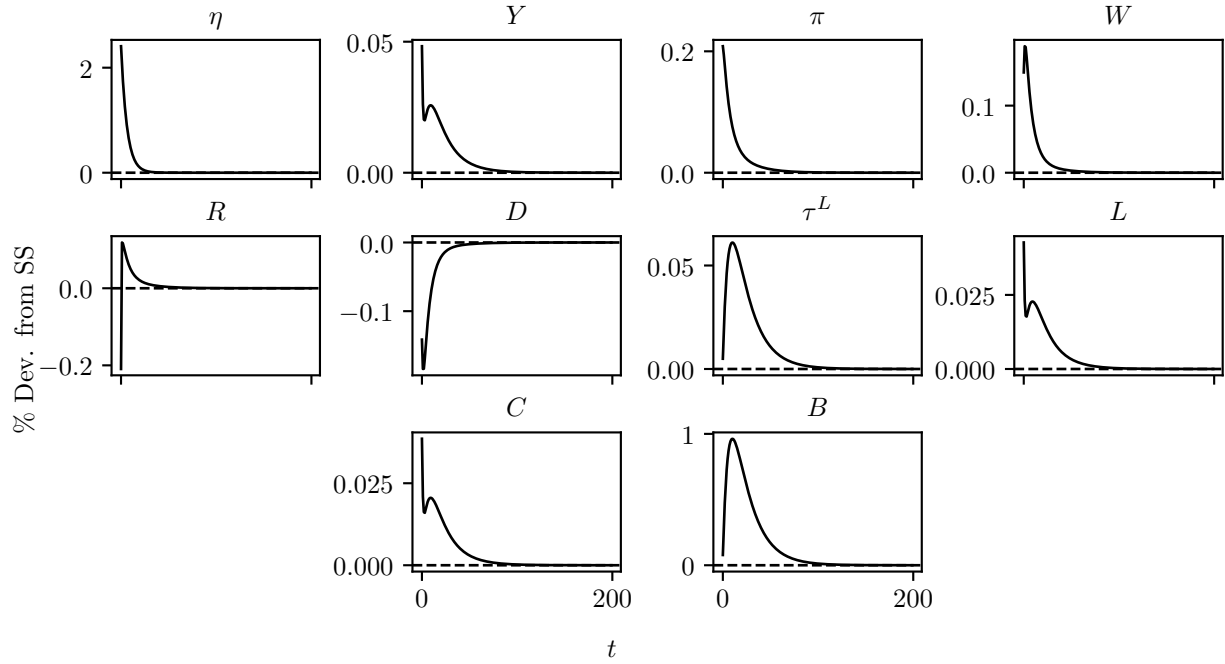


Figure E.7: Household Transfer ( $\eta$ ) Shock Impulse Response Functions



## F Forecast Error Variance Decomposition Calculation

## G Household Decision Rules

Figure G.1: Household Decision Rules

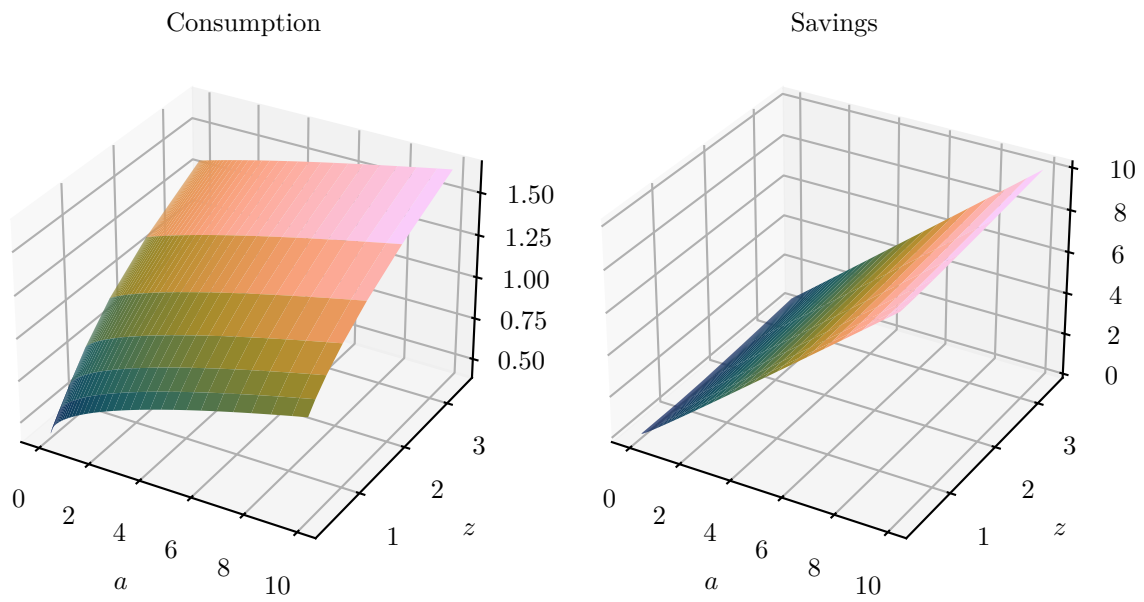


Figure G.2: Household Income Shares

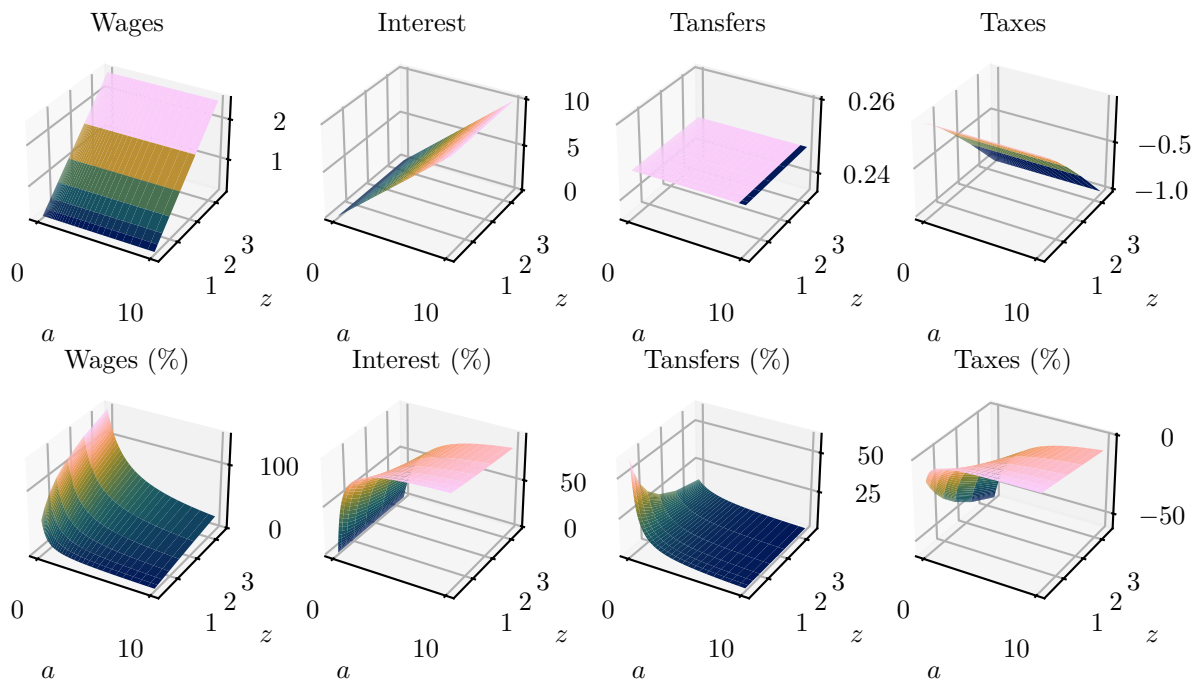




Figure G.3: Consumption Response to a TFP Shock

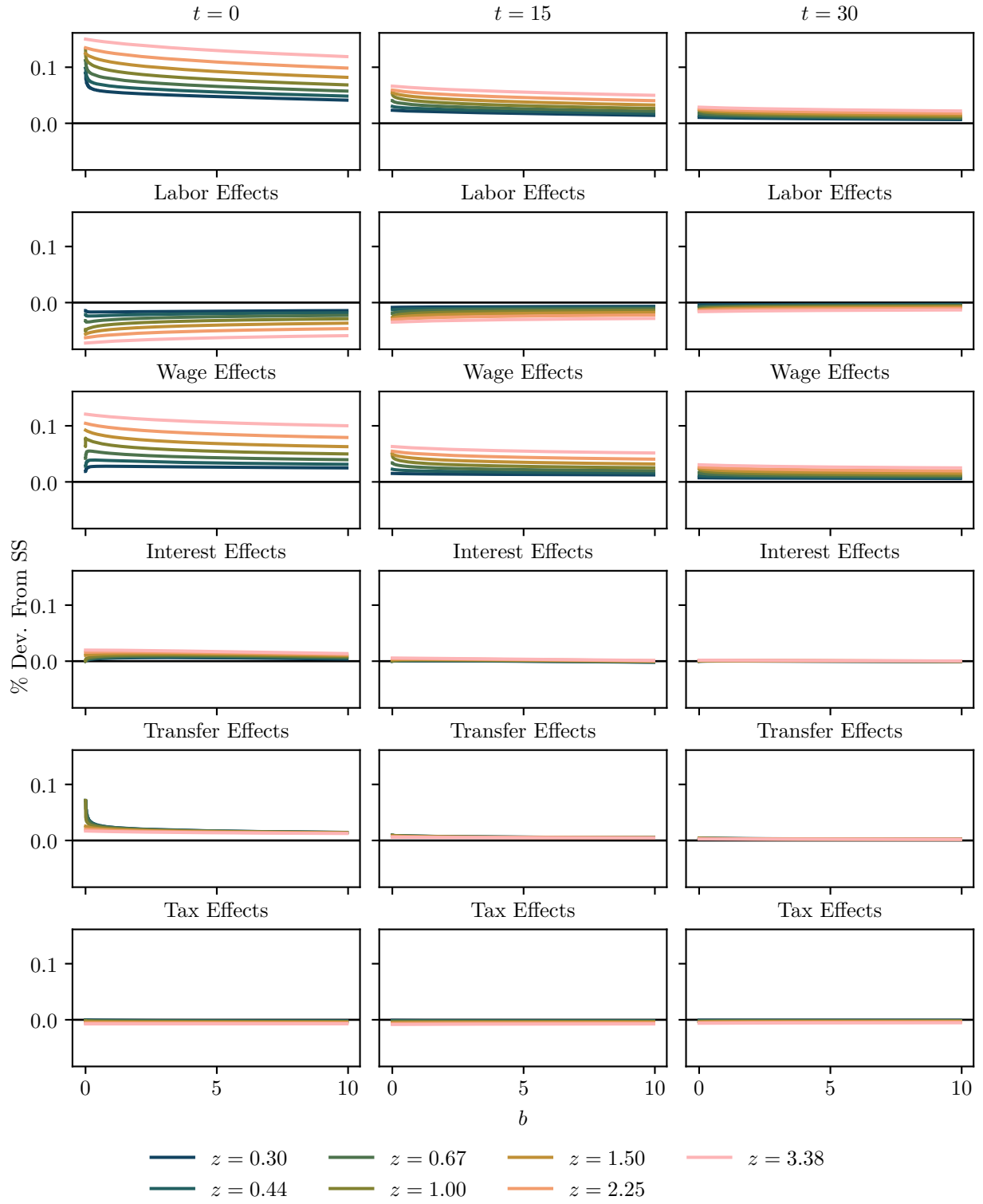


Figure G.4: Savings Response to a TFP Shock

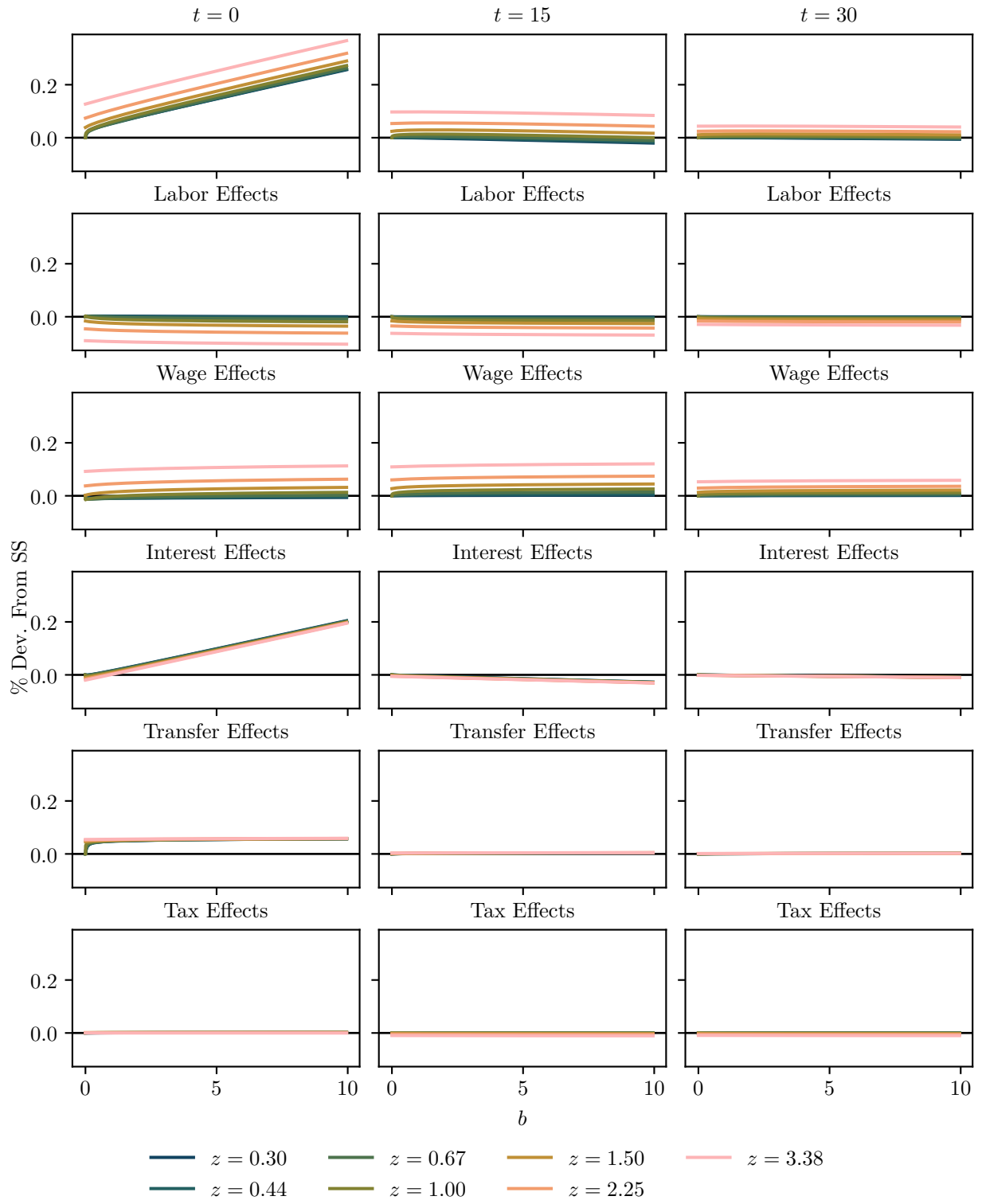


Figure G.5: Consumption Response to a Markup Shock

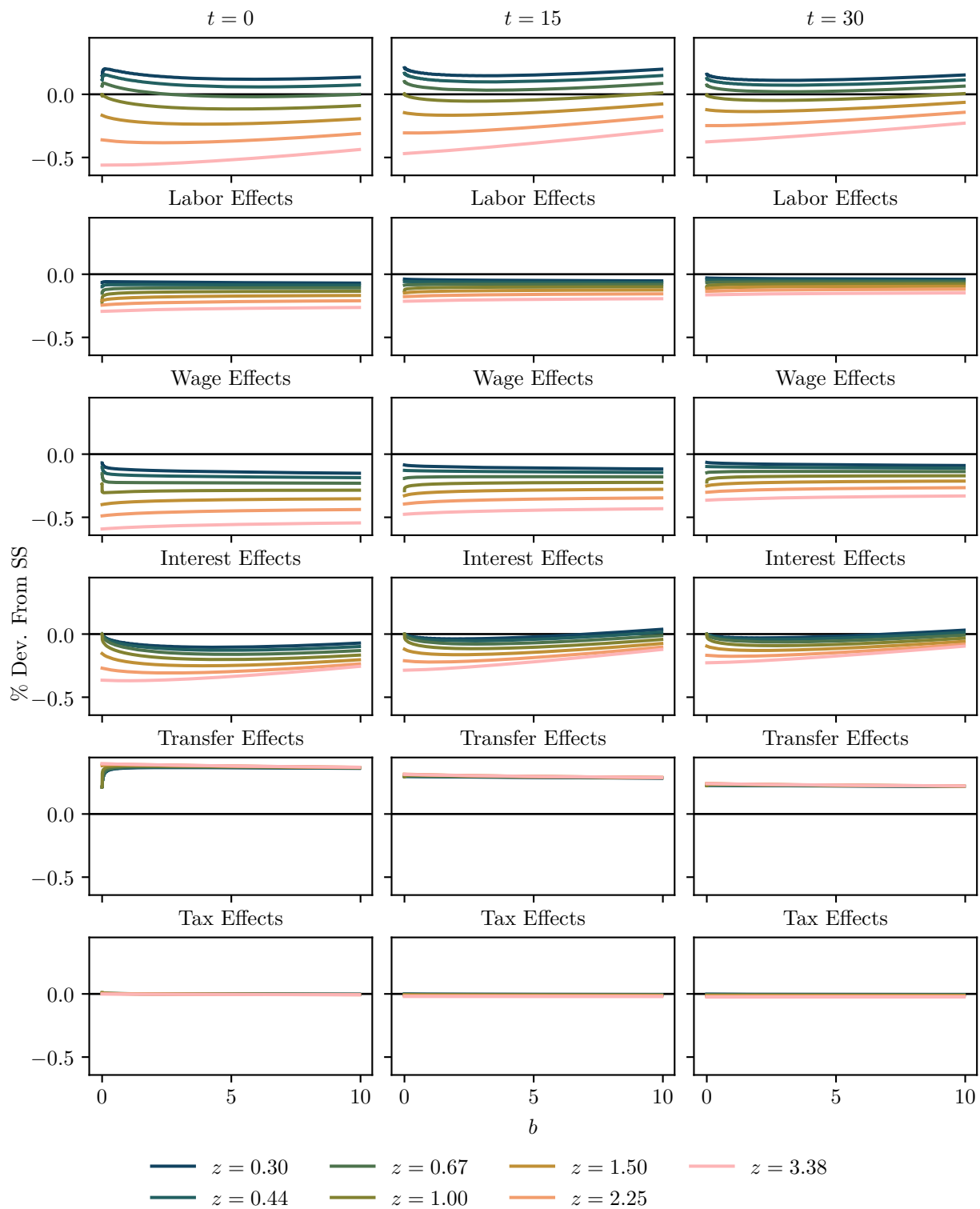


Figure G.6: Savings Response to a Markup Shock

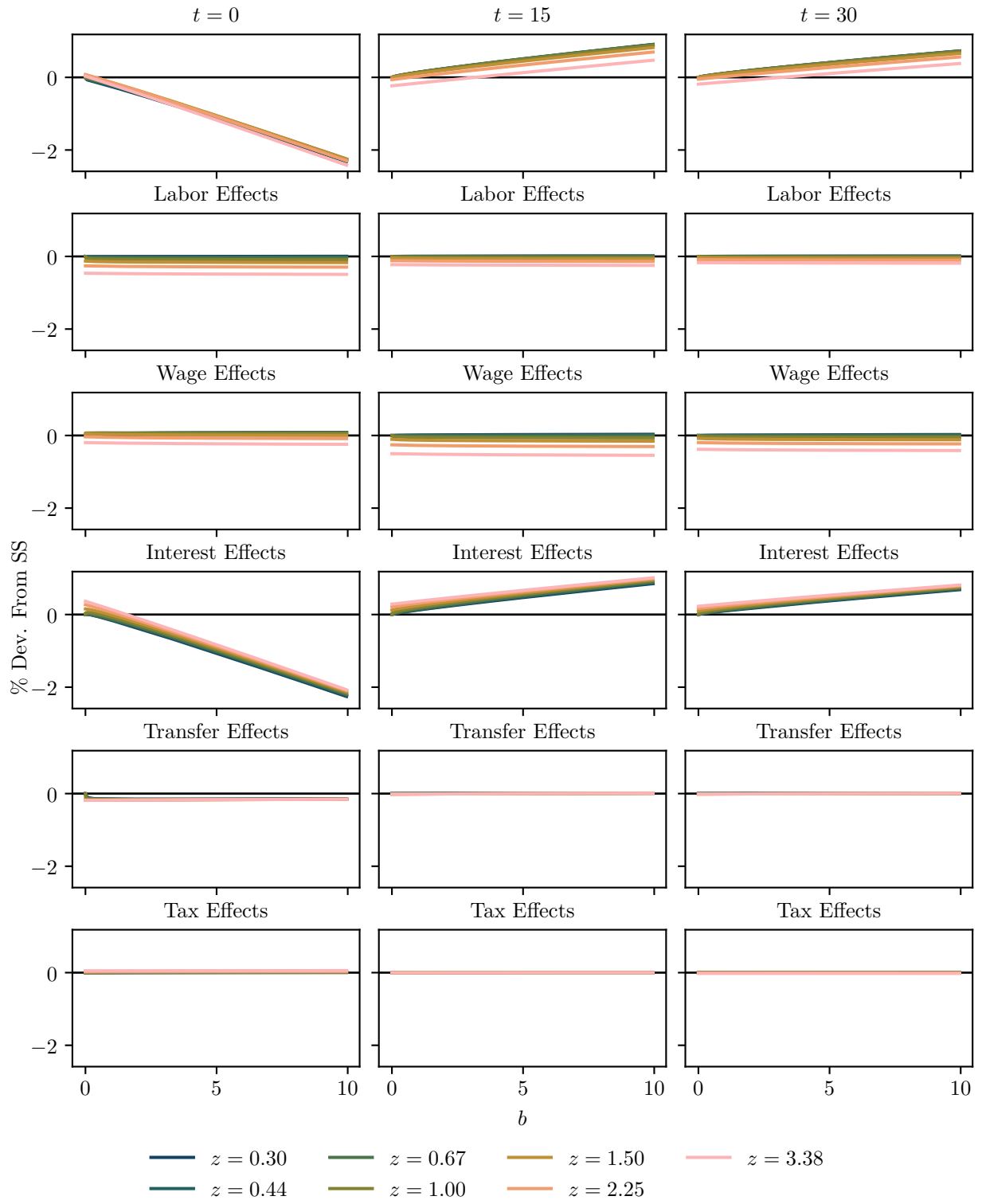


Figure G.7: Consumption Response to a Wage Markup Shock

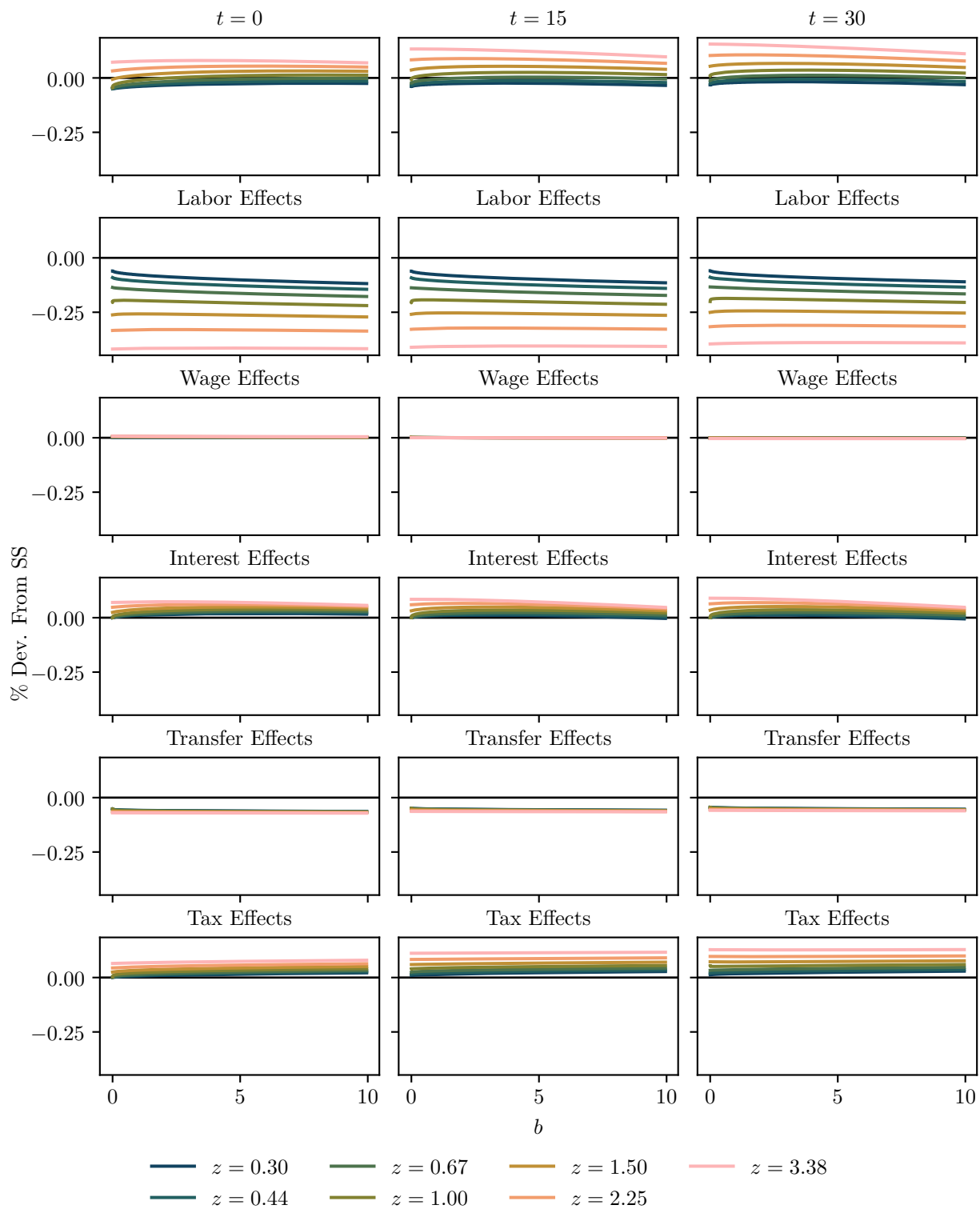


Figure G.8: Savings Response to a Wage Markup Shock

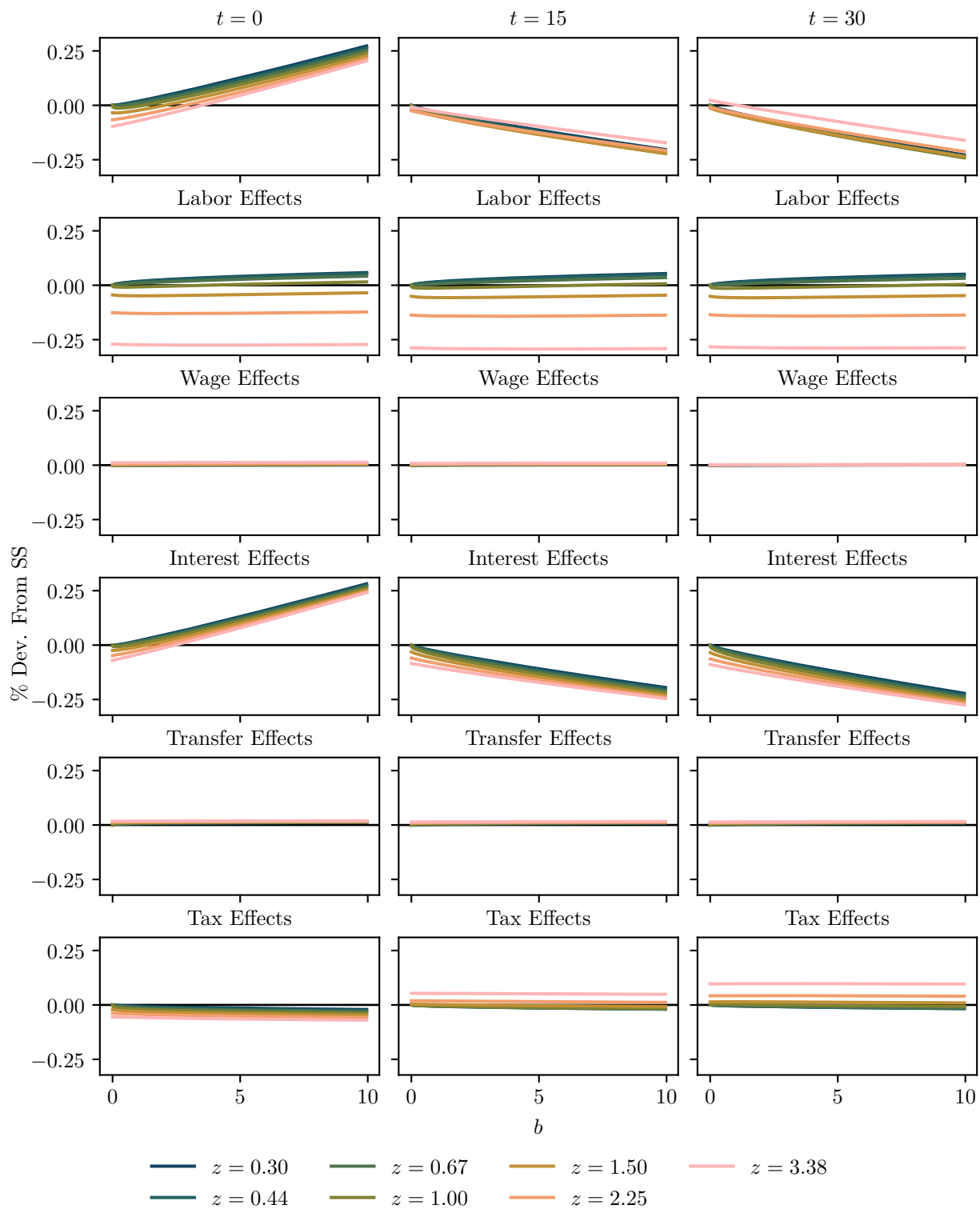


Figure G.9: Consumption Response to a Government Spending Shock

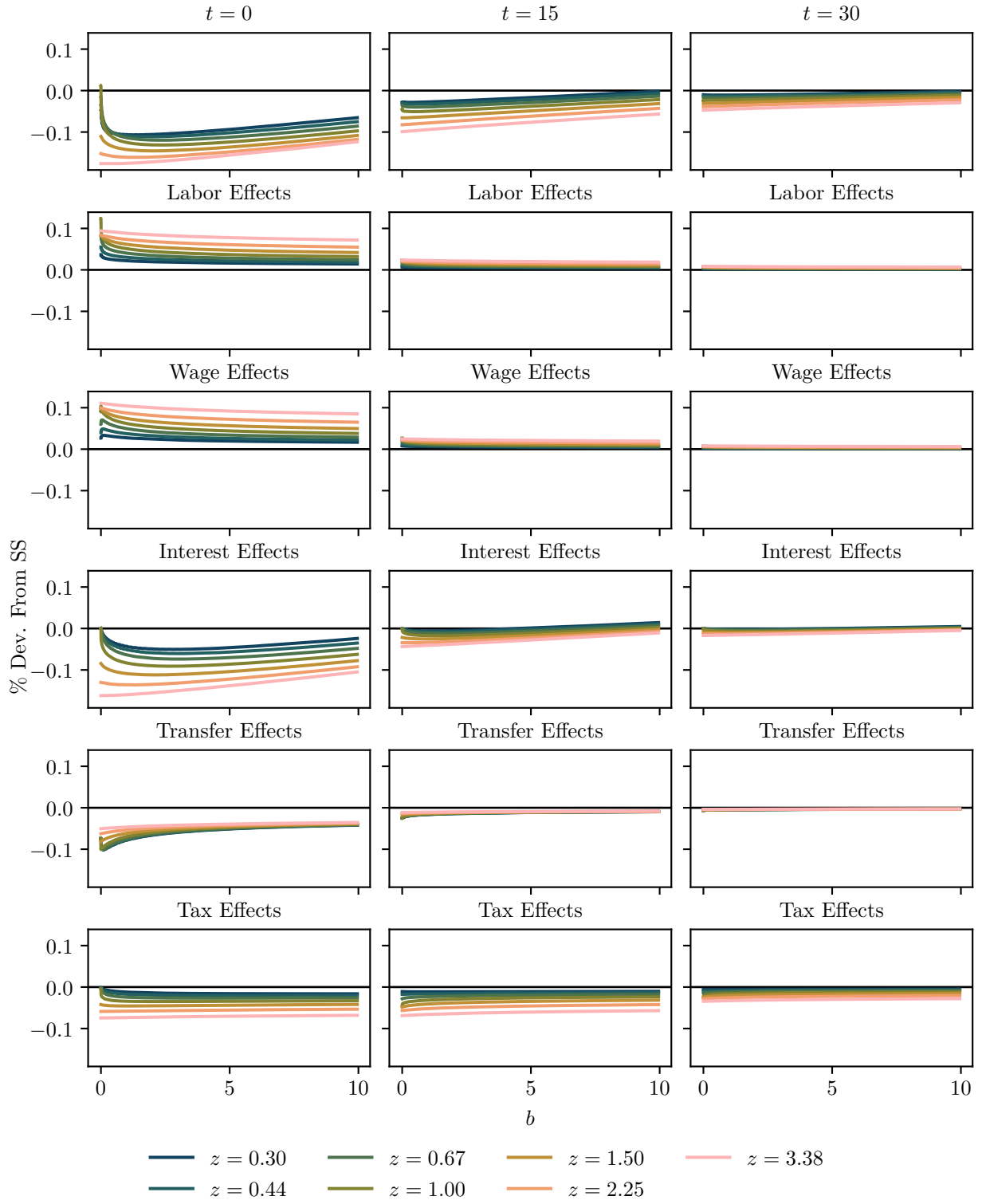


Figure G.10: Savings Response to a Government Spending Shock

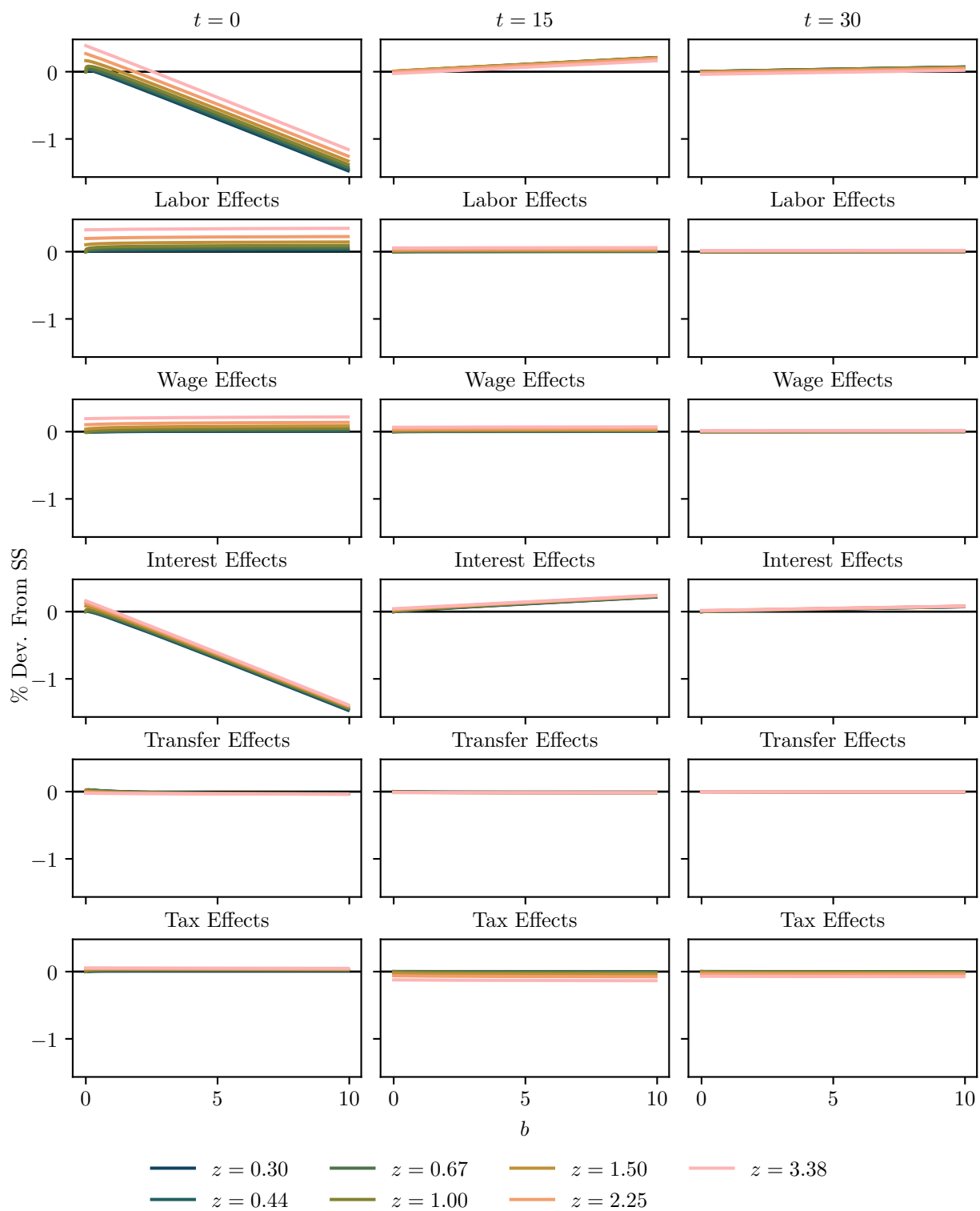




Figure G.11: Consumption Response to a Monetary Policy Shock

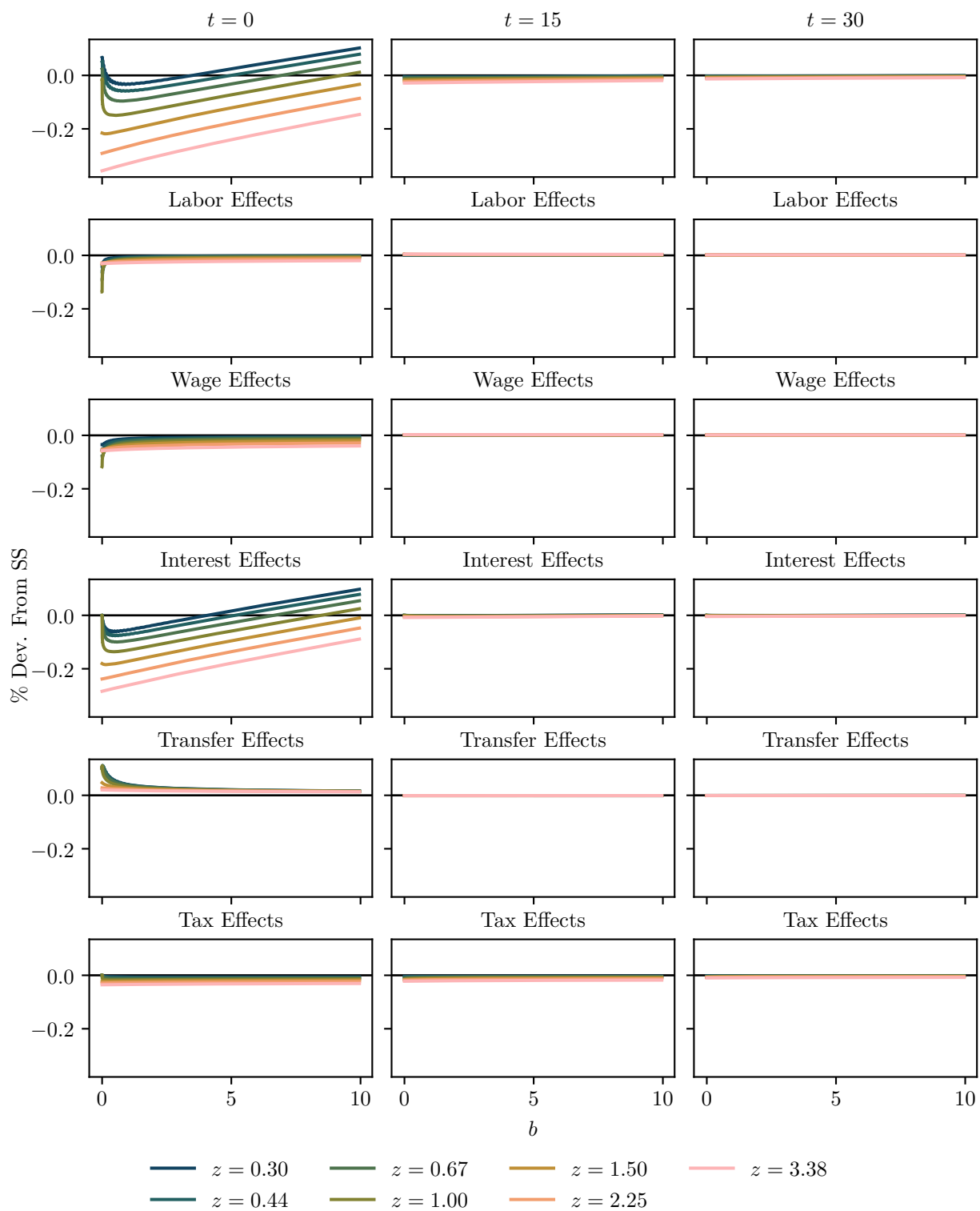


Figure G.12: Savings Response to a Monetary Policy Shock

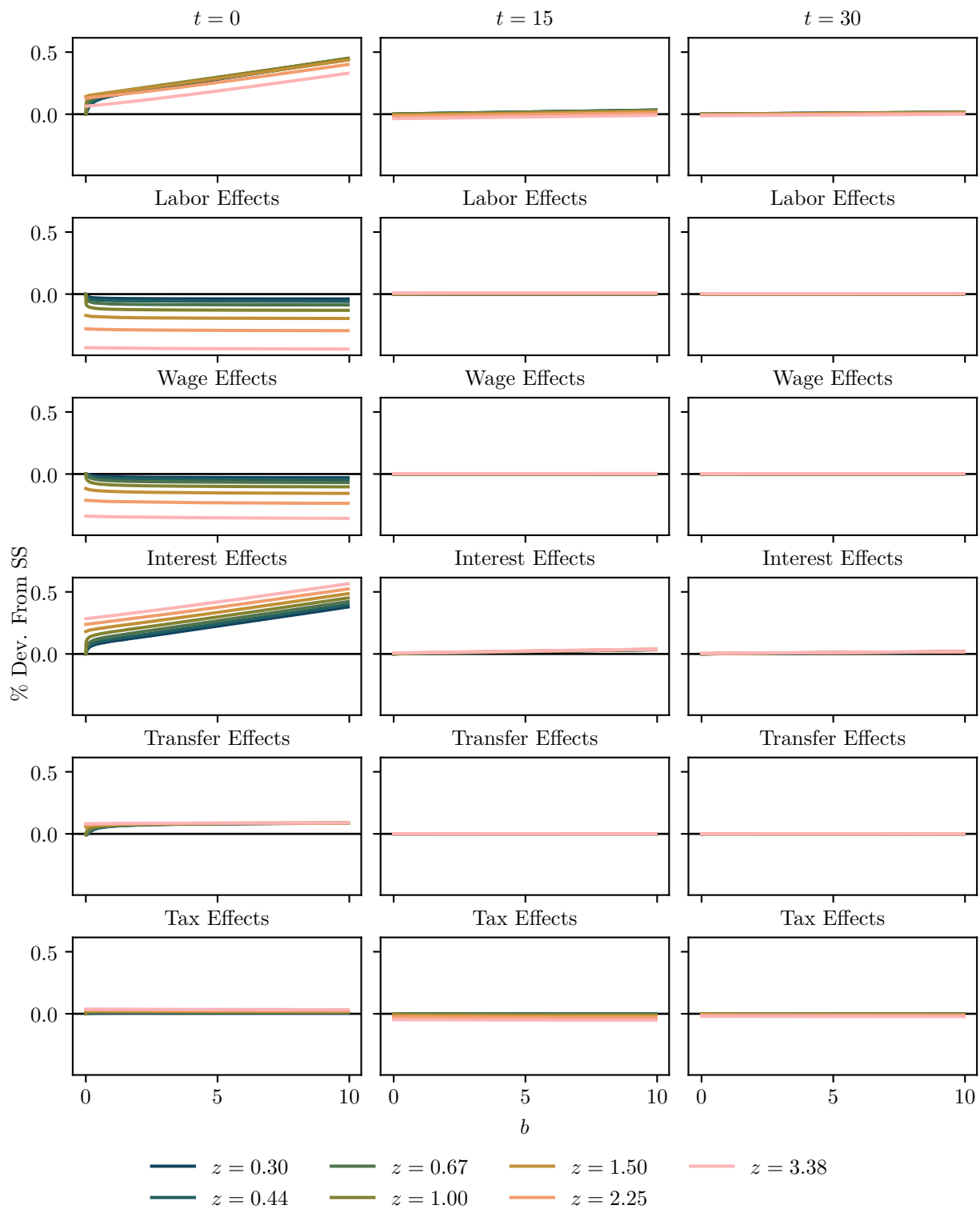


Figure G.13: Consumption Response to a Government Transfer Shock

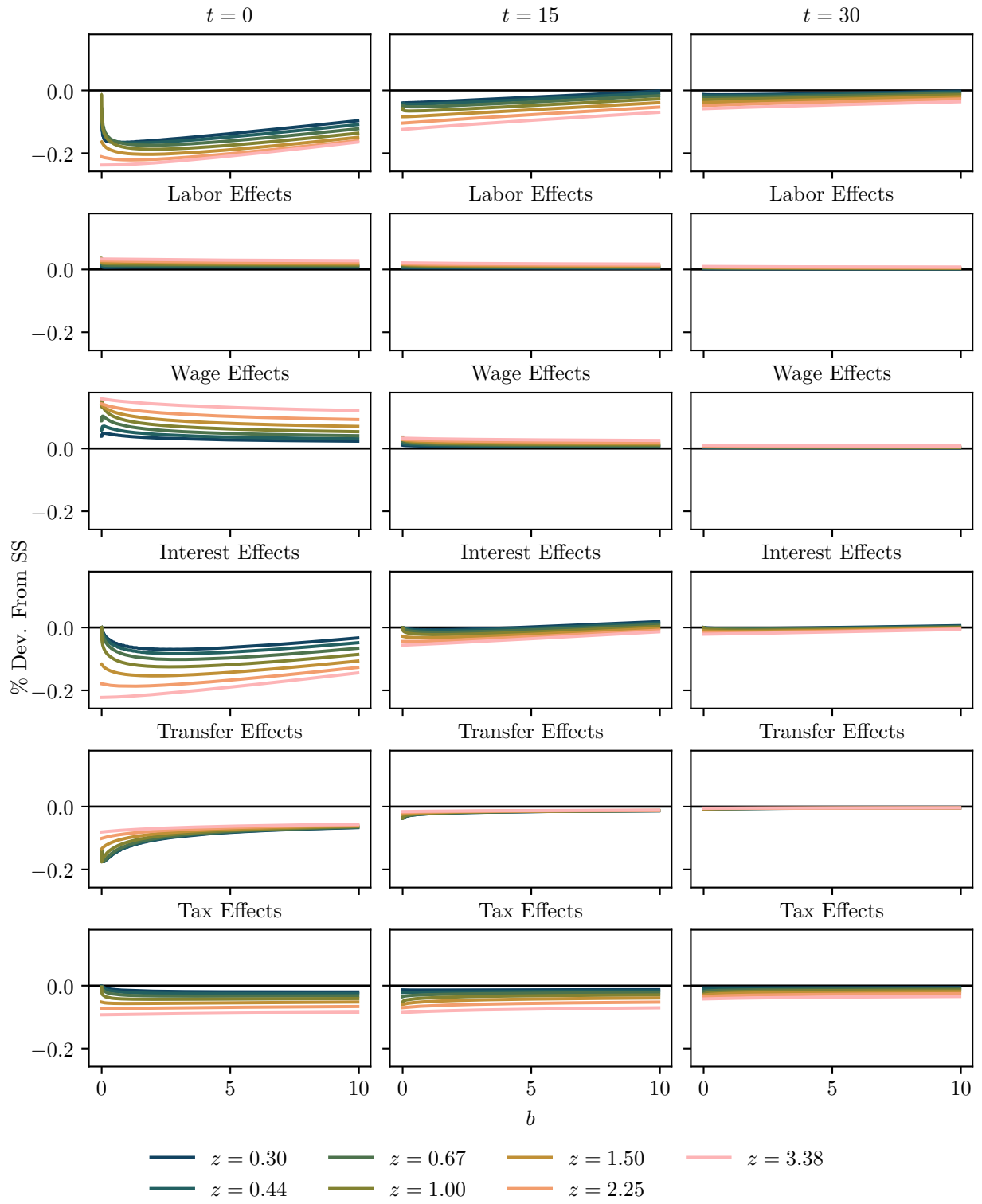


Figure G.14: Savings Response to a Government Transfer Shock

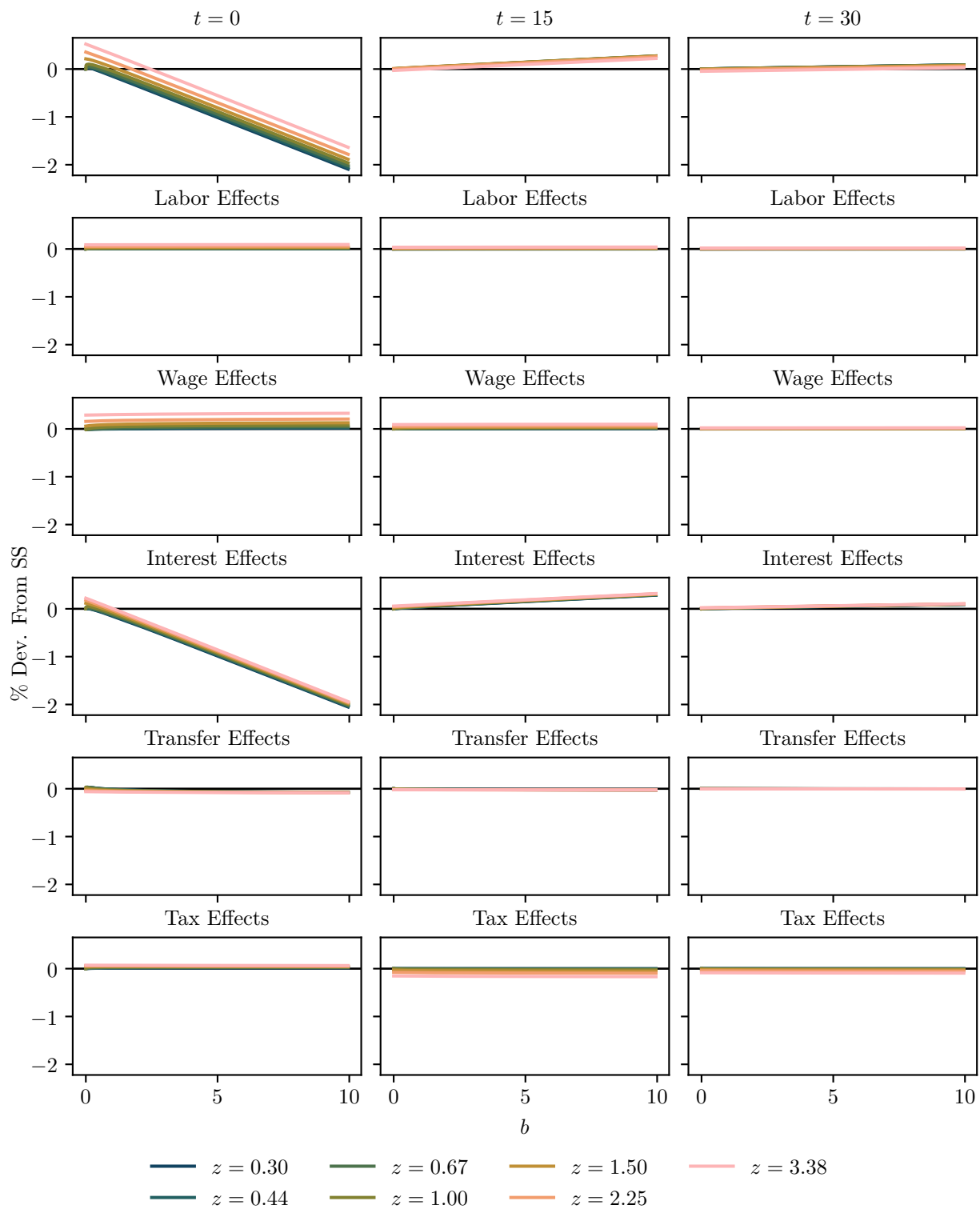


Figure G.15: Consumption Response to a Tax Progressivity Shock

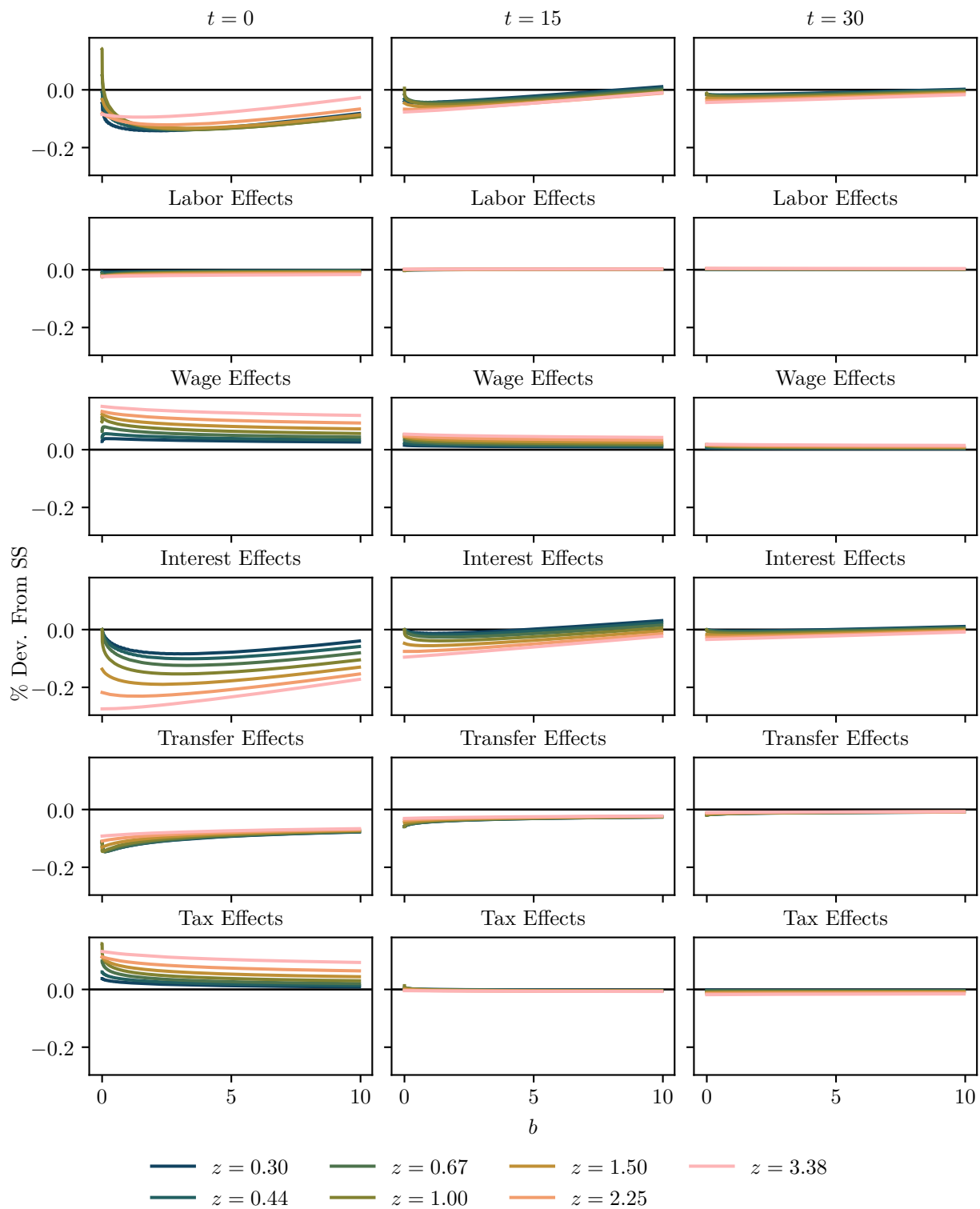
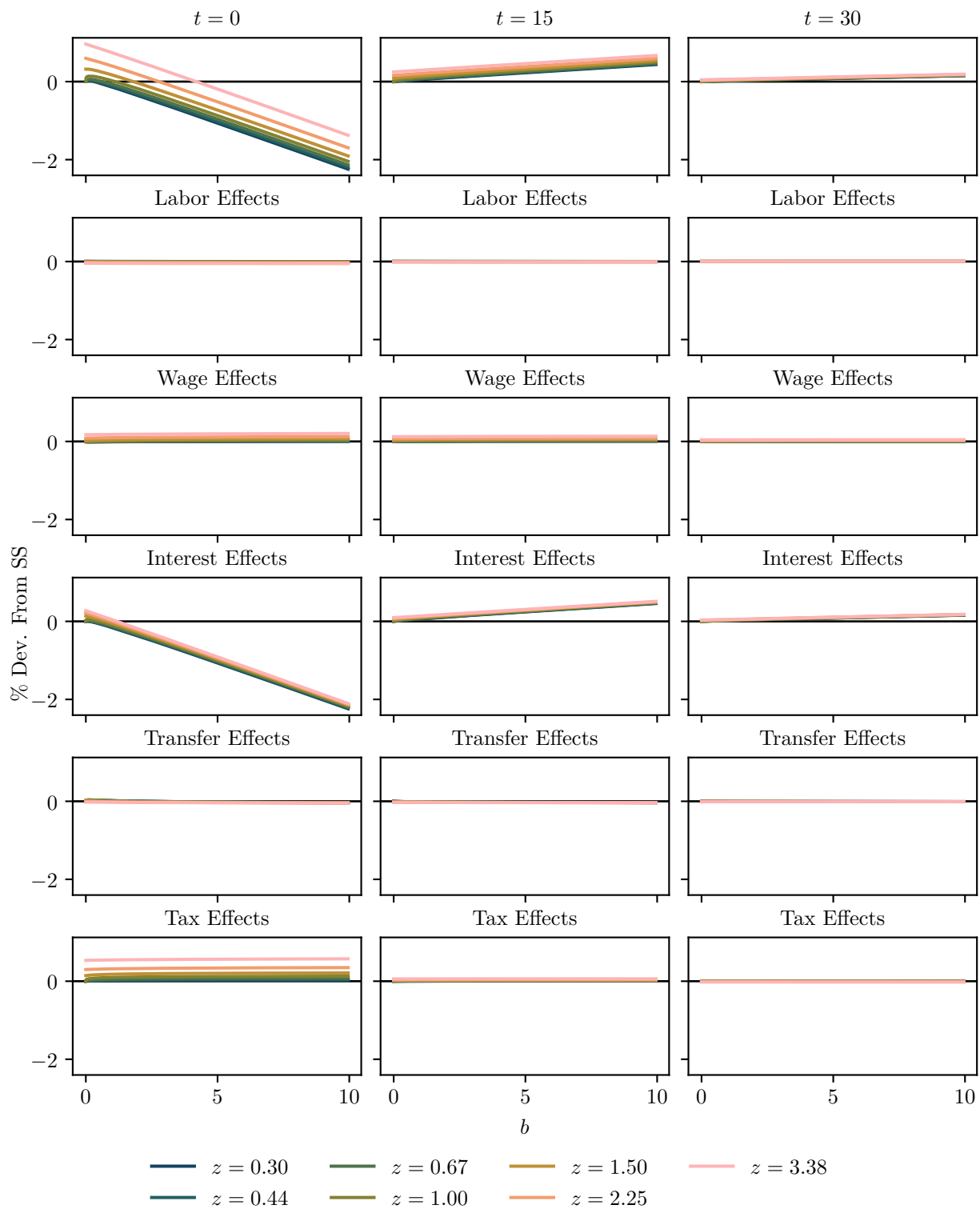


Figure G.16: Savings Response to a Tax Progressivity Shock



## H Additional Historical Decompositions

Figure H.1: Fitted Historical Decompositions

