

CANCER GENOMICS

Lecture 2:

Probabilistic Methods for Mutation Detection

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Outline: Probabilistic Methods for Mutation Detection

1. Primer on statistical modeling (cont'd)

Mixture models, inference and parameter estimation using the EM algorithm

2. Detecting Mutations in Cancer Genomes

- Visualizing somatic vs germline SNVs
- Sequencing read count data

3. Mixture Models for SNV Detection

- SNV genotyping strategy
- SNVMix probabilistic model and EM inference
- Predicting somatic SNVs in cancer



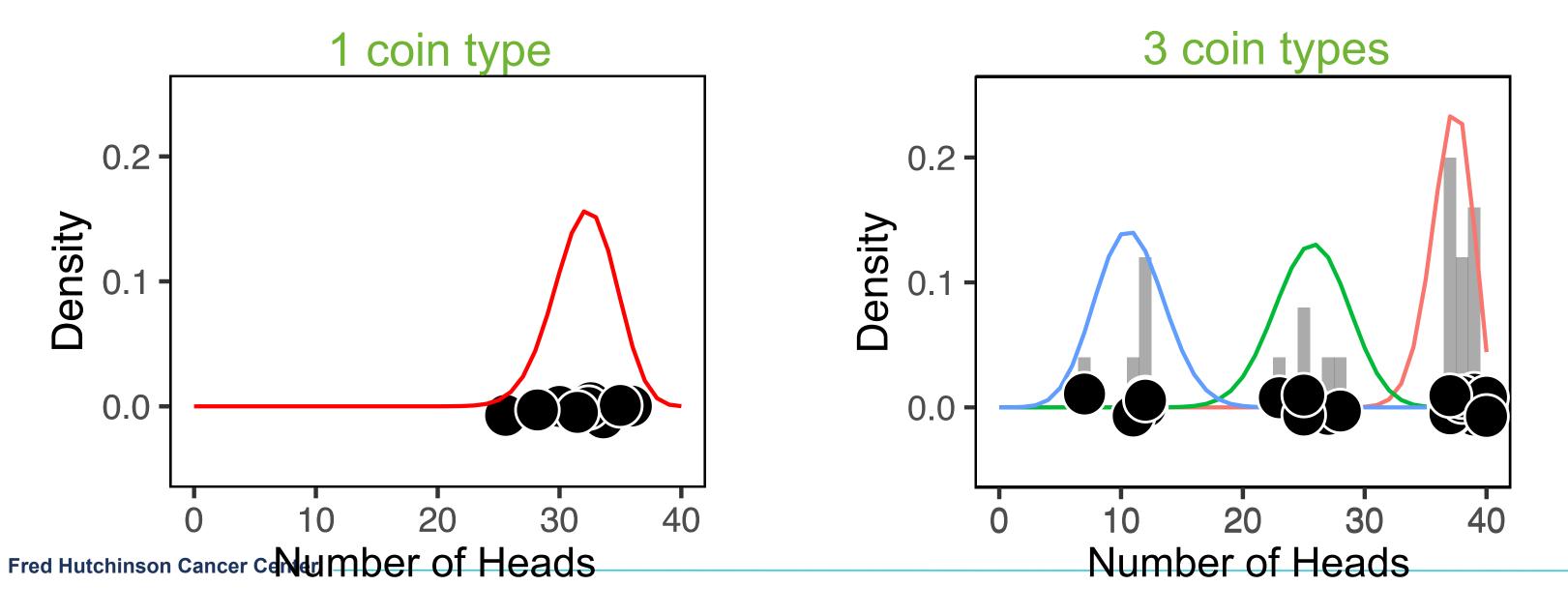
1. Primer on statistical modeling (cont'd)

- Probability
 - Unsupervised learning, probability rules & Bayes' theorem
 - Binomial distribution, Bayesian statistics
 - Beta-binomial model example
- Mixture models, EM inference & parameter learning
- References:
 - Murphy, K. (2012). Machine Learning: A Probabilistic Perspective. MIT Press. ISBN: 9780262018029
 - Bishop, C. M. (2006). Pattern Recognition and Machine Learning (Information Science and Statistics). Springer. ISBN: 0387310738

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Mixture Model: Referee example with multiple coins

- Recall: There are T different referees who tossed the same coin $N = \{1, ..., N_T\}$ times and came up with counts of heads $x = \{1, ..., x_T\}$.
- Now suppose there are **3 types of coins**: (1) probably fair, (2) unfairly favors heads, (3) unfairly favors tails denoted as { fair, heads, tails }.
- Each referee draws one coin (with replacement) from a hat containing these coin types mixed together.



Mixture Model: Referee example with multiple coins

- Recall: There are T different referees who tossed the same coin $N = \{1, ..., N_T\}$ times and came up with counts of heads $x = \{1, ..., x_T\}$.
- Now suppose there are **3 types of coins**: (1) probably fair, (2) unfairly favors heads, (3) unfairly favors tails denoted as { fair, heads, tails }.
- Each referee draws one coin from a hat that contains a bunch of these coin types mixed together.
- 1. We don't know the proportion of each coin type in the hat.
- 2. We don't know which coin each referee drew from the hat.
- 3. We don't know the fairness (probability of heads) for each type of coin.

Referee	# of tosses (N)	# of heads (x)	Prop. of heads	Type of coin used?
Referee 1	40	25	0.63	?
Referee 2	42	35	0.83	?
Referee 3	39	27	0.69	?
Referee 4	XT	N _T	x _T /N _T	?

Coin Type	Proportion in hat	Prob. of heads
"Fair"	?	?
"Heads"	?	?
"Tails	?	?

Mixture Model: Latent state model

1. What is the proportion of each coin type in the hat?

Find the probability for drawing a coin type.

- π_k is the probability of drawing coin type $k \in \{fair, heads, tails\}$
- $\pi = (\pi_{fair}, \pi_{heads}, \pi_{tails})$ are the mixture weights where $\sum_{b=1}^K \pi_k = 1$

2. Which coin did each referee draw? Define the latent variables.

- Let $Z_i = k$ be the type of coin that referee i draws
- Z_i is called a *latent variable* and follows a *Categorical* distribution with parameter π

$$p(Z_i = k \mid \pi_{1:K}) = Cat(Z_i = k \mid \pi_{1:K})$$

$$= \begin{cases} \pi_{fair} & \text{if } k = fair \\ \pi_{heads} & \text{if } k = heads \\ \pi_{tails} & \text{if } k = tails \end{cases}$$

• The proportions $\pi_{1:K}$ of the coin types follows a Dirichlet distribution (conjugate prior)

Coin Type	Proportion in hat	Prob. of heads
"Fair"	π_{fair}	?
"Heads"	π_{heads}	?
"Tails	π_{tails}	?

Referee	Type of coin used?
Referee 1	Z_1
Referee 2	Z_2
Referee 3	Z_3
Referee T	Z_T

Recognition and Machine Learning

Mixture Model: Likelihood as a mixture of binomials

3. What is the fairness (prob. of heads) for each type of coin?

Find the probability of heads for each coin type.

- Recall: for a single coin, $p(x_i | N_i, \mu) = Bin(x_i | N_i, \mu)$
- Define the likelihood for a **3-component mixture of binomials** with 3 parameters, μ_{fair} , μ_{heads} , μ_{tails} , one for each type of coin

$$p(x_i|Z_i=k,N_i,\mu_{1:K}) = Bin(x_i|N_i,\mu_k)$$
 Observed likelihood
$$p(x_i|N_i,\mu_{1:K},\pi_{1:K}) = \sum_{k=1}^K \pi_k Bin(x_i|N_i,\mu_k)$$
 Mixture model

• Beta prior distribution $p(\mu_k | \alpha_k, \beta_k) = Beta(\mu_k | \alpha_k, \beta_k)$

Log Likelihood Function of the Model

$$L(x_{1:T}, N_{1:T} | \mu_{1:K}, \pi_{1:K}) = \prod_{i=1}^{T} \sum_{k=1}^{K} \pi_k Bin(x_i | N_i, \mu_k)$$

$$\mathcal{E} = \sum_{i=1}^{T} \log \left(\sum_{k=1}^{K} \pi_k Bin(x_i | N_i, \mu_k) \right)$$

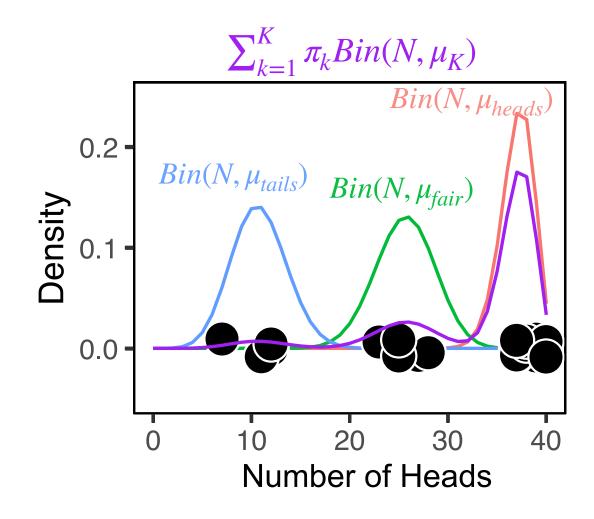
Likelihood function

Log likelihood

Coin Type	in nat	neads
"Fair"	π_{fair}	μ_{fair}
"Heads"	π_{heads}	μ_{heads}
"Tails	π_{tails}	μ_{tails}
	•	

Proportion

Prob. of



Mixture Model: Inference & parameter estimation using EM (1)

Springer



Expectation-Maximization

Initialize parameters: $\pi_{1:K}$ and $\mu_{1:K}$

E-Step: compute "responsibilities" (inference)

- 1. Which coin did each referee draw? (Posterior of the latent states $\gamma(Z_{1:T})$)
- Soft-clustering: Referee i has a probability for using each of the coins.
- **Responsibilities:** "coin that is responsible for generating observation x_i "

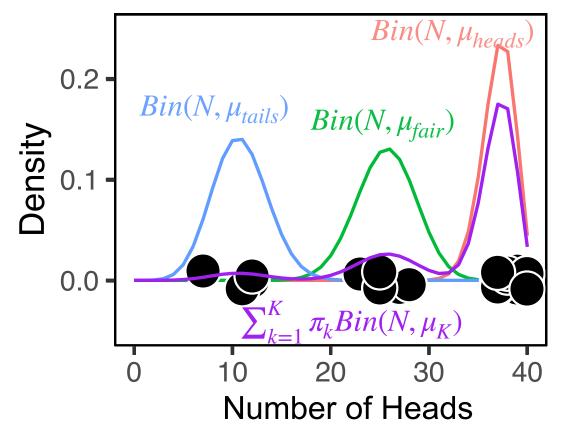
M-Step: Update parameters (learning)

- 2. What is the proportion of each coin type in the hat? $\pi_{1\cdot K}$
- 3. What is the fairness (prob. of heads) for each coin type? $\mu_{1\cdot K}$

Iterate between E-Step and M-Step,

check when log-posterior stops increasing.

Responsibilities				
Referee	Fair Coin	Heads Coin	Tails Coin	
1	$\gamma(Z_1 = F)$	$\gamma(Z_1 = H)$	$\gamma(Z_1 = T)$	
2	$\gamma(Z_2 = F)$	$\gamma(Z_2 = H)$	$\gamma(Z_2 = T)$	
3	$\gamma(Z_3 = F)$	$\gamma(Z_3 = H)$	$\gamma(Z_3=T)$	
Т	$\gamma(Z_T = F)$	$\gamma(Z_T = H)$	$\gamma(Z_T = T)$	



Section 3.3, 3.4, 11.2 in Murphy (2012). Chapter 9 in Bishop (2006). Pattern Machine Learning: A Probabilisting Recognition and Machine Learning. Perspective. MIT Press

Mixture Model: Inference & parameter estimation using EM (2)

E-Step: compute responsibilities (inference)

- 1. What is the probability for a referee to draw each coin type? (Posterior of the latent states $Z_{1:T}$)
- Find the responsibilities given the current parameters

$$p(Z_{i} = k \mid x_{i}, N_{i}, \pi_{1:K}, \mu_{1:K}) = \frac{p(x_{i} \mid Z_{i} = k)p(Z_{i} = k)}{p(x_{i})}$$

$$= \frac{Bin(x_{i} \mid N_{i}, \mu_{k})\pi_{k}}{\sum_{k'=1}^{K} Bin(x_{i} \mid N_{i}, \mu_{k'})\pi_{k'}}$$

$$= \gamma(Z_{i} = k)$$

Bayes' Rule Posterior distribution of the latent variables

Responsibilities

Matrix $T \times K$

Responsibilities = "coin that is responsible for generating observation x_i "

- Soft-clustering: Referee i has a probability for using each of the coins.
- $\gamma(Z_{1:T})$ is a matrix of probabilities with dimensions $T \times K$

Mixture Model: Inference & parameter estimation using EM (3) M-Step: Update parameters (learning)

2. What is the proportion of each coin type in the hat?

$$\hat{\pi}_k = \frac{\sum_{i=1}^T \gamma(Z_i = k) + \delta(k) - 1}{\sum_{j=1}^K \sum_{i=1}^T \left\{ \gamma(Z_i = j) + \delta(j) - 1 \right\}}$$

MAP for π

3. What is the fairness (prob. of heads) for each coin type?

$$\hat{\mu}_k = \frac{\sum_{i=1}^T \gamma(Z_i = k) x_i + \alpha_k - 1}{\sum_{i=1}^T \gamma(Z_i = k) N_i + \alpha_k + \beta_k - 2}$$

MAP for μ

Evaluate the log likelihood and log posterior: use updated parameters

$$\log \mathbb{P} = \sum_{i=1}^{T} \log \left(\sum_{k=1}^{K} \hat{\pi}_{k} Bin(x_{i} | N_{i}, \hat{\mu}_{k}) \right) + \log Dir(\hat{\boldsymbol{\pi}} | \boldsymbol{\delta}) + \sum_{k=1}^{K} \log Beta(\hat{\mu}_{k} | \alpha_{k}, \beta_{k})$$
Log likelihood Log priors

Log posterior

Iterate between E-Step and M-Step:

Stop EM when new $\log \mathbb{P}$ changes less than ϵ compared to previous EM iteration.

Perspective. MIT Press

Recall: MAP estimate

Beta-Binomial Model: Posterior distribution

$$p(\mu \mid x_i) \propto Bin(x_i \mid N_i, \mu) \times Beta(\mu \mid \alpha, \beta) = Beta(\mu \mid x_i + \alpha, N_i - x_i + \beta)$$
Posterior

• Then, what is the probability of heads, μ , of this coin given the **evidence** and the **prior**?

Maximum a posteriori (MAP) estimate

- From the posterior, we can estimate the parameter using the $\emph{maximum a posteriori (MAP)}, \hat{\mu}_{MAP}$
- MAP refers to the mode of the posterior distribution and the mode of a Beta is $\frac{\alpha-1}{\alpha+\beta-2}$
- Since the posterior has the form of a Beta distribution, then the MAP is $\frac{\alpha'-1}{\alpha'+\beta'-2}$

$$\alpha' = x_i + \alpha$$
$$\beta' = (N_i - x_i) + \beta$$

Section 3.3 in Murphy (2012). Machine Learning: A Probabilistic Perspective. MIT Press

$$\hat{\mu}_{MAP} = \frac{x_i + \alpha - 1}{N_i + \alpha + \beta - 2}$$

MAP

- 1.Take log of the posterior
- 2. Take the derivative wrt μ
- 3. Equate to 0
- 4. Solve for μ

Algorithm 1 Binomial Mixture Model Inference and Learning using EM

```
1: Inputs:
        Data: x_{1:T}, N_{1:T}
        Initial parameters: \pi_{1:K}^{(0)}, \, \mu_{1:K}^{(0)},
        Hyperparameters: \delta_{1:K}, \alpha_{1:K}, \beta_{1:K}
 2: Initialize:
        \pi_{1:K} \leftarrow \pi_{1:K}^{(0)}, \, \mu_{1:K} \leftarrow \mu_{1:K}^{(0)}
        logP \leftarrow -Inf
 4: Compute the observed likelihood using initial parameters:
         lik \leftarrow compute.binom.lik()
 6: while converged = false do
        E-Step: Compute responsibilities:
             \gamma(Z_{1:T}) \leftarrow \texttt{compute.responsibilities()}
 8:
        M-Step: Update parameters:
 9:
             \hat{\pi}_{1:K} \leftarrow \texttt{update.pi()}
10:
             \hat{\mu}_{1:K} \leftarrow \texttt{update.mu()}
11:
        Assign updated parameters:
12:
             \pi_{1:K} \leftarrow \hat{\pi}_{1:K}, \, \mu_{1:K} \leftarrow \hat{\mu}_{1:K}
13:
        Re-compute the observed likelihood using updated parameters:
14:
             obs.lik ← compute.binom.lik()
15:
        Compute the log-likelihood:
16:
             loglik ← compute.loglik()
17:
        Compute log Posterior:
18:
               logP[curr.iter] ← compute.log.posterior()
19:
        if (logP[curr.iter] - logP[prev.iter] < \epsilon) then
20:
            converged = true
21:
        end if
22:
        logP[prev.iter] ← logP[curr.iter]
24: end while
25: return Responsibilites \gamma(Z_{1:T}), Converged parameters \hat{\pi}_{1:K}, \hat{\mu}_{1:K}
```

Mixture Model: Inference & parameter estimation using EM (extra slide 1)

Incomplete data log likelihood

$$L(x_{1:T}, N_{1:T} | \mu_{1:K}, \pi_{1:K}) = \prod_{i=1}^{T} \sum_{k=1}^{K} \pi_k Bin(x_i | N_i, \mu_k)$$

The incomplete data log likelihood (plus the priors) is used to monitor EM convergence

Expected complete data log likelihood

Complete data log likelihood

$$\begin{split} L(\mu_{1:K}, \pi_{1:K} | \, x_{1:T}, Z_{1:T}, N_{1:T}) &= \prod_{i=1}^{T} \prod_{k=1}^{K} \pi_k Bin(x_i | N_i, \mu_k)^{\mathbb{I}(Z_i = k)} \\ \ell(\mu_{1:K}, \pi_{1:K} | \, x_{1:T}, Z_{1:T}, N_{1:T}) &= \sum_{i=1}^{T} \sum_{k=1}^{K} \mathbb{I}(Z_i = k) \big\{ \log \pi_k + \log Bin(x_i | N_i, \mu_k) \big\} \\ Q &= \mathbb{E} \left[\ell(\mu_{1:K}, \pi_{1:K} | \, x_{1:T}, Z_{1:T}, N_{1:T}) \right] &= \sum_{i=1}^{T} \sum_{k=1}^{K} \mathbb{E} \left[\mathbb{I}(Z_i = k) \right] \big\{ \log \pi_k + \log Bin(x_i | N_i, \mu_k) \big\} \end{split}$$

 $i=1 \ k=1$

 $= \sum_{i=1}^{n} \sum_{j=1}^{n} \gamma(Z_i = k) \left\{ \log \pi_k + \log Bin(x_i | N_i, \mu_k) \right\}$

The expected complete data log likelihood in the M-Step is used when updating parameters.

Mixture Model: Inference & parameter estimation using EM (extra slide 2)

M-Step: Update the parameters given the responsibilities

$$p(\pi_{1:K}, \mu_{1:K}) = Dir(\boldsymbol{\pi} \mid \boldsymbol{\delta}) \prod_{k=1}^{K} Beta(\mu_k \mid \alpha, \beta)$$
 Priors

$$\mathcal{O} = Q + \log p(\pi_{1:K}, \mu_{1:K})$$
 Complete data log likelihood + log priors

• The object function $\mathcal O$ is used to obtain the update equations for $\pi_{1:K}$ and $\mu_{1:K}$

$$\frac{\partial \mathcal{O}}{\partial \mu_k} = 0$$
, find $\hat{\mu}_k$ and $\frac{\partial \mathcal{O}}{\partial \pi_k} = 0$, find $\hat{\pi}_k$

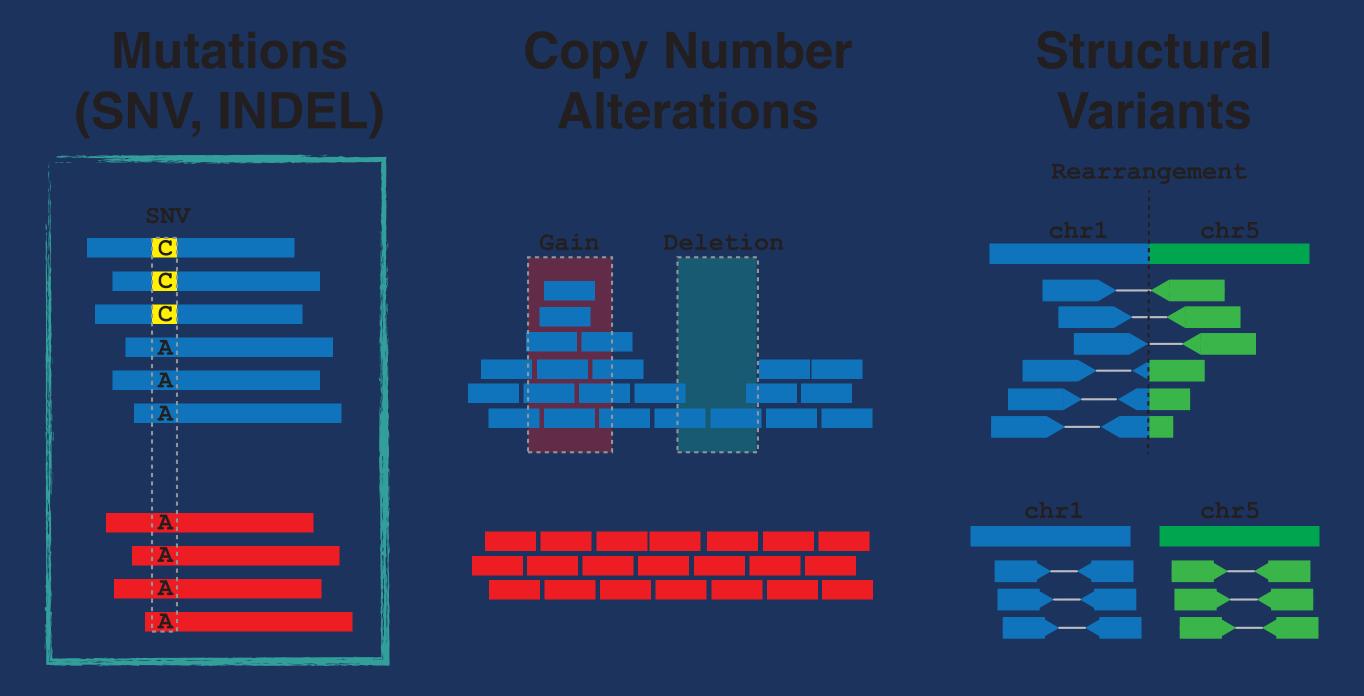
EM Convergence: after each iteration, monitor the log posterior

$$\mathcal{E} = \sum_{i=1}^{T} \log \left(\sum_{k=1}^{K} \pi_k Bin(x_i | \mu_k, N_i) \right)$$
 Incomplete Data Log likelihood

$$\log \mathbb{P}(\pi_{1:K}, \mu_{1:K} | x_{1:T}) = \ell + \log p(\pi_{1:K}, \mu_{1:K})$$
 Log posterior

- If the log posterior, $\log \mathbb{P}(\pi_{1:K}, \mu_{1:K} | x_{1:T})$, stops increasing by ϵ , then EM is converged.
- If not using a Bayesian framework, then use the log likelihood, ℓ , to monitor convergence.

2. Detecting Mutations in Cancer Genomes

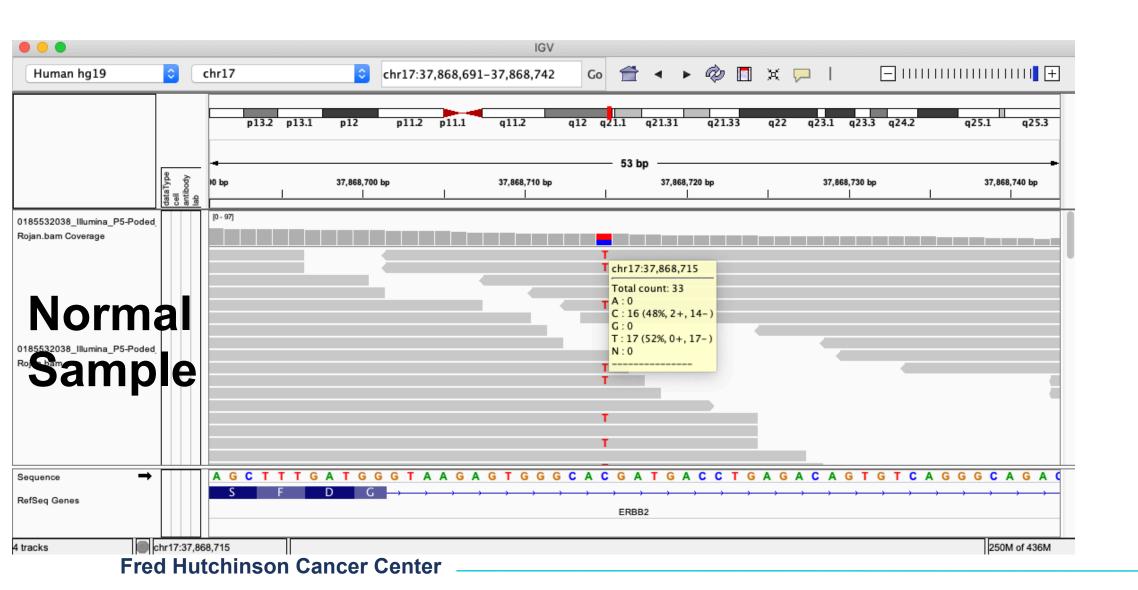


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Visual inspection using IGV: Germline SNVs

Integrative Genomics Viewer (https://software.broadinstitute.org/software/igv)

- ~1.5 to 2 million SNPs per individual
- Identify SNPs from normal peripheral blood mononuclear cells (PBMC)



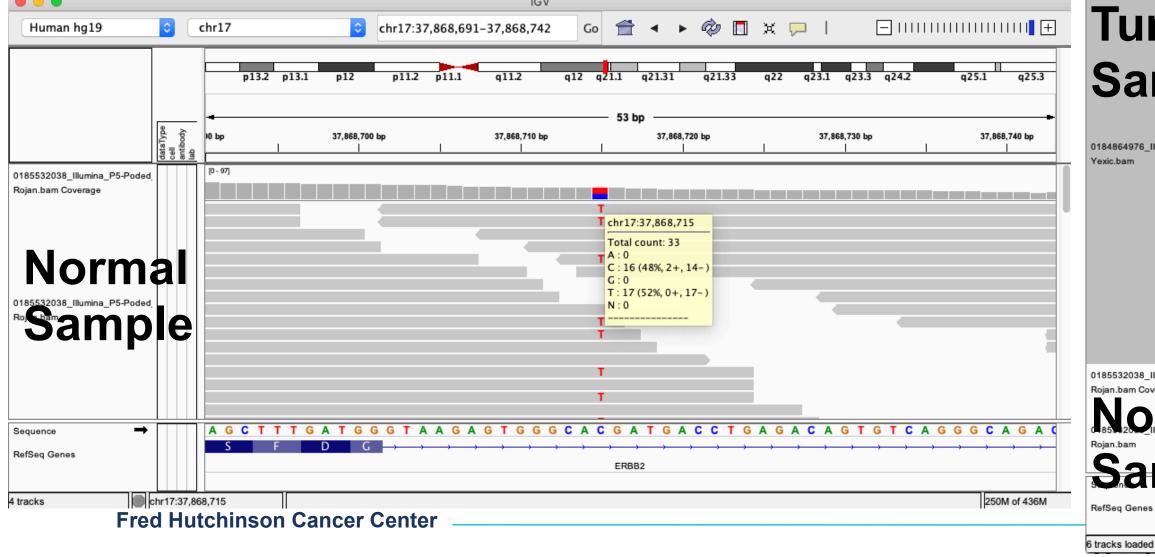
Heterozygous SNP with 17 reads containing the variant and having depth 33 reads

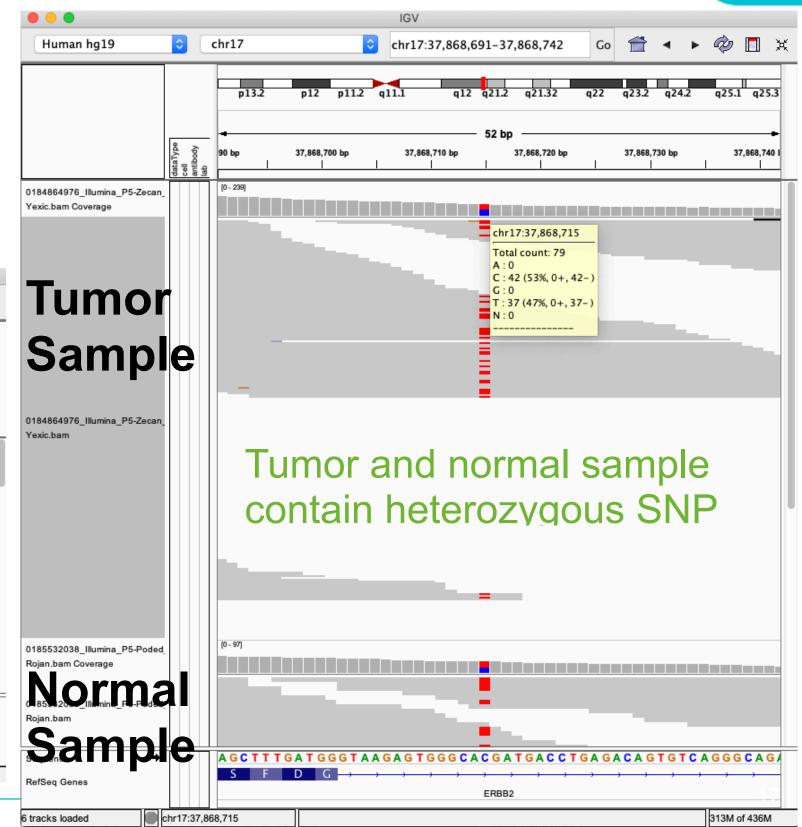
17/33 (48%) variant allele fraction (VAF)

Visual inspection using IGV: Germline SNVs

Integrative Genomics Viewer (https://software.broadinstitute.org/software/igv)

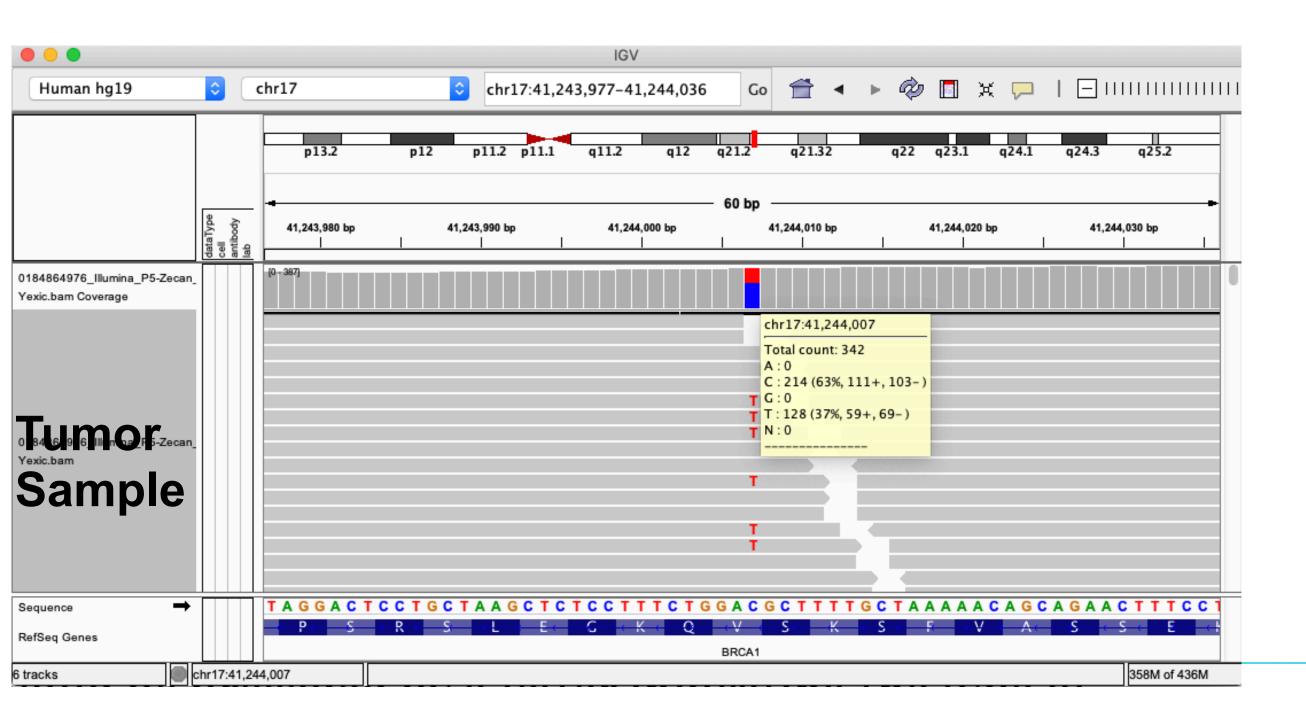
- ~1.5 to 2 million SNPs per individual
- Identify SNPs from normal peripheral blood mononuclear cells (PBMC)





Visual inspection using IGV: Somatic SNVs

- Somatic SNV requires comparing case (tumor) with control (PBMC)
- On the order of 10 to 10^4 number of mutations

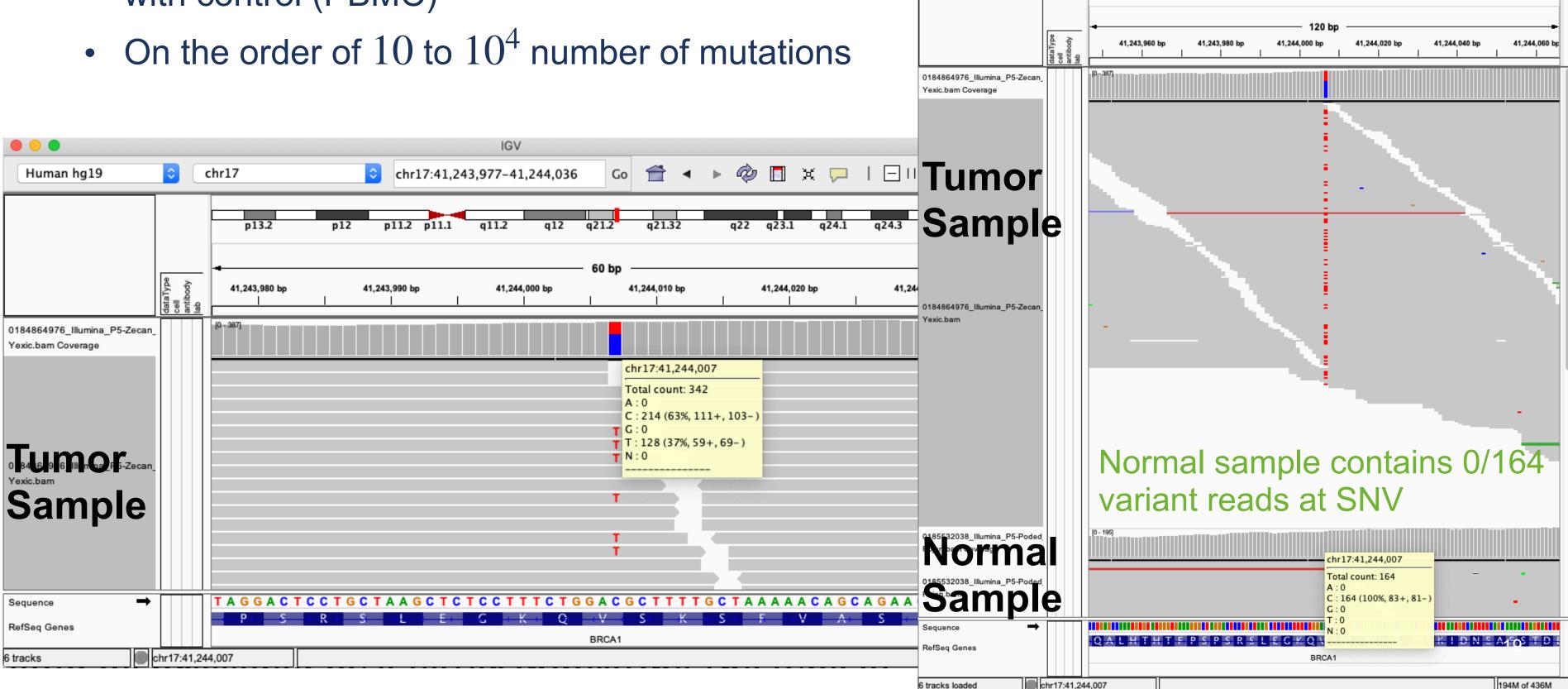


Potential SNV with 128/342 (37%) VAF

p.V1181I

Visual inspection using IGV: Somatic SNVs

Somatic **SNV** requires comparing case (tumor) with control (PBMC)

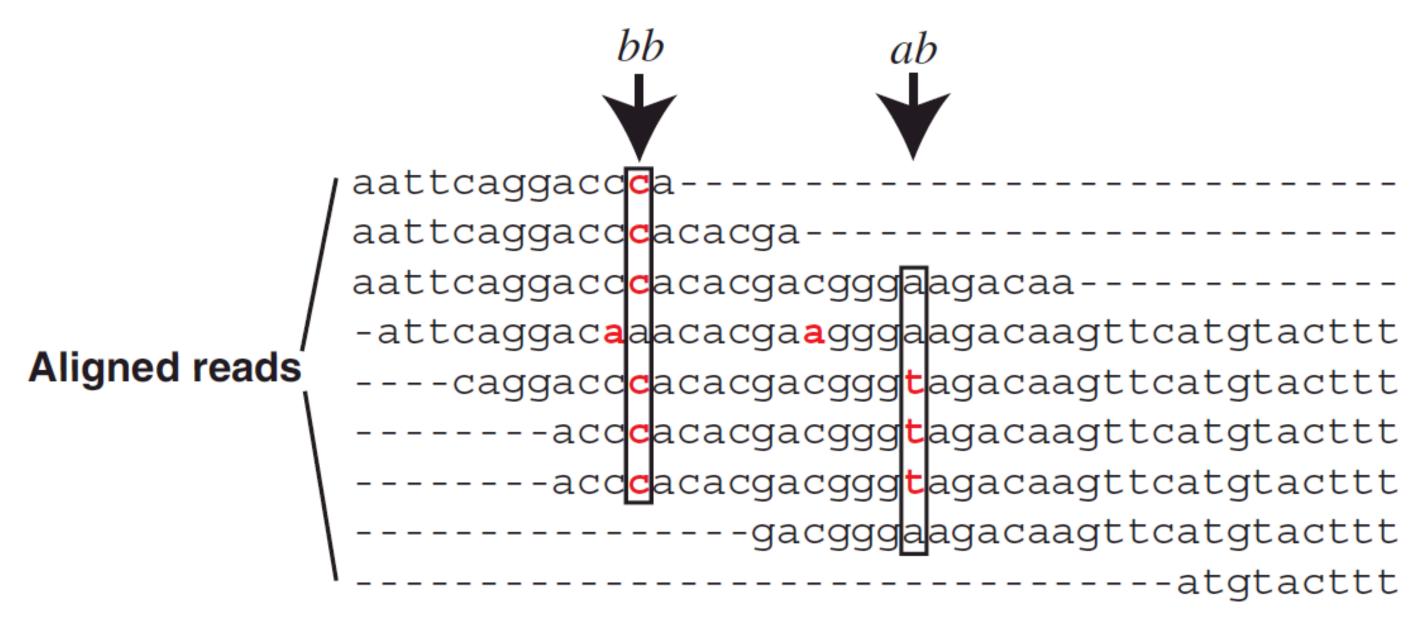


Human hg19

chr17

chr17:41,243,947-41,244,067

Single Nucleotide Variant (SNV) Calling: Single Sample



Reference seq aattcaggaccaacacgacgggaagacaagttcatgtacttt

Allelic counts

SNV Variant Allele Fraction and Genotypes

Variant Allele Fraction (VAF) Analysis

Genotypes: AA, AB, BB

Homozygous Heterozygous Homozygous Variant (not SNV) (Het SNV) (Homd SNV)

Genotype	AA	AB	BB
Allelic Fraction	~1.0	~0.5	~0

- Allelic Fraction is defined as the fraction of reference reads, $\frac{A}{N}$, where depth N=A+B
- Values in the table are the expected proportions of reference reads for each genotype
- Why might the observed allelic fractions be different than the expected values?

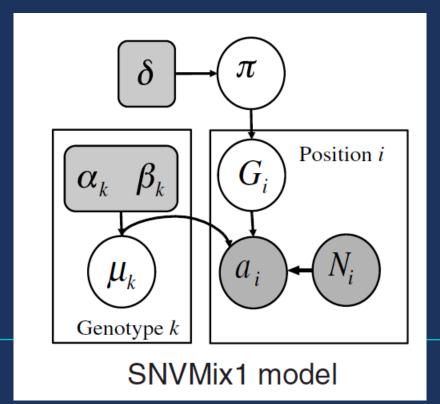
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3. Mixture Model for SNV Detection

- SNVMix probabilistic model and EM inference
- Predicting somatic SNVs in cancer

References:

- Goya et al. SNVMix: predicting single nucleotide variants from next-generation sequencing of tumors.
 Bioinformatics 26:730-36 (2010)
- Roth et al. JointSNVMix: a probabilistic model for accurate detection of somatic mutations in normal/ tumour paired next-generation sequencing data. Bioinformatics 28:907-13 (2012)



Mapping the Referee Example to Mutation Calling



Referee Coin Toss Example

<u>Data</u>

Referees $1, \dots, T$

For each Referee i

- Coin Tosses: N_i
- Count of heads: x_i
- Count of tails: $N_i x_i$

<u>Parameters</u>

Probability to draw coins: π_{fair} , π_{heads} , π_{tails}

Probability of heads for 3 types of coins

 μ_{fair} , μ_{heads} , μ_{tails}

<u>Responsibilities</u>

Probability that Referee i used coin k: $\gamma(Z_i = k)$

Mutation Calling from Sequencing Data

Data

Genomic loci 1,..., T

For each locus i

- Depth (total reads): N_i
- Count of reference reads: x_i
- Count of variant reads: $N_i x_i$

<u>Parameters</u>

Probability of genotypes: $\pi_{AA}, \ \pi_{AB}, \ \pi_{BB}$

Probability of reference base for 3 genotypes:

$$\mu_{AA}, \mu_{AB}, \mu_{BB}$$

<u>Responsibilities</u>

Probability that locus i has genotype k: $\gamma(Z_i = k)$

SNVMix: Probabilistic Model

Sequence Data

There are T different genomic loci with read depths $N = \{1, ..., N_T\}$ and reference base counts $\mathbf{x} = \{1, ..., x_T\}$. There are K = 3 different possible genotypes AA, AB, BB

Mixture Model Setup

- 1. The probabilities for the genotypes are π_{AA} , π_{AB} , π_{BB}
- 2. Thus, a specific genotype $k \in AA$, AB, BB can be assigned to the **latent state** Z_i at locus i with these probabilities

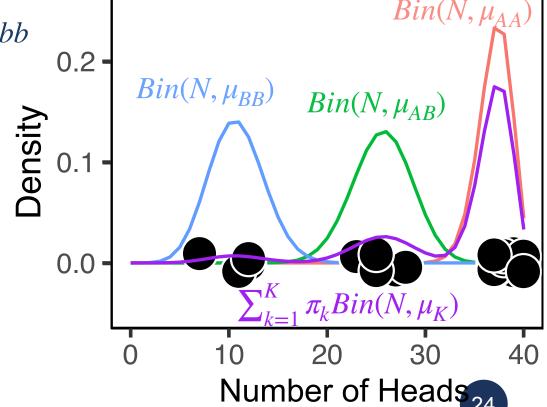
$$p(Z_i = k \mid \pi_{1:K}) = \begin{cases} \pi_{AA} \text{ if } k = AA \\ \pi_{AB} \text{ if } k = AB \\ \pi_{BB} \text{ if } k = BB \end{cases}$$

- 3. The probability of observing a reference base for the genotypes are $\mu_{aa}, \mu_{ab}, \mu_{bb}$
- 4. The likelihood is a **3-component mixture of binomials**

$$p(x_i | N_i, \mu_{1:K}, \pi_{1:K}) = \sum_{k=1}^K \pi_k Bin(x_i | N_i, \mu_k)$$

5. The **priors** for genotype $k \in \{aa, ab, bb\}$ in the model are

$$p(\pi_{1:K} | \delta_{1:K}) = Dirichlet(\pi_{1:K} | \delta_{1:K})$$
$$p(\mu_k | \alpha_k, \beta_k) = Beta(\mu_k | \alpha_k, \beta_k)$$



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SNVMix: Inference & parameter estimation using EM (revisited)

E-Step: compute responsibilities

1. What is the probability of locus i having genotype k?

$$\gamma(Z_{i} = k) = \frac{\pi_{k}Bin(x_{i} | N_{i}, \mu_{k})}{\sum_{j=1}^{K} \pi_{j}Bin(x_{i} | N_{i}, \mu_{j})}$$

Responsibilities

Matrix $T \times K$

M-Step: update parameters

2. What is the probability of genotype k?

$$\hat{\pi}_{k} = \frac{\sum_{i=1}^{T} \gamma(Z_{i} = k) + \delta(k) - 1}{\sum_{j=1}^{K} \left\{ \sum_{i=1}^{T} \gamma(Z_{i} = j) + \delta(j) - 1 \right\}}$$

MAP for π

3. What is the probability of observing a reference base for genotype k?

$$\hat{\mu}_k = \frac{\sum_{i=1}^T \gamma(Z_i = k) x_i + \alpha_k - 1}{\sum_{i=1}^T \gamma(Z_i = k) N_i + \alpha_k + \beta_k - 2}$$

MAP for μ

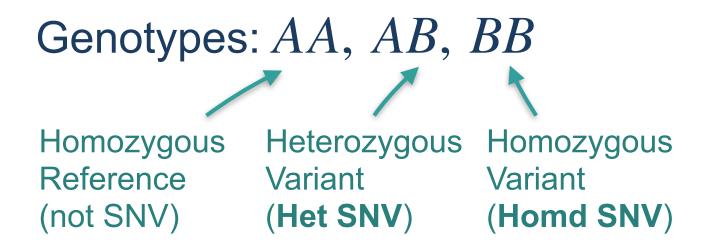
Evaluate the log likelihood and log posterior: use updated parameters

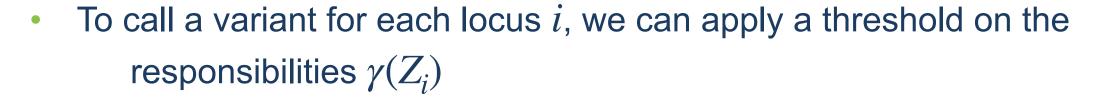
$$\log \mathbb{P} = \sum_{i=1}^{T} \log \left(\sum_{k=1}^{K} \hat{\pi}_k Bin(x_i | \hat{\mu}_k, N_i) \right) + \log Dir(\hat{\pi}_k | \delta_k) + \sum_{k=1}^{K} \log Beta(\hat{\mu}_k | \alpha_k, \beta_k)$$

Log posterior

Iterate between E-Step and M-Step: stop when $\log \mathbb{P}$ changes less than ϵ compared to previous EM iteration.

SNVMix: Calling somatic SNVs from genotype inference





Responsibilities			
Locus	AA	AB	ВВ
1	$\gamma(Z_1 = AA)$	$\gamma(Z_1 = AB)$	$\gamma(Z_1 = BB)$
2	$\gamma(Z_2 = AA)$	$\gamma(Z_2 = AB)$	$\gamma(Z_2 = BB)$
3	$\gamma(Z_3 = AA)$	$\gamma(Z_3 = AB)$	$\gamma(Z_3 = BB)$
Т	$\gamma(Z_T = AA)$	$\gamma(Z_T = AB)$	$\gamma(Z_T = BB)$

- Sum $\gamma(Z_i=AB)$ and $\gamma(Z_i=BB)$ to get the overall probability (either genotype AB or BB) that locus i is a variant containing the non-reference allele (B)
- Additional steps required for filtering and determining if variant is somatic vs germline
 - Minimum 3 variant reads $(N_i x_i)$ is typically required
 - Account for mapping and base qualities of sequenced reads (i.e. SNVMix2)
 - Compare locus i in tumor sample to (1) matched normal sample, (2) germline databases

SNV Genotyping Callers

Variant Allele Fraction Analysis

Reference Genome

Normal

Tumour

Allelic Counts

Single sample

Genotypes: AA, AB, BB

Homozygous Reference (not SNV)

Heterozygous Variant (Het SNV)

Homozygous

Variant Allelic Counts

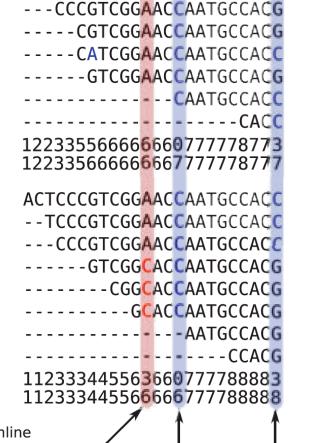
(Homd SNV)

Joint tumor-normal

Joint Genotypes:

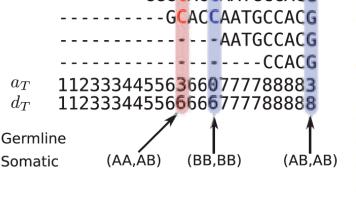
$g_N \backslash g_T$	AA	AB	ВВ	
AA	0.01	0.95	0.00	
AB	0.00	0.04	0.00	
ВВ	0.00	0.00	0.00	

ACTCCCGTCGGAACGAATGCCACG



ACTCCCGTCGGAACCAATGCC - ---CTCCCGTCGGAACCAATGCCACC

GTCG(GAACCAATG	CCACG
	- <mark>-</mark> <mark>C</mark> AATG	CCACC
	- -	-CACC
12233556666		
1223356666	5 <mark>6</mark> 66 7 7777	78777
ACTCCCGTCG	GAACCAATG	CCACC
TCCCGTCG	GAACCAATG	CCACC
CCCGTCG	GAACCAATG	CCACC
GTCG	GCACCAATG	CCACG
CG	GCACCAATG	CCACG
	GCACCAATG	CCACG
	- - - AATG	CCACG
		CCACG
11233344550		
11233344550	566667777	88888
nline	7	1
atic (AA.AB)	(BB.BB)	(AB.AB)



BB 0.00 0.00	
el or panel: Machine Learning (supervi	sed)

Variant caller	Type of variant	Single-sample mode	Type of core algorithm
BAYSIC [48]	SNV	No	Machine learning (ensemble caller)
CaVEMan [34]	SNV	No	Joint genotype analysis
deepSNV [38]	SNV	No	Allele frequency analysis
EBCall [37]	SNV, indel	No	Allele frequency analysis
FaSD-somatic [31]	SNV	Yes	Joint genotype analysis
FreeBayes [44]	SNV, indel	Yes	Haplotype analysis
HapMuC [42]	SNV, indel	Yes	Haplotype analysis
JointSNVMix2 [30]	SNV	No	Joint genotype analysis
LocHap [43]	SNV, indel	No	Haplotype analysis
LoFreq [36]	SNV, indel	Yes	Allele frequency analysis
LoLoPicker [39]	SNV	No	Allele frequency analysis
MutationSeq [45]	SNV	No	Machine learning
MuSE [40]	SNV	No	Markov chain model
MuTect [35]	SNV	Yes	Allele frequency analysis
SAMtools [8]	SNV, indel	Yes	Joint genotype analysis
Platypus [41]	SNV, indel, SV	Yes	Haplotype analysis
qSNP [24]	SNV	No	Heuristic threshold
RADIA [26]	SNV	No	Heuristic threshold
Seurat [33]	SNV, indel, SV	No	Joint genotype analysis
Shimmer [25]	SNV, indel	No	Heuristic threshold
SNooPer [47]	SNV, indel	Yes	Machine learning
SNVSniffer [32]	SNV, indel	Yes	Joint genotype analysis
SOAPsnv [27]	SNV	No	Heuristic threshold
SomaticSeq [46]	SNV	No	Machine learning (ensemble caller)
SomaticSniper [28]	SNV	No	Joint genotype analysis
Strelka [17]	SNV, indel	No	Allele frequency

analysis

Ion Torrent specific

Heuristic threshold

Heuristic threshold

Joint genotype analysis

Cohort leve

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SNV, indel

SNV

SNV, indel, SV Yes

Yes

Yes

No

SNV, indel, SV

TVC [97]

VarDict [18]

VarScan2 [9]

Virmid [29]

Somatic SNV Detection using Joint Inference from Tumor-Normal Pairs



1.Latent variable state space

- 9 genotype pairs (k_n, k_t)
- $n, t \in \{AA, AB, BB\}$

• 9 mixture weights $\pi_{(k_n,k_t)}$

Normal, n

rumor, t			
$k_n \backslash k_t$	AA	AB	ВВ
AA	0.01	0.95	0.00
AB	0.00	0.04	0.00
ВВ	0.00	0.00	0.00

Tumor t

Reference Genome

Normal

ACTCCCGTCGGAACGAATGCCACG

ACTCCCGTCGGAACCAATGCC - --CTCCCGTCGGAACCAATGCCACC ---CCCGTCGGAACCAATGCCACG ----CGTCGGAACCAATGCCACG ----CATCGGAACCAATGCCACC

----GTCGGAACCAATGCCACG

ACTCCCGTCGGAACCAATGCCACC

--TCCCGTCGGAACCAATGCCACC

---CCCGTCGGAACCAATGCCACC

----GTCGGCACCAATGCCACG

1223355666666660777778773 **Allelic Counts** 122335666666667777778777

3. Joint binomial mixture model

2. Probability of the genotypes

9-component mixture model

$$p(x_i^n, x_i^t | N_i^n, N_i^t, \mu_{1:K}^n, \mu_{1:K}^t) = \sum_{k_n=1}^K \sum_{k_t=1}^K \pi_{(k_n, k_t)} Bin(x_i^n | N_i^n, \mu_{k_n}^n) Bin(x_i^t | N_i^t, \mu_{k_t}^t)$$

with 9 parameter tuples (μ^n, μ^t)

Tumour

Allelic Counts

-----CGGCACCAATGCCACG -----GCACCAATGCCACG 112333445563660777788883

112333445566666777788888

Germline Somatic

(AA,AB)

(BB,BB)

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Homework #7: Single-nucleotide Genotype Caller

Implement a standard binomial mixture model described in Lecture 2.

- Learn the parameters and infer the genotypes
- Annotate the mutation status for a set of genomic loci.
- Expected outputs for each question will be provided so that you can check your code.
- RStudio Markdown and Python Jupyter Notebook templates provided.

Due: May 19th, 2023

