DEMOCRITUS SPECULATED that everything is made of small, indivisible units he called "atoms." He was correct, but the project of identifying and classifying these indivisible units got off to a slow start. Atoms were initially thought to be like tiny rocks whose shapes determined their properties. For example, a substance that stings when it is touched might be made of atoms covered in sharp spikes. These models provided interesting explanations, but no testable predictions about how substances interact.

Elements of Chemistry

Real progress began in the late eighteenth century when chemists, notably Antoine-Laurent de Lavoisier, began taking careful measurements of reactants and products to test theories about the identities and properties of elements. Lavoisier listed thirty-three elements in his 1789 *Elements of Chemistry*. By the late nineteenth century, chemists had identified several dozen elements and could predict the quantities of elements required to make certain compounds.

In 1871, Russian chemist Dmitri Mendeleev organized the sixtysix known elements into a repeating pattern according to their chemical properties. He used this pattern to create the first draft of the modern periodic table of the elements. The beginning of Mendeleev's table (table 1.1) shows several familiar elements in their correct positions.

Mendeleev identified several gaps in his table and predicted new elements to fill these gaps – and he predicted the new elements' properties. The discoveries of Gallium (1875), Scandium (1879), and Germanium (1886), each with the predicted properties, convinced most scientists that Mendeleev's table was correct and useful.

The periodic table of the elements, expanded by the discovery of many more elements, is the foundation of chemistry to this day. We now define "atom" as the smallest unit of an element having the chemical properties of that element. Although we will discover that there are smaller, more fundamental particles, the periodic table will always be the definitive list of atoms.

ELECTRIC SPARKS TO ELECTRON BEAMS

While chemists discovered and studied more new elements, physicists turned their attention to electricity, especially electric sparks. Sparks are exciting and easy to make, so physicists and curious children have always studied them with great enthusiasm. Physicists of the nineteenth century knew that sparks carry electrical charge from one object to another. However, sparks happen so quickly that it is not obvious which way the charge is moving.

By convention sweet and by convention bitter, by convention hot, by convention cold, by convention color; but in reality atoms and void.

Democritus c.460 – c.370 BCE

Н						
Li	Be	В	C	N	O	F
Na	Mg	Al	Si	P	S	Cl
K	Ca					

TABLE 1.1 The first periodic table of the elements, 1871

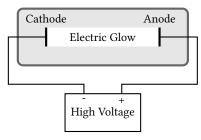


FIGURE 1.1 An evacuated tube for creating a visible beam of current. Electrons traveling from the cathode to the anode create a glow as they collide with gas molecules.

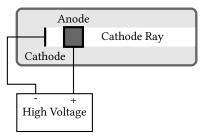


FIGURE 1.2 In a cathode-ray tube the anode is a hoop that electrons pass through. The electrons continue in a beam until reaching the end of the tube. Since the beam starts on the cathode, it is called a cathode ray.

We now know that sparks are streams of electrons. Electrons pick up speed very quickly in a spark. They move so quickly that when they collide with something, like an air molecule, the collision produces a small but visible flash. The glowing path of a spark beam is a multitude of these flashes. This is the case with small sparks from static electricity and, more spectacularly, with lightning.

Sparks are much easier to produce in the absence, or near absence, of air. Physicists produced sealed glass "tubes" (fig. 1.1) for their experiments which had nearly all air removed, allowing the electrons to travel farther between each collision. Inside the sealed tube are two metal plates held by wires going through the tube's glass wall. These wires are connected to a high voltage power supply. The metal plate connected to the power supply's negative terminal is called the cathode, while the plate connected to the positive terminal is called the anode. The power supply drives an excess of electrons to the cathode, making the cathode negatively charged. The power supply pulls electrons from the anode, leaving the anode positively charged.

Since like charges repel, the electron excess on the cathode can become great enough to accelerate electrons away from the cathode toward the anode, producing a visible beam of glowing current in the tube. Within these evacuated tubes current can travel much farther than most sparks in open air, and the current can be maintained to produce a continuous glowing beam. The beam of electrons is visible in sealed tubes with most, but not all, of the air removed. When there is no air in the tube the beam is invisible because the electrons do not run into anything along their path.

If the anode is shaped like a hoop it can mostly avoid getting hit by the electrons, as shown in figure 1.2. Electrons are attracted by the anode, but as they approach they are going so fast that they shoot right through the center of the hoop and continue until they run into the end of the tube. These continuing electrons revealed to physicists that the beam began at the cathode, and the beams became known as *cathode rays*. Tubes that are designed so that the cathode rays miss the anode and strike the tube's wall are called *cathode ray tubes*.

Twentieth century televisions are direct descendants of the nine-teenth century cathode ray tubes. At the back of the television is an electron gun that produces a cathode ray pointed at the back of the screen. The screen is covered with phosphorus or a similar material that glows brightly when hit by electrons. The cathode ray is bent by electric and magnetic fields so that it moves rapidly all over the screen. The beam's intensity changes as it moves, drawing a picture on the screen. Televisions and computer monitors of this type are often called CRTs: cathode ray tubes.

Cathode rays provided a new way for physicists to study extremely small pieces of matter. Similar beams with ever increasing energy have been become the primary tool in the search for the fundamental pieces of matter. Understanding these beams requires a little knowledge about electrical energy and one of the units used to measure energy, the *electron-volt* or eV.

The concept behind the electron-volt is quite simple. Batteries store electrical energy which can be used to run electrical devices. The energy is retrieved by allowing electrons to flow through a circuit from one end of the battery to the other. The voltage of the battery is a measure of how much energy is provided by each electron flowing through the circuit. A nine-volt battery, for example, provides nine electron volts (9 eV) of energy for every electron that makes the journey. An electron volt is a very small amount of energy, about the amount of energy released in the reaction of a single molecule in the battery. Electron volts are related to our other unit of energy, the joule.

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$

A typical nine-volt battery has about 10^{22} electrons stored that can make the journey through the circuit, so the battery can provide about 9×10^{22} eV of energy, which is a significant amount of energy of energy.

$$9 \times 10^{22} \text{ M/} \left(\frac{1.60 \times 10^{-19} \text{ J}}{1 \text{ M/}} \right) = 14\,000 \text{ J}$$

Individual chemical reaction typically release a few electron volts of energy or less, making the volt a convenient unit for items powered by chemical reactions, like batteries.

While the electron volt is a small amount of energy, it is enough to get an electron moving quite quickly. By the mid nineteenth century physicists were not using a few volts to make their sparks, but several kilovolts (1 kV = 1000 V).

EXAMPLE 1.1 A cathode ray tube is powered by a 5.0 kV power supply. If an electron makes the trip from cathode to anode without running into anything, what will its kinetic energy be when it passes the anode? Give your answer in both electron volts and joules.

A $5.0\,\mathrm{kV}$ power supply delivers $5.0\,\mathrm{keV}$ of energy to each electron. If the electron does not lose any energy in collisions, its kinetic energy will be $5.0\,\mathrm{keV}$, or

$$K = 5.0 \times 10^3 \text{ eV} \left(\frac{1.60 \times 10^{-19} \text{ J}}{1 \text{ eV}} \right) = 8.0 \times 10^{-16} \text{ J}$$

Once the electrons pass the anode they no longer feel much force and will continue with 5.0 keV of kinetic energy until they run into something.

Example 1.2 You decide to make a cathode ray whose electrons are going 5.0% of the speed of light ($c = 3.00 \times 10^8 \, \text{m/s}$). You build a tube that has no air in it, so that the electrons will not be slowed by collisions with air molecules. What voltage do you need from your power supply?

Five percent of the speed of light is $v = 1.50 \times 10^7$ m/s. This is very fast, but still slow enough that we can use the usual kinetic energy formula, $K = \frac{1}{2}mv^2$, where the mass of an electron is $m = 9.11 \times 10^{-31}$ kg. The electron's kinetic energy must be

$$K = \frac{1}{2}mv^2 = (9.11 \times 10^{-31} \text{ kg})(1.50 \times 10^7 \text{ m/s})^2 = 1.02 \times 10^{-16} \text{ J}$$

Convert this to electron volts.

$$K = 4.10 \times 10^{-14} \, \text{M} \left(\frac{1 \, \text{eV}}{1.60 \times 10^{-19} \, \text{M}} \right) = 640 \, \text{eV}$$

All of the energy provided by the power supply is going to the electron's kinetic energy, so the power supply must provide 640 eV to each electron. The power supply's voltage, therefore, must be 640 V. Kilovolt power supplies easily get electrons up to a significant fraction of the speed of light!

Example 1.3 While carefully connecting a $640\,\mathrm{V}$ power supply to your cathode ray tube, you wonder what the average force is on each electron as it is accelerated up to 10% of the speed of light. The distance from the cathode to the anode is $3.0\,\mathrm{cm}$. What is the average force?

We have not learned anything about how the power supply gives energy to the electrons (that is the next section) so we will not include the power supply or any potential energy in the system. The system will just be a single electron's kinetic energy, which is increased by work done on the electron by the mysterious power supply to the kinetic energy we found in example 1.2 above. Start with conservation of energy.

$$H_{i} + W + \cancel{Q} = H_{f}$$

$$\cancel{K}_{i} + F \Delta x = K_{f}$$

$$F = \frac{K_{f}}{\Delta x} = \frac{1.02 \times 10^{-16} \text{ J}}{3.0 \times 10^{-2} \text{ m}} = 3.4 \times 10^{-15} \text{ N}$$

We used the kinetic energy in joules to get a force in newtons. What if we had used the kinetic energy in electron volts for the last step?

Electrical Potential 5

$$F = \frac{K_{\rm f}}{\Delta x} = \frac{640 \,\text{eV}}{3.0 \times 10^{-2} \,\text{m}} = 2.1 \times 10^4 \,\text{eV/m}$$

This is the same force, 2.1×10^4 eV/m = 3.4×10^{-15} N. Sometimes measuring force in eV/m will be the more convenient, especially when dealing with tiny particles. Sometimes joules are more convenient. Both are acceptable units of force.

ELECTRICAL POTENTIAL

The *electrical potential*, *V*, is a field that exists everywhere. At any location the electrical potential can be positive, negative, or zero. It is mostly zero, but electric charges alter the electrical potential. Positive charges produce a region of positive potential, while negative charges create a region of negative potential. Electrical potential obeys the superposition principle (just like waves), so that the potential at any location is the sum of the contributions coming from all of the charges in the area.

Electrical potential energy is energy stored in the electrical potential. Notice that electrical potential and electrical potential energy are two distinct things. While the general mathematical formula for this energy is quite daunting, we will be interested only in situations where the answer is quite simple. When a charge q is placed at a location where the potential is V, the electrical potential energy is

$$U = qV$$

The potential V is the potential produced by any other charges, not including the charge q. The charge q can never get away from its own contribution to the electrical potential, so that energy is not convertible to other forms and we just leave it out. (Leaving it out also avoids some mathematical headaches.)

The charge q can be positive or negative, and the potential V produced by other charges can also be positive or negative, so the potential energy U can be positive or negative. Objects that have no charge are neutral, q=0, so they do not have electrical potential energy. Similarly, a charge q in a region where the electrical potential is zero also has no potential energy. While the electrical potential field exists everywhere, we sometimes say that a region has no electrical potential. This actually means that the value of the electrical potential is zero in that region.

Armed with the formula for electrical potential energy, we have all of the tools we need to explain the well known facts that *opposite* charges attract while like charges repel. First, find the electric potential due to one charge. Next, find the potential energy when the second charge is added. Finally, use Hamilton's equation to find the force. For opposite charges the force on the second charge will be toward the first charge. For like charges the force on the second will be away from the first. The method can be reversed to find the force

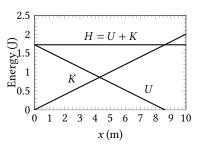


FIGURE 1.3 The block's energy as a function of position for example ??.

on the first charge, which will give an equal and opposite force, in agreement with Newton's Third Law.

The forces determined from the electric potential are enough to determine the motion of the charges, which can be done with a computer simulation or, in simple cases, with calculus.

PARTICLES IN ELECTRIC FIELDS

Finding the electric force on a charge q is easy with the *electric field*, denoted by \vec{E} .

$$\vec{F} = q\vec{E}$$

The electric field is a vector field which exists everywhere in space. (The electric field vector could be the zero vector if there are no charges around.) A charge placed where the electric field is not zero will feel a force. A positive charge feels a force is in the direction of the electric field, while a negative charge feels a force in the opposite direction. A neutral particle does not feel any force from electric fields.

The electric field is computed from the electric potential; it is not independent. The electric field vector points in the direction of decreasing electric potential. The electric field's magnitude is the magnitude of electric potential's slope in that direction. The vector's individual components are the potential's slope in the coordinate directions.

$$E_x = -\frac{\Delta V}{\Delta x}$$
 $E_y = -\frac{\Delta V}{\Delta y}$ $E_z = -\frac{\Delta V}{\Delta k}$

Since the electric potential is measured in volts, the electric field is in volts per meter.

These equations for the electric field due to the electric potential look very much like Hamilton's equations for the force due to potential energy, including the minus signs. That is no coincidence! The similarity is the reason the electric field is so useful. The electric field gives another – often more convenient – route for finding the force on a charge.

The first route for finding the force on a charge q, which you already learned, is to start with the electric potential, multiply by q to get the potential energy, and then find the slope to get the force. The second method is to start with the potential, find the slope to get the electric field, and then multiply by q to get the force. Either method gives the same force.

The hard step in either method is finding the slope, which can require calculus or drawing tangent lines on graphs. Using the electric field gets that step out of the way. The remaining steps – finding the field's direction and multiplying by the other charge – do not require sophisticated mathematics.

The direction of the electric field is always towards lower potential. A positive charge creates a region of positive potential, with the highest potential close to the charge, so the electric field points away from a positive charge, toward the lower potential far away. A negative charge creates a region of negative potential, with the most negative potential close to the charge, so the the electric field points toward a negative charge, toward the nearby lower potential. In both cases the electric field has the greatest magnitude close to the charge, where the potential is changing most rapidly with distance. Far from the charge, where the potential is inching towards zero, the magnitude of the electric field is small.

The electric field gives another explanation for why like charges repel and opposite charges attract. For example, a positive charge produces an electric field that points away from it. Another positive charge will feel a force in the direction of this field, so the second positive charge is repelled by the first. If the second charge is negative, it will feel a force opposite the electric field and be attracted to the positive charge. Take a moment to determine the direction of the force that a negative particle would exert on another charge, either positive or negative.

The electric field, like the electric potential, obeys the superposition principle, but the electric field vectors must be added *as vectors* which makes the addition more complicated than it is for the electric potential. A charge does not feel its own electric field, only the total field produced by all other charges.

Historically, all of the steps above were discovered in reverse order. The force law between charges was discovered by Charles Coulomb in 1785, and is called Coulomb's law. The electric field was described by Michael Faraday in his *Experimental Researches in Electricity*, begun in 1831. The derivation of the electrical field from the electric potential was given by James Clerk Maxwell in *A Dynamical Theory of the Electromagnetic Field*, published in 1865.

MAGNETIC FIELD AND MAGNETIC FORCE

The magnetic field, like the electric field, is a vector field that exists everywhere. The value of the magnetic field can be zero, but this is actually rare. Earth is not electrically charged, so it does not produce an electric field, but Earth does produce a huge magnetic field which extends far out into space. This magnetic field is produced by electric currents deep in Earth's molten core, powered by convection currents and Earth's rotation. This magnetic field protects Earth from the dangerous solar wind, a wind of fast charged particles coming at us constantly from the Sun.

Mars, being somewhat smaller than Earth, cooled more quickly after the formation of the solar system, so it no longer has a molten core and therefore has lost its magnetic field, exposing it to the solar

wind. The solar wind gradually blew Mars's atmosphere away, making it a rather inhospitable place. Most planets, as well as the Sun, have significant magnetic fields.

Like the electric field, the magnetic field exerts a force on charged particles, but only on changed particles that are moving. The direction of the magnetic force is *perpendicular* to the direction of the field and also *perpendicular* to the particle's direction of motion. This is described by a vector cross product.

$$\vec{F} = q\vec{v} \times \vec{B}$$

The magnitude of a cross product is the area of the little parallelogram made by the two vectors, in this case the vector $q\vec{v}$ and the vector \vec{B} . If the charged particle is moving perpendicular to the magnetic field's direction, then the vectors $q\vec{v}$ and \vec{B} are perpendicular, forming a rectangle with area qvB. If the particle is traveling along the magnetic field, then vector $q\vec{v}$ and \vec{B} are parallel (either pointing in exactly the same direction, or in exactly opposite directions), the parallelogram collapses, and the area is zero. In general, the vectors $q\vec{v}$ and \vec{B} make some angle θ and the magnitude of the field is

$$F = |q| vB \sin \theta$$

Again, for motion perpendicular to the field the angle between $q\vec{v}$ and \vec{B} is 90° and F = |q|vB. For motion parallel to the field the angle is 0° or 180° and F = 0.

The direction of the magnetic field is determined using the right hand rule. This is a fully three dimensional exercise, so you will need to train with an experienced right-hand-rule practitioner to avoid sign errors and potential injury. The three vectors in the magnetic force formula are assigned to different fingers on your right hand. The vector $q\vec{v}$ is assigned to your index finger, as if you are firing the charge like an imaginary bullet out of your straight, extended finger. However, if q is negative then you need to point your index finger in the direction *opposite* the velocity vector \vec{v} , keeping it extended and straight while reversing your entire hand.

The magnetic field vectors are assigned to your remaining fingers – lots of fingers for the lots of magnetic field vectors. These fingers are not extended and should bend naturally in the direction of the magnetic field. If the magnetic field is in the direction of $q\vec{v}$, so that all four fingers are extended, or if the magnetic field is opposite $q\vec{v}$ so that the three field fingers bend back into the palm of the hand, then the force is *zero*.

If the index finger and the remaining fingers produce some angel between 0° and 180° , then the thumb, the most forceful of fingers, shows the direction of the force. The thumb should be extended and

straight, perpendicular to both the extended index finger and the remaining bent fingers.

Gravitational forces are responsible for the orbits of celestial objects – moons obit planets, planets orbit stars, and stars orbit galaxies. Electrical forces are responsible for the orbits of electrons around the nucleus of an atom. In both cases the field, gravitational or electrical, is produced by an object at the center which causes an attractive force holding the smaller object in orbit.

Magnetic orbits are totally different because they have *nothing* at the center. This is possible because the magnetic force is perpendicular to the particle's motion, changing the particle's direction, but not its speed. As the particle's path bends, the direction of the force also changes, staying always perpendicular to the particle's velocity. This changing force will curve the particle's path around into a circle or a helix.

Circular magnetic orbits are used to keep particles orbiting in circular particle colliders. Charged particles in the solar wind follow tight helical orbits that follow Earth's magnetic field to the poles, where the particles crash into the atmosphere producing northern and southern lights.

The electric potential and the electric field are both very useful. The electric potential is especially useful when you want to understand the energy in the system, while the electric field is especially convenient when you want to understand the electric forces. We have learned about the magnetic field, which is convenient when we want to understand the magnetic forces. (The magnetic field is not quite as convenient as the electric field because of the cross product and the right hand rule, but it works.) Surely, you are now anxious to learn about the magnetic potential for situations where you want to study magnetic potential energy.

Unfortunately, I have bad news. The magnetic potential is quite complicated. It is actually a *vector* potential. This is related to the fact the magnetic force involves the velocity, which is also a vector. The magnetic potential energy involves the charge, the magnetic vector potential, and the velocity vector, which makes it complicated. The real killer, however, is the magnetic vector potential's contribution to a magnetic potential momentum! The formula is not complicated, but working with the potential momentum requires extreme mental discipline.

Fortunately, I have good news, too. Because the magnetic force is perpendicular to the charge's motion, magnetic forces never do any work! Magnetic potential energy only interacts with the kinetic energy of changes and currents though electric forces, which can do work. While I recommend learning vector calculus so you can contemplate the supreme beauty of the magnetic vector potential, you won't actually need the magnetic vector potential for any problems

		e			
Н					
Li Be	В	C	N	Ο	F
Na Mg	Al	Si	P	S	Cl
K Ca					

Table 1.2 The electron is lighter than any element and does not fit among the elements in the periodic table, 1897

in introductory physics. Use the $\it electric$ force, the magnetic force will not work! $^{\scriptscriptstyle 1}$

DISCOVERY OF THE FIRST SUB-ATOMIC PARTICLE

Cathode rays can be deflected by magnetic or electric fields. In 1897, J. J. Thompson performed a clever experiment where the magnetic and electric deflections would cancel out. The strengths of the electric and magnetic field that produced the cancelation could then be used to determine the velocity and mass of the electrons in the rays.

Electrons are far too light to be one of the elements, and they do not fit the pattern of the periodic table. These new particles provided our first glimpse into the world within the atom.

Notes

¹ Kenobi, Obi-Wan. Private communication.