

Part a:

~~Time~~ $\log(\log n)$ The runtime of void f1 would be $\log(\log n)$ because the algorithm is exponentially increasing in an exponential way.

~~$\log(n^n) = n \log n$~~

1	2	3	4	5
2	4	16	256	65,536
2^1	2^2	$(2^2)^2$	$((2^2)^2)^2$	$((2^2)^2)^2$

Part b: outside loop: $i/\sqrt{n} == 0$ gives us a run-time of \sqrt{n}

~~inside loop~~ ~~$\sum_{i=1}^{\sqrt{n}} i^3$~~ inside loop: $\sum_{i=1}^{\sqrt{n}} 1 = i^3 \quad \theta = n^3$

$$\sum_{i=1}^{\sqrt{n}} \theta(i) + \sum_{i=1}^{\sqrt{n}} \cdot \theta(n^3) = \theta(n^3 \cdot \sqrt{n}) = \theta(n^{\frac{7}{2}})$$

Part c: outer loop: $i: \theta = n$

outer loop: $k: \theta = n$

for loop: $\theta = \log n$ because of "m=m+m"

total run-time = $\theta(n^2) + \theta(n \log n) = \theta(n^2)$

↓ \rightarrow the inner for loop only runs $n \cdot \log n$

the if statement runs n^2 times

Part d: outer loop: $\theta = n$ $\sum_{n=2}^{n-1} \theta(1) = n \cdot \theta(1)$

(for)

first / two lines: $\theta(1) \cdot 2$

total runtime = $\theta(n) + \theta(1) + \sum_{k=1}^{\log_2(\frac{n}{10})} \theta(10 \cdot (\frac{3}{2})^{k-1})$

$$= \theta(n) + \theta(1) + \theta(10 \cdot (\frac{3}{2})^{\log_2(\frac{n}{10}) - 1})$$

$$= \theta(n) + \theta(1) + \theta(n)$$

$$= \theta(n)$$

1	2	3	...	k
10	$10 \cdot (\frac{3}{2})^{k-1}$	$10 \cdot (\frac{3}{2})^2$...	$10 \cdot (\frac{3}{2})^{k-1}$

$n = 10 \cdot (\frac{3}{2})^{k-1}$

$\log_2(\frac{n}{10}) = k-1$

$k = 1 + \log_2(\frac{n}{10})$

$k = \theta(\log_2(\frac{n}{10}))$