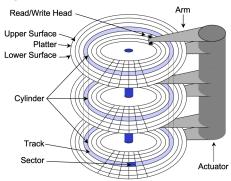
CS3223 AY23/24 SEM 2

01. DBMS STORAGE

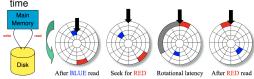
- · store data on non-volatile disk
- process data in main memory (RAM) (volatile storage)

Magnetic HDD



- · disk access time =

 - ullet rotational delay ullet wait for block to rotate under head
 - average rotational delay = time for $\frac{1}{2}$ revolutions
 - $\bullet = 0.5 imes rac{60}{ ext{rotational speed (RPM)}}$
 - ullet transfer time ullet move data to/from disk surface
 - = time for 1 revolution × # of requested sectors on the same track
- response time for disk access = queuing delay+access time



- command processing time: interpreting access command by disk controller (part of access time, considered negligible)
- small requests are dominated by seek time; large requests dominated by transfer time
- · access order:
 - 1. contiguous blocks within the same track (same surface)
 - 2. cylinder tracks within the same cylinder
 - 3. next cylinder

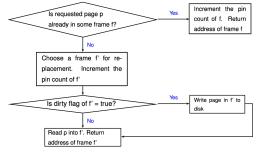
SSD (Solid-State Drive)

- no mechanical moving parts
- advantages: \checkmark significantly faster than HDD
- √ higher data transfer rate √ lower power consumption
- disadvantages: × update to a page requires erasure of multiple pages before overwriting page
- × limited number of times a page can be erased

Buffer Manager

- data is stored & retrieved in disk blocks (pages)
- each block = sequence of > 1 contiguous sectors
- buffer pool: main memory allocated for DBMS

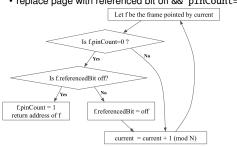
- partitioned into frames (block-sized pages)
- pin count: number of clients using page (initialised 0)
 - ¿0 ⇒ page is utilised by some transaction; don't replace
- · dirty flag: initialised false
 - $\operatorname{dirty} \to \operatorname{page}$ is modified & not updated on the disk
 - dirty page must be written back to the disk if the transaction has committed



! unpinning: update dirty flag to true if page is dirty

replacement policies

- decide which unpinned (pinCount==0) page to replace
- LRU uses a queue of pointers to frames with pinCount==0
- clock: cheaper than LRU, used in postgres
 - referenced bit turns on when pinCount==0
 - replace page with referenced bit off && pinCount==0

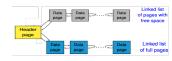


File abstraction

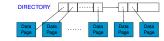
- · each relation is a file of records
- each record has a unique record identifier, RID
- heap file → unordered file
 - · vs sorted/hashed file: records are ordered/hashed

heap file implementations

- · linked list implementation
 - · header page: metadata about the file

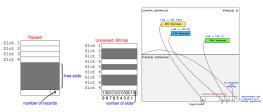


- page directory implementation: more efficient
 - maintain directory structure with one entry per page
 - · stores address of and amount of free space on page
 - insertion: scan directory to find page with enough space to store the new record
 - insertion worst case: scan number of pages + data page itself (vs LL worst case: entire list)



Page Formats

- RID = (page ID, slot number)
- fixed-length records
 - packed organisation: inefficient deletion (transferring last record to deleted record changes RID of record)
- · variable-length records: slotted page organisation



Record formats

- fixed-length records: store consecutively
- variable-length records:
- Delimit fields with special symbols

Data entry formats

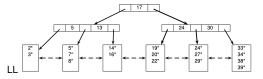
- 1. k^* is an actual **data record** (with search key k)
- 2. k* is of the form (k, RID) fixed length (k, •)
- 3. k* is of the form (k, RID-list) e.g. (k, {RID11, RID12})

02. TREE-BASED INDEXING

- **search key** \rightarrow sequence of k data attributes, $k \ge 1$
 - composite search key \rightarrow if k > 1
- unique index → search key is a candidate key
- clustered index
 → order of data entries ≈ order of records
 - Format-1 is always clustered
 - · at most one clustered index for each relation
- dense index → there is an index record for every search key value in the data. unclustered index must be dense

B⁺-tree Index

- leaf nodes: sorted data entries (k^* is of form (k, RID))
- internal nodes: stores index entries $(p_0, k_1, p_1, \dots, p_n)$ for $k_1 < k_2 \dots < k_n$ where p_i is the page disk address
- each (k_i, p_i) is an **index entry**
- for k* in index subtree T_i rooted at $p_i, k \in [k_i, k_{i+1}]$
- order of index tree, $d \in \mathbb{Z}^+$
- 1. each non-root node contains m entries, $m \in [d, 2d]$
- 2. root node contains [1, 2d] entries
- equality search: at each internal node N, find the largest k_i s.t. $k > k_i$. search subtree at p_i if k_i exists, else p_0
- range search: find first matching record; traverse doubly



insertion: splitting

- \bullet splitting leaf node: distribute d+1 entries to a new leaf node
- if parent overflows: push the middle (d+1) key up to parent
- · root node overflows: create new root (parent of current root)

insertion: redistribution (of leaf nodes only)

- try right sibling first, then left sibling, else use splitting
- sibling → two nodes at the same level & same parent node

deletion: redistribution - try right sibling, then left, else merge

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• if leaf underflows: delete parent key, combine with sibling

> 2d(key byte size) + (2d + 1)(disk page addr byte size)

- if internal node underflows: pull down its index entry in parent, combine with sibling, push a key back up
 - · becomes the new root if parent is root & becomes empty

finding order of B^+ tree with page byte size

min number of nodes at level i

 $=2\times (d+1)^{i-1}$ for $i\geq 1$ max number of nodes at level i

Bulk Loading a B⁺-tree

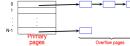
 $=2(d+1)^{i}$

- 1. sort data entries by search key and store sequentially
- 2. construct leaf pages with 2d entries
- construct internal pages by attempting to insert leaf pages into rightmost parent page

03. HASH-BASED INDEXING

Static Hashing

- hash record to $B_i \in B_0, \dots, B_{N-1}$ with $i = h(k) \mod N$
- when full, reconstruct hash table with more buckets

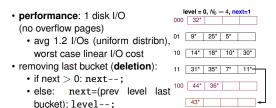


each bucket:

- 1 primary data page
- $\stackrel{\bullet}{\geq}$ 0 overflow data pages

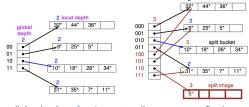
Linear Hashing (Dynamic)

- · grows linearly: split when some bucket overflows
- how to split bucket B_i :
 - 1. add a new bucket $B_i = B_{i+N_i}$ (split image of B_i)
- 2. redistribute entries in B_i between B_i and B_i
- 3. next++; if $next==N_{level}$: level++; next=0
- file size at the beginning of round i, $N_i = 2^i N_0$ • at round i, hash $x = B_x$ has been split ? $h_i(k)$: $h_{i+1}(k)$
- $N_0 = 2^m$; $N^i = 2^{m+i}$;
- Look at m+i+1 bits if bucket has been split, m+i bits only otherwise



Extendible Hashing (Dynamic)

- add a new bucket whenever existing bucket overflows
- no overflow pages unless # collisions ; page capacity
- directory of pointers to buckets 2^d entries $(b_d b_{d-1} \dots b_1)$
- d =global depth of hashed file
- **corresponding** directory entries differ only in the d^{th} bit
- entries in a bucket of **local depth** $\ell \in [0, d]$: same last ℓ
- a split bucket & its image have the same local depth
- number of directory entries pointing to a bucket = $2^{d-\ell}$
- Look at last l bits when adjusting pointers



- splitting bucket: ℓ++ (repeat until no more overflow)
 - if $\ell = d$: directory doubles; d++
 - else $\ell < d$: redistribute and increment ℓ
- deletion: if bucket B_i becomes empty or B_i and B_i can
 - deallocate B_i and decrement ℓ -- for split image B_i
 - · if each pair of corresponding entries point to the same bucket, the directory can be halved
- performance: at most 2 disk I/Os (for equality query)
- · collisions: when 2 data entries have the same hashed value
 - use **overflow pages** if # collisions exceeds page capacity

04.1 SORTING

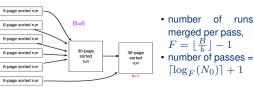
External Merge Sort

- sorted run → sorted data records written to a file on disk
- $N_0 = \lceil N/B \rceil$
- Num of passes = $\lceil \log_{B-1} N_0 \rceil + 1$
- · divide and conquer
 - 1. create temporary file R_i for each B pages of R sorted
 - 2. merge: use B-1 pages for input, 1 page for output
- total I/O = $2N(\lceil \log_{B-1}(N_0) \rceil + 1)$
 - 2N to create $\lceil N/B \rceil$ sorted runs of B pages each
- merging sorted runs: $2N \times \lceil \log_{B-1} N_0 \rceil$

optimisation with blocked I/O

sequential I/O - read/write in buffer blocks of b pages

• one block (b pages) for output, remaining blocks for input



Sorting with B⁺-trees

- when sort key is a prefix of the index key of the B⁺-tree
- sequentially scan leaf pages of B⁺-tree
- for Format-2/3, use RID to retrieve data records

04.2 SELECTION: $\sigma_n(R)$

- $\sigma_n(R)$: selects rows from relation R satisfying predicate p
- · access path: a way of accessing data records/entries
 - table scan → scan all data pages
 - index scan
 ⇒ scan index pages
 - index intersection → combine results from index
- selectivity of an access path \rightarrow number of index & data pages retrieved to access data records/entries
 - more selective = fewer pages retrieved
- index I is a **covering index** for query $Q \rightarrow$ if all attributes referenced in Q are part of the key or include cols of I
- Q can be evaluated using I without any RID lookup (index-only plan)

Matching Predicates

- term \rightarrow of form R.A op c or $R.A_i$ op $R.A_i$
- conjunct → one or more terms connected by ∨
 - disjunctive conjunct → contains ∨
- conjunctive normal form, **CNF predicate** \rightarrow comprises one or more conjuncts connected by \(\) disjunctive conjunct



B⁺-tree matching predicates

• for index $I=(K_1,K_2,\ldots,K_n)$ and non-disjunctive CNF predicate p, I matches p if p is of the form

$$\underbrace{\left(K_{1}=c_{1}\right)\wedge\cdots\wedge\left(K_{i-1}=c_{i-1}\right)}_{\text{zero or more equality predicates}}\wedge\left(K_{i}\text{ op}_{i}\text{ }c_{i}\right),\ i\in\left[1,n\right]$$

- · at most one non-equality comparison operator which must be on the last attribute of the prefix (K_i)
- · matching index: matching records are in contiguous pages non-matching index: not contiguous ⇒ less efficient

Hash index matching predicates

• for hash index $I = (K_1, K_2, \dots, K_n)$ and non-disjunctive CNF predicate p, I matches p if p is of form

$$(K_1 = c_1) \wedge (K_2 = c_2) \wedge \cdots \wedge (K_n = C_n)$$

Primary/Covered Conjuncts

- **primary conjuncts** \rightarrow subset of conjuncts that I matches • e.g. $p = (age \ge 18) \land (age \le 20) \land (weight=65)$
- for I = (age, weight, height) covered conjuncts
 → subset of conjuncts covered by I each attribute in covered conjuncts appears in key or
- primary conjuncts ⊆ covered conjuncts

include cols of I

Cost of Evaluation

let p' = primary conjuncts of p, p_c = covered conjuncts of p

B⁺-tree index evaluation of p

1. navigate internal nodes to find first leaf page

$$\mathsf{cost}_\mathsf{internal} = \begin{cases} \lceil \log_F(\lceil \frac{||R||}{b_d} \rceil) \rceil & \text{if I is a format-1 index} \\ \lceil \log_F(\lceil \frac{||R||}{b_d} \rceil) \rceil & \text{otherwise} \end{cases}$$

2. scan leaf pages to access all qualifying data entries

scan lear pages to access all qualifying data entries
$$\cos t_{\text{leaf}} = \begin{cases} \lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil & \text{if I is a format-1 index} \\ \lceil \frac{||\sigma_{p'}(R)||}{b_s} \rceil & \text{otherwise} \end{cases}$$

3. retrieve qualified data records via RID lookups

$$\mathsf{cost}_{\mathsf{RID}} = \begin{cases} 0 & \text{if I is a covering format-1 index}, \\ ||\sigma_{p_c}(R)|| & \text{otherwise} \end{cases}$$

reduce cost with clustered data records (sort RIDs):

$$\lceil \frac{||\sigma_{p_c}(R)||}{b_d} \rceil \le \mathsf{cost}_{RID} \le \min\{||\sigma_{p_c}(R)||, |R|\}$$

hash index evaluation of p

- $\begin{array}{ll} \bullet \text{ format-1:} & \text{cost to retrieve data records} \geq \lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil \\ \bullet \text{ format-2:} & \text{cost to retrieve data entries} \geq \lceil \frac{||\sigma_{p'}(R)||}{b_i} \rceil \\ \end{array}$ cost to retrieve data records =
- 0 if I is a covering index, $||\sigma_{p_c}(R)||$ otherwise

05.1 PROJECTION $\pi_{A_1,\ldots,A_m}(R)$

• $\pi_L(R)$ eliminates duplicates, $\pi_L^*(R)$ preserves duplicates

Sort-based approach



cost analysis

- 1. extract attributes: $|R| \operatorname{scan} + |\pi_L^*(R)|$ output temp result
- 2. sort records: $2|\pi_I^*(R)|(\log_m(N_0)+1)$
- 3. remove duplicates: $|\pi_{\tau}^*(R)|$ to scan records

optimised sort-based approach

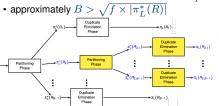


- if $B > \sqrt{|\pi_{\tau}^*(R)|}$, same I/O cost as hash-based approach
 - $N_0 = \lfloor \frac{|R|}{B} \rfloor \approx \sqrt{|\pi_L^*(R)|}$ initial sorted runs $\log_{B-1}(N_0) \approx 1$ merge passes

Hash-based approach

- 1. **partitioning phase**: hash each tuple $t \in R$
 - $R = R_1 \cup R_2 \cup \cdots \cup R_{R-1}$
 - for each $R_i \& R_j$, $i \neq j$, $\pi_I^*(R_i) \cap \pi_I^*(R_i) = \emptyset$
 - for each t: project attributes to form t', hash h(t') to one output buffer, flush output buffer to disk when full
 - one buffer for input, (B-1) buffers for output
- 2. **duplicate elimination** from each partition $\pi_I^*(R_i)$
 - for each R_i : initialise in-mem hash table, hash each $t \in R_i$ to bucket B_i with $h' \neq h$, insert if $t \notin B_i$
 - · write tuples in hash table to results

- Buffer for $\pi_L^*(R_1)$ Buffer for $\pi_L^*(R_2)$ Input
- I/O cost (no partition overflow): $|R| + 2|\pi_I^*(R)|$
 - partitioning cost: $|R| + |\pi_I^*(R)|$
- duplicate elimination cost: $[\pi_I^*(R)]$
- · partition overflow: recursively apply partitioning
 - to avoid, B > size of hash table for $R_i = \frac{|\pi_L^*(R)|}{R_i} \times f$



Projection using Indexes

• if index search key contains all wanted attributes as a prefix · index scan data entries in order & eliminate duplicates

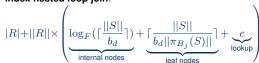
05.2 JOIN $R\bowtie_{\theta} S$

R = outer relation (smaller relation); S = inner relation! for format-2 index, add cost of retrieving record

nested loop joins and UDA

- **tuple-based** nested loop join: $|R| + ||R|| \times |S|$
- page-based nested loop join: $|R| + |R| \times |S|$
- block nested loop join: $|R| + (\lceil \frac{|R|}{R-2} \rceil \times |S|)$,
 - 1 page output, 1 page input, (B-2) pages to read R
 - for each (B-2) pages of R: for each P_S of S: check
- · index nested loop join:

same amount of entries



- joining $R(A,B)\bowtie_A S(A,C)$ with B+tree index on
- for each tuple $r \in R$, use r to probe S's index for match • In a B^+ tree or Hash Index, assume each leaf/bucket has
- If $R \bowtie_{R,a=S,b} S$ and S.b is the primary key. Assume each S tuple joins with ||R||/||S|| tuples

NOTATION

Notation	Meaning
r	relational algebra expression
r	number of tuples in output of r
r	number of pages in output of r
b _d	number of data records that can fit on a page
b_i	number of data entries that can fit on a page
F	average fanout of B ⁺ -tree index (i.e., number of pointers to child nodes)
h	height of B ⁺ -tree index (i.e., number of levels of internal nodes)
	$h = \lceil \log_F(\lceil \frac{ R }{b_i} \rceil) \rceil$ if format-2 index on table R
В	number of available buffer pages