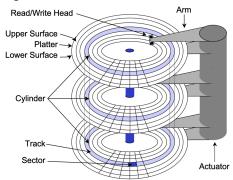
CS3223 AY22/23 SEM 2 github/jovyntls

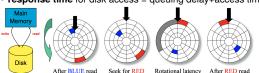
01. DBMS STORAGE

- · store data on non-volatile disk
- process data in main memory (RAM) (volatile storage)

Magnetic HDD



- · disk access time =
 - seek time → move arms to position disk head on track
 - rotational delay \rightarrow wait for block to rotate under head
 - average rotational delay = time for $\frac{1}{2}$ revolutions
 - ullet transfer time ullet move data to/from disk surface
 - = time for 1 revolution × # of requested sectors on the same track # of sectors in track
- response time for disk access = queuing delay+access time



- command processing time: interpreting access command by disk controller (part of access time, considered negligible)
- small requests are dominated by seek time; large requests dominated by transfer time
- access order:
 - 1. contiguous blocks within the same track (same surface)
 - 2. cylinder tracks within the same cylinder
 - 3. next cylinder

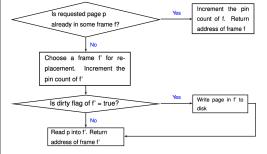
SSD (Solid-State Drive)

- · no mechanical moving parts
- advantages: √ significantly faster than HDD
- √ higher data transfer rate √ lower power consumption
- disadvantages: x update to a page requires erasure of multiple pages before overwriting page
- \times limited number of times a page can be erased

Buffer Manager

- · data is stored & retrieved in disk blocks (pages)
 - each block = sequence of ≥ 1 contiguous sectors
- buffer pool: main memory allocated for DBMS
- partitioned into frames (block-sized pages)
- pin count: number of clients using page (initialised 0)
- >0 ⇒ page is utilised by some transaction; don't replace

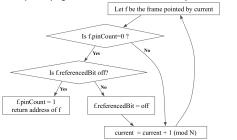
- dirty flag: initialised false
 - dirty → page is modified & not updated on the disk
- dirty page must be written back to the disk if the transaction has committed



! unpinning: update dirty flag to true if page is dirty

replacement policies

- decide which unpinned (pinCount==0) page to replace
- LRU uses a queue of pointers to frames with pinCount==0
- clock: cheaper than LRU, used in postgres
 - referenced bit turns on when pinCount==0
 - replace page with referenced bit off && pinCount==0

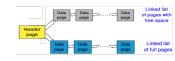


File abstraction

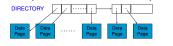
- each relation is a file of records
- · each record has a unique record identifier, RID
- **heap file** → unordered file
 - · vs sorted/hashed file: records are ordered/hashed

heap file implementations

- · linked list implementation
 - · header page: metadata about the file

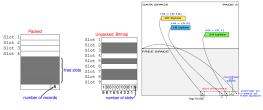


- · page directory implementation: more efficient
 - · maintain directory structure with one entry per page
 - stores address of and amount of free space on page
 - insertion: scan directory to find page with enough space to store the new record
 - insertion worst case: scan number of pages + data page itself (vs LL worst case: entire list)



Page Formats

- RID = (page ID, slot number)
- fixed-length records
- packed organisation: inefficient deletion (transferring last record to deleted record changes RID of record)
- variable-length records: slotted page organisation



Record formats

- fixed-length records: store consecutively
- variable-length records:
- Delimit fields with special symbols

F1 | \$ | F2 | \$ | F3 | \$ | F4

► Use an array of field offsets

Data entry formats

- 1. k^* is an actual **data record** (with search key k)
- 2. k* is of the form (k, RID) fixed length (k, •)
- 3. k* is of the form (k, RID-list) e.g. (k, {RID11, RID12})

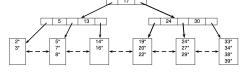
02. TREE-BASED INDEXING

- **search key** \rightarrow sequence of k data attributes, $k \ge 1$
 - composite search key \rightarrow if k > 1
- unique index → search key is a candidate key
- clustered index → order of data entries ≈ order of records
 - · Format-1 is always clustered
 - · at most one clustered index for each relation

B⁺-tree Index

- leaf nodes: sorted data entries (k^* is of form (k, RID))
- internal nodes: stores index entries $(p_0, k_1, p_1, \dots, p_n)$ for $k_1 < k_2 \dots < k_n$ where p_i is the page disk address
 - each (k_i, p_i) is an **index entry**
 - for k* in index subtree T_i rooted at $p_i, k \in [k_i, k_{i+1}]$
- order of index tree, $d \in \mathbb{Z}^+$
- 1. each non-root node contains m entries, $m \in [d,2d]$
- 2. root node contains [1, 2d] entries

 equality search: at each internal node N, find the largest k.
- s.t. $k \geq k_i$ search subtree at p_i if k_i exists, else p_0
- range search: find first matching record; traverse doubly LL



insertion: splitting

- ullet splitting leaf node: distribute d+1 entries to a new leaf node
- if parent overflows: push the middle (d+1) key up to parent
- root node overflows: create new root (parent of current root)

insertion: redistribution (of leaf nodes only)

- · try right sibling first, then left sibling, else use splitting
- **sibling** \rightarrow two nodes at the *same level & same parent node* **deletion: redistribution** try right sibling, then left, else merge **deletion: merging** (siblings have d entries) try right first
- if leaf underflows: delete parent key, combine with sibling
- if internal node underflows: pull down its index entry in parent, combine with sibling, push a key back up
 - becomes the new root if parent is root & becomes empty

Bulk Loading a B⁺-tree

- 1. sort data entries by search key and store sequentially
- 2. construct leaf pages with 2d entries
- construct internal pages by attempting to insert leaf pages into rightmost parent page

03. HASH-BASED INDEXING

Static Hashing

- hash record to $B_i \in B_0, \dots, B_{N-1}$ with i = h(k) mod N
- · when full, reconstruct hash table with more buckets



Linear Hashing (Dynamic)

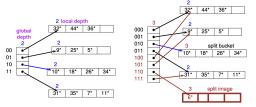
- · grows linearly: split when some bucket overflows
- how to split bucket B_i :
 - 1. add a new bucket $B_i = B_{i+N_i}$ (split image of B_i)
 - 2. redistribute entries in B_i between B_i and B_j 3. next++; if next== N_{level} : level++; next=0
- file size at the beginning of round i, $N_i = 2^i N_0$
- at round i, hash $x = B_x$ has been split ? $h_i(k)$: $h_{i+1}(k)$

10 14* 18* 10* 30*

- worst case linear I/O cost
- removing bucket (deletion):
 if next > 0: next--;
 - else: next=(prev level last bucket); level--;

Extendible Hashing (Dynamic)

- · add a new bucket whenever existing bucket overflows
- no overflow pages unless # collisions > page capacity
- directory of pointers to buckets 2^d entries $(b_d b_{d-1} \dots b_1)$
- d = global depth of hashed file • corresponding directory entries differ only in the d^{th} bit
- corresponding directory entries differ only in the dth bit
 entries in a bucket of local depth ℓ ∈ [0, d]: same last ℓ bits
- a split bucket & its image have the same local depth number of directory entries pointing to a bucket = $2^{d-\ell}$



splitting bucket: ℓ++ (repeat until no more overflow)

- if $\ell = d$: directory doubles; d++
- else $\ell < d$: redistribute and increment ℓ
- deletion: if bucket B_i becomes empty or B_i and B_i can
 - deallocate B_i and decrement ℓ -- for split image B_i
 - if each pair of corresponding entries point to the same bucket, the directory can be halved
- performance: at most 2 disk I/Os (for equality query)
- · collisions: when 2 data entries have the same hashed value
 - use overflow pages if # collisions exceeds page capacity

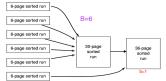
04.1 SORTING

External Merge Sort

- sorted run → sorted data records written to a file on disk
- · divide and conquer
- 1. create temporary file R_i for each B pages of R sorted
- 2. merge: use B-1 pages for input, 1 page for output
- total I/O = $2N(\lceil \log_{B-1}(N_0) \rceil + 1)$
 - 2N to create $\lceil N/B \rceil$ sorted runs of B pages each
 - merging sorted runs: $2N \times \lceil \log_{B-1} N_0 \rceil$

optimisation with blocked I/O

- sequential I/O read/write in buffer blocks of b pages
- one block (b pages) for output, remaining blocks for input



- · number of runs merged per pass, $F = \lfloor \frac{B}{b} \rfloor - 1$
- number of passes = $\lceil \log_F(N_0) \rceil + 1$

Sorting with B⁺-trees

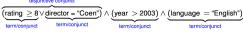
- when sort key is a prefix of the index key of the B⁺-tree
- sequentially scan leaf pages of B⁺-tree
 - · for Format-2/3, use RID to retrieve data records

04.2 SELECTION: $\sigma_n(R)$

- $\sigma_p(R)$: selects rows from relation R satisfying predicate p
- access path: a way of accessing data records/entries
- table scan → scan all data pages
- index scan
 ⇒ scan index pages
- index intersection → combine results from index scans
- selectivity of an access path → number of index & data pages retrieved to access data records/entries
- · more selective = fewer pages retrieved
- index I is a **covering index** for guery $Q \rightarrow$ if all attributes referenced in Q are part of the key of I
 - Q can be evaluated using I without any RID lookup (index-only plan)

Matching Predicates

- term \rightarrow of form R.A op c or $R.A_i$ op $R.A_i$
- conjunct → one or more terms connected by ∨
- disjunctive conjunct → contains ∨
- conjunctive normal form, CNF predicate → comprises one or more conjuncts connected by \(\lambda \)



B⁺-tree matching predicates

- for index $I = (K_1, K_2, \dots, K_n)$ and non-disjunctive CNF predicate p, I matches p if p is of the form
- $(K_1=c_1)\wedge\cdots\wedge(K_{i-1}=c_{i-1})\wedge(K_i\ op_i\ c_i),\ i\in[1,n]$ zero or more equality predicates
- at most one non-equality comparison operator which must be on the last attribute of the prefix (K_i)
- matching index: matching records are in contiguous pages
- non-matching index: not contiguous ⇒ less efficient

Hash index matching predicates

• for hash index $I = (K_1, K_2, \dots, K_n)$ and non-disjunctive CNF predicate p, I matches p if p is of form

$$(K_1 = c_1) \wedge (K_2 = c_2) \wedge \cdots \wedge (K_n = C_n)$$

Primary/Covered Conjuncts

- **primary conjuncts** \rightarrow subset of conjuncts that I matches
 - e.g. $p = (age > 18) \land (age < 20) \land (weight=65)$ for I = (age, weight, height)
- **covered conjuncts** \rightarrow subset of conjuncts covered by I
 - each attribute in covered conjuncts appears in key of I
- primary conjuncts ⊆ covered conjuncts

Cost of Evaluation

let p' = primary conjuncts of p. p_c = covered conjuncts of p

B⁺-tree index evaluation of p

- 1. navigate internal nodes to find first leaf page
- $\operatorname{cost}_{\mathsf{internal}} = \begin{cases} \lceil \log_F(\lceil \frac{||R||}{b_d} \rceil) \rceil & \text{if I is a format-1 index} \\ \lceil \log_F(\lceil \frac{||R||}{b_i} \rceil) \rceil & \text{otherwise} \end{cases}$ 2. scan leaf pages to access all qualifying data entries

scan leaf pages to access all qualifying data entries
$$\text{cost}_{\text{leaf}} = \begin{cases} \lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil & \text{if I is a format-1 index} \\ \lceil \frac{||\sigma_{p'}(R)||}{b_i} \rceil & \text{otherwise} \end{cases}$$

- 3. retrieve qualified data records via RID lookups
 - if I is a covering format-1 index, $cost_{RID} =$ $||\sigma_{p_c}(R)||$ otherwise
 - reduce cost with clustered data records (sort RIDs): $\lceil \frac{||\sigma_{p_c}(R)||}{h_d} \rceil \leq \operatorname{cost}_{RID} \leq \min\{||\sigma_{p_c}(R)||, |R|\}$

hash index evaluation of p

- $\begin{array}{ll} \textbf{ format-1:} & \text{cost to retrieve data records} \geq \lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil \\ \textbf{ format-2:} & \text{cost to retrieve data entries} \geq \lceil \frac{||\sigma_{p'}(R)||}{b_i} \rceil \\ \end{array}$

 $\text{cost to retrieve data records} = \begin{cases} 0 & \text{if I is a covering index,} \\ ||\sigma_{v'}(R)|| & \text{otherwise} \end{cases}$

05.1 PROJECTION $\pi_{A_1,\ldots,A_m}(R)$

• $\pi_L(R)$ eliminates duplicates, $\pi_L^*(R)$ preserves duplicates

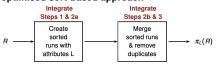
Sort-based approach



cost analysis

- 1. extract attributes: $|R| \operatorname{scan} + |\pi_{\tau}^{*}(R)|$ output temp result
- 2. sort records: $2|\pi_L^*(R)|(\log_m(\bar{N}_0)+1)$
- 3. remove duplicates: $|\pi_{\tau}^*(R)|$ to scan records

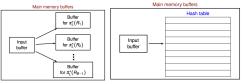
optimised sort-based approach



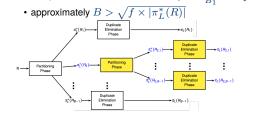
- if $B > \sqrt{|\pi_I^*(R)|}$, same I/O cost as hash-based approach
 - $N_0 = \lfloor \frac{|R|}{B} \rfloor \approx \sqrt{|\pi_L^*(R)|}$ initial sorted runs $\log_{B-1}(N_0) \approx 1$ merge passes

Hash-based approach

- 1. **partitioning phase**: hash each tuple $t \in R$
 - $R = R_1 \cup R_2 \cup \cdots \cup R_{B-1}$
 - for each $R_i \& R_i$, $i \neq j$, $\pi_I^*(R_i) \cap \pi_I^*(R_i) = \emptyset$
 - for each t: project attributes to form t', hash h(t') to one output buffer, flush output buffer to disk when full
 - one buffer for input, (B-1) buffers for output
- 2. **duplicate elimination** from each $\pi_I^*(R_i)$
 - for each R_i : initialise in-mem hash table, hash each $t \in R_i$ to bucket B_i with $h' \neq h$, insert if $t \notin B_i$
 - · write tuples in hash table to results



- I/O cost (no partition overflow): $|R| + 2|\pi_T^*(R)|$
 - partitioning cost: $|R| + |\pi_L^*(R)|$
 - duplicate elimination cost: $|\pi_I^*(R)|$
- · partition overflow: recursively apply partitioning • to avoid, B > size of hash table for $R_i = \frac{|\pi_L^*(R)|}{B_1} \times f$



Projection using Indexes

- if index search key contains all wanted attributes as a prefix
 - · index scan data entries in order & eliminate duplicates

05.2 JOIN $R\bowtie_{\theta} S$

R = outer relation (smaller relation); S = inner relation ! for format-2 index, add cost of retrieving record

nested loop joins

- tuple-based nested loop join: $|R| + |R| \times |S|$
- page-based nested loop join: $|R| + |R| \times |S|$
- block nested loop join: $|R| + (\lceil \frac{|R|}{B-2} \rceil \times |S|), \ |R| \leq |S|$
 - 1 page output, 1 page input, $(\bar{B} 2)$ pages to read R• for each (B-2) pages of R: for each P_S of S: check r,s
- index nested loop join:

$$\begin{split} |R| + ||R|| \times \left(\log_F(\lceil\frac{||S||}{b_d}\rceil) + \lceil\frac{||S||}{b_d||\pi_{B_j}(S)||}\rceil\right) \\ \bullet \text{ joining } R(A,B) \bowtie_A S(A,C) \text{ with B+tree index on } S.A \end{split}$$

• sort R & S: $2|R|(\log_m(N_R) + 1) + 2|S|(\log_m(N_S) + 1)$ • merge cost: |R| + |S| (worst case $|R| + |R| \times |S|$) optimised sort-merge join

- merge sorted runs until B > N(R, i) + N(S, i); then do merge and join at the same time
- I/O cost: $3 \times (|R| + |S|)$

sort-merge join

- if $B > \sqrt{2|S|}$, one pass to merge initial sorted runs
- 2(|R| + |S|) for initial sorted runs, |R| + |S| for merging

• for each tuple $r \in R$, use r to probe S's index for match

hash join

- 1. partition R and S into k partitions on join column
 - $\pi_A(R_i) \cap \pi_B(S_i) = \emptyset \quad \forall R_i, S_i, i \neq j$
 - $R = R_1 \cup R_2 \cup \cdots \cup R_k$, $t \in R_i \iff h(t.A) = i$ • $S = S_1 \cup S_2 \cup \cdots \cup S_k$, $t \in S_i \iff h(t.B) = i$
- 2. join corresponding partitions:

$$R \bowtie_{R.A \equiv S.B} S = (R_1 \bowtie S_1) \cup \cdots \cup (R_k \bowtie S_k)$$

Grace hash ioin

for build relation R and probe relation S.

- 1. **partition** R and S into k partitions each, k = B 1
- 2. **probing phase**: hash $r \in R_i$ with h'(r,A) to table T
- 2.1. $\forall s \in S_i, r \in \text{bucket } h'(s.B)$: output (r, s) if match
- I/O cost: 3(|R| + |S|) (no partition overflow) • $B>\frac{f\times |R|}{B-1}+2$ (input & output buffer) $\approx B>\sqrt{f\times |R|}$
- during probing, B > size of each partition +2• partition overflow if R_i cannot fit in memory
 - · recursively apply partitioning to overflow partition

General join conditions

· multiple equality-join conditions:

$$(R.A = S.A) \wedge (R.B = S.B)$$

- index nested loop join: use index on some/all join attribs
- · sort-merge join: sort on combination of attributes
- · other algos: no change
- inequality-ioin conditions: (R.A < S.A)
 - index nested loop join: requires B⁺-tree index · not applicable: sort-merge join (too much rewinding), hash-based ioins
 - · other algos: no change

NOTATION

Notation	Meaning
r	relational algebra expression
r	number of tuples in output of r
r	number of pages in output of r
b _d	number of data records that can fit on a page
b_i	number of data entries that can fit on a page
F	average fanout of B+-tree index (i.e., number of pointers to child nodes)
h	height of B+-tree index (i.e., number of levels of internal nodes)
	$h = \lceil \log_F(\lceil \frac{ R }{b_i} \rceil) \rceil$ if format-2 index on table R
В	number of available buffer pages