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**Algorithm 1:** identify Row Context

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**Input:**  $r_i$ ,  $Backgrd(T_i)=T_1, T_2, \dots, T_n$  and similarity threshold  $\theta_r$

**Output:**  $con(r_i)$

```
1  $con(r_i) = \Phi$ ;  
2 for  $j = 1; j \leq n; j \neq i$  do  
3   float  $maxSim = 0$ ;  
4    $r^{maxSim} = null$ ;  
5   while not end of  $T_j$  do  
6     compute  $Jaro(r_i, r_m) (r_m \in T_j)$ ;  
7     if  $(Jaro(r_i, r_m) \geq \theta_r) \wedge (Jaro(r_i, r_m) \geq r^{maxSim})$  then  
8       replace  $r^{maxSim}$  with  $r_m$ ;  
9    $con(r_i) = con(r_i) \cup r^{maxSim}$ ;  
10 return  $con(r_i)$ ;
```

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**Algorithm 2:** Service checkpoint image storage node and routing path selection

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**Input:** host server  $PM_s$  that  $SerImg_k$  is fetched from,  $subnet_s$  that  $PM_s$  belongs to,  $pod_s$  that  $PM_s$  belongs to

**Output:** Service image storage server  $storageserver$ , and the image transfer path  $path$

```
1  $storageserver = \text{Storage node selection}(PM_s,$   
    $SerImg_k, subnet_s, pod_s)$ ;  
2 if  $storageserver \neq null$  then  
3   select a path from  $storageserver$  to  $PM_s$  and assign the path to  
    $path$ ;  
4 final ;  
5 return  $storageserver$  and  $path$ ;
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**Algorithm 3:** Storage node selection

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**Input:** host server  $PM_s$  that the checkpoint image  $Img$  is fetched from,  $subnet_s$  that  $PM_s$  belongs to,  $pod_s$  that  $PM_s$  belongs to

**Output:** Image storage server  $storageserver$

```
1 for each host server  $PM_i$  in the same subnet with  $PM_s$  do
2   if  $PM_i$  is not a service providing node or checkpoint image
     storage node of  $S_k$  then
3      $PM_i$  add to  $candidateList$  ;
4 sort  $candidateList$  by reliability desc;
5 init  $storageserver$  ; for each  $PM_k$  in  $candidateList$  do
6   if  $SP(PM_k) \geq E(SP)$  of  $pod_i$  and  $BM_k \leq \text{size of } Img$  then
7     assign  $PM_k$  to  $storageserver$ ;
8   goto final;
9 clear  $candidateList$ ;
10 add all other subnets in  $pod_s$  to  $netList$ ;
11 for each subnet  $subnet_j$  in  $netList$  do
12   clear  $candidateList$ ;
13   for each  $PM_i$  in  $subnet_j$  do
14     if  $PM_i$  is not a service providing node or checkpoint image
         storage node of  $S_k$  then
15        $PM_i$  add to  $candidateList$ ;
16   sort all host in  $candidateList$  by reliability desc;
17   for each  $PM_k$  in  $candidateList$  do
18     if  $SP(PM_k) \geq E(SP)$  of  $pod_i$  and  $BM_k \leq \text{size of } Img$  then
19       assign  $PM_k$  to  $storageserver$  ;
20     goto final;
21 final ;
22 return  $storageserver$ ;
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**Algorithm 4:** component matrices computing
 

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**Input:**  $\mathcal{X} \in \mathbb{R}^{l_1 \times l_2 \times \dots \times l_N}, \varepsilon, \lambda, \delta, R$

**Output:**  $A^{(j)}$ s for  $j = 1$  to  $N$

```

1 Initialize all  $A^{(j)}$ s //which can be seen as the  $0^{th}$  round iterations;
2  $l'' = L$  //if we need to judge whether (11) is true then  $l''$  denotes
    $L|_{t-1}$ ;
3 for each  $A_{i_j r}^j (1 \leq j \leq N, 1 \leq i_j \leq I_j, 1 \leq r \leq R)$  do
4   //1st round iterations;
5    $g_{i_j r}^{(j)'} = g_{i_j r}^{(j)}$ ;
6    $A_{i_j r}^{(j)'} = A_{i_j r}^{(j)}$  //if the rollback shown as (12) is needed,  $A_{i_j r}^{(j)'$ 
     denotes  $A_{i_j r}^{(j)}|_{t-1}$ ;
7    $A_{i_j r}^{(j)} = A_{i_j r}^{(j)} - \mathbf{sign} \left( g_{i_j r}^{(j)} \right) \cdot \delta_{i_j r}^{(j)}$ ;
8 repeat //other rounds of iterations for computing component
   matrices
9    $l' = L$  //if we need to judge whether (11) is true then  $l'$  denotes
      $L|_t$ ;
10  for each  $A_{i_j r}^j (1 \leq j \leq N, 1 \leq i_j \leq I_j, 1 \leq r \leq R)$  do
11    if  $g_{i_j r}^{(j)} \cdot g_{i_j r}^{(j)'} > 0$  then
12       $A_{i_j r}^{(j)'} = A_{i_j r}^{(j)}$ ;
13       $g_{i_j r}^{(j)'} = g_{i_j r}^{(j)}$ ;
14       $\delta_{i_j r}^{(j)} = \min \left( \delta_{i_j r}^{(j)} \cdot \eta^+, Max\_Step\_Size \right)$ ;
15       $A_{i_j r}^{(j)} = A_{i_j r}^{(j)} - \mathbf{sign} \left( g_{i_j r}^{(j)} \right) \cdot \delta_{i_j r}^{(j)}$ ;
16    else if  $g_{i_j r}^{(j)} \cdot g_{i_j r}^{(j)'} < 0$  then
17      if  $l' > l''$  then
18         $g_{i_j r}^{(j)'} = g_{i_j r}^{(j)}$ ;
19         $A_{i_j r}^{(j)} = A_{i_j r}^{(j)'} // if (11) is true then rollback as (12);
20         $\delta_{i_j r}^{(j)} = \max \left( \delta_{i_j r}^{(j)} \times \eta^-, Min\_Step\_Size \right)$ ;
21      else
22         $A_{i_j r}^{(j)'} = A_{i_j r}^{(j)}$ ;
23         $g_{i_j r}^{(j)'} = g_{i_j r}^{(j)}$ ;
24         $\delta_{i_j r}^{(j)} = \max \left( \delta_{i_j r}^{(j)} \cdot \eta^-, Min\_Step\_Size \right)$ ;
25         $A_{i_j r}^{(j)} = A_{i_j r}^{(j)} - \mathbf{sign} \left( g_{i_j r}^{(j)} \right) \cdot \delta_{i_j r}^{(j)}$ ;
26      else
27         $A_{i_j r}^{(j)'} = A_{i_j r}^{(j)}$ ;
28         $g_{i_j r}^{(j)'} = g_{i_j r}^{(j)}$ ;
29         $A_{i_j r}^{(j)} = A_{i_j r}^{(j)} - \mathbf{sign} \left( g_{i_j r}^{(j)} \right) \cdot \delta_{i_j r}^{(j)}$ ;
30     $l'' = l'$ ;
31 until  $L \leq \varepsilon$  or maximum iterations exhausted;$ 
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**Algorithm 5:** Learning algorithm of R2P

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**Input:** ratings  $R$ , joint demographic representations  $Y$ , learning rate  $\eta$ , maximum iterative number  $maxIter$ , negative sampling number  $k$ ;

**Output:** interaction matrix  $\mathbf{W}$ , movie vectors  $V$ ;

```
1 Initialize  $\mathbf{W}, V$  randomly;
2  $t = 0$ ;
3 For convenience, define  $\vec{\varphi}_n = \sum_{m \in S_n} r_{m,n} \vec{v}_m$ ;
4 while not converged or  $t > maxIter$  do
5    $t = t + 1$ ;
6   for  $n = 1; n \leq N; n++$  do
7      $\mathbf{W} = \mathbf{W} + \eta(1 - \sigma(\vec{\varphi}_n^T \mathbf{W} \vec{y}_n)) \vec{\varphi}_n \vec{y}_n^T$ ;
8     for  $m \in S_n$  do
9        $\vec{v}_m = \vec{v}_m + \eta(1 - \sigma(\vec{\varphi}_n^T \mathbf{W} \vec{y}_n)) r_{m,n} \mathbf{W} \vec{y}_n$ ;
10    for  $i = 1; i \leq k; i++$  do
11      sample negative sample  $\vec{y}_i$  from  $P_n$ ;
12       $\mathbf{W} = \mathbf{W} - \eta(1 - \sigma(-\vec{\varphi}_n^T \mathbf{W} \vec{y}_i)) \vec{\varphi}_n \vec{y}_i^T$ ;
13      for  $m \in S_n$  do
14         $\vec{v}_m = \vec{v}_m - \eta(1 - \sigma(-\vec{\varphi}_n^T \mathbf{W} \vec{y}_i)) r_{m,n} \mathbf{W} \vec{y}_i$ ;
15     $\mathbf{W} = \mathbf{W} - 2\lambda\eta \mathbf{W}$ ;
16     $V = V - 2\lambda\eta V$ ;
17 return  $\mathbf{W}, V$ ;
```

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