

Statistics Basics Week 3 SGA

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Let X be the random variable that denotes the number of people who became happier after avoiding using social network for a week.

Let H_0 be probability of becoming happier is $= \frac{1}{2}$

Let H_1 be probability of becoming happier is $> \frac{1}{2}$

Since there is no clear information of the distribution of X , we are going to assume that

$$X \sim \text{Binomial}(n, p)$$

where $n = 20$ and $p = \frac{1}{2}$

Then we can find the p-value:

$$p(X \geq X_{obs}|H_0) = p(X = 20|H_0) + p(X = 19|H_0) + p(X = 18|H_0) + p(X = 17|H_0) + p(X = 16|H_0)$$

$$\begin{aligned} p(X \geq X_{obs}|H_0) &= \\ &= \binom{20}{20} \left(\frac{1}{2}\right)^{20} \left(\frac{1}{2}\right)^0 + \\ &= \binom{20}{19} \left(\frac{1}{2}\right)^{19} \left(\frac{1}{2}\right)^1 + \\ &= \binom{20}{18} \left(\frac{1}{2}\right)^{18} \left(\frac{1}{2}\right)^2 + \\ &= \binom{20}{17} \left(\frac{1}{2}\right)^{17} \left(\frac{1}{2}\right)^3 + \\ &= \binom{20}{16} \left(\frac{1}{2}\right)^{16} \left(\frac{1}{2}\right)^4 \\ &= 0.0059 \end{aligned} \tag{1}$$

This means p-value < 0.05 and we can conclude that people are happier without social

networks.