

Assignment  
Solving the 8-Puzzle Problem Using A\*  
Algorithm

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# Introduction

A sliding puzzle that constitutes a 3X3 grid together with tiles numbered from 1 to 8 and one blank space is called 8-puzzle problem, being a classic example of it. What needs to be done is moving these tiles around up to a point where they are supposed to be. In Artificial Intelligence this is the best area of search algorithms to explore especially with the efficiency of A\* (A-star) algorithm in locating the fastest track to the answer.

## Problem Formulation

1. **State Representation:** Each state of the puzzle can be represented by a 3x3 matrix where each cell contains a number from 1 to 8 or 0 to represent the blank space.
2. **Initial State:** This is the starting configuration of the puzzle.
3. **Goal State:** The target configuration we want to reach.
4. **Actions:** The possible moves are sliding a tile into the blank space. This can be represented as four possible actions: move blank up, down, left, or right.

## Solution Methodology:

To solve the 8-puzzle problem, we use the A\* algorithm, which is a best-first search algorithm that finds the least-cost path from a given initial state to the goal state. The key components of A\* are:

- **Cost Function ( $f(n)$ ):** This combines the actual cost to reach a node ( $g(n)$ ) and the estimated cost to reach the goal from that node ( $h(n)$ ):  
 $g(n)g(n)g(n)$ : The cost to reach the current node from the start node.  
 $h(n)h(n)h(n)$ : The heuristic estimate of the cost to reach the goal from the current node.
1. **Heuristic Function:** A\* uses heuristics to estimate the cost to reach the goal. Common heuristics for the 8-puzzle include:

- **Manhattan Distance:** The sum of the absolute values of the differences in the tile's positions between the current state and the goal state. It is both admissible overestimates and consistent.
- **Misplaced Tiles:** The number of tiles that are not in their goal position.

## Implementation Details

The implementation of the A\* algorithm for solving the 8-puzzle problem involves the following steps:

1. **Node Structure:** Define a node structure to represent each state of the puzzle. Each node contains:
  - The current board configuration.
  - The cost to reach this state (g).
  - The heuristic estimate to the goal (h).
  - The total cost ( $f = g + h$ ).
  - A pointer to the parent node for solution reconstruction.
2. **Minheap for Open Set:** A priority queue (min-heap) is used to manage the nodes to be explored based on their f values.
3. **State Expansion:** Expand the current node by generating its possible child nodes (resulting from valid moves of the blank space) and calculating their g, h, and f values.
4. **Goal Test:** Check if the current node matches the goal state. If yes, reconstruct the path from the start state to the goal state by following parent pointers.
5. **Closed Set:** Keep track of the visited states to avoid revisiting and expanding the same state.

## Conclusion

The 8-puzzle problem exemplifies how heuristic search algorithms like A\* can efficiently solve combinatorial problems. By leveraging a cost function that combines both the actual cost to reach a state and an estimated cost to reach the goal, A\* navigates the state space effectively, ensuring that the shortest path to the solution is found. This approach, while implemented here for the 8-puzzle, is widely applicable to various other search problems in artificial intelligence.

## References:

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