



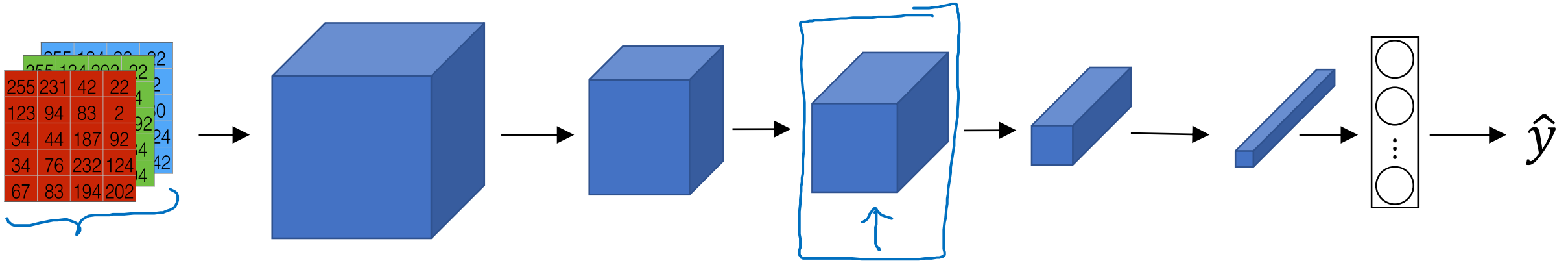
deeplearning.ai

# Neural Style Transfer

---

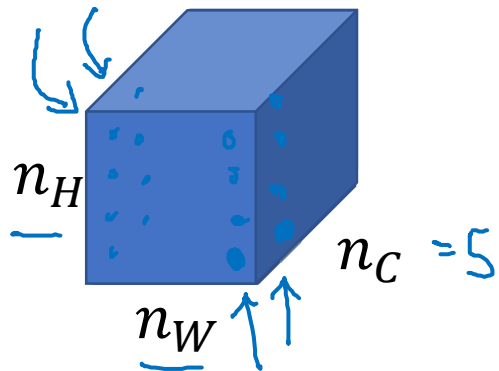
## Style cost function

# Meaning of the “style” of an image



Say you are using layer  $l$ 's activation to measure “style.”

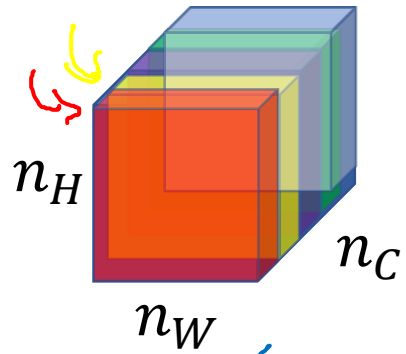
Define style as correlation between activations across channels.



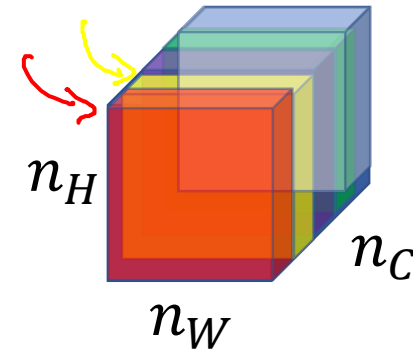
How correlated are the activations  
across different channels?

# Intuition about style of an image

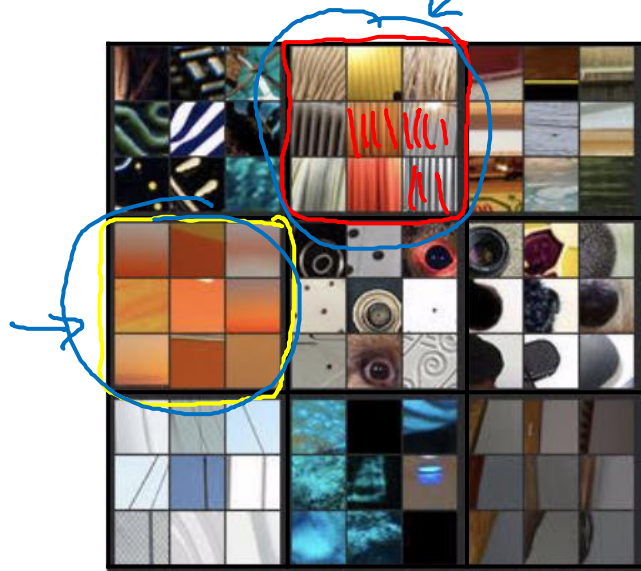
Style image



Generated Image



Correlated?  
Uncorrelated



Correlation: Are the feature going to happen together?  
Together -> correlated  
Not together -> uncorrelated.

# Style matrix

Let  $a_{i,j,k}^{[l]}$  = activation at  $(i, j, k)$ .  $G^{[l]}$  is  $n_c^{[l]} \times n_c^{[l]}$

H w c  
↓ ↓ ↙

$n_c$   
 $G_{kk'}^{[l]}$   
↑ ↑  
 $k = 1, \dots, n_c$

$$\begin{aligned} \rightarrow G_{kk'}^{[l]}(S) &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l]}(S) a_{ijk'}^{[l]}(S) \\ \rightarrow G_{kk'}^{[l]}(G) &= \sum_{i=1}^{n_H^{[l]}} \sum_{j=1}^{n_W^{[l]}} a_{ijk}^{[l]}(G) a_{ijk}^{[l]}(G) \end{aligned}$$

"Gram matrix"

$$\begin{aligned} \beta \uparrow J_{\text{style}}^{[l]}(S, G) &= \frac{1}{(\dots)} \|G^{[l]}(S) - G^{[l]}(G)\|_F^2 \\ &= \frac{1}{(2n_H^{[l]}n_W^{[l]}n_c^{[l]})^2} \sum_k \sum_{k'} (G_{kk'}^{[l]}(S) - G_{kk'}^{[l]}(G))^2 \end{aligned}$$

# Style cost function

$$\|G^{TL(S)} - G^{TL(G)}\|_F^2$$

$$J_{style}^{[l]}(S, G) = \frac{1}{\left(2n_H^{[l]}n_W^{[l]}n_C^{[l]}\right)^2} \sum_k \sum_{k'} (G_{kk'}^{[l](S)} - G_{kk'}^{[l](G)})^2$$

Individual style cost function for layer l

$$J_{style}(S, G) = \sum_l \lambda_l J_{style}^{TL}(S, G)$$

Overall style cost function taking all layers into account.

$$\underline{J(G)} = \alpha J_{content}(G) + \beta J_{style}(S, G)$$

Overall cost function using both content cost function as well as style cost function.