



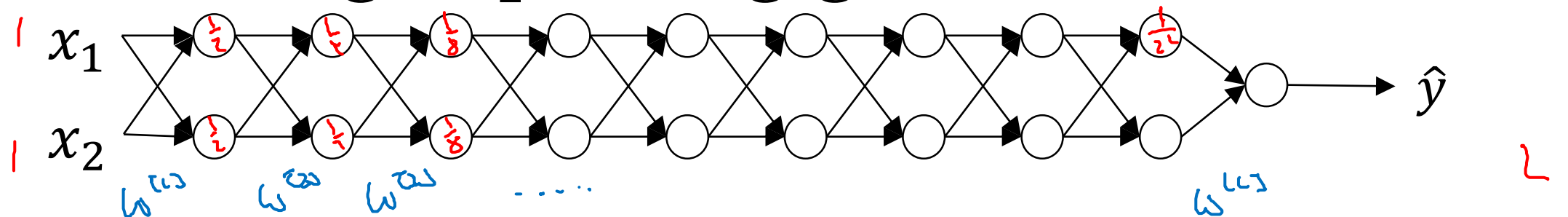
deeplearning.ai

Setting up your  
optimization problem

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Vanishing/exploding  
gradients

# Vanishing/exploding gradients



$$g(z) = z \quad b^{(L)} = 0$$

$$\hat{y} = W^{(L)} \left( W^{(L-1)} W^{(L-2)} \dots W^{(2)} W^{(1)} x \right)$$

$$W^{(1)} > I$$

$$W^{(2)} < I \quad \begin{bmatrix} 0.9 & \\ & 0.9 \end{bmatrix}$$

$$W^{(2)} = \begin{bmatrix} 1.5 & 0 \\ 0 & 0.5 \end{bmatrix}$$

$$\hat{y} = W^{(L)} \left[ \begin{bmatrix} 1.5 & 0 \\ 0 & 0.5 \end{bmatrix}^{L-1} x \right]$$

$$z^{(t)} = W^{(t)} x$$

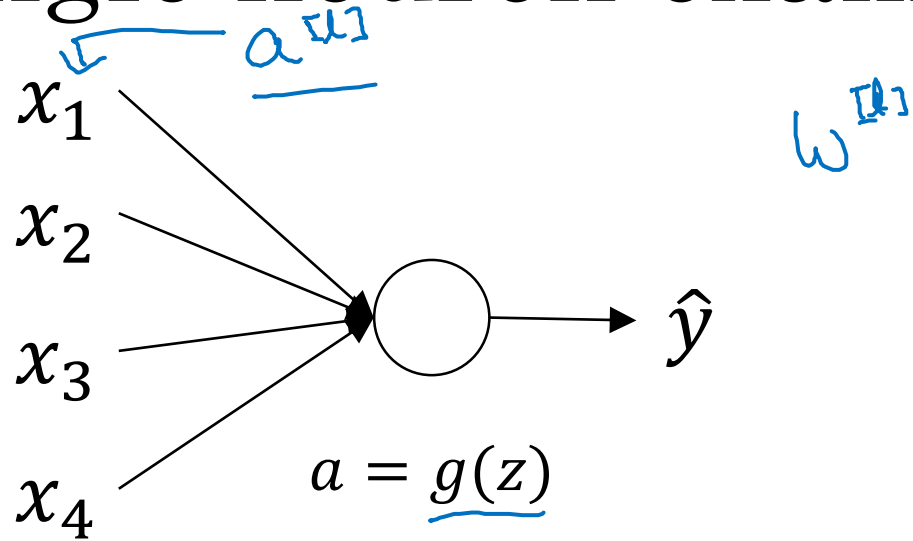
$$a^{(t)} = g(z^{(t)}) = z^{(t)}$$

$$a^{(t)} = g(z^{(t)}) = g(W^{(t)} a^{(t-1)})$$

$$1.5^{L-1} x$$

$$0.5^{L-1} x$$

# Single neuron example



$$z = w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

large  $n \rightarrow$  Smaller  $w_i$

$$\text{Var}(w_i) = \frac{1}{n} \frac{2}{n}$$

$$\underline{W^{[1]}} = \text{np.random.randn}(\text{shape}) * \text{np.sqrt}\left(\frac{2}{n^{[1-1]}}\right)$$

ReLU  $g^{[2]}(z) = \text{ReLU}(z)$

Other variants:

tanh

$$\frac{1}{n^{[l-1]}}$$

Xavier initialization ↑

$$\sqrt{\frac{2}{n^{[l-1]} + n^{[1]}}}$$

↑