



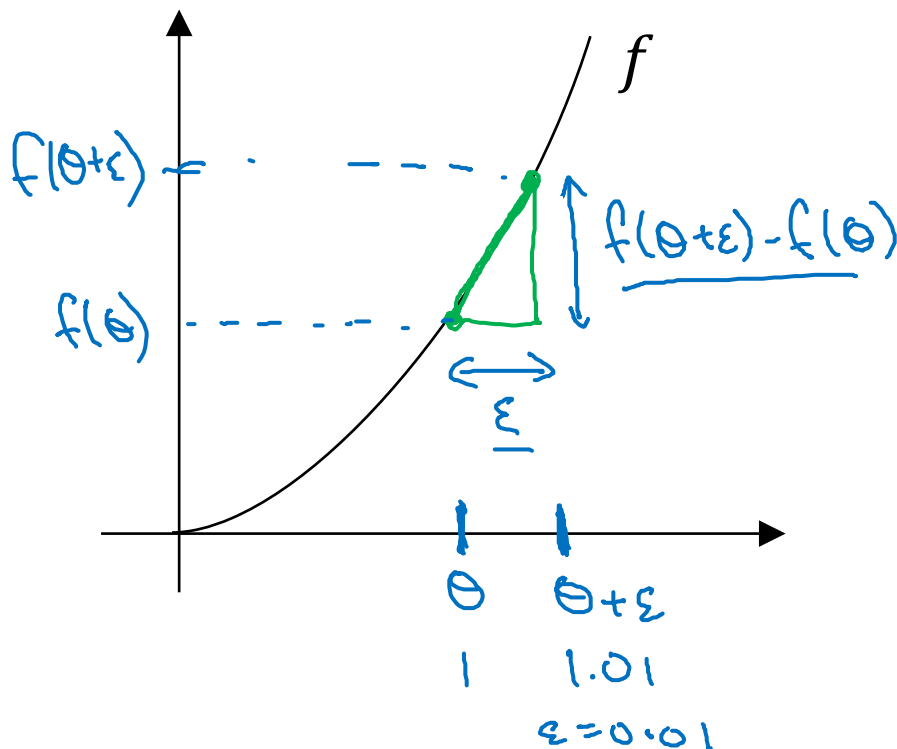
deeplearning.ai

Setting up your
optimization problem

Numerical approximation
of gradients

Checking your derivative computation

I $f(\theta) = \theta^3$
 $\theta \in \mathbb{R}.$



$$g(\theta) = \frac{d}{d\theta} f(\theta) = f'(\theta)$$

$g(\theta) = 3\theta^2$

$g(\theta) = 3 \cdot (1)^2 = 3$
 when $\theta = 1$

$\frac{dw}{db}$

$$\frac{f(\theta + \epsilon) - f(\theta)}{\epsilon} \approx g(\theta)$$

$$\frac{(1.01)^3 - 1^3}{0.01} = 3.0301 \approx 3$$

Annotations for the calculation above:

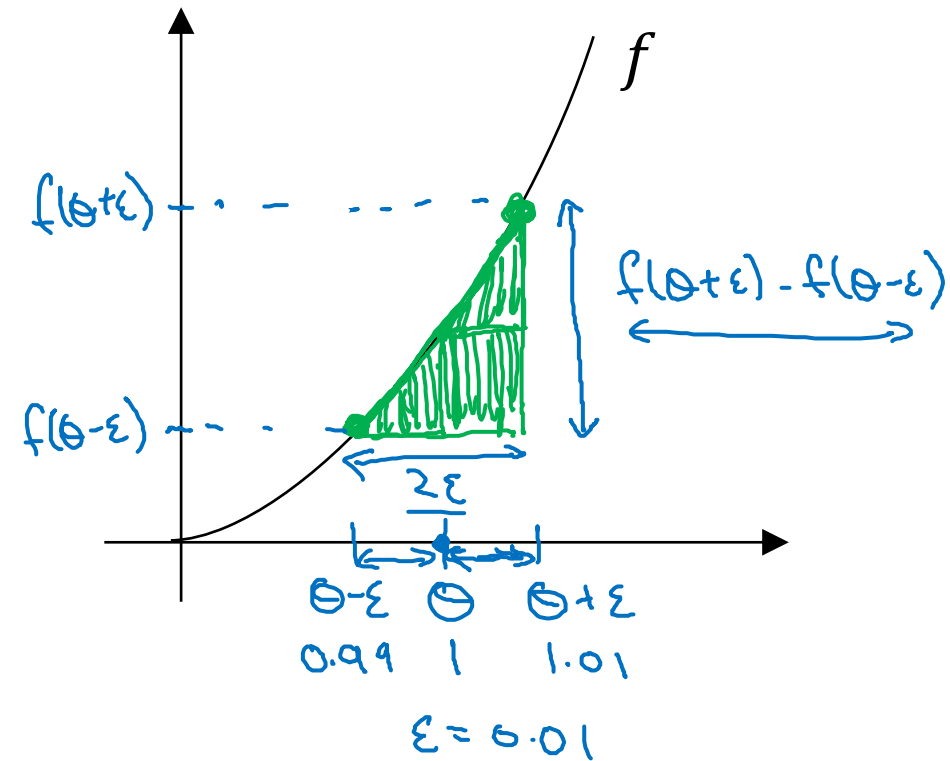
- $1.01^3 = 1.030301$
- $1.030301 - 1 = 0.0301$
- $0.0301 / 0.01 = 3.0301$
- $3.0301 \approx 3$

$\theta = 1$
 $\theta + \epsilon = 1.01$

Checking your derivative computation

$$\underline{f(\theta) = \theta^3}$$

Better



$$\left[\frac{f(\theta + \epsilon) - f(\theta - \epsilon)}{2\epsilon} \approx \underline{g(\theta)} \right]$$

$$\frac{(1.01)^3 - (0.99)^3}{2(0.01)} = 3.0001 \approx 3$$

$$g(\theta) = 3\theta^2 = 3$$

approx error: 0.0001

(prev slide: 3.0301. error: 0.03)

$$\left\{ f'(\theta) = \lim_{\epsilon \rightarrow 0} \frac{f(\theta + \epsilon) - f(\theta - \epsilon)}{2\epsilon} \right.$$

$$\underline{O(\epsilon^2)}$$

$$0.01$$

$$\underline{0.0001}$$

$$\frac{f(\theta + \epsilon) - f(\theta)}{\epsilon}$$

$$\text{error: } \underline{O(\epsilon)}$$

$$0.01$$