

**Instructions**

- Try the following questions and upload your answer script as a zip file to the given link in the UGVLE on/before **16<sup>th</sup> November at 10 PM.**
- It's an individual task. The deadline is 10:00 PM. Submissions will be accepted until midnight with a late penalty of 5% deducted for each hour past the deadline.
- Note: Rename your zip file as indexNo\_1\_last\_namefname.zip.

**01.** Define what an algorithm is and explain whether this program meets the definition of an algorithm.

```
int findMax(int A[], int n) {  
    int max = A[0];  
    for (int i = 1; i < n; i++) {  
        if (A[i] > max)  
            max = A[i];  
    }  
    return max;  
}
```

Analyze the efficiency of this algorithm and express its time complexity using Big notation.

**02.** Define time complexity and explain why it is independent of machine hardware.

**03.** Given two algorithms with time complexities  $T_1(n)=10n$  and  $T_2(n)=n^2$ , determine which is faster for small  $n$  and which for large  $n$ , explaining with rate-of-growth reasoning.

**04.** Remember, Big-O time complexity gives us an idea of the growth rate of a function. In other words, for a large input size  $N$ , as  $N$  increases, in what order of magnitude is the volume of statements executed expected to increase. Rearrange the following functions in increasing order of their big-O complexity:

$4n^2$	$\log_3 n$	$20n$	$n^{2.5}$
$n^{0.00000001}$	$\log n!$	$n^n$	$2^n$
$2^{n+1}$	$2^{2n}$	$3^n$	$n \log n$
$100 n^{2/3}$	$\log [(\log n)^2]$	$n!$	$(n-1)!$

**05.** Find the big-O time complexity of each of the following code fragments:

**(a)**

```
int i = 1;
while (i <= n) {
    System.out.println("*");
    i = 2 * i;
}
```

**(b)**

```
int i = n;
while (i > 0) {
    for (int j = 0; j < n; j++)
        System.out.println("*");
    i = i / 2;
}
```

**(c)**

```
while (n > 0) {
    for (int j = 0; j < n; j++)
        System.out.println("*");
    n = n / 2;
}
```

**(d)**

```
for (int i = 0; i < n; i++) // loop 1
    for (int j = i+1; j > i; j--) // loop 2
        for (int k = n; k > j; k--) // loop 3
            System.out.println("*");
```

**06.** Draw a line from each of the five functions in the center to the best big- $\Omega$  value on the left, and the best big- $O$  value on the right.

$\Omega(1/n)$		$O(1/n)$
$\Omega(1)$		$O(1)$
$\Omega(\log \log n)$		$O(\log \log n)$
$\Omega(\log n)$		$O(\log n)$
$\Omega(\log^2 n)$		$O(\log^2 n)$
$\Omega(\sqrt[3]{n})$		$O(\sqrt[3]{n})$
$\Omega(n/\log n)$	$1/(\log n)$	$O(n/\log n)$
$\Omega(n)$	$7n^5 - 3n + 2$	$O(n)$
$\Omega(n^{1.00001})$	$(n^2 + n)/(\log^2 n + \log n)$	$O(n^{1.00001})$
$\Omega(n^2/\log^2 n)$	$2^{\log^2 n}$	$O(n^2/\log^2 n)$
$\Omega(n^2/\log n)$	$3^n$	$O(n^2/\log n)$
$\Omega(n^2)$		$O(n^2)$
$\Omega(n^{3/2})$		$O(n^{3/2})$
$\Omega(2^n)$		$O(2^n)$
$\Omega(5^n)$		$O(5^n)$
$\Omega(n^n)$		$O(n^n)$
$\Omega(n^{n^2})$		$O(n^{n^2})$