
Computer Systems

Kasun Gunawardana

E-mail: kgg

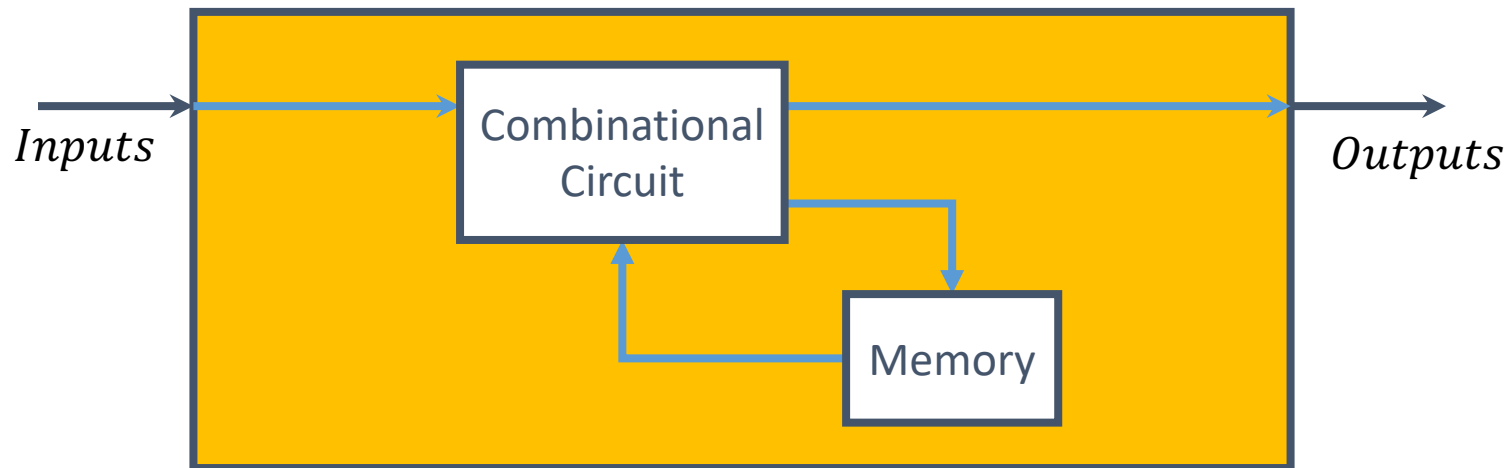


University of Colombo School of Computing

Sequential Logic Circuits

Combinational / Sequential

- **Combinational Circuits:** Outputs only depend on immediate inputs.
- **Sequential Circuits:** Outputs depend not only on immediate inputs, but also previous outputs.



Sequence

- Memory element's transition among states.
- The next state of the memory element is determined by its inputs and the present state.
- A circuit can be seen as a time sequence of inputs, outputs, and internal states.

Sequential Circuits

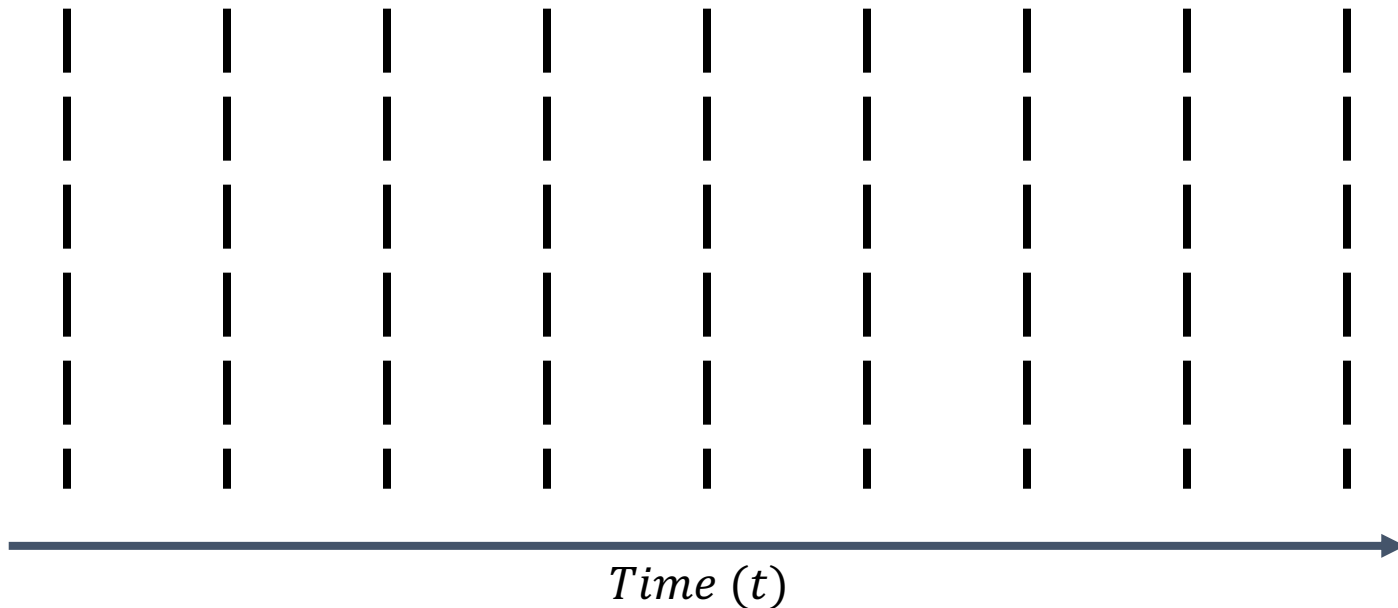
- Asynchronous – State changes immediately after inputs are changed.
- Synchronous – State changes only within discrete time intervals.

Asynchronous Sequential Circuits

- The state of a circuit changes as soon as the inputs change.
- Faster due to immediate state changes.
 - Only propagation delays affects the speed.
- A combinational circuit with feedback.
- Due to this nature, circuit may become unstable.
- Difficult to design circuits with Asynchronous Sequential circuits.

Synchronous Sequential Circuits

- Synchronization is achieved by making the circuit changes its state at discrete intervals of time.

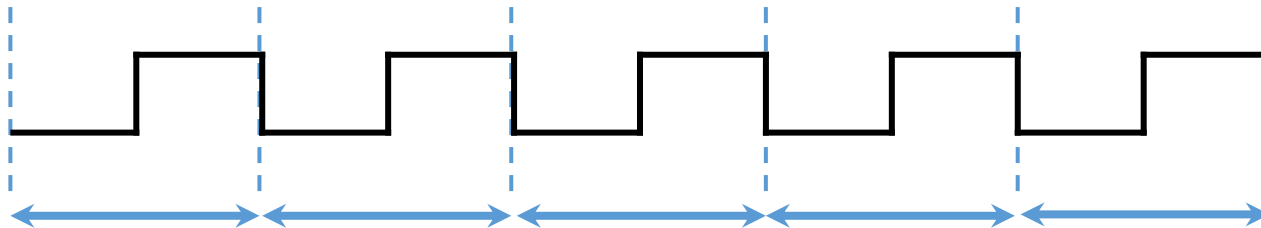
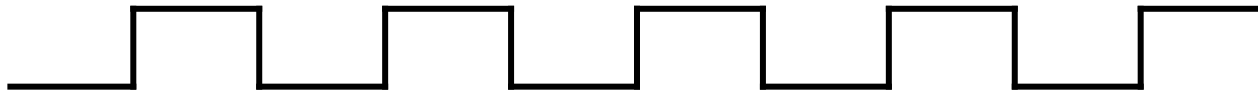


Clocked Synchronous Seq. Circuits

- Separate controller signal for the synchronization.
- A clock can be used to generate signals (pulses).
- Storage elements' states are changed with clock pulses.
- Clock signal is connected to all the storage elements in the circuit.
- Pulses determine **when** the state changes occur.
- Other inputs determine **what** changes will be made.

Clock Signal

Clock Signal



Discrete Time Intervals

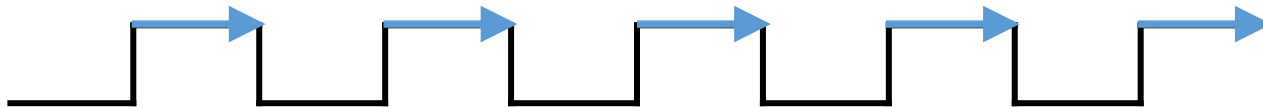
Flip - Flop

- A storage elements used in Clocked Synchronus Sequential Circuits (C.S.S.C) are called **Flip-Flops**.
- It can store one bit of information.
- A C.S.S.C may contain many flip-flops.
- Propagation delays and Clock interval are critical.
- State changes are triggered by the clock pulse transition (Edge sensitive).



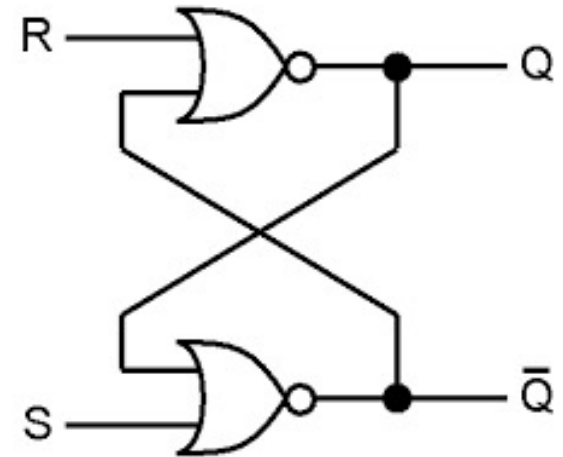
Latch

- A storage element that operates on signal levels rather than signal transition (level sensitive), is called a latch.
- Not operates on clock edges.
- Asynchronus device (Not synchronus).
- Latches are the building blocks for Flip-Flops.



S-R Latch

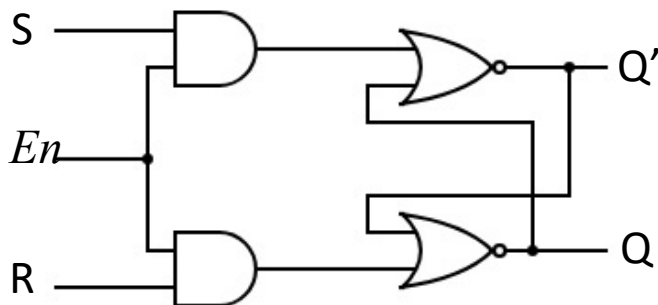
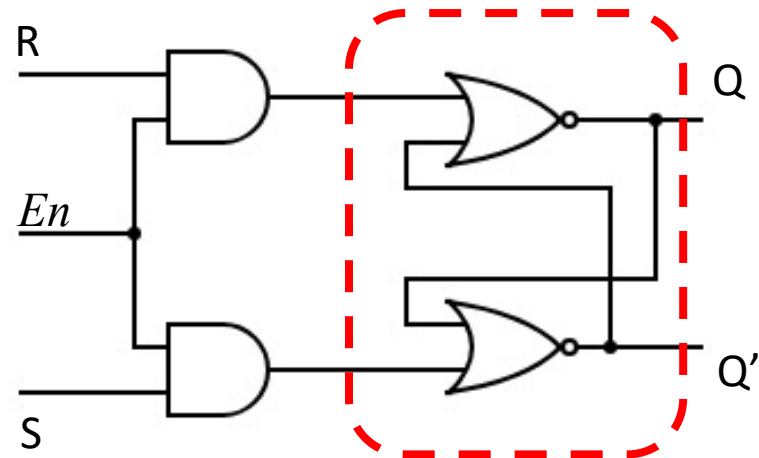
- **S** – Set, **R** – Reset
- Two cross coupled NAND gates can also be used.
- Two outputs; One is the complement of the other.
- When $Q=1 \rightarrow$ Set State
- Otherwise Reset State



S	R	$Q(t+1)$
0	0	$Q(t)$
0	1	0
1	0	1
1	1	Forbidden

S-R Latch with Control Signal

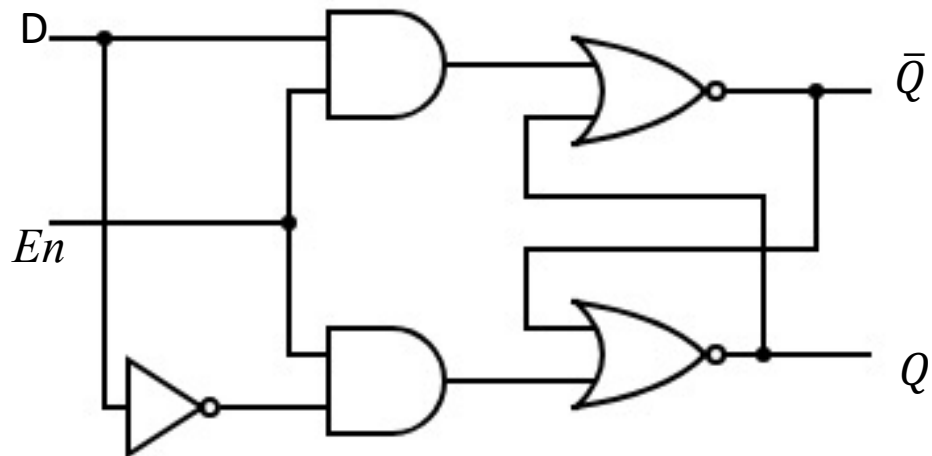
- En – Enable
- When $En = 0$ circuit is a SR Latch with $S=0$ and $R=0$
- En should be triggered to make the S-R Latch operational.



En	S	R	Q(t+1)
0	X	X	Q(t)
1	0	0	Q(t)
1	0	1	0
1	1	0	1
1	1	1	Forbidden

D Latch

- Eliminate undesirable condition of S-R Latch



En	D	Q(t+1)
0	X	Q(t)
1	0	0
1	1	1

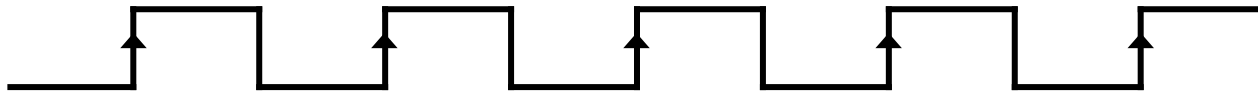
- Value in goes to out (Q) when the circuit is enabled.
- When disabled value Q remains unchanged.

Latches with Clock

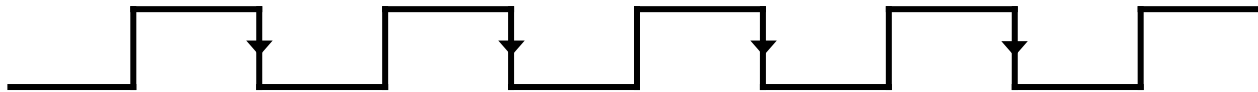
- A clock can be used as a control signal in latches.
- When control signal is active latches make transitions.
- If inputs are changed during clock pulse active period, then within a single clock pulse the latch generates two outputs.
- Latches have the problem of level sensitivity.
- Flip-Flops solves this problem by being edge sensitive.

Edge Sensitive

- Positive Edge (Rising Edge)

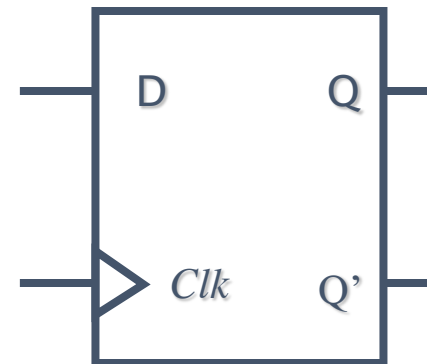


- Negative Edge (Falling Edge)



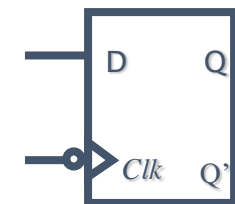
D Flip-Flop

- Edge triggered storage device.
- Store only one bit.



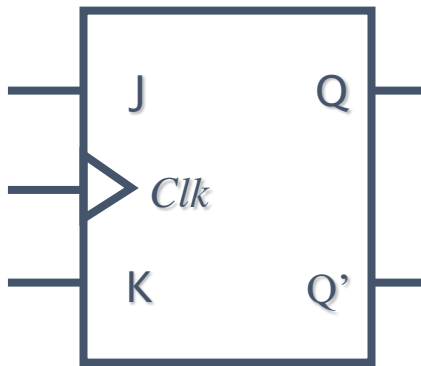
D	Clk	Q(t+1)
0	0	Q(t)
0	1	0
1	0	Q(t)
1	1	1

D	Q(t+1)
0	0
1	1



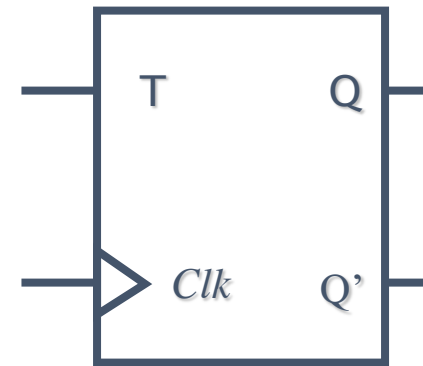
Negative Edge Sensitive
D Flip-Flop

J-K Flip-Flop and T Flip-Flop



J-K Flip-Flop

J	K	$Q(t+1)$
0	0	$Q(t)$
0	1	0
1	0	1
1	1	$Q'(t)$



T Flip-Flop

T	$Q(t+1)$
0	$Q(t)$
1	$Q'(t)$

Next...

Common Applications of Flip-Flops

Computer Systems

Kasun Gunawardana

E-mail: kgg



University of Colombo School of Computing

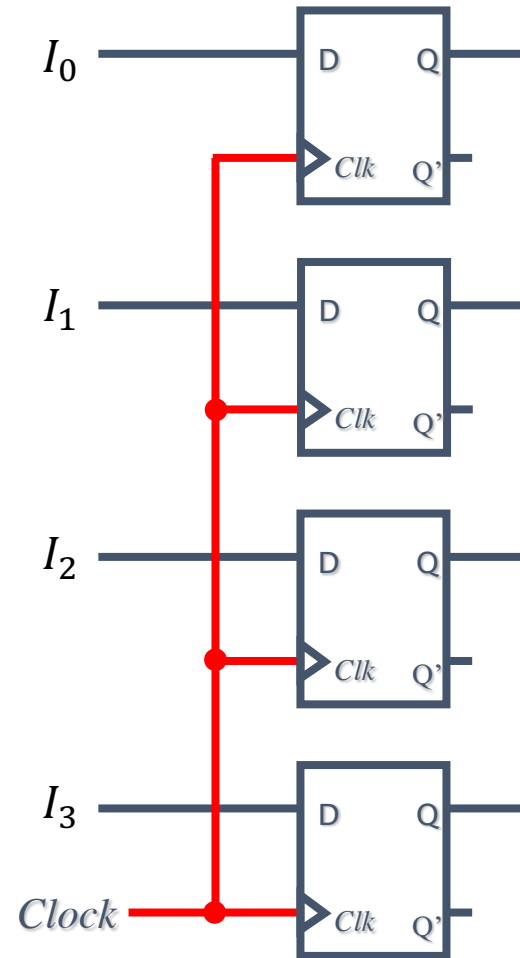
Common Applications of Flip-Flops

Registers

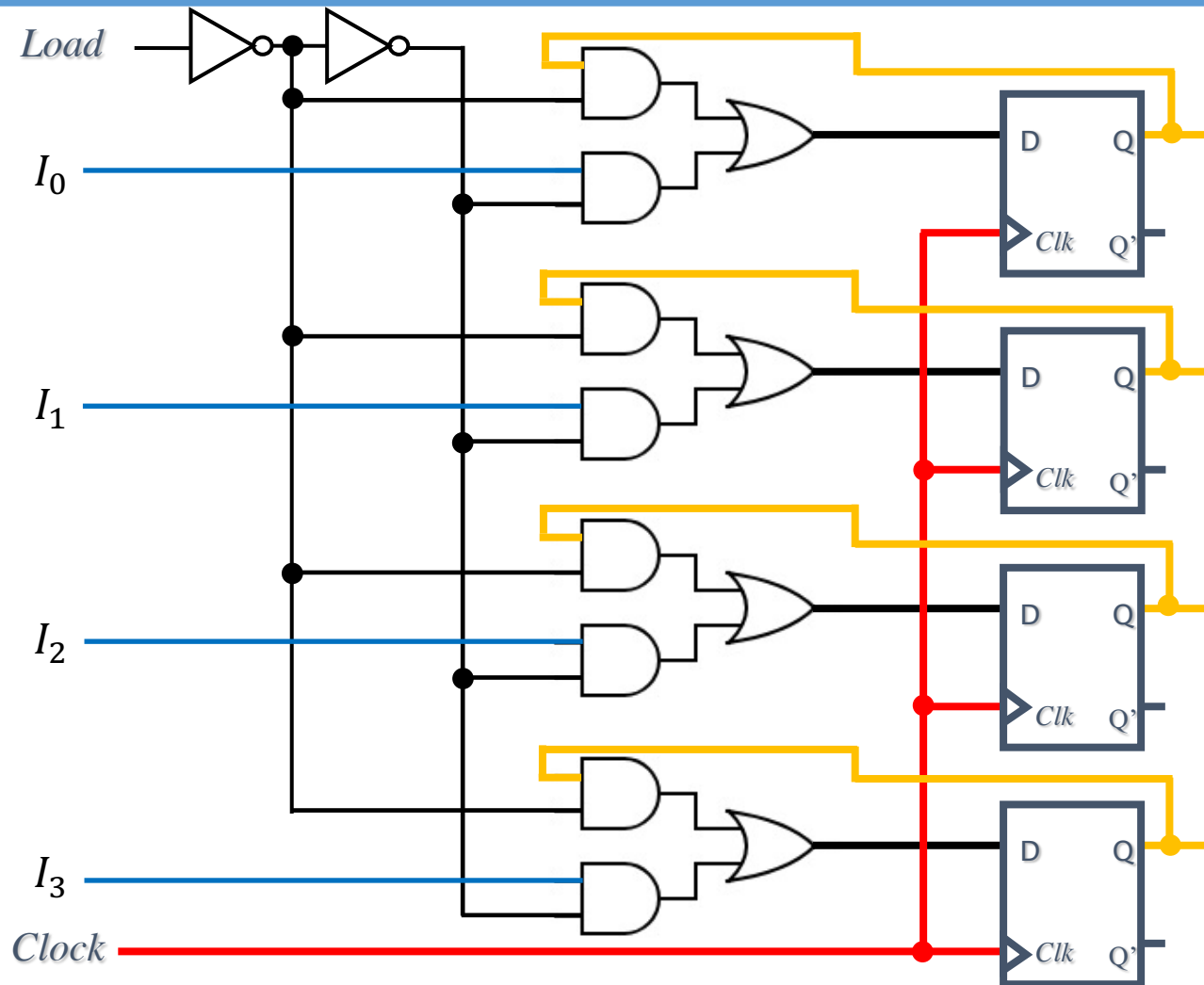
- A series of flip-flops with a common clock input is considered as a Register.
 - Ex. A 32 bit register consists of 32 flip-flops.
- A combinational circuit may combine with a register to aid additional operations.
 - Flip-flops to hold the information
 - Combinational circuit to process/ transfer the information

Storage Register

- Simplest Register
- A group of D Flip-Flops
- Binary inputs will be stored at the flip-flops with a clock signal.
- Stored information can be read at anytime.
- Can have separate asynchronus input signal to clear all flip-flops.



4 bit Register with Parallel Load



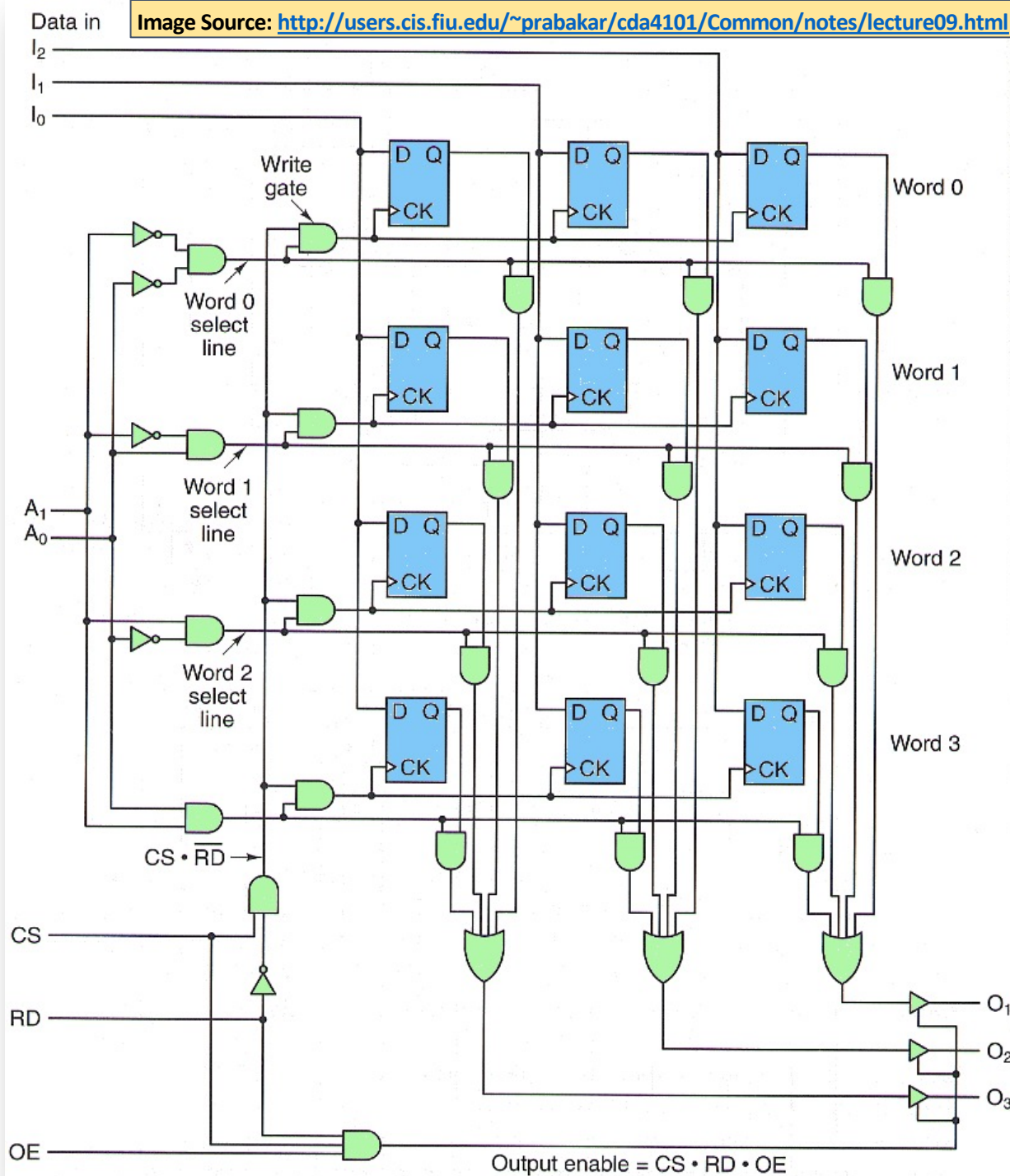
Shift Registers

Explore about “*Shift Registers*”

Start from

- https://en.wikipedia.org/wiki/Shift_register

RAM



4 words
Word Size = 3 bits

Data bus: $I_2 - I_0$

Address bus = $A_1 - A_0$

CS: Internal Activation
RD: Read Enable
OE: Output Enable

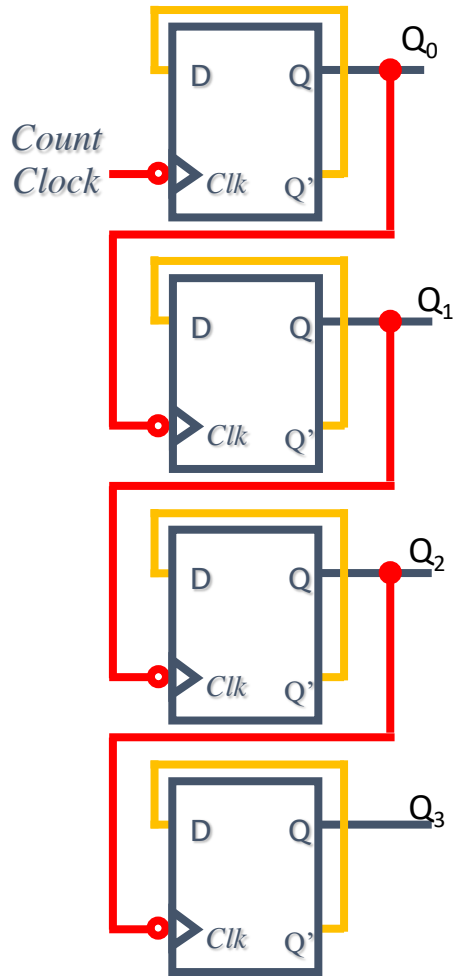
Recognize the Decoder,
Multiplexers here...

Counters

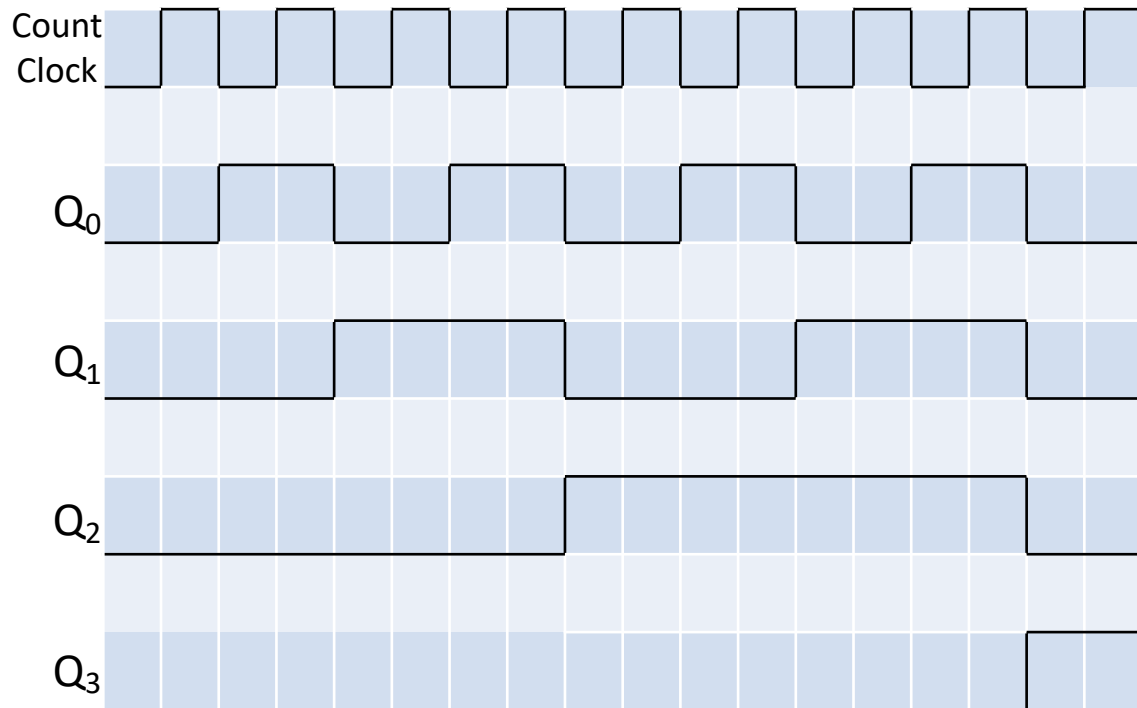
An ordered set of Flip-Flops can produce a defined sequence of states upon a series of triggers.

- **Ripple Counters:** Each Flip-Flop is triggered not by a clock, but by the another flip-flop output transition.
- **Synchronous Counters:** Flip-Flops are triggered by a common clock.

Binary Ripple Counter

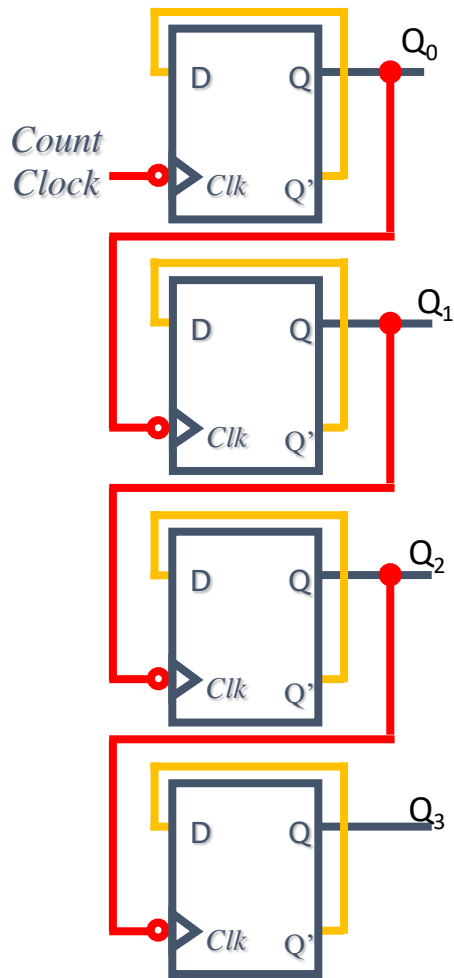


Timing Diagram

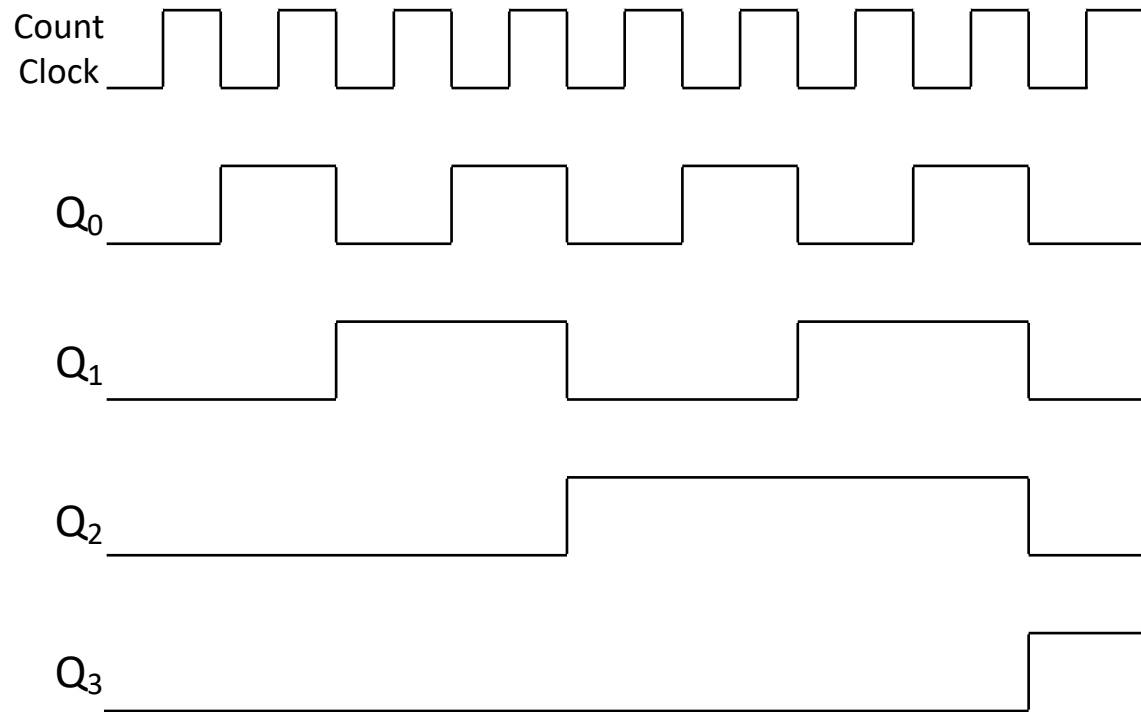


Note: Negative edge sensitive D Flip-Flops

Binary Ripple Counter (Cont.)

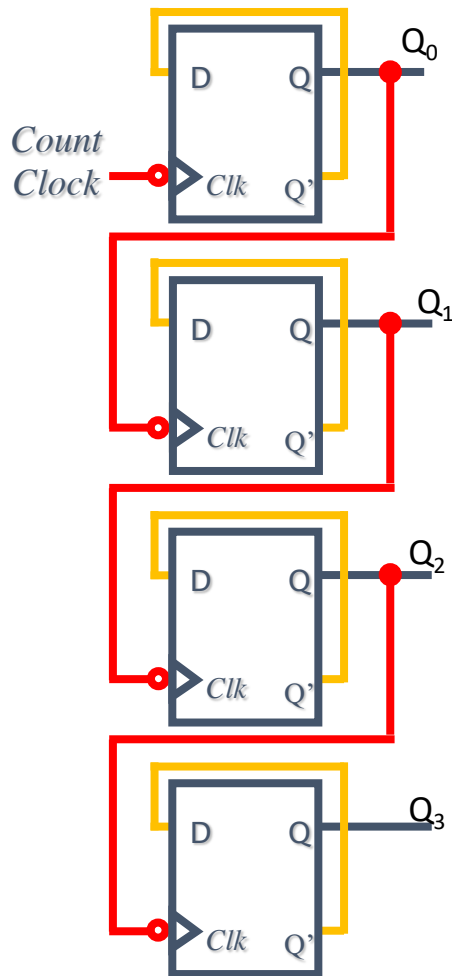


Timing Diagram

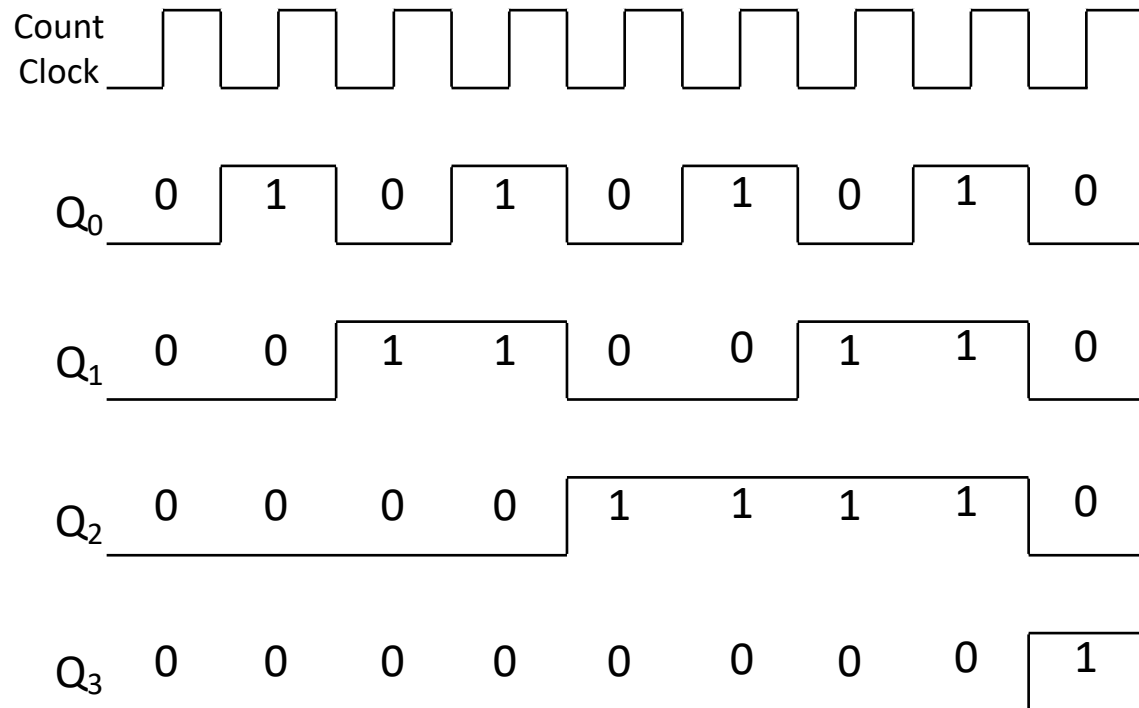


Note: Negative edge sensitive D Flip-Flops

Binary Ripple Counter (Cont.)

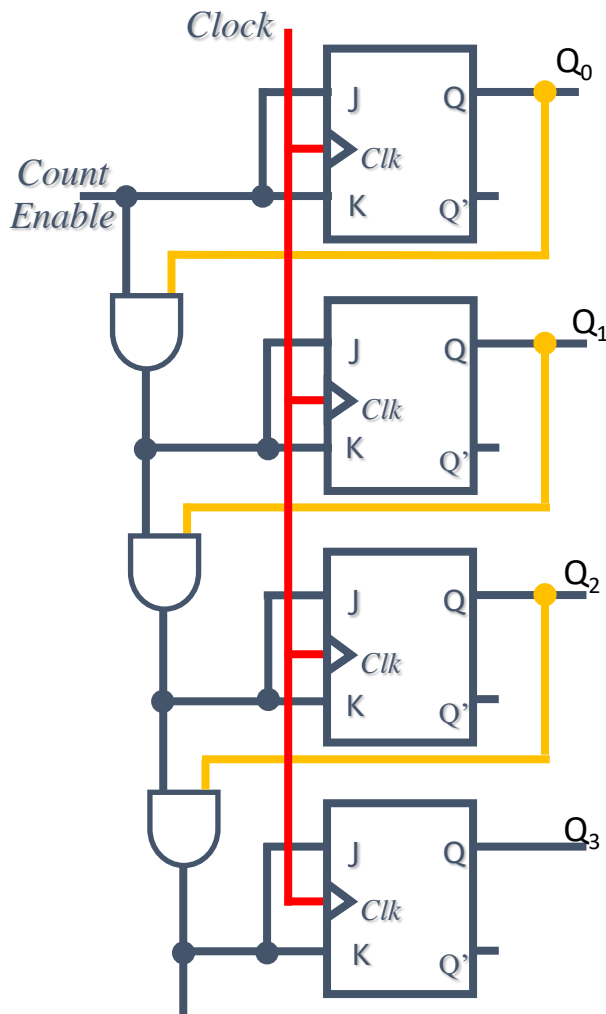


Timing Diagram



Note: Negative edge sensitive D Flip-Flops

Synchronous Binary Counter



Set Up

- Q_0, Q_1, Q_2, Q_3 are zeros at the beginning
- Positive Edge triggered J-K Flip-Flops
- *Count Enable* is set 1
- Common Clock is connected to all Flip-Flops

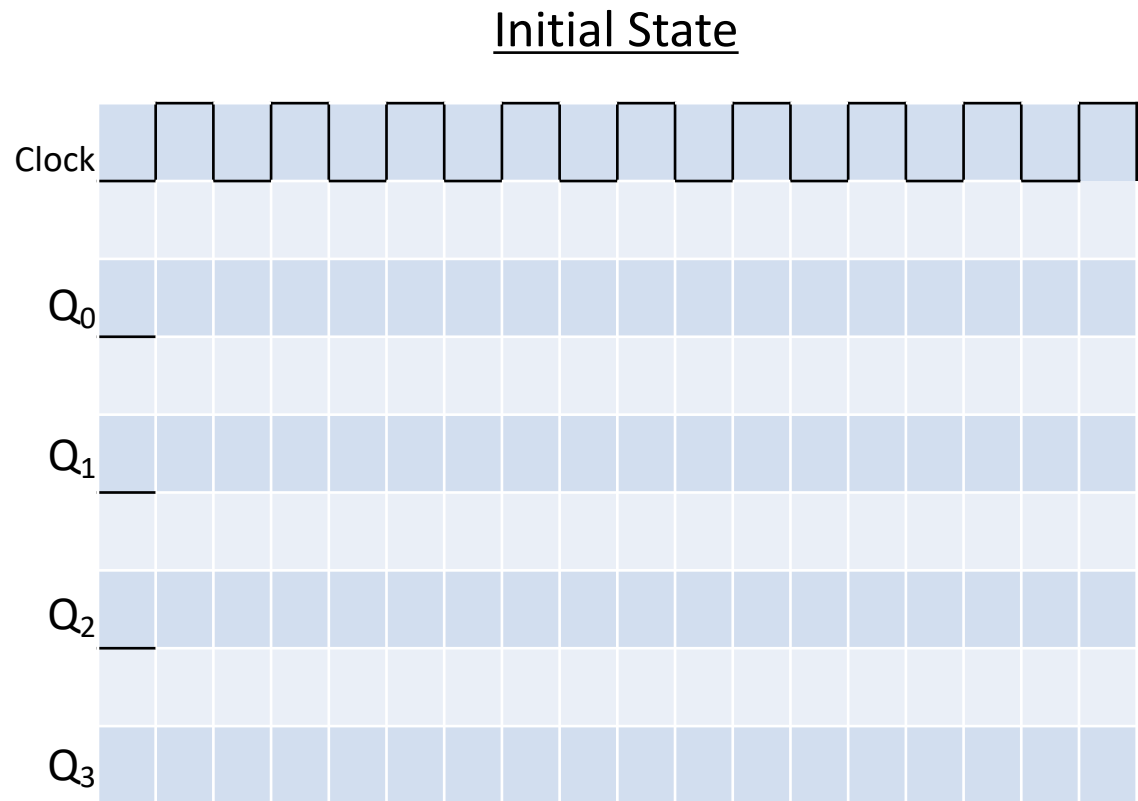
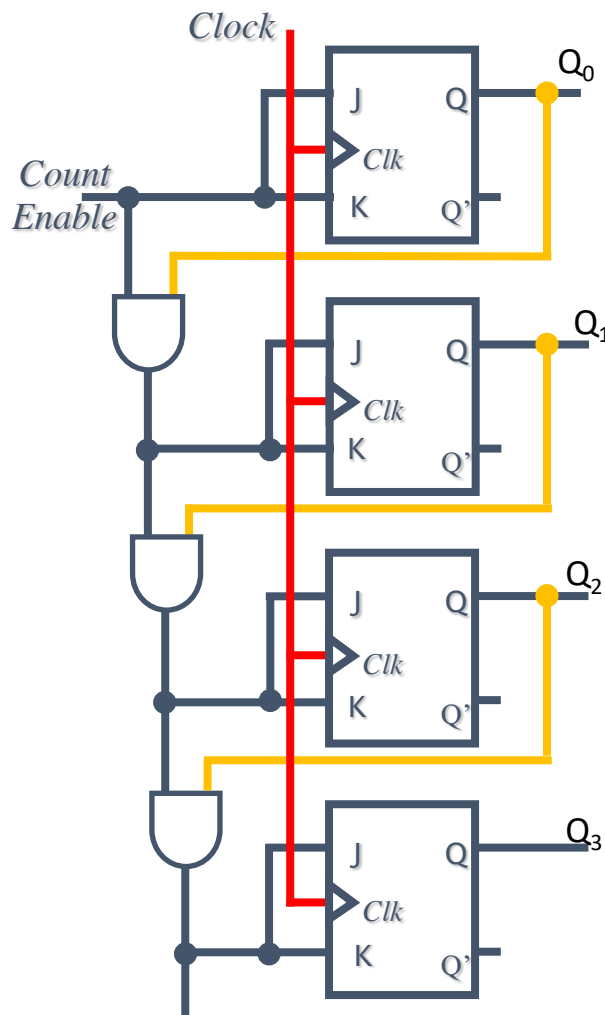
At the very first positive edge of the clock pulse

- First Flip-Flop's J and K inputs are at logical 1
- Second Flip-Flop's J and K inputs are at logical 0
- Third Flip-Flop's J and K inputs are at logical 0
- Fourth Flip-Flop's J and K inputs are at logical 0

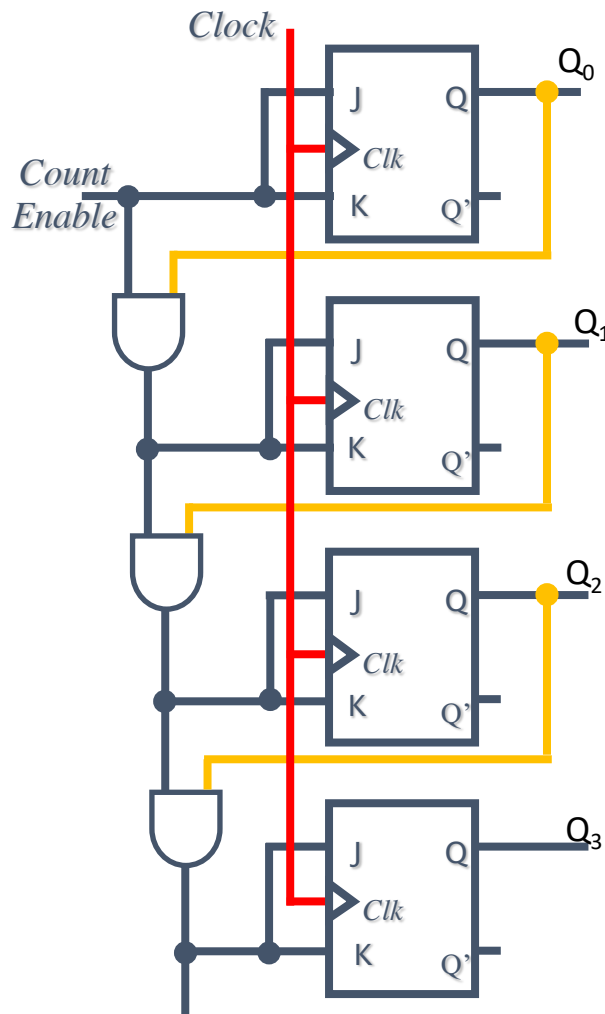
Effect

- Only the first Flip-Flop changes its value
- All the other Flip-Flops remain unchanged
- States are unchanged until it sees the next positive edge clock signal

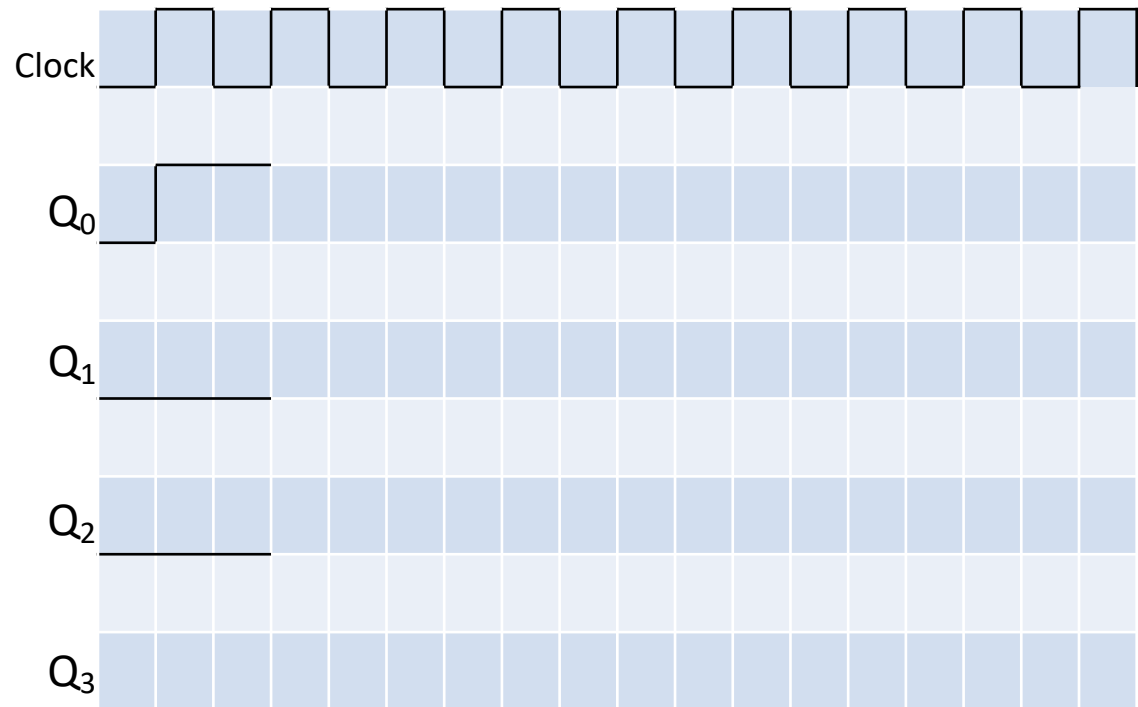
Synchronous Binary Counter (Cont.)



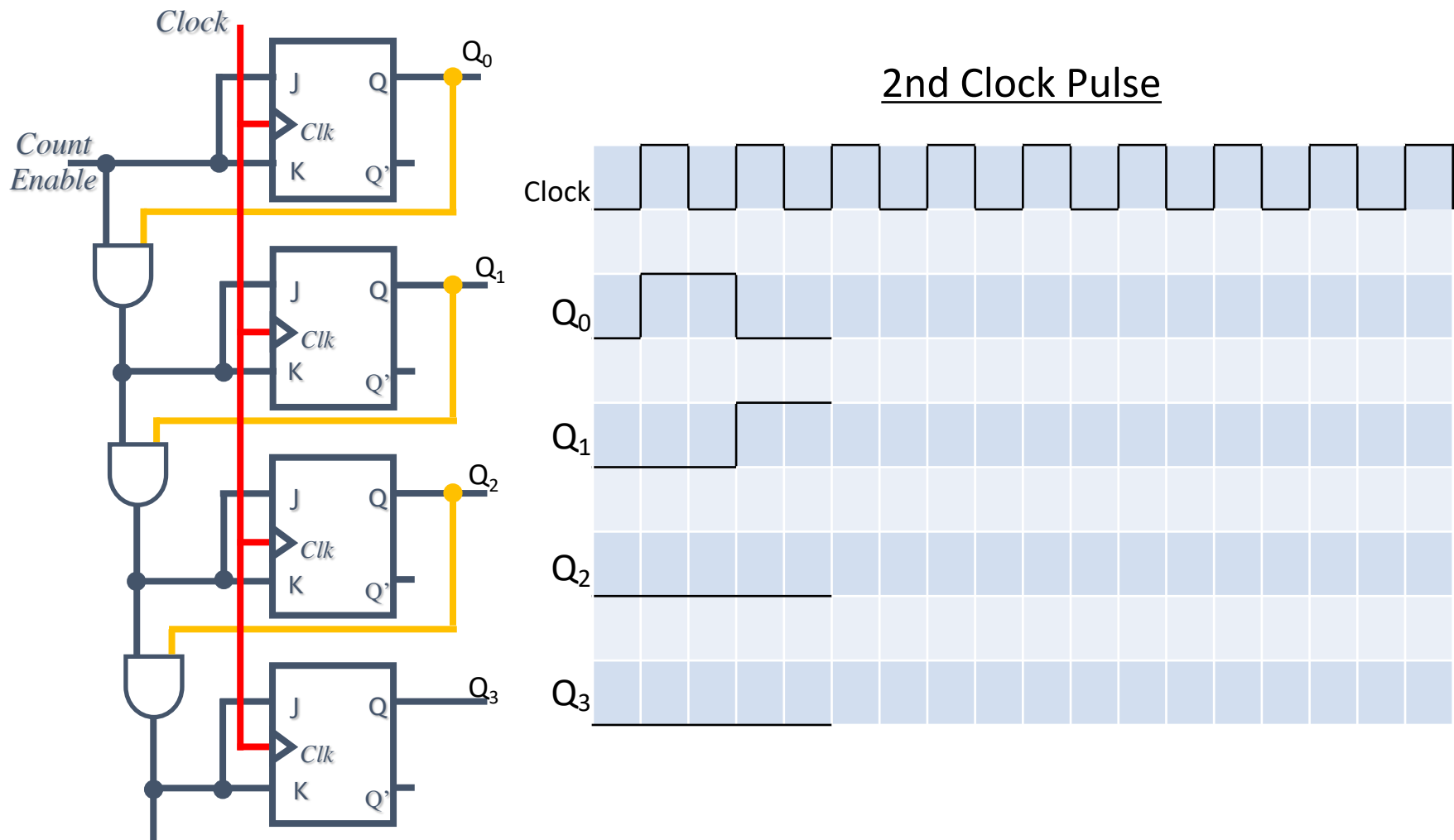
Synchronous Binary Counter (Cont.)



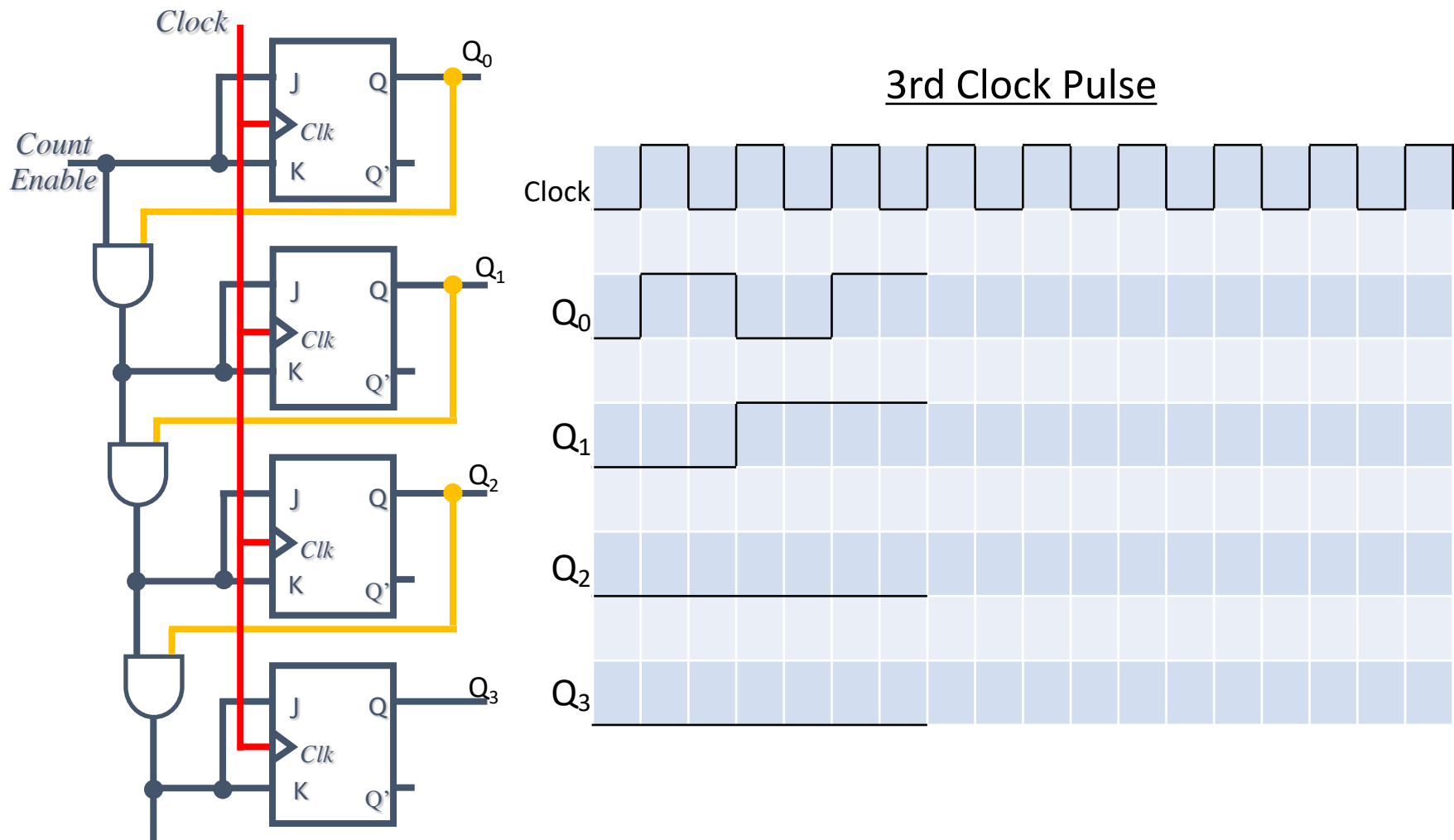
1st Clock Pulse (Positive Edge)



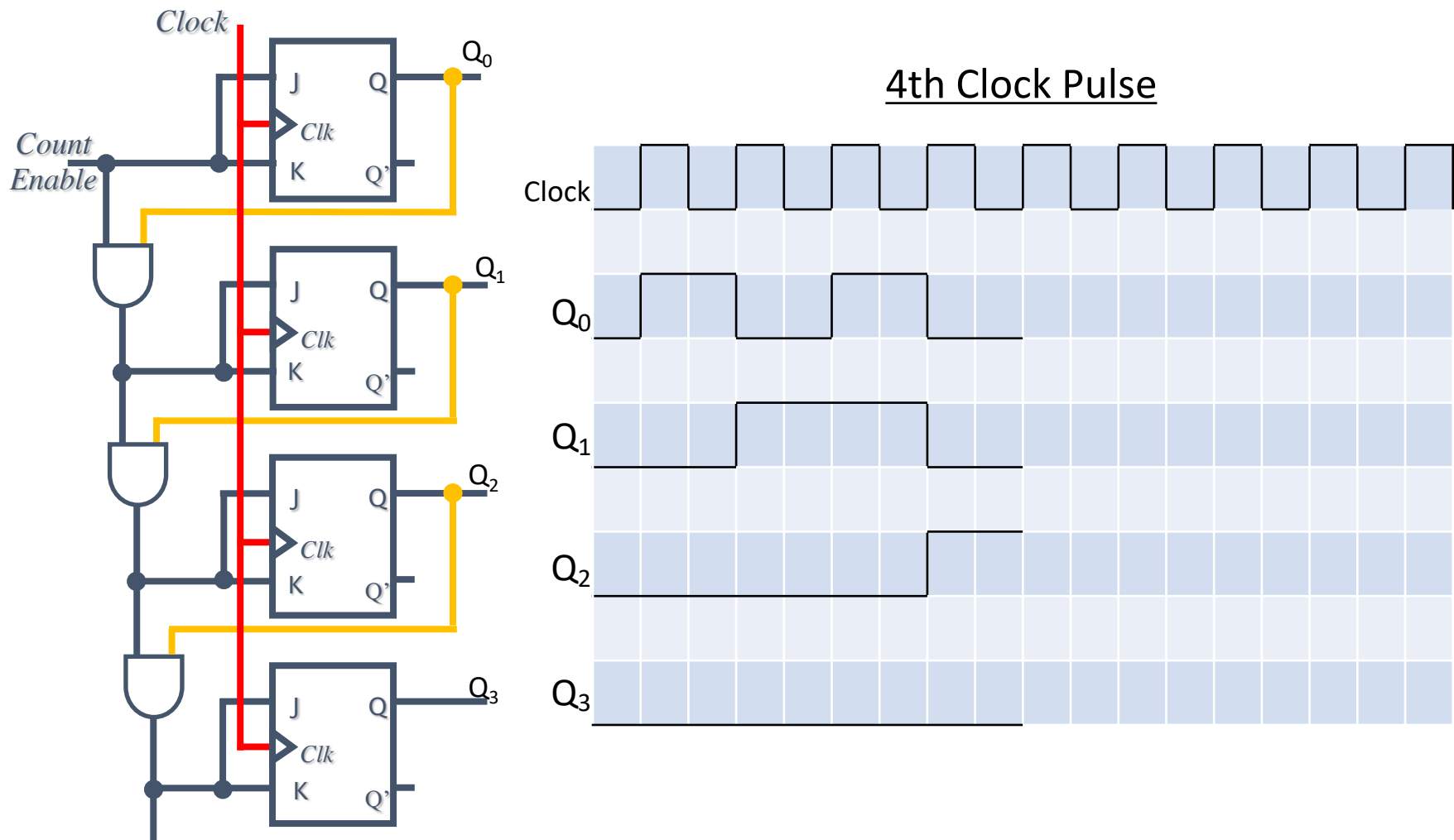
Synchronous Binary Counter (Cont.)



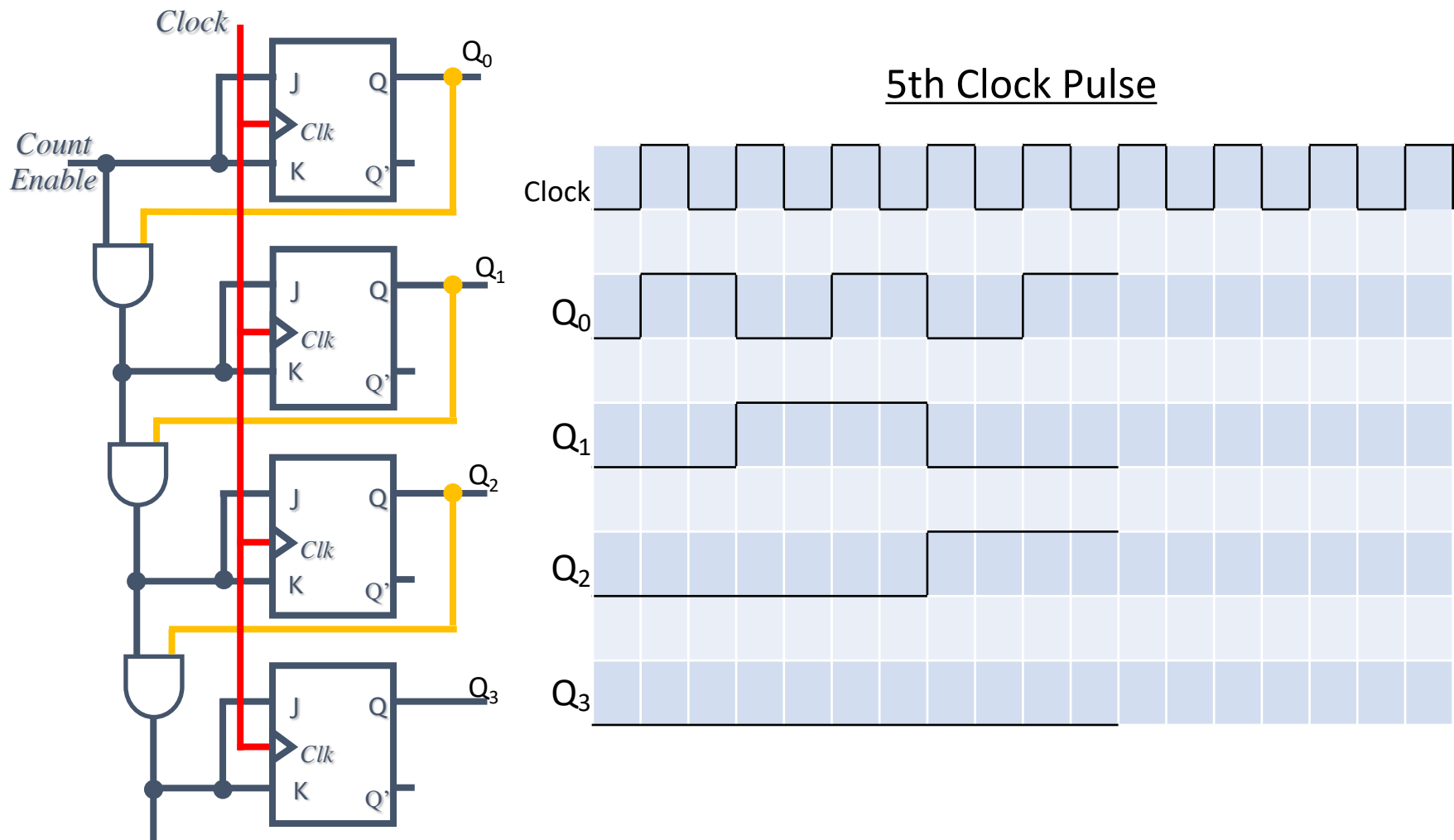
Synchronous Binary Counter (Cont.)



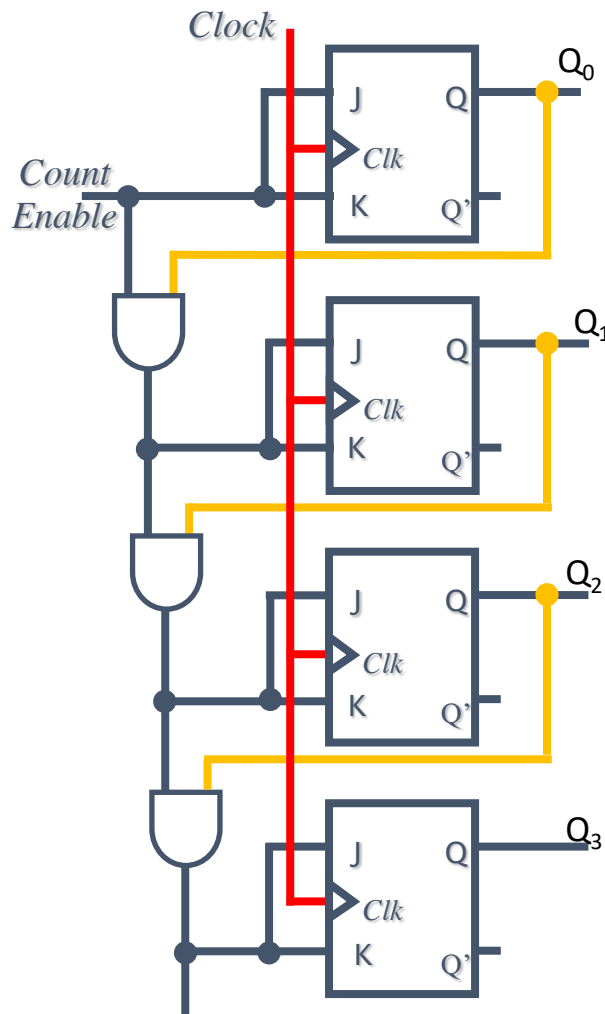
Synchronous Binary Counter (Cont.)



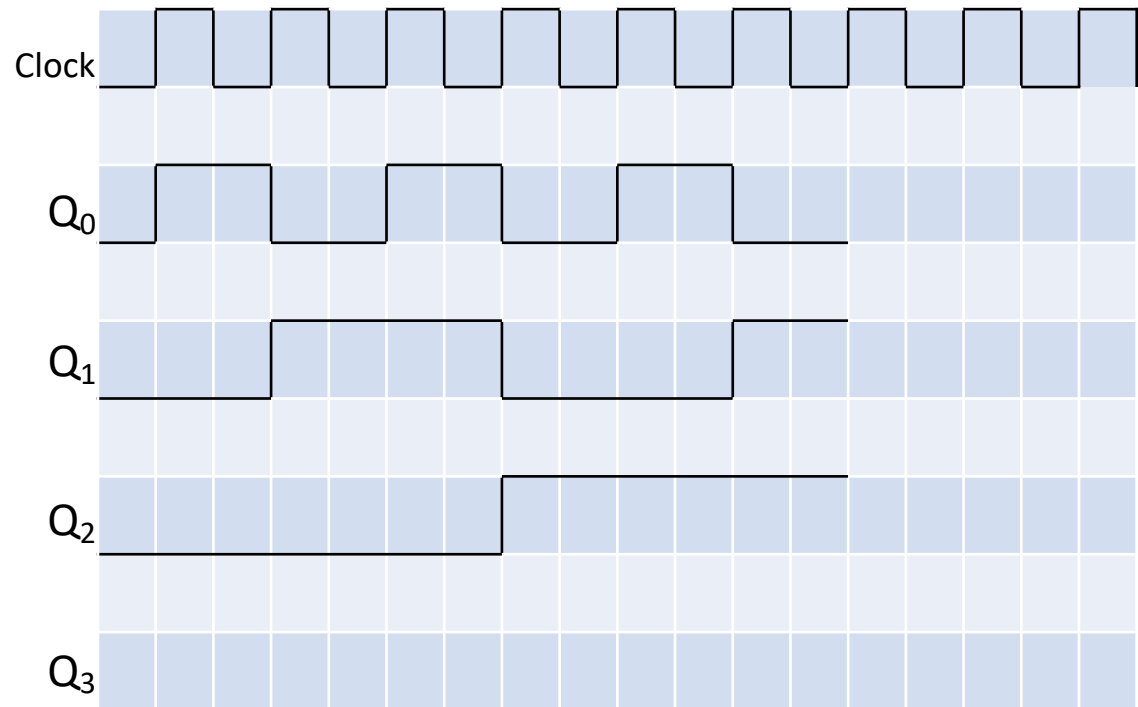
Synchronous Binary Counter (Cont.)



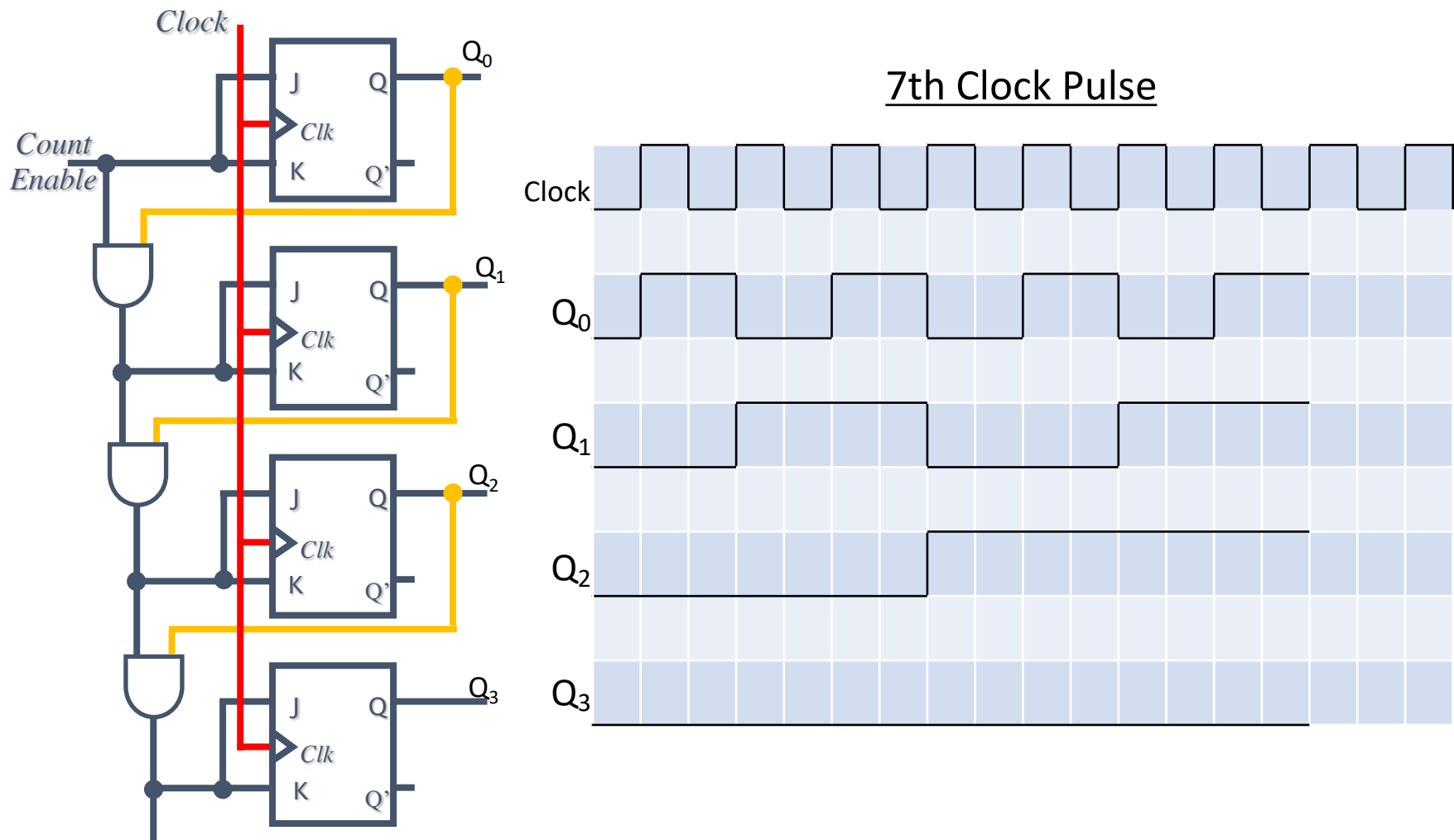
Synchronous Binary Counter (Cont.)



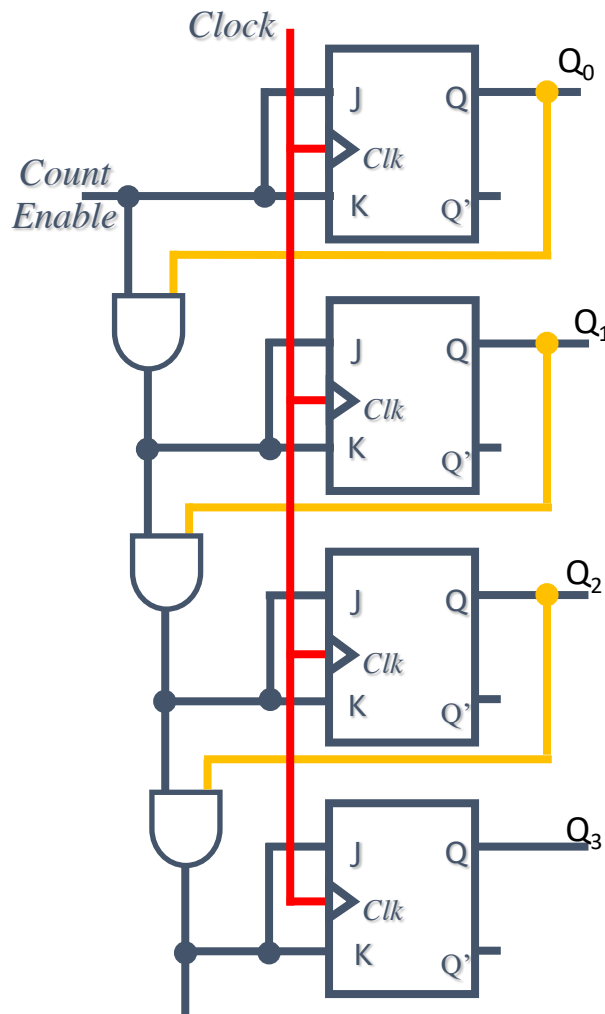
6th Clock Pulse



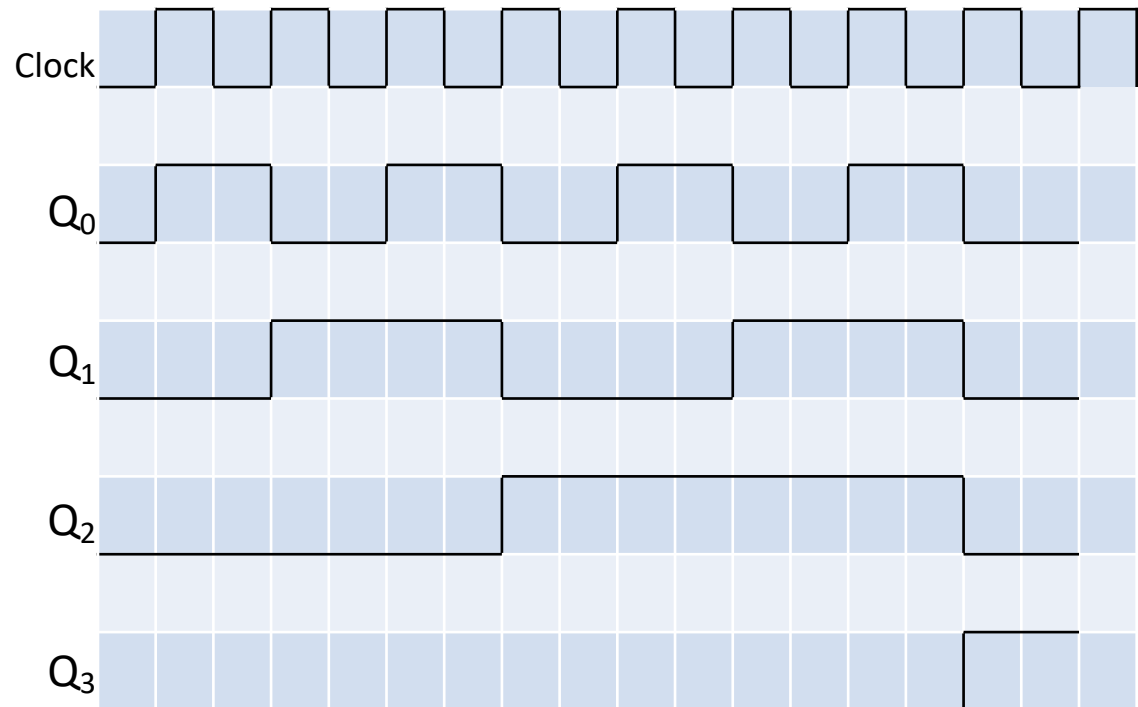
Synchronous Binary Counter. (Cont.)



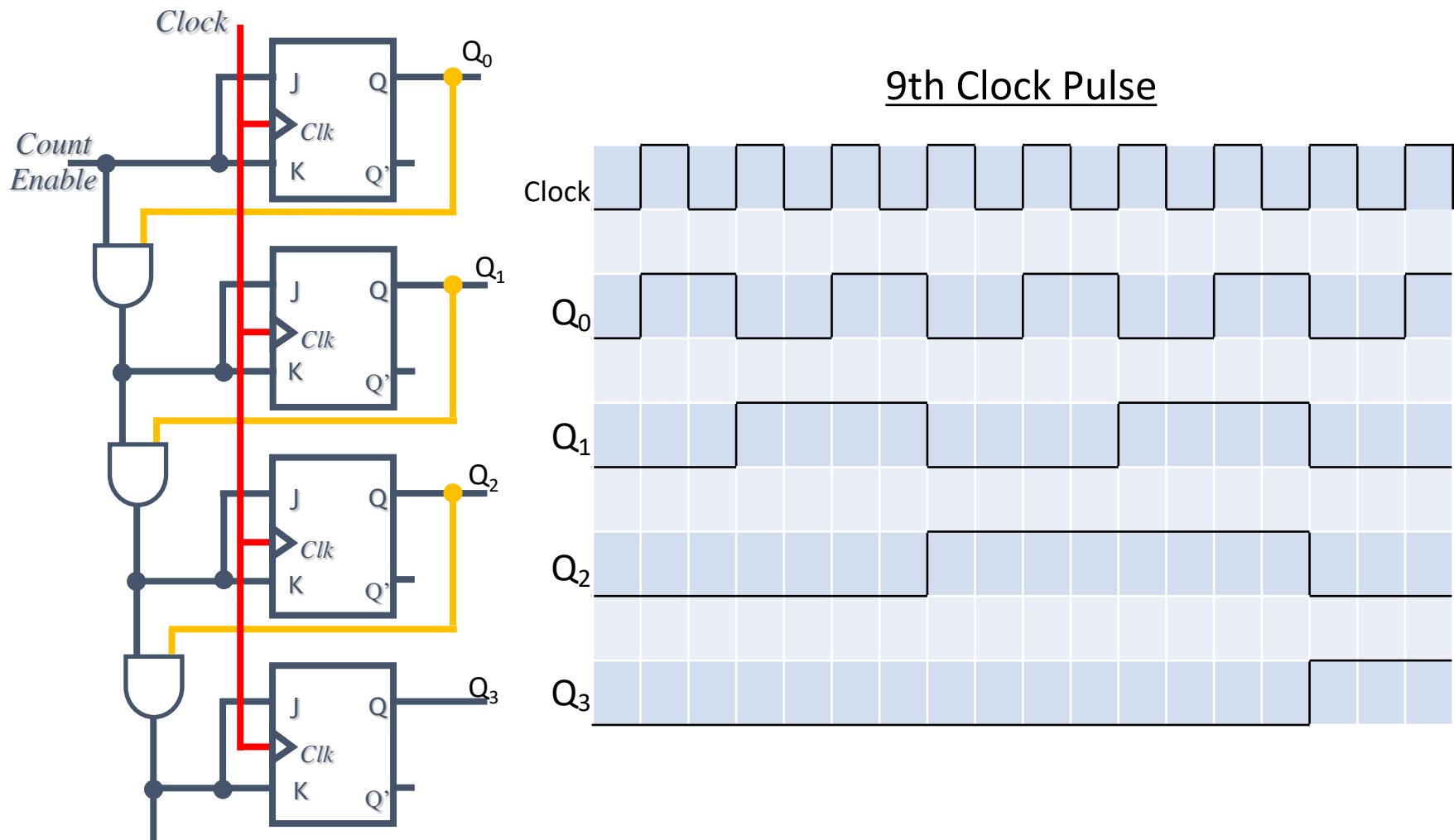
Synchronous Binary Counter (Cont.)



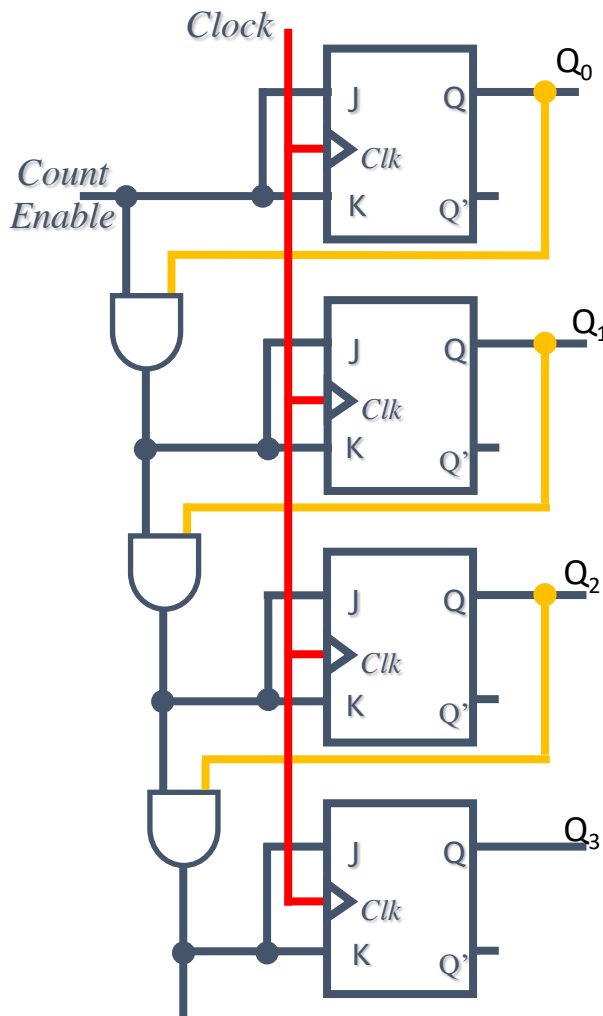
8th Clock Pulse



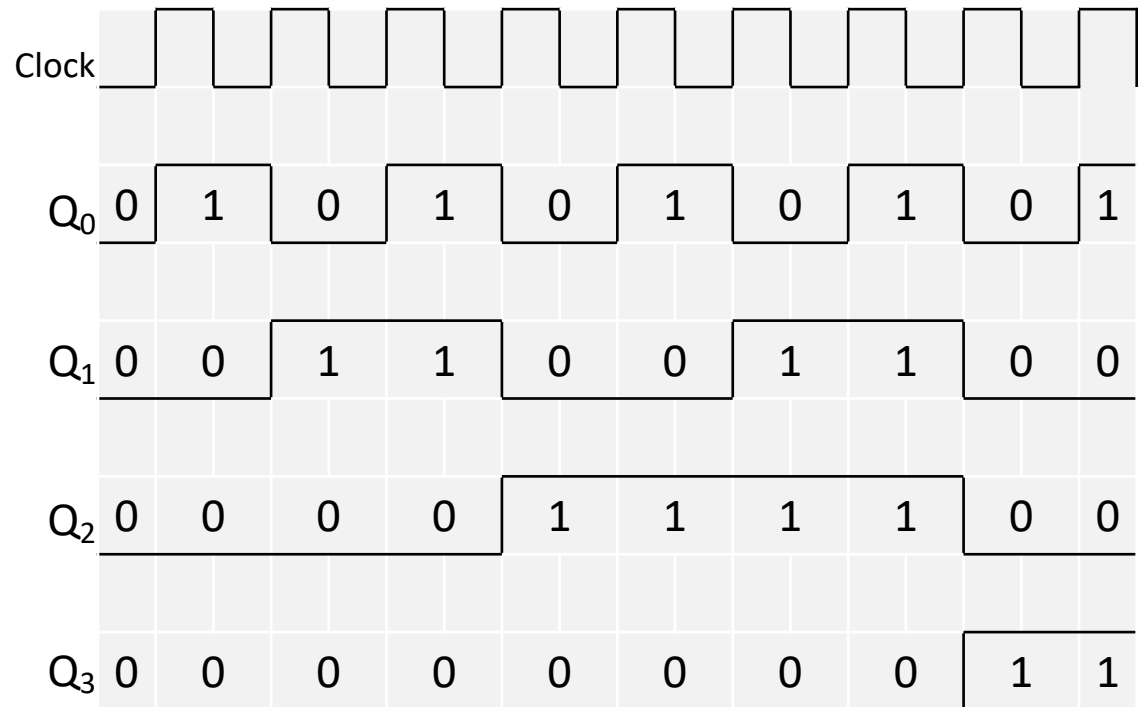
Synchronous Binary Counter. (Cont.)



Synchronous Binary Counter. (Cont.)



9th Clock Pulse



External References

- <http://users.cis.fiu.edu/~prabakar/cda4101/Common/notes/lecture09.html>

Thank You..!
