

Day 13

Assignment 3: Implementing Heap Operations

Code a min-heap in java with methods for insertion, deletion, and fetching the minimum element. Ensure that the heap property is maintained after each operation."

A)

Sure! Below is the implementation of a min-heap in Java with methods for insertion, deletion, and fetching the minimum element, ensuring that the heap property is maintained after each operation.

Java code:

```
package Day13;
import java.util.ArrayList;
public class MinHeap {
    private ArrayList<MinHeapNode> heap;

    public MinHeap() {
        heap = new ArrayList<>();
    }

    // Inserts a new value into the heap
    public void insert(int value) {
        heap.add(new MinHeapNode(value));
        heapifyUp(heap.size() - 1);
    }

    // Removes and returns the minimum element from the heap
    public int deleteMin() {
        if (heap.isEmpty()) {
            throw new IllegalStateException("Heap is empty");
        }
        int min = heap.get(0).getValue();
        MinHeapNode lastElement = heap.remove(heap.size() - 1);
        if (!heap.isEmpty()) {
            heap.set(0, lastElement);
            heapifyDown(0);
        }
        return min;
    }

    // Returns the minimum element from the heap without removing it
    public int getMin() {
        if (heap.isEmpty()) {
            throw new IllegalStateException("Heap is empty");
        }
        return heap.get(0).getValue();
    }

    // Maintains the heap property after insertion
    private void heapifyUp(int index) {
```

```

        int parentIndex = (index - 1) / 2;
        if (index > 0 && heap.get(index).getValue() < heap.get(parentIndex).getValue()) {
            swap(index, parentIndex);
            heapifyUp(parentIndex);
        }
    }

    // Maintains the heap property after deletion
    private void heapifyDown(int index) {
        int smallest = index;
        int leftChildIndex = 2 * index + 1;
        int rightChildIndex = 2 * index + 2;

        if (leftChildIndex < heap.size() && heap.get(leftChildIndex).getValue() <
            heap.get(smallest).getValue()) {
            smallest = leftChildIndex;
        }

        if (rightChildIndex < heap.size() && heap.get(rightChildIndex).getValue() <
            heap.get(smallest).getValue()) {
            smallest = rightChildIndex;
        }

        if (smallest != index) {
            swap(index, smallest);
            heapifyDown(smallest);
        }
    }

    // Swaps two elements in the heap
    private void swap(int i, int j) {
        MinHeapNode temp = heap.get(i);
        heap.set(i, heap.get(j));
        heap.set(j, temp);
    }

    public static void main(String[] args) {
        MinHeap minHeap = new MinHeap();
        minHeap.insert(3);
        minHeap.insert(1);
        minHeap.insert(6);
        minHeap.insert(5);
        minHeap.insert(2);
        minHeap.insert(4);

        System.out.println("Minimum element: " + minHeap.getMin()); // Output: 1
        System.out.println("Deleted minimum element: " + minHeap.deleteMin()); // Output: 1
        System.out.println("Minimum element after deletion: " + minHeap.getMin()); // Output: 2
    }

```

```
}  
}
```

Output:

```
true  
true  
true  
true  
false  
false  
false
```

Explanation:**1. MinHeap Class:**

- Uses an ArrayList to store the elements of the heap.
- Provides methods for insertion, deletion, and fetching the minimum element.

2. insert Method:

- Adds the new value to the end of the list.
- Calls heapifyUp to maintain the heap property, moving the new element up to its correct position.

3. deleteMin Method:

- Removes and returns the minimum element, which is the root of the heap (index 0).
- Replaces the root with the last element in the list and removes the last element.
- Calls heapifyDown to maintain the heap property, moving the new root down to its correct position.

4. getMin Method:

- Returns the minimum element without removing it. Throws an exception if the heap is empty.

5. *heapifyUp Method*:

- Moves an element up to its correct position by comparing it with its parent and swapping if necessary.

6. heapifyDown Method:

- Moves an element down to its correct position by comparing it with its children and swapping with the smallest child if necessary.

7. swap Method:

- Swaps two elements in the list.

8. Main Method:

- Demonstrates the usage of the MinHeap class by inserting elements, fetching the minimum, and deleting the minimum element.

This implementation ensures that the heap property is maintained after each operation, with insertion and deletion operations having a time complexity of $O(\log n)$, where n is the number of elements in the heap.