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ASSIGNMENT-14

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Download all python codes from

https://github.com/Gayathri1729/SRFP/tree/main/ Assignment14

and latex-tikz codes from

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1 OPTIMIZATION 2.2

Find the maximum profit that a company can make, if the profit function is given by $p(x) = 41 - 72x - 18x^2$

2 SOLUTION

Lemma 2.1. A function f(x) is said to be convex if following inequality is true for $\lambda \in [0, 1]$:

$$\lambda f(x_1) + (1 - \lambda)f(x_2) \ge f(\lambda x_1 + (1 - \lambda)x_2)$$
 (2.0.1)

Given the profit function of the company is

$$p(x) = 41 - 72x - 18x^2 (2.0.2)$$

Checking convexity of p(x):

$$\lambda \left(41 - 72x_1 - 18x_1^2\right) + (1 - \lambda)\left(41 - 72x_2 - 18x_2^2\right)$$

$$\geq \left(41 - 72(\lambda x_1 + (1 - \lambda)x_2) - 18(\lambda x_1 + (1 - \lambda)x_2)^2\right)$$
(2.0.3)

resulting in

$$18\lambda(\lambda - 1)(x_1 - x_2)^2 \ge 0 \tag{2.0.4}$$

$$\implies \lambda(\lambda - 1) \ge 0$$
 (2.0.5)

is not true.

 \implies The function is not convex. Consider the derivative of p(x),

$$\frac{dp(x)}{dx} = -36x - 72\tag{2.0.6}$$

Critical point is given by

$$\frac{dp(x)}{dx} = 0\tag{2.0.7}$$

$$\implies x = -2 \tag{2.0.8}$$

is the point where the profit function will be maximum. And the maximum profit will be p(-2)

$$p(-2) = 41 - 72(-2) - 18(-2)^2 = 113$$
 (2.0.9)

Maxima =
$$113$$
 (2.0.10)

$$Maxima Point = -2$$
 (2.0.11)

It is clear from the Fig.2.1

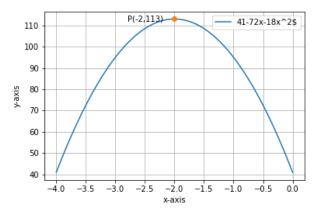


Fig. 2.1: $p(x) = 41 - 72x - 18x^2$