

ASSIGNMENT-14

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Download all python codes from

<https://github.com/Gayathri1729/SRFP/tree/main/Assignment14>

and latex-tikz codes from

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Taking $x_0 = 2, \alpha = 0.001$ and precision = 0.00000001, values obtained using python are:

$$\text{Maxima} = 112.99999999999876 \approx 113 \quad (2.0.8)$$

$$\text{Maxima Point} = -1.9999997364868565 \approx -2 \quad (2.0.9)$$

It is clear from the Fig.2.1

1 OPTIMIZATION 2.2

Find the maximum profit that a company can make, if the profit function is given by $p(x) = 41 - 72x - 18x^2$

2 SOLUTION

Lemma 2.1. A function $f(x)$ is said to be convex if following inequality is true for $\lambda \in [0, 1]$:

$$\lambda f(x_1) + (1 - \lambda)f(x_2) \geq f(\lambda x_1 + (1 - \lambda)x_2) \quad (2.0.1)$$

Given the profit function of the company is

$$p(x) = 41 - 72x - 18x^2 \quad (2.0.2)$$

Checking convexity of $p(x)$:

$$\begin{aligned} & \lambda(41 - 72x_1 - 18x_1^2) + (1 - \lambda)(41 - 72x_2 - 18x_2^2) \\ & \geq (41 - 72(\lambda x_1 + (1 - \lambda)x_2) - 18(\lambda x_1 + (1 - \lambda)x_2)^2) \end{aligned} \quad (2.0.3)$$

resulting in

$$18\lambda(\lambda - 1)(x_1 - x_2)^2 \geq 0 \quad (2.0.4)$$

$$\Rightarrow \lambda(\lambda - 1) \geq 0 \quad (2.0.5)$$

is not true .

\Rightarrow The function is not convex.

Using gradient ascent method we can find its maxima,

$$x_{n+1} = x_n + \alpha \nabla f(x_n) \quad (2.0.6)$$

$$\Rightarrow x_{n+1} = x_n + \alpha (-36x_n - 72) \quad (2.0.7)$$

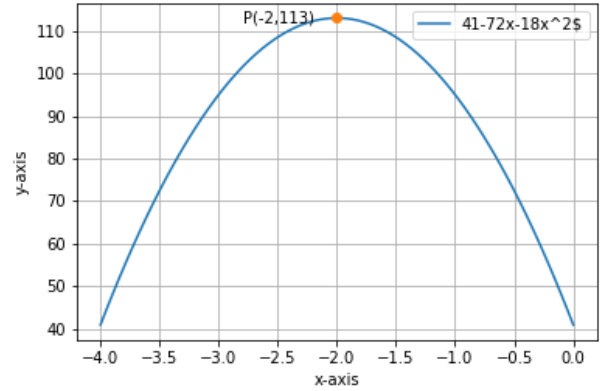


Fig. 2.1: $p(x) = 41 - 72x - 18x^2$