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### 1. Aim:

To train and test a Feedforward Neural Network for MNIST Digit Classification. The model is to be built

- Using library functions (Keras is used here)
- From scratch using gradient descent

### 2. Brief description:

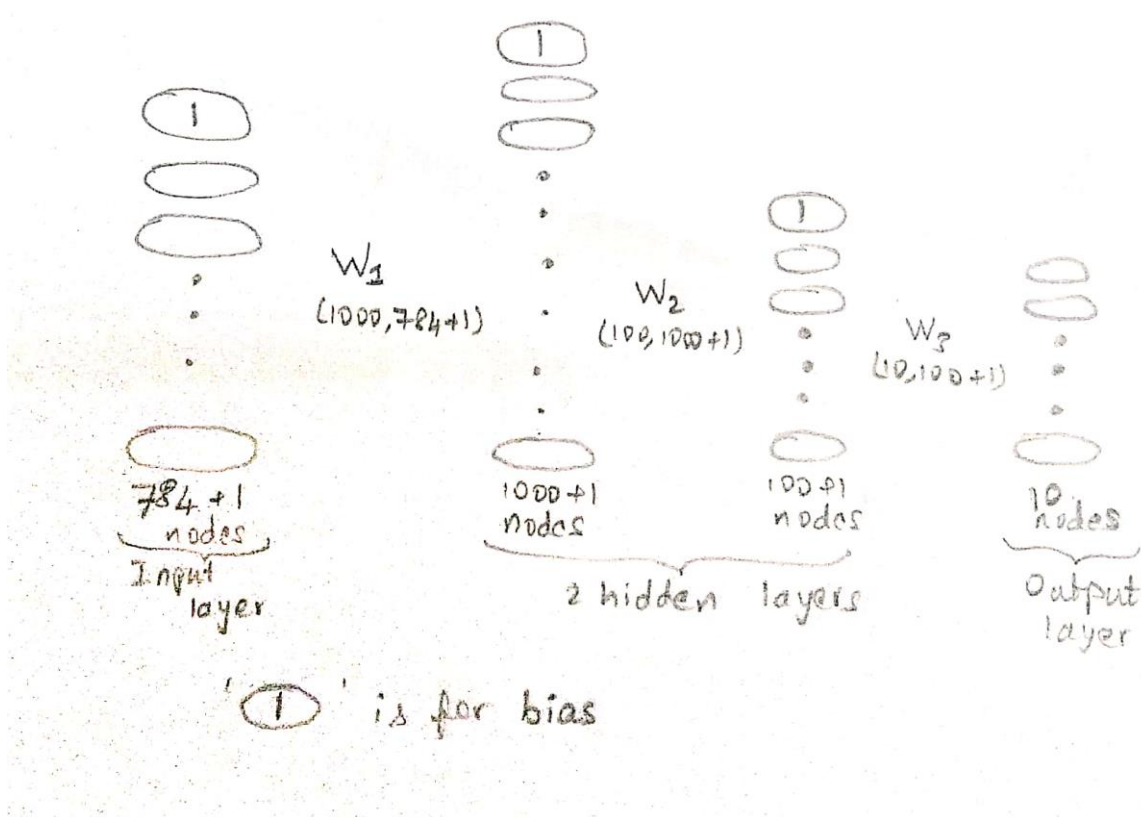


Fig. Model Architecture

The activation functions used are 'tanh' for the hidden layers and 'sigmoid' for the output layer. If 'm' represents the number of samples, the input dimensions are  $(785, m)$  and output dimensions are  $(10, m)$ .

### 3. Procedure and Results:

→ The MNIST dataset is imported, split into training and test data, bias ones are added to the input features  $x$ , and the  $y$  labels are one hot encoded.

#### a) Using Keras:

- Keras and other required libraries are imported
- The model is designed following the diagram
- The stochastic gradient descent optimizer and categorical cross entropy loss function are used to compile the model

→ The model is trained, for 10 epochs with a batch size of 100, tested and the accuracies achieved are

Training accuracy: 95.69%

Testing accuracy: 96.58%

b) From scratch:

→ The required libraries are imported

→ Functions for training, which includes forward and back-propagation, and testing, which includes only the forward propagation using the trained weights, are defined.

→ While back-propagating, the difference between the predicted and true labels are taken and back-propagated to find the weight gradients

$$\Delta W(l) = \delta(l+1) * g'(\Delta Net(l)) * x(l).T$$

where,  $g'$  = activation function's gradient

$l$  = layer

$T$  = transpose

$\delta$  = error

$\Delta Net = W * x$

→ Using a stochastic gradient descent optimizer and mean square error as the cost function, the model is trained, for 200 epochs, tested and the accuracies achieved are

Training accuracy: 91.87%

Testing accuracy: 92.38%

|   | 0   | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 0 | 472 | 0   | 1   | 2   | 1   | 1   | 4   | 2   | 0   | 0   |
| 1 | 0   | 545 | 5   | 2   | 0   | 4   | 0   | 1   | 4   | 0   |
| 2 | 7   | 8   | 429 | 5   | 6   | 2   | 5   | 5   | 14  | 3   |
| 3 | 1   | 4   | 16  | 439 | 0   | 17  | 1   | 7   | 3   | 6   |
| 4 | 0   | 4   | 7   | 0   | 506 | 0   | 7   | 0   | 1   | 16  |
| 5 | 10  | 2   | 3   | 19  | 4   | 375 | 10  | 1   | 8   | 4   |
| 6 | 2   | 2   | 1   | 0   | 3   | 6   | 481 | 0   | 4   | 0   |
| 7 | 6   | 7   | 4   | 0   | 13  | 0   | 0   | 501 | 1   | 10  |
| 8 | 2   | 9   | 6   | 10  | 2   | 6   | 4   | 0   | 422 | 3   |
| 9 | 8   | 2   | 0   | 5   | 10  | 3   | 2   | 15  | 2   | 449 |

Fig. Confusion matrix of test data; rows → true labels, columns → predicted labels

→ The accuracy achieved from five-fold cross validation training and testing is 90.25%

