

#8

# Banked Roads

Circular Motion

PhD Series



$\theta$



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## List of Content on Eduniti YouTube Channel:

1. PYQs Video Solution Topic Wise:  
(a) JEE Main 2018/2020/2021 Feb & March
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# ***BANKED ROADS***

**PhD SERIES**

1. Lets Understand all Cases
2.  $V$  minimum
3.  $V$  maximum
4. Conclusion
5. 2021 PYQs

"JOIN"



# 1. Lets Understand all Cases

*Refer Video to understand it.*





## 2. V minimum

$$f = \mu N$$

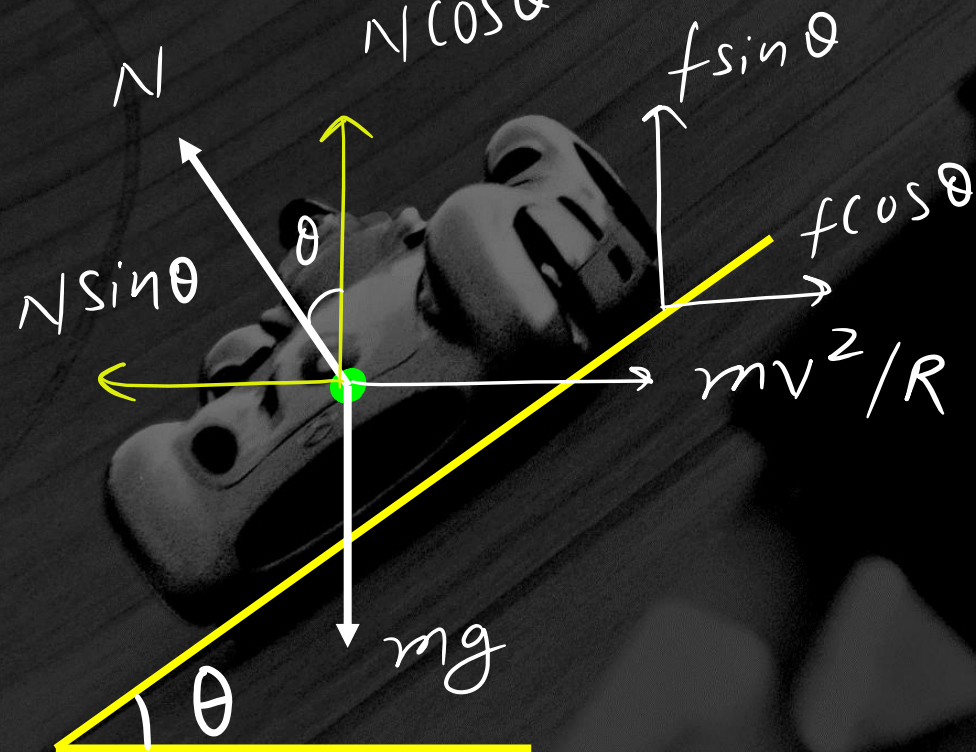
$$N \sin \theta = \frac{mv^2}{R} + f \cos \theta \Rightarrow N(\sin \theta - \mu \cos \theta) = \frac{mv^2}{R} \quad \text{--- (1)}$$

$$N \cos \theta + f \sin \theta = mg \Rightarrow N(\cos \theta + \mu \sin \theta) = mg \quad \text{--- (2)}$$

① / ②

$$\frac{\sin \theta - \mu \cos \theta}{\cos \theta + \mu \sin \theta} = \frac{v^2}{Rg}$$

$$\Rightarrow V_{\min} = \sqrt{Rg \left( \frac{\tan \theta - \mu}{1 + \mu \tan \theta} \right)}$$





### 3. V maximum

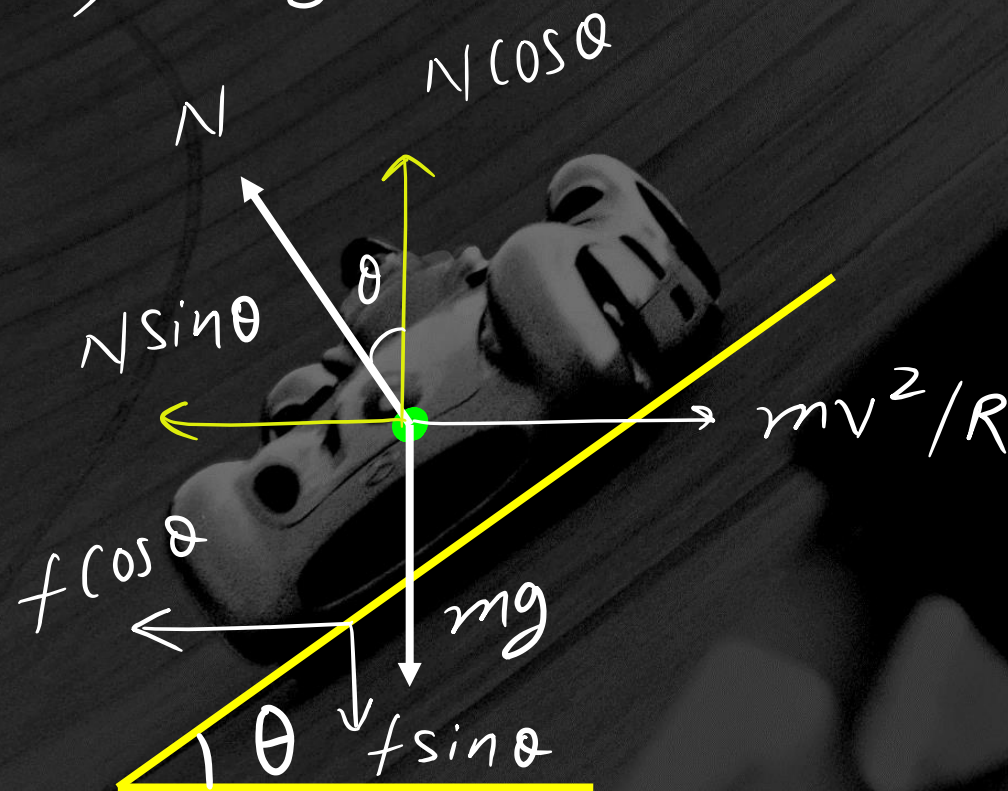
$$f = \mu N$$

$$N \sin \theta + f \cos \theta = \frac{mv^2}{R} \Rightarrow N(\sin \theta + \mu \cos \theta) = \frac{mv^2}{R} \quad (1)$$

$$N \cos \theta = mg + f \sin \theta \Rightarrow N(\cos \theta - \mu \sin \theta) = mg \quad (2)$$

$$\frac{(1)}{(2)} \Rightarrow \frac{\sin \theta + \mu \cos \theta}{\cos \theta - \mu \sin \theta} = \frac{v^2}{Rg}$$

$$\Rightarrow V_{\min} = \sqrt{Rg \left( \frac{\tan \theta + \mu}{1 - \mu \tan \theta} \right)}$$



## 4. CONCLUSION

1. For no slipping  $\sqrt{Rg \left( \frac{\tan \theta - \mu}{1 + \mu \tan \theta} \right)} \leq v \leq \sqrt{Rg \left( \frac{\tan \theta + \mu}{1 - \mu \tan \theta} \right)}$
2. If  $v = \sqrt{Rg \tan \theta}$ ,  $f = 0$  (car can turn on slippery road + no wear & tear of tyres)
3. If  $v > \sqrt{Rg \tan \theta}$ ,  $f$  acts down the slope  
 &  $v < \sqrt{Rg \tan \theta}$ ,  $f$  acts up the slope





The normal reaction 'N' for a vehicle of 800 kg mass, negotiating a turn on a  $30^\circ$  banked road at maximum possible speed without skidding is \_\_\_\_\_  $\times 10^3 \text{ kg m/s}^2$ . ( $\cos 30^\circ = 0.87$ ,  $\mu_s = 0.2$ )

- (1) 10.2      (2) 7.2      (3) 12.4      (4) 6.96

Q1 ↗

2021 July

<https://youtu.be/hCShMjLXnFo>

## 5. 2021 PYQs

Q3 ↗

[https://youtu.be/zUu5ccnsB\\_4](https://youtu.be/zUu5ccnsB_4)



**Statement I :** A cyclist is moving on an unbanked road with a speed of  $7 \text{ kmh}^{-1}$  and takes a sharp circular turn along a path of radius of 2m without reducing the speed. The static friction coefficient is 0.2. The cyclist will not slip and pass the curve ( $g = 9.8 \text{ m/s}^2$ )

**Statement II :** If the road is banked at an angle of  $45^\circ$ , cyclist can cross the curve of 2m radius with the speed of  $18.5 \text{ kmh}^{-1}$  without slipping.

In the light of the above statements, choose the correct answer from the options given below.

- (1) Statement I is incorrect and statement II is correct
- (2) Statement I is correct and statement II is incorrect
- (3) Both statement I and statement II are false
- (4) Both statement I and statement II are true

2021 March





→ PYQs (2020, 2021)

→ Concept Videos

→ Advanced problems

→ Part and Full Test

→ PhD series

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<https://bit.ly/2VhOGFF>

