

JEE MAIN | IIT JEE

Newton's Laws of Motion

REVISION in 45 Min

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Topics to covered

1. Common Forces acting on a Body
2. Static Equilibrium
3. Pulley Block Systems
4. Concept of Weighing Machine
5. Concept of Spring Balance
6. Spring Cutting & Combination
7. FBD – Most Important Point
8. Pseudo Force
9. Variable Force
10. Important Links for NLM



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Chapter	Formulae_Concept VIDEO LINK		
Unit & Dimensions	https://youtu.be/wdd-wlZF4Hk	Electrostatics	https://youtu.be/3stXbGRMcrk
Errors and Vectors		Capacitors	https://youtu.be/EXEiickNUkY
Vernier Calliper	https://youtu.be/pVoN045dV8I	Current Electricity	https://youtu.be/gm8FUfjrX18
Screw Gauge	https://youtu.be/gYd2PtMz0mw	Moving Charges and Magnetic Effect of Current	https://youtu.be/ULD2Ok1CGJk
Kinematics_Motion in 1d	https://youtu.be/U4NNxFaFliE	Earth's Magnetism	https://youtu.be/a4CT5uVwAK4
Kinematics_Motion in 2d	https://youtu.be/4_Zo5WhMf7w	Magnetic Properties	https://youtu.be/63 cwdYXNIYE
Laws of Motion		EMI	https://youtu.be/puVavm_GFRM
Work Energy Power	https://youtu.be/kjrXoE-kDI8	Alternating Current	https://youtu.be/74dT Y-pzM_o
Centre of Mass		Ray Optics	https://youtu.be/BhnyTWzIIBA
Centre of Mass of Standard Bodies	https://youtu.be/oCeACfryB-U	Wave Optics Part 1_Interference	https://youtu.be/LG5nIE8XTel
Collision		Wave Optics Part 2_Diffraction_Polarization	https://youtu.be/ymMyyJGGqnY
Rotational Motion_Moment of Inertia	https://youtu.be/9ckZdOhy3z0	Optical Instruments	https://youtu.be/OQssbDH0A4I
Gravitation	https://youtu.be/rAj2huLVaEk	Electromagnetic Waves	https://youtu.be/bcVXgEkyQZY
Properties of Solids	https://youtu.be/gSXxjk89l_c	Semiconductors_Basics + Zener Diode	https://youtu.be/_A2JomQ7-50
Fluids Statics (Part 1)	https://youtu.be/RFKx9B9yo3M	Semiconductors_Transistors	https://youtu.be/psDwl84Nzb0
Fluid Dynamics (Part 2)	https://youtu.be/Y717vQpUEjQ	Semiconductors_Logic Gates	https://youtu.be/pZdQAzLbFTo
Fluid Properties (Part 3)	https://youtu.be/V8xUWWK2oT0	Communication Systems	https://youtu.be/8NgMqK9X79Y
Simple Harmonic Motion	https://youtu.be/Rlb7ofNG09I	Modern Physics_Part 1_Atomic Physics	https://youtu.be/9VKUnE3mpHk
Thermal Properties		Modern Physics_Part 2_Photoelectric Effect	https://youtu.be/24oTQp84jrk
KTG	https://youtu.be/XO1tvFhla0I	Modern Physics_Part 3_Dual Nature of Light	https://youtu.be/0zoR_saMAQY
Thermodynamics	https://youtu.be/iz_kf1jRDRw	Modern Physics_Part 4_Radioactivity	https://youtu.be/AdX3YBhQyog
Wave Motion -Organ Pipes and Resonance Tube	https://youtu.be/fB7pfJ77za8	Modern Physics_Part 5_Nuclear Physics	https://youtu.be/VDWqVahGixc
Wave Motion - Doppler's Effect	https://youtu.be/9-BxOaamnwg	Modern Physics_Part 6_X Rays	https://youtu.be/dSHXdzX7NX0



$$\sum \vec{F} = 0 \quad (\text{Static Equilibrium})$$

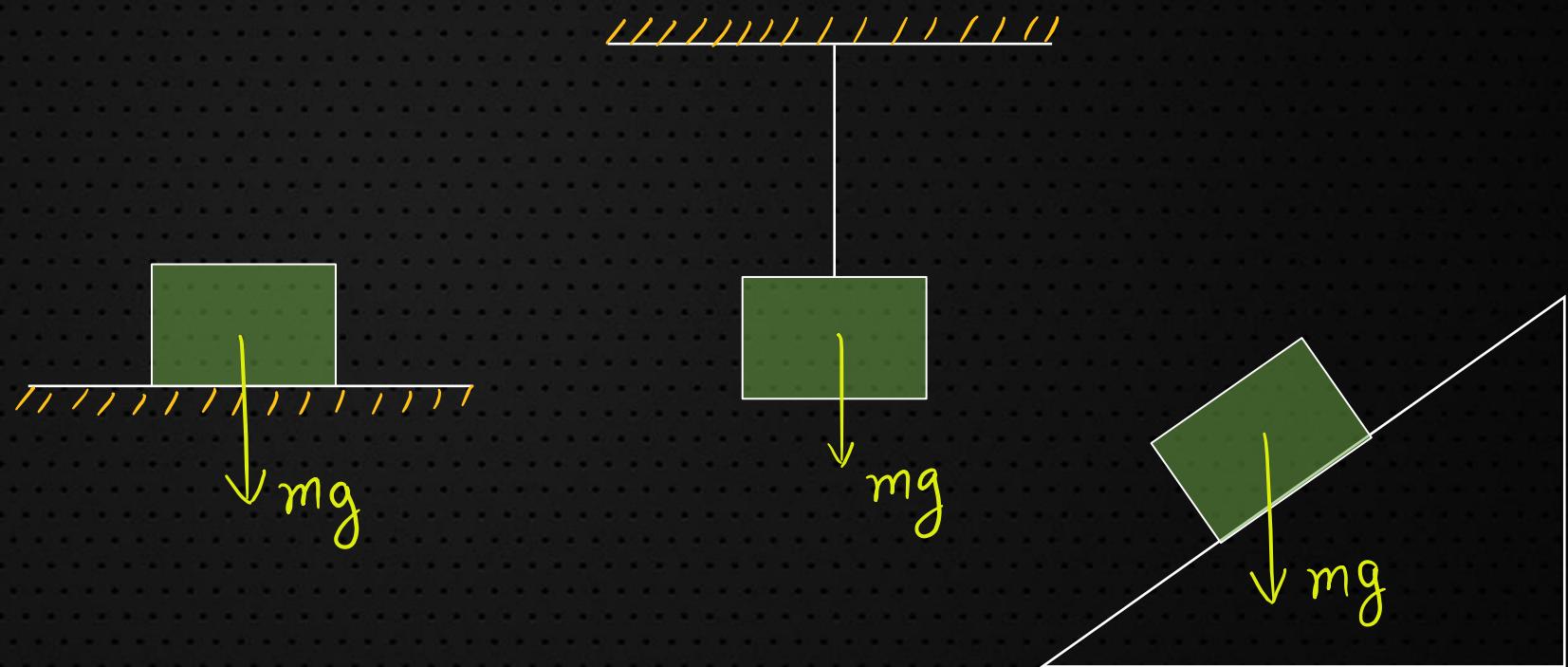
OR

$$\sum \vec{F} = M\vec{a} \quad (2^{\text{nd}} \text{ law})$$



1. Common Forces acting on body

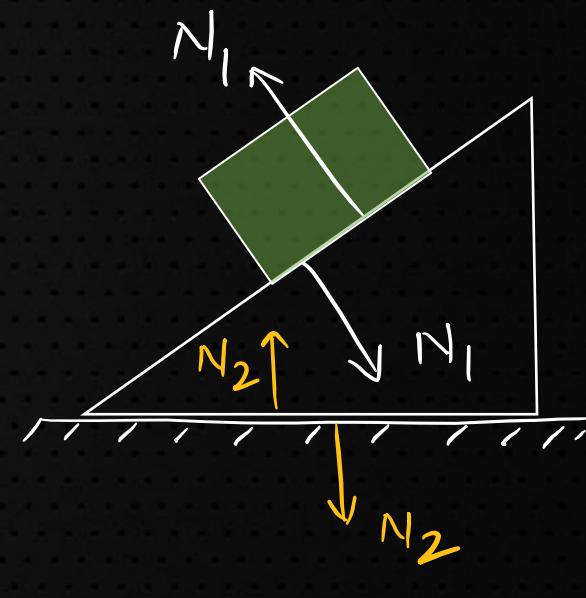
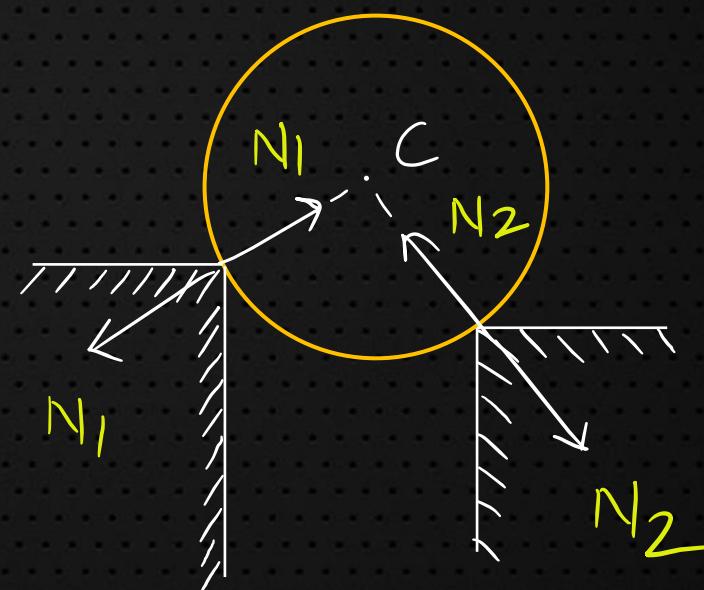
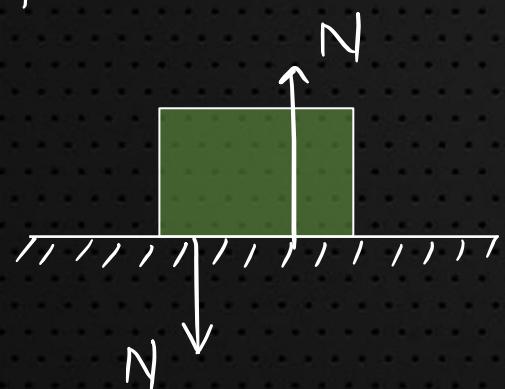
- Weight, mg → Due to gravitational pull
(acts vertical downwards, towards centre
of earth)
- Normal, N
- Tension, T
- friction, f



1. Common Forces acting on body

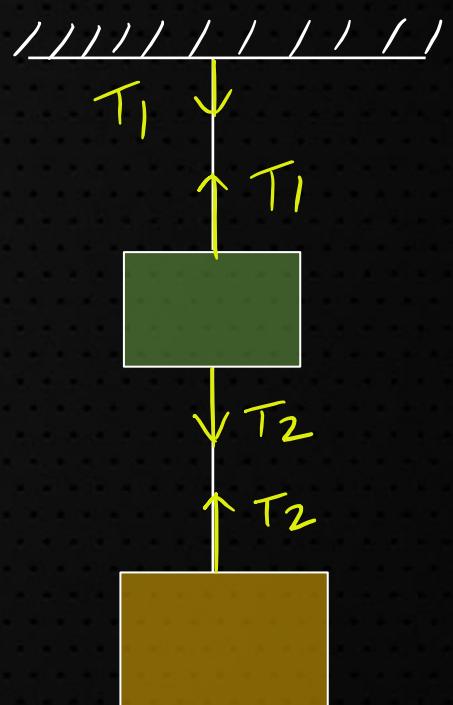
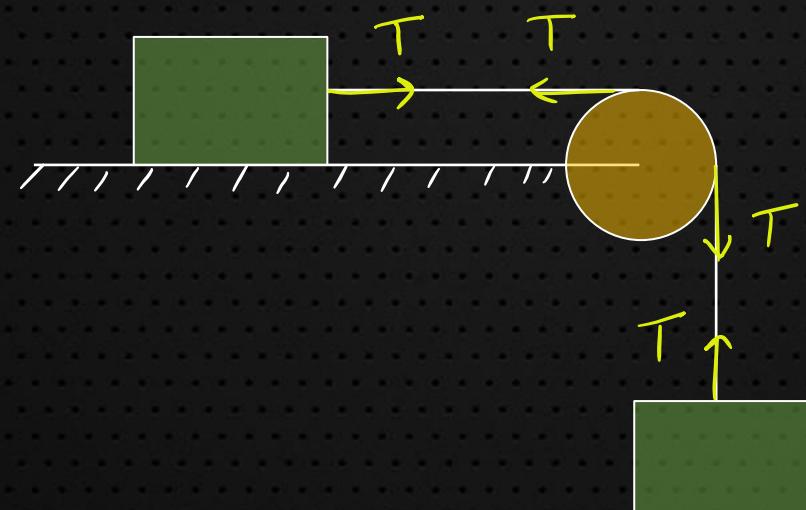
- Weight, mg
- Normal, N
- Tension, T
- friction, f

→ Normal, $N \rightarrow$ Two bodies in contact Press against each other
(acts \perp to contact surface)



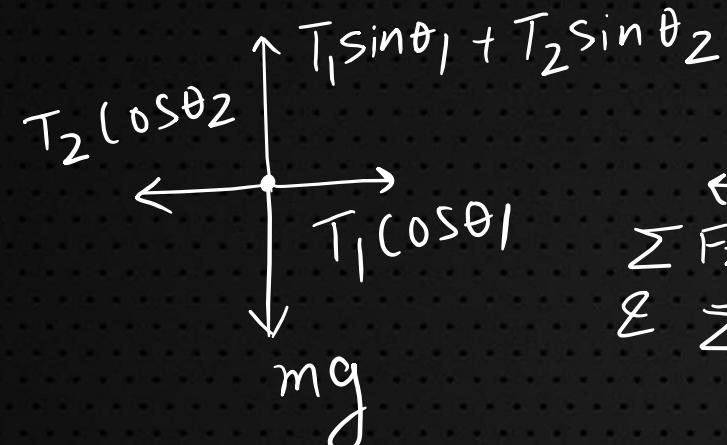
1. Common Forces acting on body

- Weight, mg
- Normal, N
- Tension, T → A taut string is under Tension
(pulling force, along the string)
- friction, f



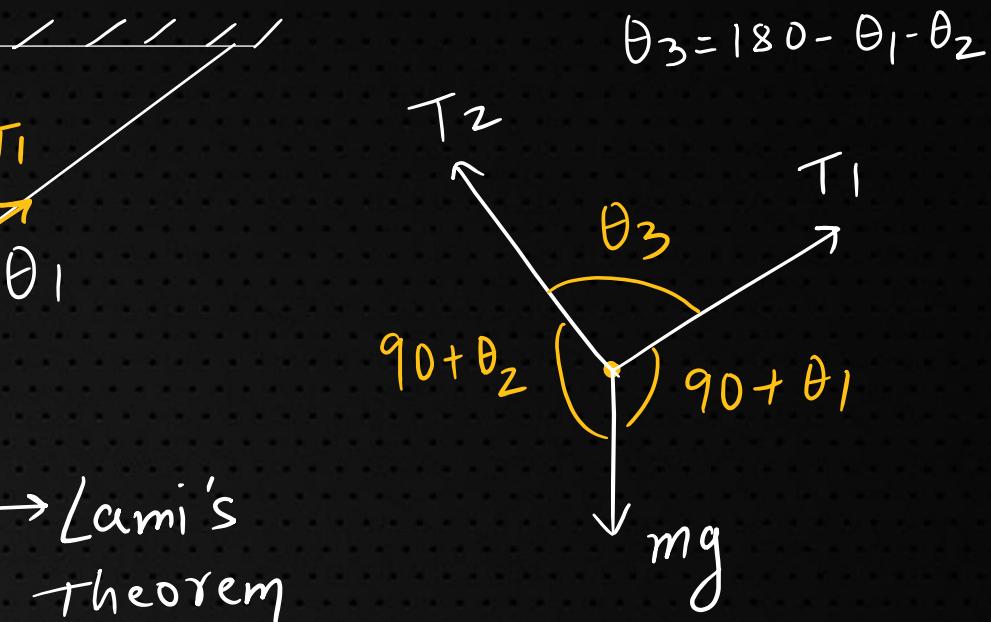
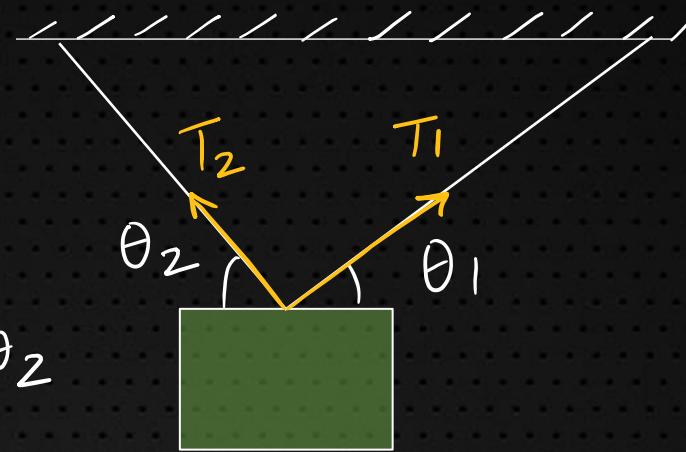
2. Static Equilibrium

$\sum \vec{F} = 0$ (body at rest)



$$T_1 \sin \theta_1 + T_2 \sin \theta_2 = mg$$

$$T_1 \cos \theta_1 = T_2 \cos \theta_2$$



$$\frac{mg}{\sin \theta_3} = \frac{T_1}{\sin(90^\circ + \theta_2)} = \frac{T_2}{\sin(90^\circ + \theta_1)}$$

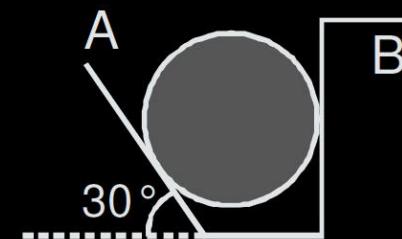
$$\theta_3 = 180^\circ - \theta_1 - \theta_2$$

Lami's theorem



... continued

The 50 kg homogeneous smooth sphere rests on the 30° incline A and bears against the smooth vertical wall B. Calculate the contact forces at A and B.



... continued

The 50 kg homogeneous smooth sphere rests on the 30° incline A and bears against the smooth vertical wall B. Calculate the contact forces at A and B.

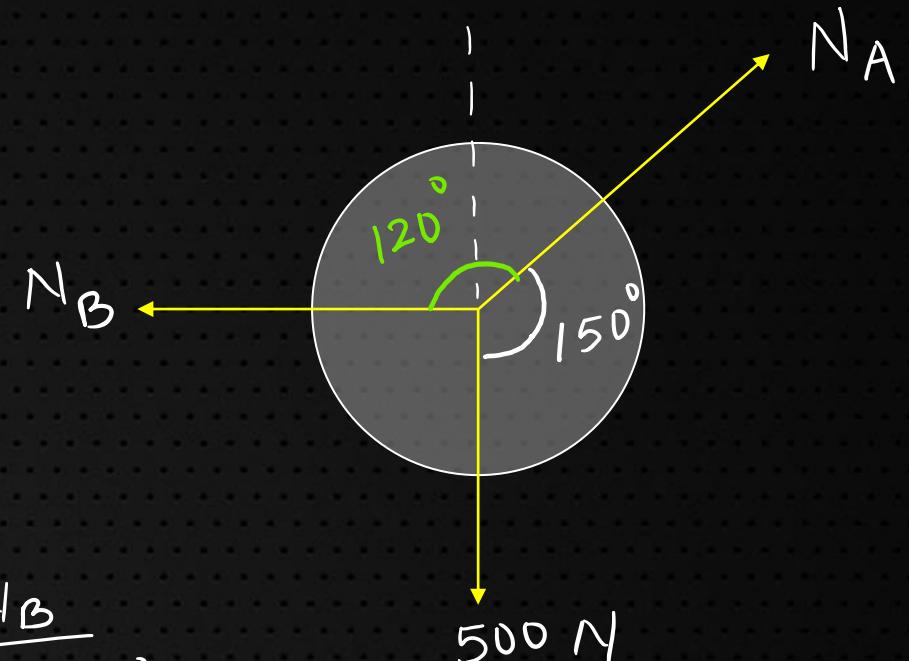


Solⁿ:

$$\frac{N_A}{\sin 90^\circ} = \frac{500}{\sin 120^\circ} = \frac{N_B}{\sin 150^\circ}$$

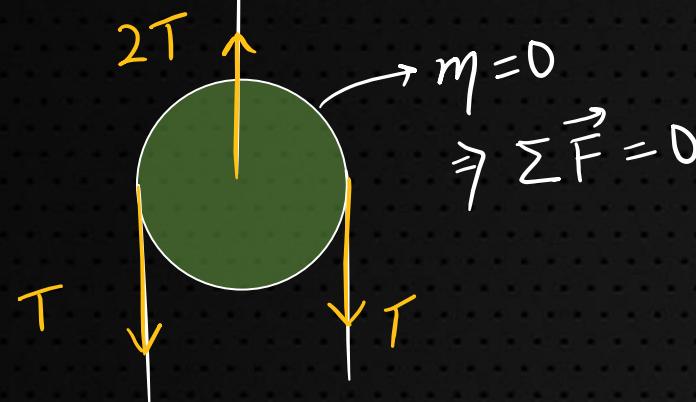
$$(i) \quad N_A = \frac{500 \times 1}{\sqrt{3}/2} = \frac{1000}{\sqrt{3}} \text{ N}$$

$$(ii) \quad N_B = \frac{500 \times 1/2}{\sqrt{3}/2} = \frac{500}{\sqrt{3}} \text{ N}$$



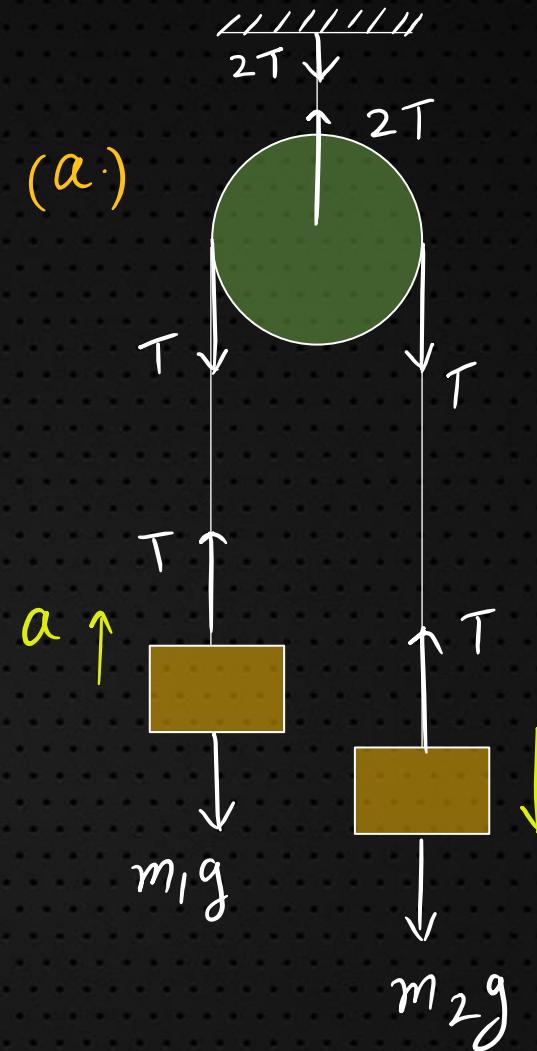
3. Pulley-Block Systems

↳ Pulley is massless & smooth



$$m=0 \Rightarrow \sum \vec{F} = 0$$

(a)



$$\sum F = ma$$

$$m_2 g - T = m_2 a \quad (i)$$

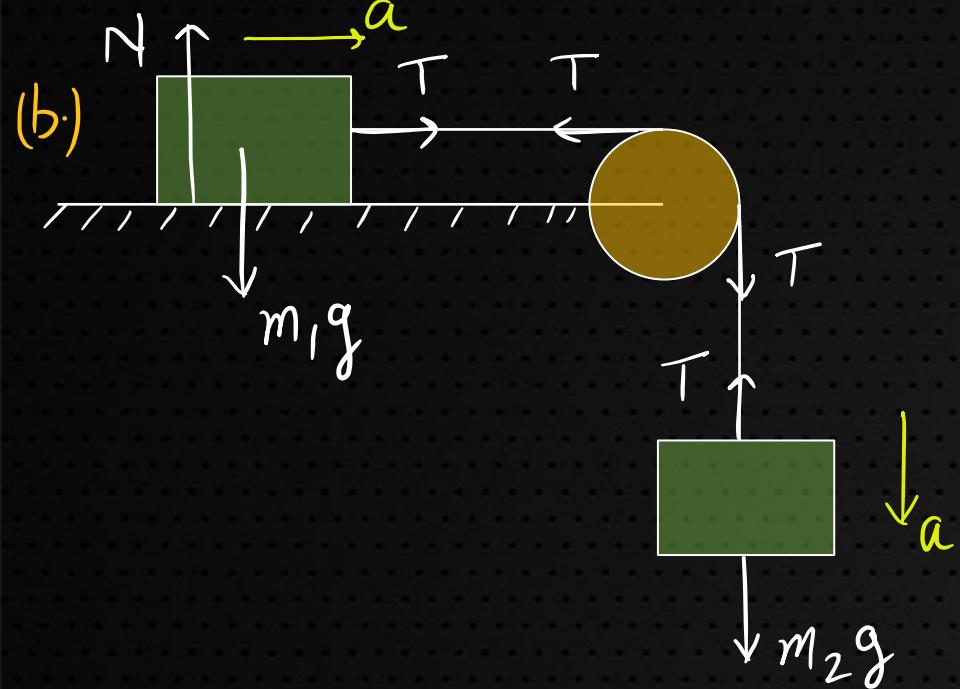
$$T - m_1 g = m_1 a \quad (ii)$$

$$\therefore T = \frac{2m_1 m_2 g}{m_1 + m_2}$$

$$\# a = \left(\frac{m_2 - m_1}{m_1 + m_2} \right) g$$



...Continued



$$m_2 g - T = m_2 a$$

$$T = m_1 a$$

$$N = m_1 g$$



$$\sum \vec{T} \cdot \vec{a} = 0$$

$$\Rightarrow T a_1 - 2 T a_2 = 0$$

$$\therefore a_1 = 2 a_2$$

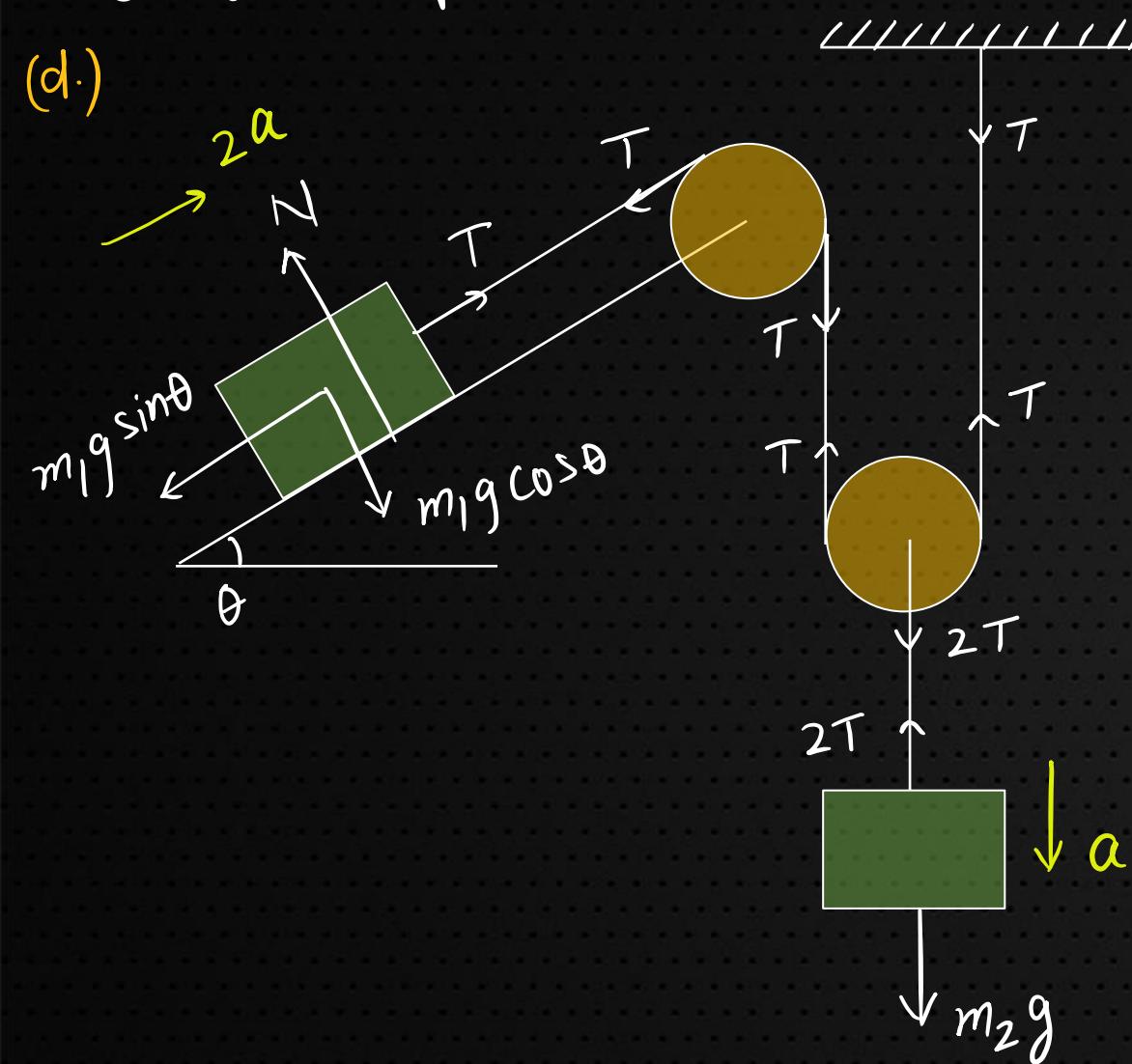
$$m_2 g - 2T = m_2 a \quad \text{--- (i)}$$

$$T = m_1 \times 2a \quad \text{--- (ii)}$$



...Continued

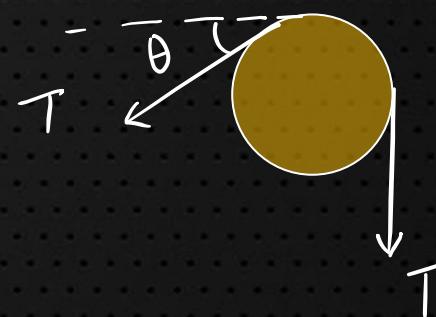
(d.)



$$m_2 g - 2T = m_2 a \quad \text{--- (i)}$$

$$T - m_1 g \sin \theta = m_1 \times 2a \quad \text{--- (ii)}$$

$$N = m_1 g \cos \theta \quad \text{--- (iii)}$$



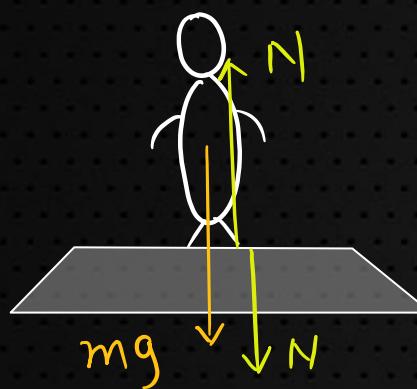
Clamp Force

$$= \sqrt{T^2 + T^2 + 2T^2 \cos(\pi - \theta)}$$



4. Concept of Weighing Machine

→ Measures Normal reaction acting on surface of m/c.



$$N = mg$$

$$\text{Reading} = \frac{N}{g} = m$$

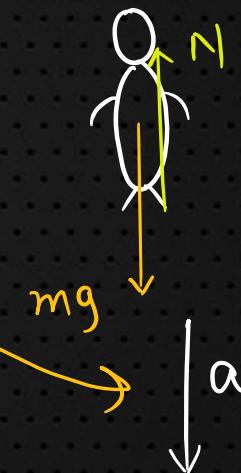


$$N - mg = ma$$

$$\Rightarrow N = m(g + a)$$

$$\text{Reading} = N/g$$

$$= m\left(1 + \frac{a}{g}\right)$$



$$mg - N = ma$$

$$\Rightarrow N = m(g - a)$$

$$\text{Reading} = N/g$$

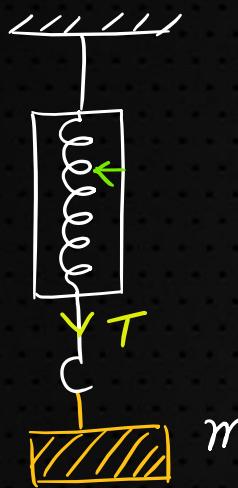
$$= m\left(1 - \frac{a}{g}\right)$$

If $N = 0$
 \Rightarrow weightlessness → ex: free fall



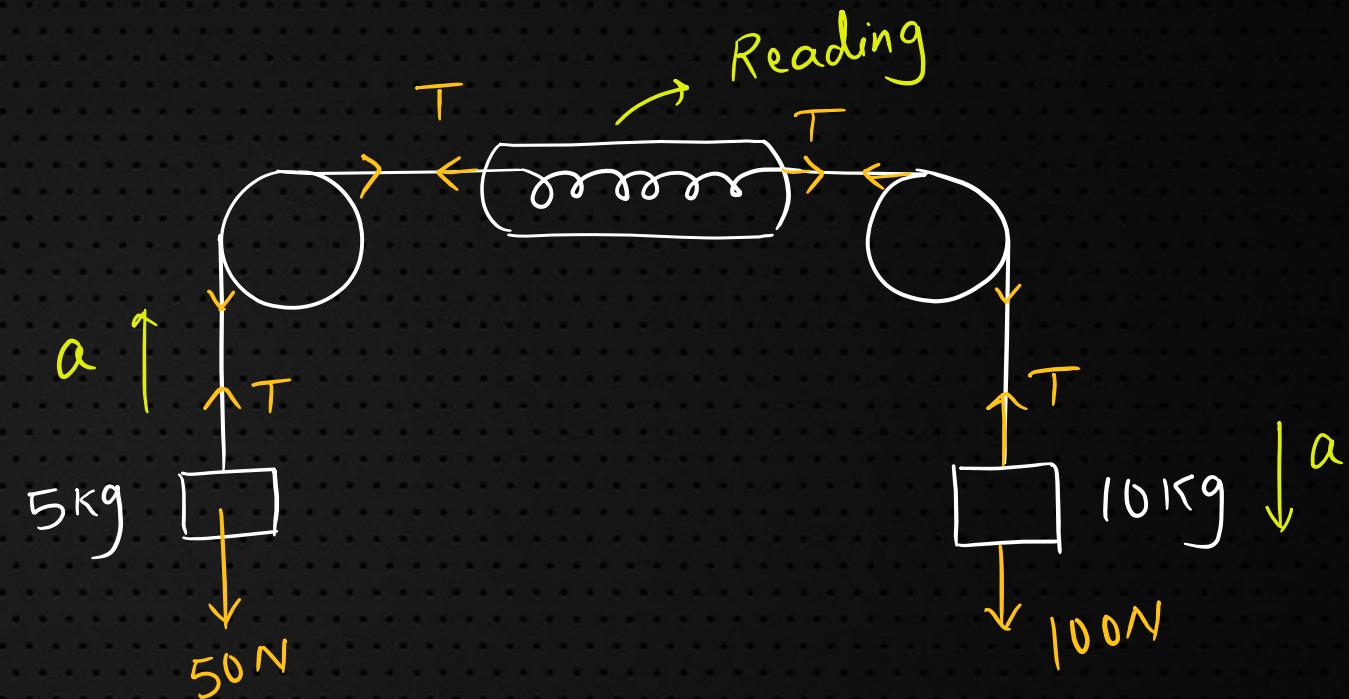
5. Concept of Spring Balance (massless spring)

↳ Measures Tension in string attached to it.



$$T = mg$$

$$\text{Reading} = T/g \\ = m$$



$$100 - T = 10a \quad \text{--- (i)} \quad \therefore T = 200/3 \text{ N}$$

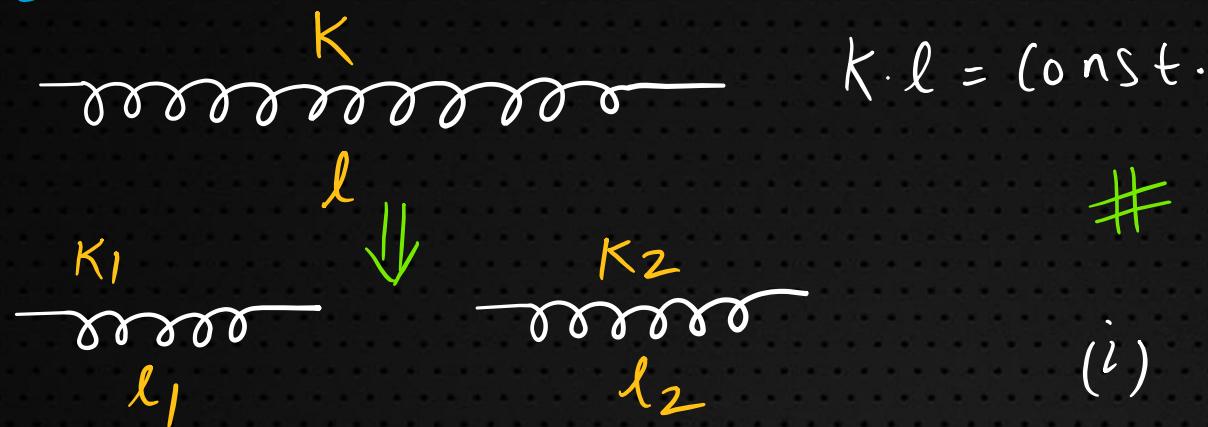
$$T - 50 = 5a \quad \text{--- (ii)}$$

$$\text{Reading} = \frac{20}{3} \text{ kg}$$



6. spring cutting & combination

Cut



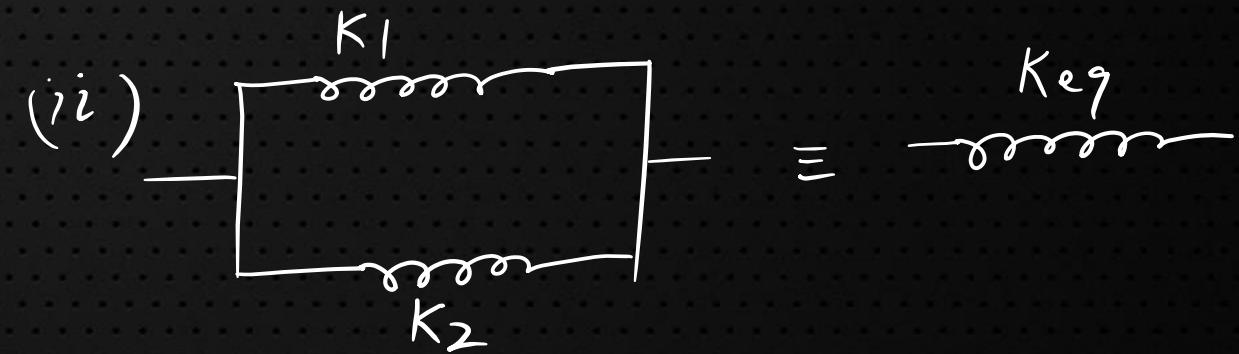
$$K_1 = \frac{Kl}{l_1}$$

$$K_2 = \frac{Kl}{l_2}$$

Combination



$$\frac{1}{K_{\text{eq}}} = \frac{1}{K_1} + \frac{1}{K_2}$$



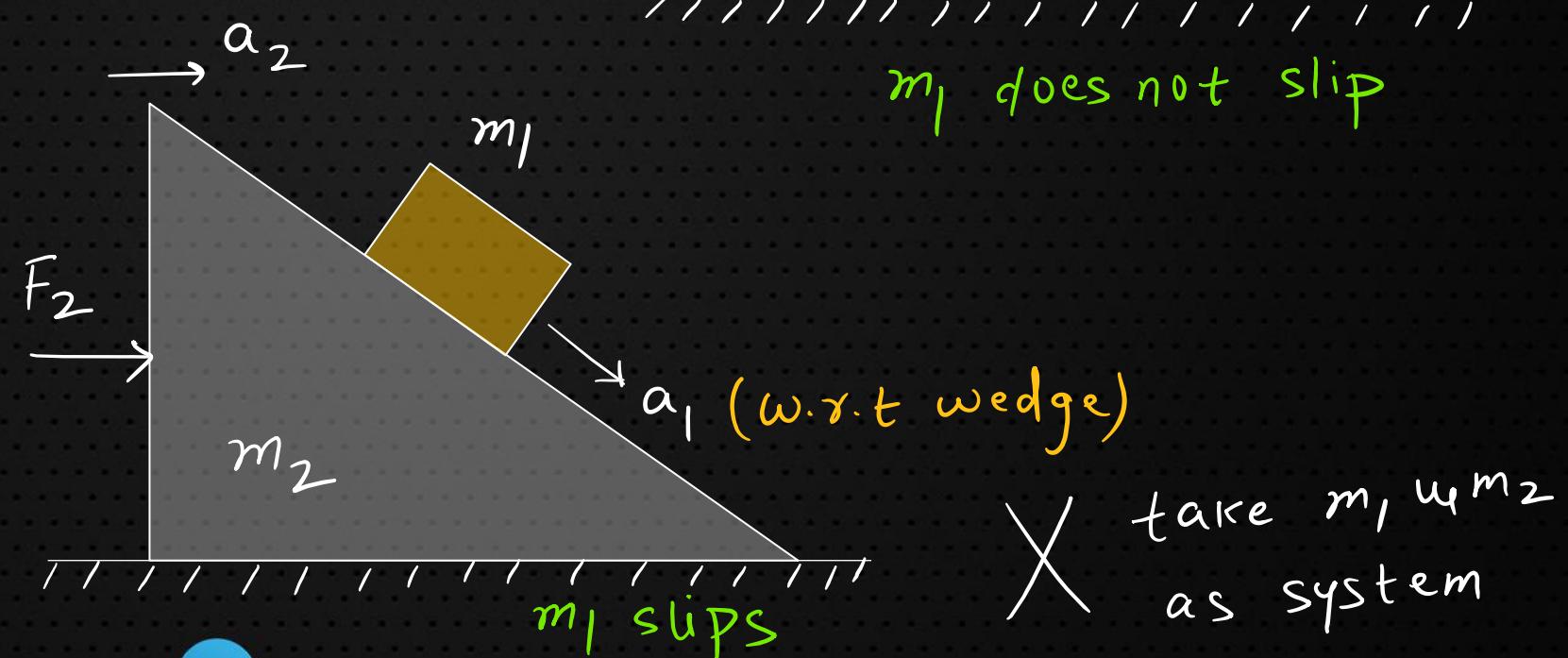
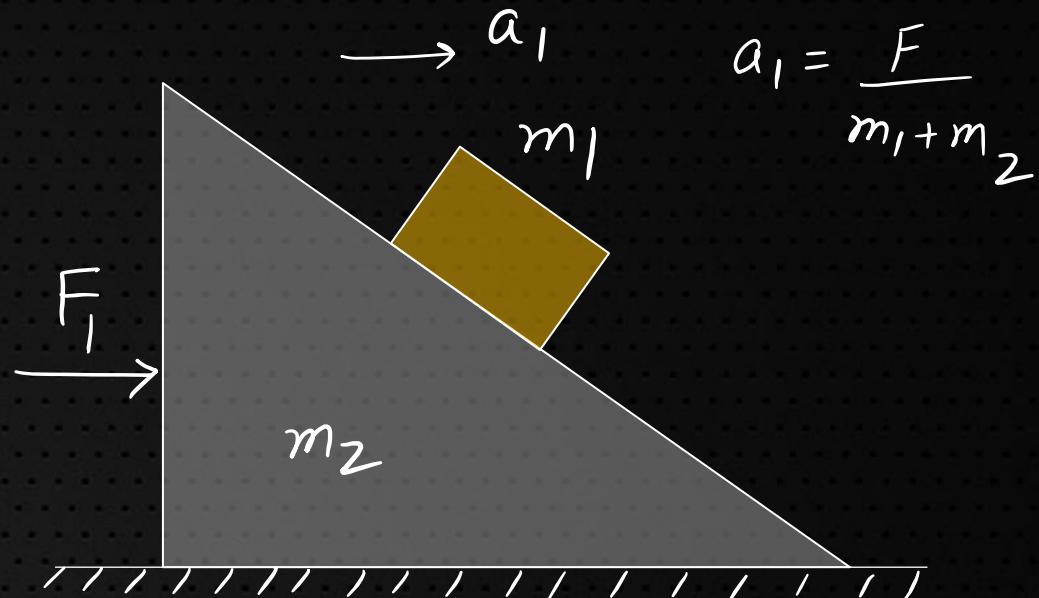
$$K_{\text{eq}} = K_1 + K_2$$



7. F.B.D - Most Imp. pt.

↳ Selection of System

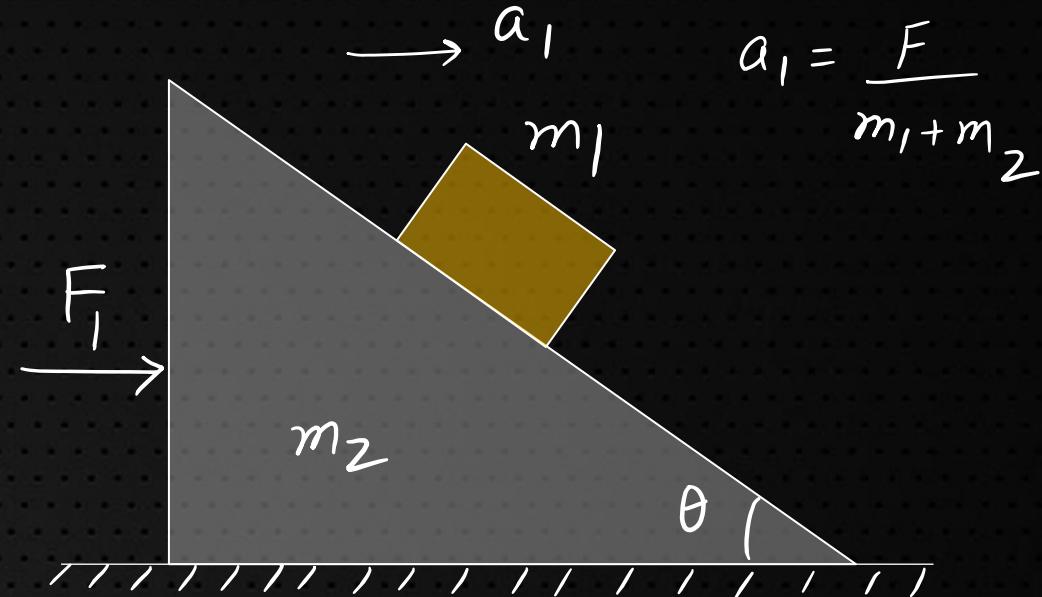
Two or more bodies can be taken as system if all bodies have same \vec{a} .



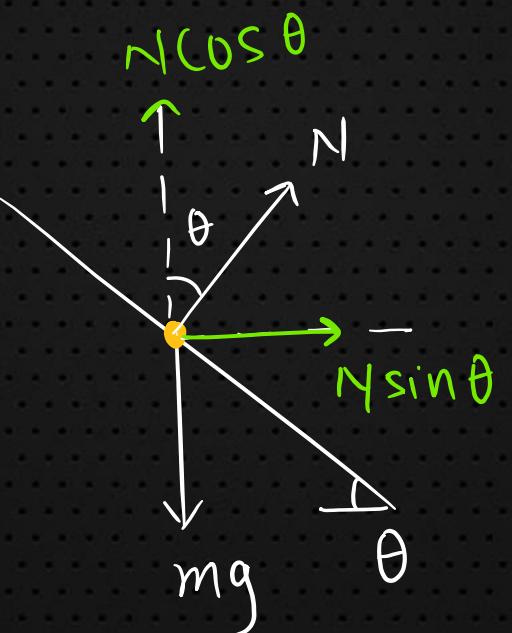
7. F.B.D - Most Imp. pt.

↳ Selection of System

Two or more bodies can be taken as system if all bodies have same \vec{a} .



$$a_1 = \frac{F}{m_1 + m_2}$$



$$\begin{aligned} N\sin\theta &= m a_1 \\ N\cos\theta &= mg \end{aligned}$$

on dividing

$$\tan\theta = a_1/g$$

$$\Rightarrow a_1 = g \tan\theta$$

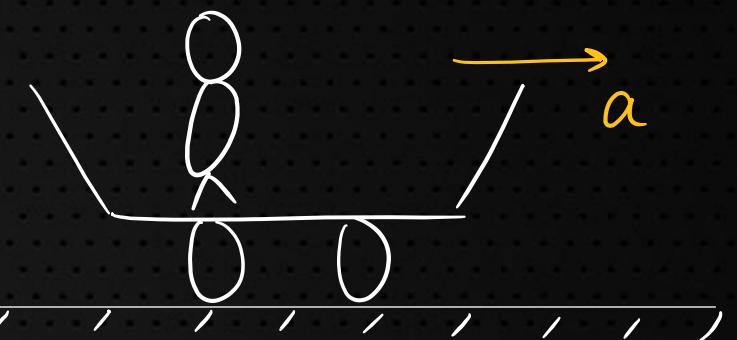


8. Pseudo Force

Inertial frame ($a=0$)



($a \neq 0$)
Non-Inertial
frame



obs A. \rightarrow Body is at rest



\therefore accelerated, thus
force acting on it must be

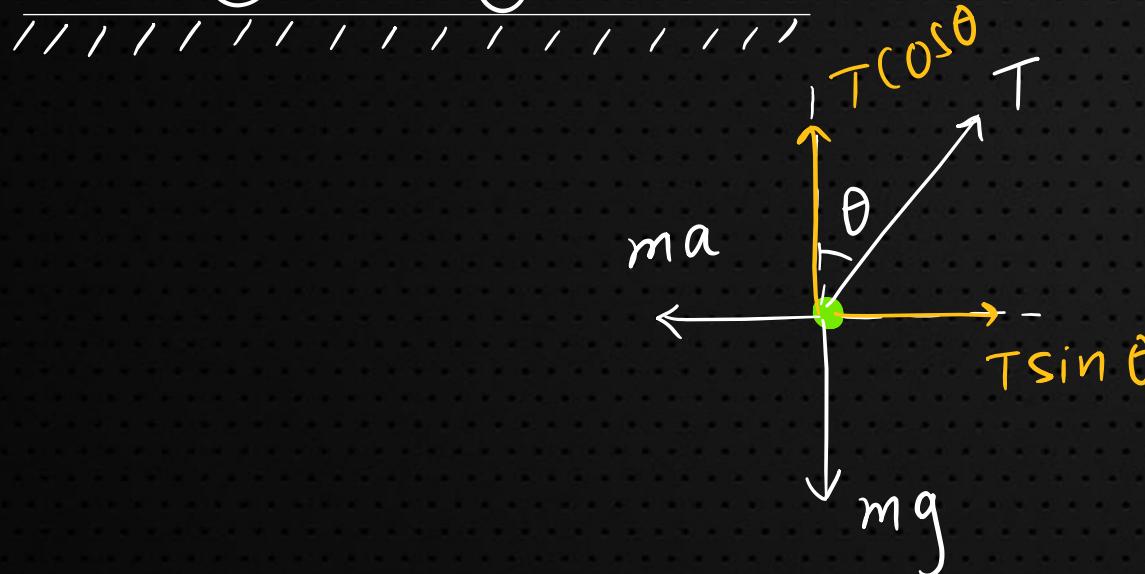
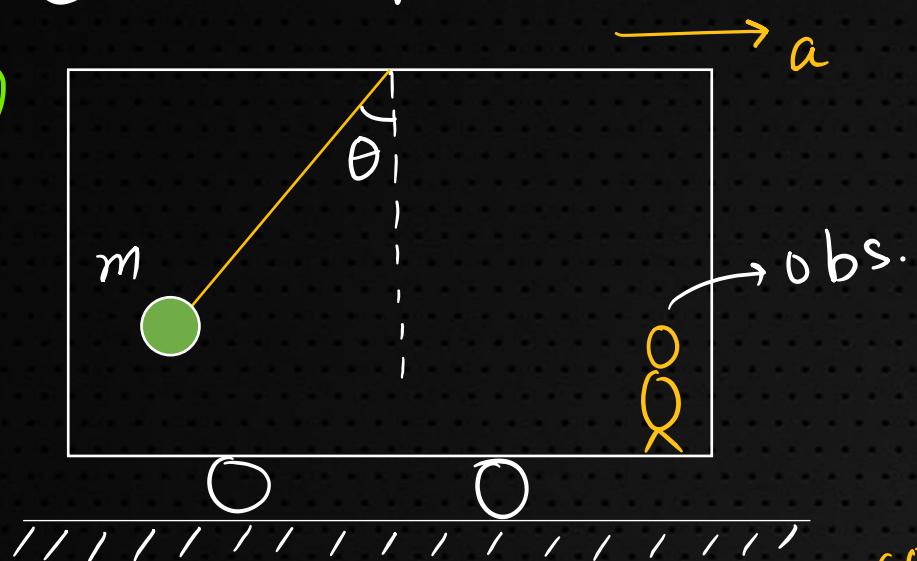
$$F_P = ma$$

→ false force



... Continued

(a)



To observer, m is at rest.

$$T \sin \theta = ma \quad \text{--- (i)}$$

$$T \cos \theta = mg \quad \text{--- (ii)}$$

on dividing :

$$\tan \theta = a/g \Rightarrow a = g \tan \theta$$

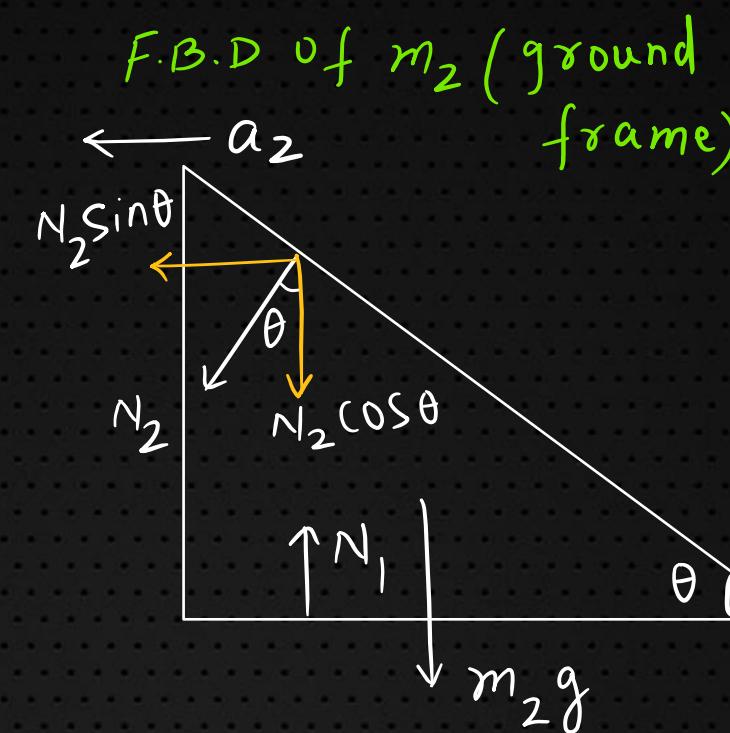
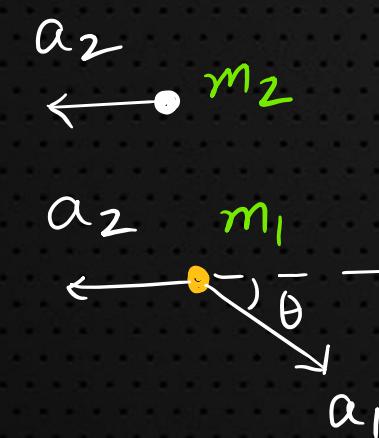
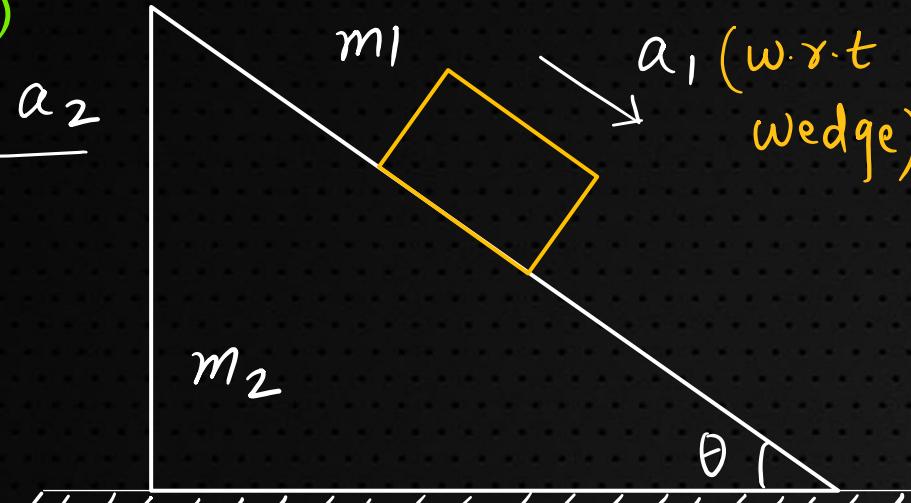
$$(i)^2 + (ii)^2$$

$$T = m \sqrt{a^2 + g^2}$$



... Continued

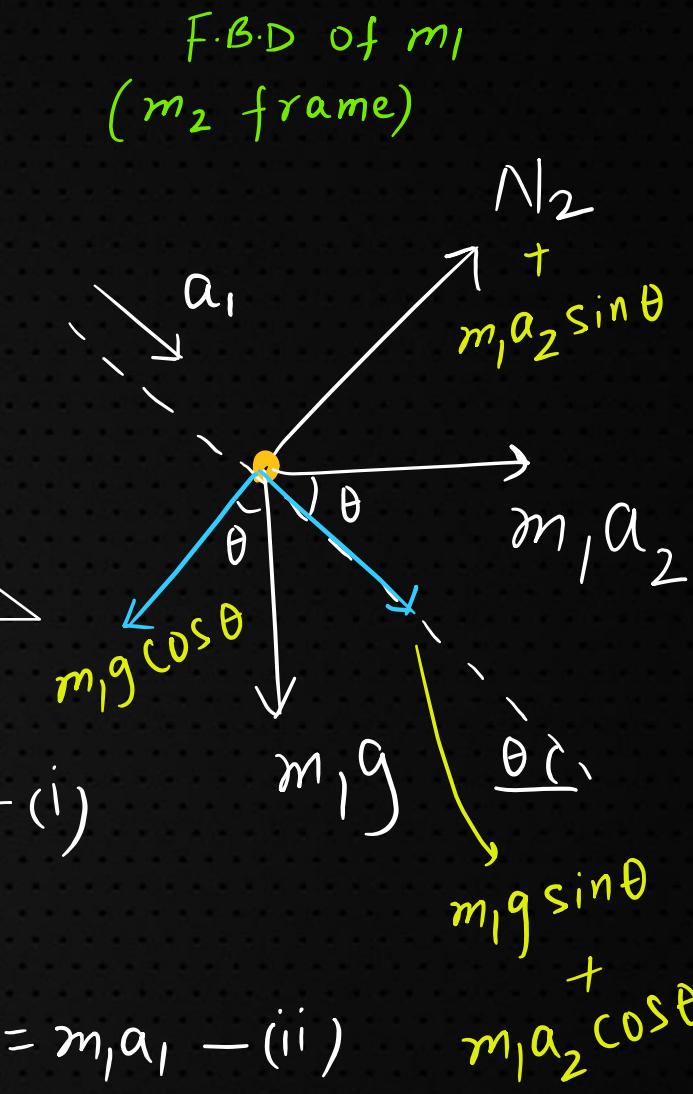
(b)



$$N_2 \sin \theta = m_2 a_2 \quad \text{---(i)}$$

$$m_1 g \sin \theta + m_1 a_2 \cos \theta = m_1 a_1 \quad \text{---(ii)}$$

$$N_2 + m_1 a_2 \sin \theta = m_1 g \cos \theta \quad \text{---(iii)}$$



Solve (i), (ii) & (iii).



q. Variable Force



$$\begin{aligned}
 & F(t) \rightarrow F(t) = m \frac{dv}{dt} \Rightarrow \int_0^t F(t) dt = \int_u^v m dv \\
 & F(x) \rightarrow F(x) = m v \frac{dv}{dx} \Rightarrow \int_0^x F(x) dx = \int_u^v m v dv \\
 & F(v) \rightarrow F(v) = m v \frac{dv}{dx} \Rightarrow \int_0^x dx = \int_u^v \frac{m v}{F(v)} dv \\
 & F(v) = m \frac{dv}{dt} \Rightarrow \int_0^t dt = \int_u^v m \frac{dv}{F(v)}
 \end{aligned}$$



... Continued

Ex Ball dropped from H height.

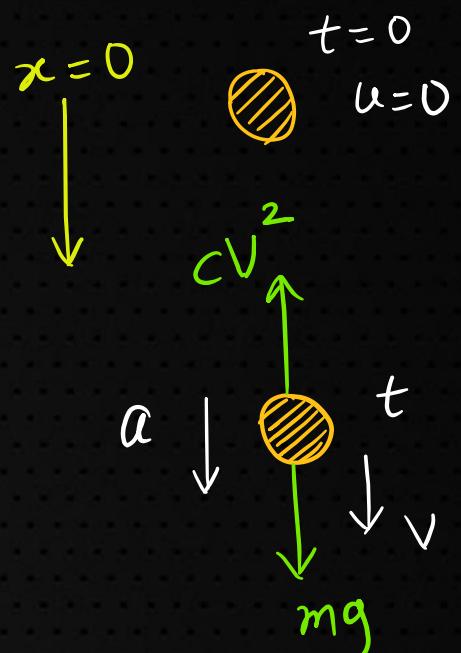
A air resistive force $f = CV^2$ acts on ball. Find its speed after falling H height.

$$\text{sol}^n: mg - CV^2 = ma$$

$$\Rightarrow mg - CV^2 = m v \frac{dv}{dx}$$

$$\Rightarrow \int_0^H dx = m \int_0^{v_0} \frac{v dv}{mg - CV^2}$$

Integrate to get v_0





Short Trick #3 'In 60 Sec'



Mohit Goenka | IIT Kharagpur

Constraint Motion in Rigid Rods

Constraint Motion in Wedge

Constraint Motion in Strings

Constraint Motion in Pulley Block 1

Constraint Motion in Pulley Block 2

<https://youtu.be/MZwkIpJcJKo>

<https://youtu.be/42pQCxIhdCQ>

<https://youtu.be/Fw8QOdxct18>

https://youtu.be/widSCjr_5nE

<https://youtu.be/MadNy-jmV-8>

<https://youtu.be/bSD16ug4gsk>



NLM PYQs LINKS (JEE MAIN)

2021 Feb	2021 March	2021 July	2021 August	2020	Top PYQs / Mix Years
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<https://youtu.be/2xuXY66RQW> https://youtu.be/zUu5ccnsB_4 https://youtu.be/hCShMjLX_nFo <https://youtu.be/VqOrOiq0> <https://youtu.be/AxW4lbc0> <https://youtu.be/ZUQ1hff7Ov4>



CLICK

(Practice these Questions)



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JEE Main PYQs Link <https://bit.ly/2S54jzh>

Chapter wise 2021, 2020, 2018

GoldMine Link <https://bit.ly/2VhOGFF>

