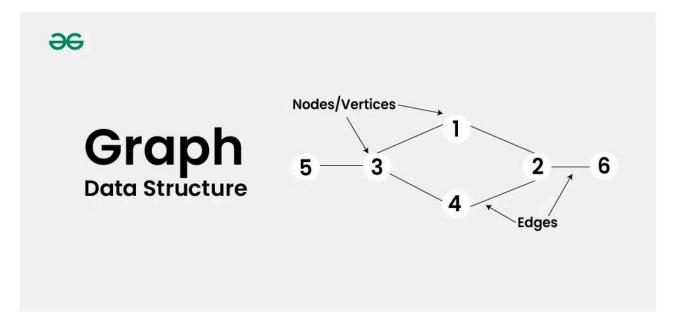


# **Graph Data Structure And Algorithms**

Last Updated: 03 Apr, 2024

**Graph Data Structure** is a collection of **nodes** connected by **edges**. It's used to represent relationships between different entities. **Graph algorithms** are methods used to manipulate and analyze graphs, solving various problems like **finding the shortest path** or **detecting cycles**.



#### **Table of Content**

- What is Graph Data Structure?
- Components of a Graph
- Basic Operations on Graphs



- Applications of Graph
- Basics of Graph
- BFS and DFS in Graph
- Cycles in Graph
- Shortest Path in Graph
- Minimum Spanning Tree
- Topological Sorting
- Connectivity in Graph
- Maximum Flow in Graph
- Some must do Problems on Graph
- Some Quizzes

## What is Graph Data Structure?

Graph is a non-linear data structure consisting of vertices and edges. The vertices are sometimes also referred to as nodes and the edges are lines or arcs that connect any two nodes in the graph. More formally a  $\underline{\mathsf{Graph}}$  is composed of a set of vertices ( $\mathsf{V}$ ) and a set of edges ( $\mathsf{E}$ ). The graph is denoted by  $\mathsf{G}(\mathsf{V},\mathsf{E})$ .

Graph data structures are a powerful tool for representing and analyzing complex relationships between objects or entities. They are particularly useful in fields such as social network analysis, recommendation systems, and computer networks. In the field of sports data science, graph data structures can be used to analyze and understand the dynamics of team performance and player interactions on the field.

DSA Data Structures Array String Linked List Stack Queue Tree Binary Tree Binary Search Tree Heap Hashing Graph Tr

- **Vertices:** Vertices are the fundamental units of the graph. Sometimes, vertices are also known as vertex or nodes. Every node/vertex can be labeled or unlabeled.
- Edges: Edges are drawn or used to connect two nodes of the graph. It can be ordered pair of nodes in a directed graph. Edges can connect any two nodes in any possible way. There are no rules. Sometimes, edges are also known as arcs. Every edge can be labelled/unlabelled.

#### **Basic Operations on Graphs:**

Below are the basic operations on the graph:

- Insertion of Nodes/Edges in the graph Insert a node into the graph.
- Deletion of Nodes/Edges in the graph Delete a node from the graph.
- Searching on Graphs Search an entity in the graph.
- Traversal of Graphs Traversing all the nodes in the graph.

#### **Applications of Graph:**

Following are the real-life applications:

• Graph data structures can be used to represent the interactions between players on a team, such as passes, shots, and tackles. Analyzing these interactions can provide insights into team

- dynamics and areas for improvement.
- Commonly used to represent social networks, such as networks of friends on social media.
- Graphs can be used to represent the topology of computer networks, such as the connections between routers and switches.
- Graphs are used to represent the connections between different places in a transportation network, such as roads and airports.
- Graphs are used in Neural Networks where vertices represent neurons and edges represent the synapses between them. Neural networks are used to understand how our brain works and how connections change when we learn. The human brain has about 10^11 neurons and close to 10^15 synapses.

## **Basics of Graph:**

- Introduction to Graphs
- Graph and its representations
- Types of Graphs with Examples
- Basic Properties of a Graph
- Applications, Advantages and Disadvantages of Graph
- Transpose graph
- <u>Difference between graph and tree</u>

#### BFS and DFS in Graph:

- Breadth First Traversal for a Graph
- <u>Depth First Traversal for a Graph</u>
- Applications of Depth First Search
- Applications of Breadth First Traversal

- Iterative Depth First Search
- BFS for Disconnected Graph
- Transitive Closure of a Graph using DFS
- <u>Difference between BFS and DFS</u>

#### Cycles in Graph:

- Detect Cycle in a Directed Graph
- Detect cycle in an undirected graph
- Detect cycle in a direct graph using colors
- Detect a negative cycle in a Graph | (Bellman Ford)
- Cycles of length n in an undirected and connected graph
- <u>Detecting negative cycle using Floyd Warshall</u>
- Clone a Directed Acyclic Graph
- Union By Rank and Path Compression in Union-Find Algorithm
- Introduction to Disjoint Set Data Structure or Union-Find Algorithm

# **Shortest Path in Graph:**

- <u>Dijkstra's shortest path algorithm</u>
- Bellman–Ford Algorithm
- Floyd Warshall Algorithm
- Johnson's algorithm for All-pairs shortest paths
- Shortest Path in Directed Acyclic Graph
- Dial's Algorithm
- Multistage Graph (Shortest Path)
- Shortest path in an unweighted graph

- Karp's minimum mean (or average) weight cycle algorithm
- 0-1 BFS (Shortest Path in a Binary Weight Graph)
- Find minimum weight cycle in an undirected graph

#### Minimum Spanning Tree:

- Prim's Minimum Spanning Tree (MST)
- Kruskal's Minimum Spanning Tree Algorithm
- Difference between Prim's and Kruskal's algorithm for MST
- Applications of Minimum Spanning Tree Problem
- Minimum cost to connect all cities
- Total number of Spanning Trees in a Graph
- Minimum Product Spanning Tree
- Reverse Delete Algorithm for Minimum Spanning Tree
- Boruvka's algorithm for Minimum Spanning Tree

## **Topological Sorting:**

- <u>Topological Sorting</u>
- All topological sorts of a Directed Acyclic Graph
- Kahn's Algorithm for Topological Sorting
- Maximum edges that can be added to DAG so that is remains DAG
- Longest Path in a Directed Acyclic Graph
- <u>Topological Sort of a graph using departure time of vertex</u>

#### **Connectivity in Graph:**

Articulation Points (or Cut Vertices) in a Graph

- Biconnected Components
- Bridges in a graph
- Eulerian path and circuit
- Fleury's Algorithm for printing Eulerian Path or Circuit
- Strongly Connected Components
- Count all possible walks from a source to a destination with exactly k edges
- Euler Circuit in a Directed Graph
- Length of shortest chain to reach the target word
- Find if an array of strings can be chained to form a circle
- Tarjan's Algorithm to find strongly connected Components
- Paths to travel each nodes using each edge (Seven Bridges of Königsberg)
- <u>Dynamic Connectivity | Set 1 (Incremental)</u>

## Maximum Flow in Graph:

- Max Flow Problem Introduction
- Ford-Fulkerson Algorithm for Maximum Flow Problem
- Find maximum number of edge disjoint paths between two vertices
- Find minimum s-t cut in a flow network
- Maximum Bipartite Matching
- Channel Assignment Problem
- Introduction to Push Relabel Algorithm
- Karger's Algorithm- Set 1- Introduction and Implementation
- <u>Dinic's algorithm for Maximum Flow</u>

## Some must do Problems on Graph:

- Find length of the largest region in Boolean Matrix
- Count number of trees in a forest
- A Peterson Graph Problem
- Clone an Undirected Graph
- Graph Coloring (Introduction and Applications)
- Traveling Salesman Problem (TSP) Implementation
- Vertex Cover Problem | Set 1 (Introduction and Approximate Algorithm)
- K Centers Problem | Set 1 (Greedy Approximate Algorithm)
- Erdos Renyl Model (for generating Random Graphs)
- Chinese Postman or Route Inspection | Set 1 (introduction)
- Hierholzer's Algorithm for directed graph
- Check whether a given graph is Bipartite or not
- Snake and Ladder Problem
- Boggle (Find all possible words in a board of characters)
- Hopcroft Karp Algorithm for Maximum Matching-Introduction
- Minimum Time to rot all oranges
- Construct a graph from given degrees of all vertices
- Determine whether a universal sink exists in a directed graph
- Number of sink nodes in a graph
- Two Clique Problem (Check if Graph can be divided in two Cliques)

## Some Quizzes:

- Quizzes on Graph Traversal
- Quizzes on Graph Shortest Path
- Quizzes on Graph Minimum Spanning Tree

Quizzes on Graphs

#### **Quick Links:**

- Top 10 Interview Questions on Depth First Search (DFS)
- Some interesting shortest path questions
- Practice Problems on Graphs
- Videos on Graphs

#### **Recommended:**

• Learn Data Structure and Algorithms | DSA Tutorial

"The DSA course helped me a lot in clearing the interview rounds. It was really very helpful in setting a strong foundation for my problem-solving skills. Really a great investment, the passion Sandeep sir has towards DSA/teaching is what made the huge difference." - **Gaurav | Placed at Amazon** 

Before you move on to the world of development, **master the fundamentals of DSA** on which every advanced algorithm is built upon. Choose your preferred language and start learning today:

DSA In JAVA/C++

DSA In Python

DSA In JavaScript

Trusted by Millions, Taught by One- Join the best DSA Course Today!

**Recommended Problems** 

#### Frequently asked DSA Problems

Solve Problems

4

Suggest improvement

Next

Introduction to Graphs - Data Structure and Algorithm Tutorials

Share your thoughts in the comments

Add Your Comment

#### **Similar Reads**

Static Data Structure vs Dynamic Data Structure

Applications of Graph Data Structure

What is Graph Data Structure?

Graph terminology in data structure

Top 100 Data Structure and Algorithms DSA Interview Questions Topic-wise

Maths for Data Structure and Algorithms (DSA) | A Complete Guide

Top 12 Data Structure Algorithms to Implement in Practical Applications in 2021

Connect a graph by M edges such that the graph does not contain any cycle and Bitwise AND of connected vertices is maximum

Data Structure Alignment: How data is arranged and accessed in Computer Memory?

Difference between data type and data structure

H harendra...

**Article Tags:** DSA, Graph

Practice Tags: Graph

A-143, 9th Floor, Sovereign Corporate Tower, Sector-136, Noida, Uttar Pradesh -201305





Company	Explore	Languages	DSA	Data Science &	Web
About Us	Job-A-Thon Hiring	Python	Data Structures	ML	Technologies
Legal	Challenge	Java	Algorithms	Data Science With	HTML
Careers	Hack-A-Thon	C++	DSA for Beginners	Python	CSS
In Media	GfG Weekly Contest	PHP	Basic DSA Problems	Data Science For	JavaScript
Contact Us	Offline Classes	GoLang	DSA Roadmap	Beginner	TypeScript
Advertise with us	(Delhi/NCR)	SQL	DSA Interview	Machine Learning	ReactJS
GFG Corporate	DSA in JAVA/C++	R Language	Questions	Tutorial	NextJS
Solution	Master System	Android Tutorial	Competitive	ML Maths	NodeJs
Placement Training	Design		Programming	Data Visualisation Tutorial	Bootstrap
Program	Master CP			Pandas Tutorial	Tailwind CSS
	GeeksforGeeks				
	Videos			NumPy Tutorial	
	Geeks Community			NLP Tutorial	
				Deep Learning Tutorial	

<b>Python Tutorial</b>	Computer	DevOps	System Design	School Subjects	Commerce
Python Programming	Science	Git	High Level Design	Mathematics	Accountancy
Examples	GATE CS Notes	AWS	Low Level Design	Physics	Business Studies
Django Tutorial	Operating Systems	Docker	UML Diagrams	Chemistry	Economics
Python Projects	Computer Network	Kubernetes	Interview Guide	Biology	Management
Python Tkinter	Database	Azure	Design Patterns	Social Science	HR Management
Web Scraping	Management System	GCP	OOAD	English Grammar	Finance
OpenCV Tutorial	Software Engineering	DevOps Roadmap	System Design		Income Tax
Python Interview	Digital Logic Design		Bootcamp		
Question	Engineering Maths		Interview Questions		
LIDSC Study	Droparation	Competitive	More Tutorials	Free Online Tools	Write & Farn
UPSC Study	Preparation	Competitive	More Tutorials	Free Online Tools	Write & Earn
UPSC Study Material	Preparation Corner	Competitive Exams	More Tutorials  Software	Free Online Tools  Typing Test	Write & Earn Write an Article
•	•	•			
Material	Corner	Exams	Software	Typing Test	Write an Article
Material Polity Notes	Corner Company-Wise	<b>Exams</b> JEE Advanced	Software Development	Typing Test Image Editor	Write an Article Improve an Article
Material Polity Notes Geography Notes	Corner  Company-Wise Recruitment Process	Exams  JEE Advanced  UGC NET	Software Development Software Testing	Typing Test Image Editor Code Formatters	Write an Article Improve an Article Pick Topics to Write
Material  Polity Notes  Geography Notes  History Notes	Corner  Company-Wise Recruitment Process Resume Templates	Exams  JEE Advanced  UGC NET  SSC CGL	Software Development Software Testing Product Management	Typing Test Image Editor Code Formatters Code Converters	Write an Article Improve an Article Pick Topics to Write Share your
Material  Polity Notes  Geography Notes  History Notes  Science and	Corner  Company-Wise Recruitment Process Resume Templates Aptitude Preparation	Exams  JEE Advanced  UGC NET  SSC CGL  SBI PO	Software Development Software Testing Product Management Project Management	Typing Test Image Editor Code Formatters Code Converters Currency Converter	Write an Article Improve an Article Pick Topics to Write Share your Experiences
Material  Polity Notes  Geography Notes  History Notes  Science and Technology Notes	Corner  Company-Wise Recruitment Process Resume Templates Aptitude Preparation Puzzles	Exams  JEE Advanced  UGC NET  SSC CGL  SBI PO  SBI Clerk  IBPS PO	Software Development Software Testing Product Management Project Management Linux	Typing Test Image Editor Code Formatters Code Converters Currency Converter Random Number	Write an Article Improve an Article Pick Topics to Write Share your Experiences
Material  Polity Notes  Geography Notes  History Notes  Science and Technology Notes  Economy Notes	Corner  Company-Wise Recruitment Process Resume Templates Aptitude Preparation Puzzles Company-Wise	Exams  JEE Advanced  UGC NET  SSC CGL  SBI PO  SBI Clerk	Software Development Software Testing Product Management Project Management Linux Excel	Typing Test Image Editor Code Formatters Code Converters Currency Converter Random Number Generator	Write an Article Improve an Article Pick Topics to Write Share your Experiences

@GeeksforGeeks, Sanchhaya Education Private Limited, All rights reserved