

Reviewer1#451C

a. Proof Process of Differences in Signal Quality

To illustrate the Differences in Signal Quality (DSQ) phenomenon, we analyzed the results of the CNN model¹ on simulated data with a signal-to-noise ratio (SNR) of 15. The analysis focused on three types of signals: the clean signal $Clean_{sn}$, the noisy signal $Noisy_{sn}$, and the predicted signal $Pred_{sn}$. Based on these signals, three metrics were calculated to evaluate the quality of individual signals: *Noise*, *Fitting Error*, and *Reconstruction Error*(*Recon Error*).

Because the closeness of a signal to $Clean_{sn}$ serves as an indicator of its quality, *Noise* can be used to evaluate the quality of $Noisy_{sn}$. *Recon Error* can be used to evaluate the quality of $Pred_{sn}$. It should be noted that smaller values of *Noise* and *Recon Error* indicate that the corresponding $Noisy_{sn}$ or $Pred_{sn}$ is closer to $Clean_{sn}$, and therefore has higher quality.

These metrics can be calculated as follows:

$$Noise = \sqrt{(Noisy_{sn} - Clean_{sn})^2} \quad (1)$$

$$FittingError = \sqrt{(Pred_{sn} - Noisy_{sn})^2} \quad (2)$$

$$ReconError = \sqrt{(Pred_{sn} - Clean_{sn})^2} \quad (3)$$

In the CNN¹ simulation experiment, we calculated the mean Noise and mean Recon Error of all signals and plotted their variations with training epochs, as shown in Fig. 1. Noise refers to the difference between the original noisy signals and the clean signals; its mean value remains constant across epochs and therefore appears as a horizontal line in the figure. Recon Error, in contrast, denotes the difference between the predicted signals and the clean signals. As the number of epochs increases, the predicted signals are continuously updated. Therefore, the mean Recon Error varies with the Epoch.

At epoch 1, the mean Recon Error of the model is higher than the mean Noise. Because smaller values of Noise and Recon Error indicate that the corresponding $Pred_{sn}$ and $Noisy_{sn}$ are closer to $Clean_{sn}$, reflecting higher overall signal quality. Therefore, at epoch 1, the overall quality of $Pred_{sn}$ is lower than that of $Noisy_{sn}$. This can be attributed to the fact that the model is still in the early training stage and has not yet effectively learned the signal features, resulting in a lower quality of $Pred_{sn}$. As training progresses, the mean Recon Error gradually decreases, indicating that the overall quality of $Pred_{sn}$ improves and eventually surpasses that of $Noisy_{sn}$ in later epochs. This phenomenon can be summarized as **Phenomenon 1**: As training progresses, the predicted signals progressively surpass the noisy signals in overall quality.

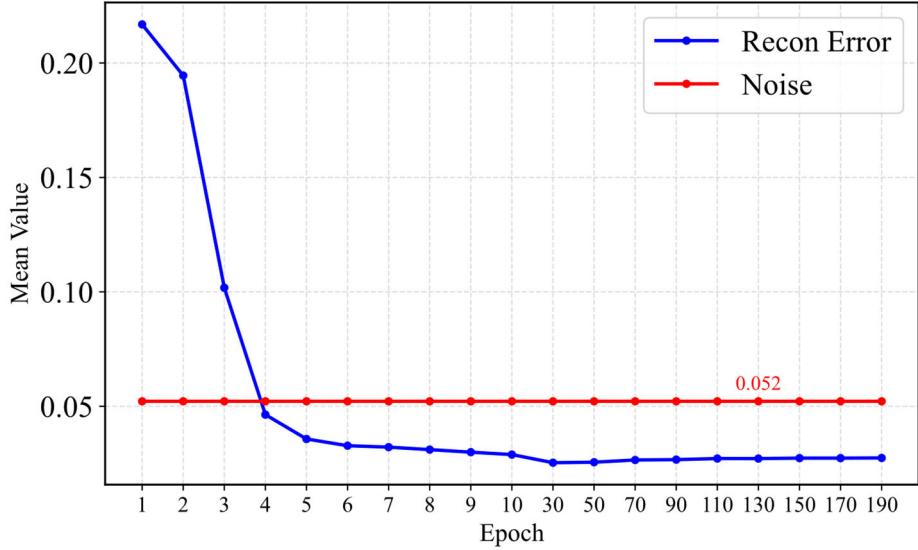


Figure 1: Mean Noise (red) and mean Recon Error(blue) of all signals across training epochs, computed according to Eq. 2 and Eq. 4. After epoch 10, Recon Error becomes stable. Therefore, metrics are reported every 20 epochs starting from epoch 10. Data are derived from the CNN¹ simulation experiment with SNR = 15.

To further investigate the signal characteristics within a single epoch, a refined analysis was conducted based on Fig. 1. Specifically, all signals within one epoch were grouped according to their Fitting Error, which was calculated as Eq. 3. It should be noted that while the overall mean Noise across all signals is fixed, the mean Noise within each subgroup varies due to differences in the sampled signals. To enhance the reliability of the conclusions, the relationships among Noise, Recon Error, and Fitting Error were examined across multiple epochs (30, 50, 100). The results are presented in Fig. 2.

From Fig. 2, another phenomenon can be observed: as the Fitting Error increases, the mean Noise increases significantly, while the mean Recon Error decreases slightly. This phenomenon can be observed for all epochs greater than 10. Because smaller values of Noise and Recon Error indicate signals closer to the clean signal, reflecting higher overall quality, this phenomenon can be summarized as **Phenomenon 2**: After extended training, as the Fitting Error increases, the overall quality gap between predicted signals and noisy signals increases.

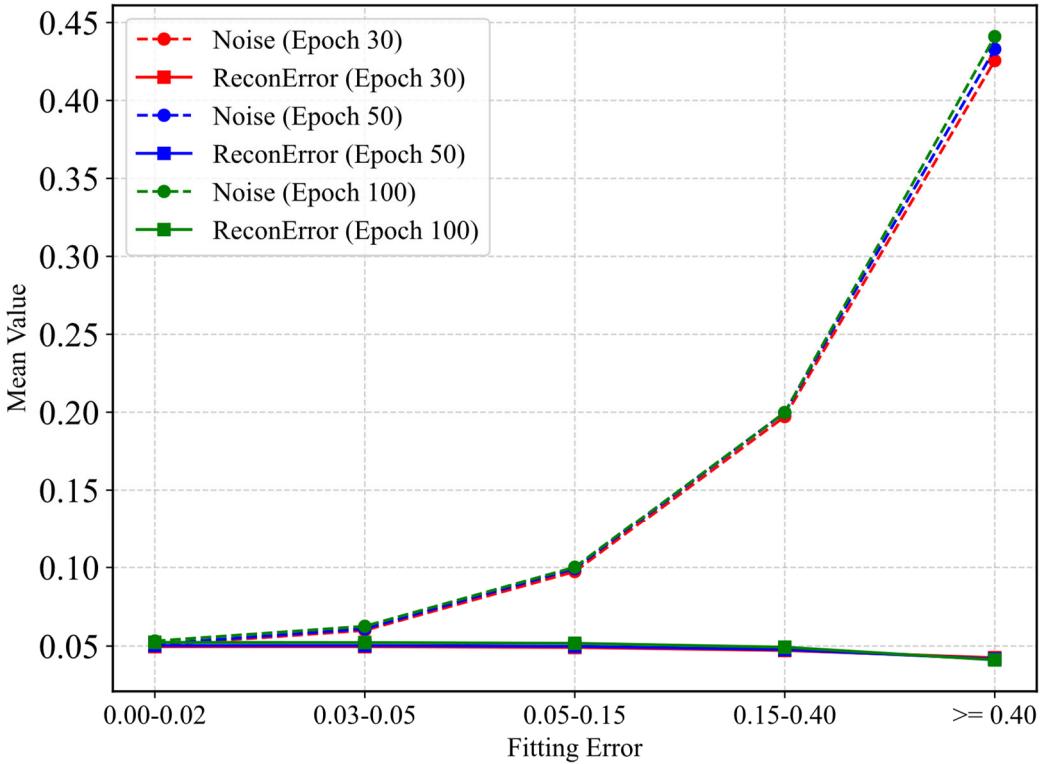


Figure 2: Mean Noise (dashed) and mean Recon Error (solid) of signals grouped by Fitting Error within a single epoch. Fitting Error intervals are left-closed, right-open. Data from epochs 30, 50, and 100 are shown in red, blue, and green curves, respectively. Data are derived from the CNN¹ simulation experiment with SNR = 15.

The verification process for Phenomena 1 and 2 is as follows:

Consider n clean signals across all voxels and all b -values, with the normalized clean signals denoted as s_i and the noise introduced during acquisition denoted as ϵ_i . The noisy signal is represented as $n_i = s_i + \epsilon_i$. The predicted signal obtained from an unsupervised model using n_i as input is denoted as p_i , and the corresponding fitting error is defined as $f_i = p_i - n_i$.

To reflect the overall quality of the predicted signals, we define the metric Q_p as follows:

$$Q_p = \frac{1}{n} \sum_{i=1}^n |p_i - s_i| \quad (4)$$

Since Q_p represents the differences between the predicted signals p_i and the clean signals s_i , a smaller value of Q_p indicates that p_i is closer to s_i , reflecting higher overall signal quality. Similarly, we define Q_n to quantify the overall quality of the noisy signals n_i :

$$Q_n = \frac{1}{n} \sum_{i=1}^n |n_i - s_i| \quad (5)$$

From the definitions of f_i and n_i , we have $p_i = n_i + f_i$ and $n_i - s_i = \epsilon_i$, which leads to:

$$|p_i - s_i| = |n_i + f_i - s_i| = |(n_i - s_i) + f_i| = |\epsilon_i + f_i| \quad (6)$$

$$Q_p = \frac{1}{n} \sum_{i=1}^n |p_i - s_i| = \frac{1}{n} \sum_{i=1}^n |\epsilon_i + f_i| \quad (7)$$

$$Q_n = \frac{1}{n} \sum_{i=1}^n |n_i - s_i| = \frac{1}{n} \sum_{i=1}^n |\epsilon_i| \quad (8)$$

The study by Zhang et al² demonstrated that, after extended training, the error in the loss function is primarily attributable to noise. To reduce the loss, the model tends to learn the noise ϵ_i and suppress its influence, thereby driving the predicted signal closer to the clean signal. Since $p_i = n_i + f_i$, the fitting error f_i can be regarded as the correction made by the model when processing the noisy signal n_i . Consequently, after sufficient training, for the vast majority of voxels and b-value signals, f_i is oriented in the opposite direction of ϵ_i , with its magnitude being smaller than that of ϵ_i , thus:

$$|\epsilon_i + f_i| < |\epsilon_i| \quad (9)$$

Therefore:

$$|p_i - s_i| = |\epsilon_i + f_i| < |\epsilon_i| = |n_i - s_i| \quad (10)$$

On average over all signals, we have:

$$Q_p = \frac{1}{n} \sum_{i=1}^n |p_i - s_i| < \frac{1}{n} \sum_{i=1}^n |\epsilon_i| = Q_n \quad (11)$$

Smaller values of Q_p and Q_n indicate that the corresponding predicted signals p_i and noisy signals n_i exhibit higher overall quality. This finding strongly supports Phenomenon 1: As training progresses, the predicted signals progressively surpass the noisy signals in overall quality.

The quality metric of a single predicted signal is defined as $q_p = |p_i - s_i|$, while the quality metric of a single noisy signal is defined as $q_n = |n_i - s_i|$. The quality difference between the two is represented as $\Delta_i = q_p - q_n$.

Smaller values of q_p and q_n indicates that the corresponding predicted signal p_i or noisy signal n_i is closer to the clean signal s_i , thereby reflecting higher quality. Therefore, if $\Delta_i < 0$, the predicted signal p_i has higher quality than the noisy signal n_i ; if $\Delta_i > 0$, the predicted signal p_i has lower quality than the noisy signal n_i , with larger values of $|\Delta_i|$ indicating a greater quality difference between p_i and n_i .

Expanding Δ_i as:

$$\Delta_i = q_p - q_n = |p_i - s_i| - |n_i - s_i| \quad (12)$$

Substituting Eq. 11 into Eq. 13:

$$\Delta_i = |\epsilon_i + f_i| - |\epsilon_i| \quad (13)$$

Discussion by cases:

$$\Delta_i = \begin{cases} -|f_i|, & |\epsilon_i + f_i| < |\epsilon_i| \\ |f_i|, & |\epsilon_i + f_i| > |\epsilon_i| \end{cases} \quad (14)$$

From Eq. 10, it follows that after extended training, for the vast majority of voxels and b-value signals, $|\epsilon_i + f_i| < |\epsilon_i|$, in this case $\Delta_i = -|f_i|$. That means the larger the absolute value of the fitting error $|f_i|$, the larger $|\Delta_i|$ and the smaller Δ_i , indicating a more significant quality improvement of the predicted signal p_i relative to the noisy signal n_i .

Since this relationship holds for the vast majority of voxels and b-value signals,

the predicted signals exhibit higher overall quality than the noisy signals across all voxels and b-values. Moreover, the larger the absolute value of the fitting error $|f_i|$, the more pronounced this advantage becomes. This finding strongly supports Phenomenon 2: After extended training, as the Fitting Error increases, the overall quality gap between predicted signals and noisy signals increases. It should be noted that, in the actual statistical analysis, the fitting error is assumed to be positive by default; therefore, fitting error in Phenomenon 2 refers to $|f_i|$ rather than f_i .

b. Related Experimental Logs

Simulation experiment

2025.4.10

ssh running study

sicnn lamuda05 simulation snr	status
8	over
10	over
12	over
15	over
20	over
25	over
33	over
50	over
75	over
100	over

2025.4.11

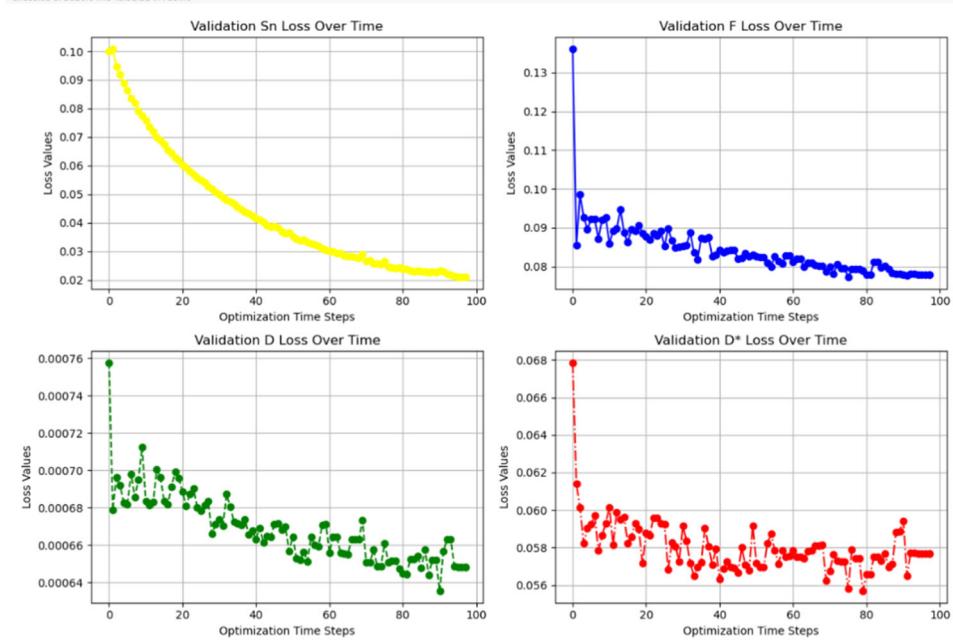
running

sicnn around simulation snr 8	training time(minutes)	val_sn_loss	val_f_loss	val_d_loss	val_d*_loss
lamuda0.01	43, 46	0.020934	0.077988	0.000648	0.057689
lamuda0.5	7, 10	0.031245	0.123295	0.001034	0.082674
lamuda0.001	118, 134	0.020476	0.075563	0.000744	0.058039
lamuda0.1	19, 17	0.021232	0.074345	0.000723	0.056163
lamuda0.05	27, 27	0.020923	0.076196	0.000749	0.056033

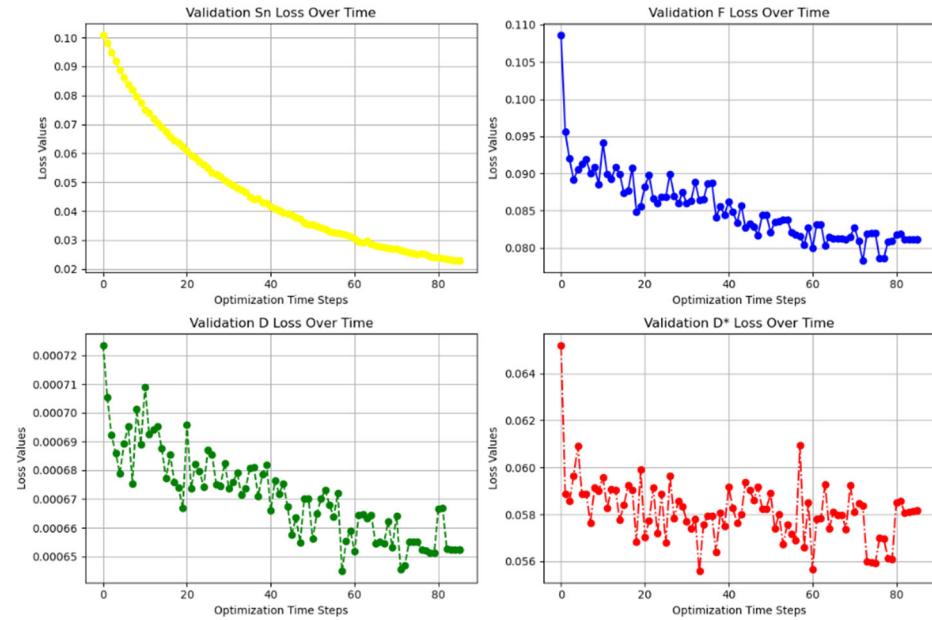
sicnn use for show time simulation snr	当前状态
8	training
10	training
12	training
15	training
20	training
25	training
33	training
50	training
75	training
100	training

2025.4.14

sicnn snr8 result



sicnn snr8 fitting error 0.03, distance 0.02



2025.5.28

si_cnn(fix_new_net,dropout=0.01,lr=4,batch25,lambda=0.01,fitting error 0.03,distance 0.02); adjust for best parameters

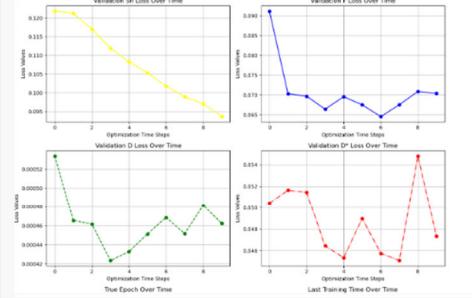
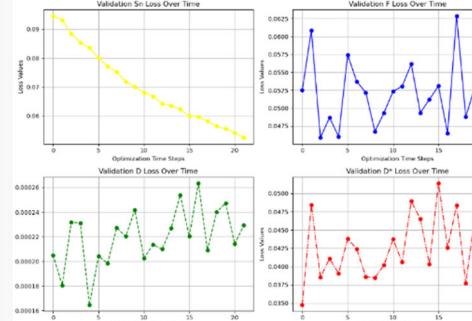
simulation : around_si_cnn	training status	parameters	others	compare with other (fitting error and distance)
8	over	snr8,lr1e-4,batch25,delta005,fitting error 0.03,distance 0.02,lambda=0.01		yes
10	OVER	snr10,lr1e-4,batch25,delta005,fitting error 0.03,distance 0.02,lambda=0.01		yes
12	over	snr12,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01		F,D better, d*worse
15	over	snr15,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01		F,D better, d*worse
20	over	snr20,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01,autosave		yes
25	over	snr25,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01,autosave		yes
33	over	snr33,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01,autosave		yes
50	over	snr50,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,autosave,limit200		yes
75	over	snr75,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01,autosave,limit200		yes
100	test	snr100,lr1e-4,batch5,delta005,fitting error 0.03,distance 0.02,lambda=0.01,autosave,limit200		yes
ALL			around,fitting_max influence heavy	

2025.5.31 keep trying for better result

simulation : around_si_cnn	training status	parameters	others	result
8		snr8,lr1e-4,batch25,delta005,around003,fitting_max002,lambda=0.01		
10		snr10,lr1e-4,batch25,delta005,around003,fitting_max002,lambda=0.01		
12		snr12,batch25,delta005,around003,fitting_max002,lambda=0.01		val_f_loss: 0.0485508106648922 val_d_loss: 0.00044553776388056576 val_dstar_loss: 0.04398658126592636
15		snr15,batch25,delta005,around003,fitting_max002,lambda=0.01		val_f_loss 0.038111 val_d_loss 0.000351 val_dstar_loss 0.036368
20		snr20,batch25,delta005,around003,fitting_max002,lambda=0.01,autosave		
25		snr25,batch25,delta005,around003,fitting_max002,lambda=0.01,autosave		val_f_loss: 0.024040494114160538 val_d_loss: 0.00018500156875234097 val_dstar_loss: 0.026606647297739983
33		snr33,batch25,delta005,around003,fitting_max002,lambda=0.01,autosave		val_f_loss 0.019424 val_d_loss 0.000130 val_dstar_loss 0.021947
50	test	snr50,batch25,delta005,around003,fitting_max002,lambda=0.01		val_f_loss 0.012880 val_d_loss 0.000077 val_dstar_loss 0.016127
75	test	snr75,batch25,delta005,around003,fitting_max002,lambda=0.01,autosave		val_f_loss 0.009439 val_d_loss 0.000052 val_dstar_loss 0.012861
100		snr100,batch25,delta005,around003,fitting_max002,lambda=0.01		val_f_loss: 0.007904388941824436 val_d_loss: 4.495037137530744e-05 val_dstar_loss: 0.011166084557771683

2025.6.3 true experiment

sicnn batch5,delta005,fitting_error 003,fitting_max002,lambda001

sicnn	status	results	results
snr12	over	val_f_loss 0.065930 val_d_loss 0.000441 val_dstar_loss 0.036248	val_f_loss: 0.06088801845908165 val_d_loss: 0.00040284631540998816 val_dstar_loss: 0.03552285581827164
snr12	wrong		
snr33	over	val_f_loss 0.043301 val_d_loss 0.000200 val_dstar_loss 0.025823	
snr33	test		
snr33	test		
after validation, around_diff = 0.02, fitting_max=0.03, result better			val_f_loss 0.041317 val_d_loss 0.000177 val_dstar_loss 0.020673
snr33 around_si_cnn_limit80			
snr33 around_si_cnn_batchsize40			
snr33 around_si_cnn_batchsize60			

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a. convergence plot

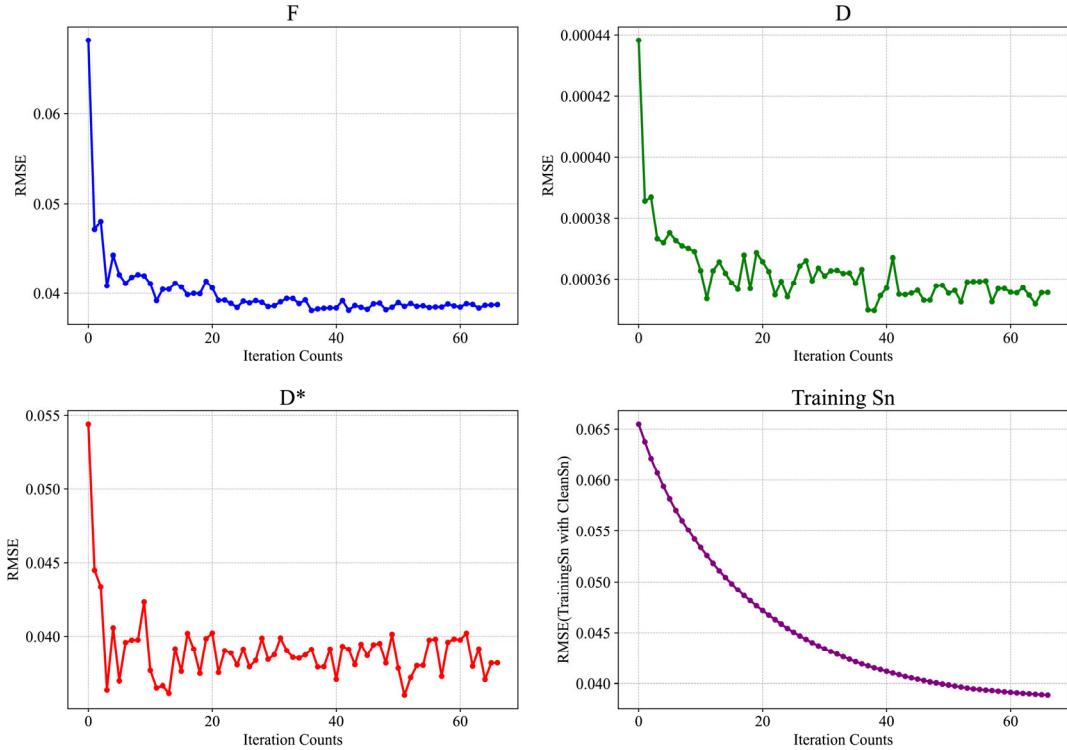


Figure 3: RMSE of SI-CNN in predicting F, D, and D* parameters (computed as the mean squared error between the predicted parameters and the ground truth) and RMSE of training signals (computed as the mean squared error between the training signals and the clean signals) as a function of the times of iterations for simulated abdominal data at SNR = 15. The x-axis indicates the times of data iterations.◦

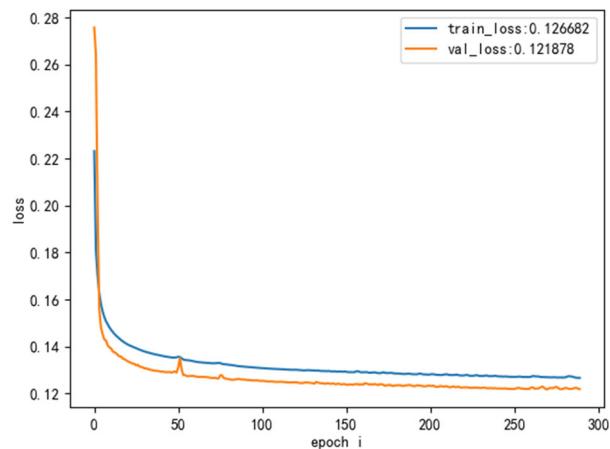


Figure 4: Training and Validation Loss.

Reference

1. Huang, H. M. (2022). An unsupervised convolutional neural network method or estimation of intravoxel incoherent motion parameters. *Physics in Medicine & Biology*, 67(21), 215018.
2. Zhang, K., Zuo, W., Chen, Y., Meng, D., & Zhang, L. (2017). Beyond a gaussian denoiser: Residual learning of deep cnn for image denoising. *IEEE transactions on image processing*, 26(7), 3142-3155.