Lexical Analysis/Scanning

## Input and Output

The input is a stream of characters (ASCII codes) of the source program.

The output is a stream of tokens or symbols corresponding to different syntactic categories. The output also contains attributes of tokens. Examples of tokens are different keywords, identifiers, constants, operators, delimiters etc.



The scanner removes the comments, white spaces, evaluates the constants, keeps track of the line numbers etc.

This stage performs the main I/O and reduces the complexity of the syntax analyzer.

The syntax analyzer invokes the scanner whenever it requires a token.

# Token

A token is an identifier (name/code) corresponding to a syntactic category of the language grammar. In other word it is the terminal alphabet of the grammar. Often we use an integer code for this.

# Pattern

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A pattern is a description (formal or informal) of the set of objects corresponding to a terminal (token) symbol of the grammar. Examples are the set of *identifier* in C language, set of integer constants etc.

#### Lexeme and Attribute

A lexeme is an actual string of characters that matches with a pattern and generates a token. An attribute of a token is a value that the scanner extracts from the corresponding lexeme and supplies to the syntax analyzer.

# Specification of Token

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The set of strings corresponding to a token (terminals) of a programming language is often a regular set and is specified by a regular expression.

### Scanner from the Specification

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The collection of tokens of a programming language can be specified by a set of regular expressions. A scanner or lexical analyzer for the language uses a DFA (recognizer of regular languages) in its core. Different final states of the DFA identifies different tokens. Synthesis of this DFA from the set of regular expressions can be automated.

## Regular Expression

- 1.  $\varepsilon$ ,  $\emptyset$  and all  $a \in \Sigma$  are regular expressions.
- 2. If r and s are regular expressions, then so are (r|s), (rs),  $(r^*)$  and (r). Nothing else is a regular expression.

We can reduce the use of parenthesis by introducing precedence and associativity rules. Binary operators are left associative and the precedence rule is \* >concat > |.

### IEEE POSIX Regular Expression

An enlarged set of operators (defined) for the regular expressions are introduced in different softwares e.g. awk, grep, lex etc.<sup>a</sup>.

- \x is the character itself (a few exceptions are \n, \t, \r etc.).
- . is any character other than ' $\n'$ .
- [xyz] is x | y | z.

<sup>&</sup>lt;sup>a</sup>Consult the manual pages of lex/flex and Wikipedia for the details of IEEE POSIX standard of regular expressions.

## IEEE POSIX Regular Expression

- [abg-pT-Y] any character a, b,g, ..., p, T, ..., Y.
- [ $^G$ -Q] not any one of G, H, ..., P, Q.
- r+ one or more r's.
- r? one or zero r's.
- $r\{2,\}$  two or more r's etc.

### Language of a Regular Expression

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The language of a regular expression is defined in a usual way on the inductive structure of the definition.

$$L(\varepsilon) = \{\varepsilon\}, L(\emptyset) = \emptyset, L(a) = \{a\} \text{ for all } a \in \Sigma, L(r|s) = L(r) \cup L(s), L(rs) = L(r)L(s), L(r^*) = L(r)^*, L(r^*) = L(r) \cup \{\varepsilon\} \text{ etc.}$$

## C Identifier

The regular expression for the C identifier is [\_a-zA-Z] [\_a-zA-Z0-9]\*

The first character is an underscore or an English alphabet. From the second character on a decimal digit can also be used.

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## Regular definition

We can give name to a regular expression for the convenience of use. The name of a regular expression can be used within the following regular expressions.

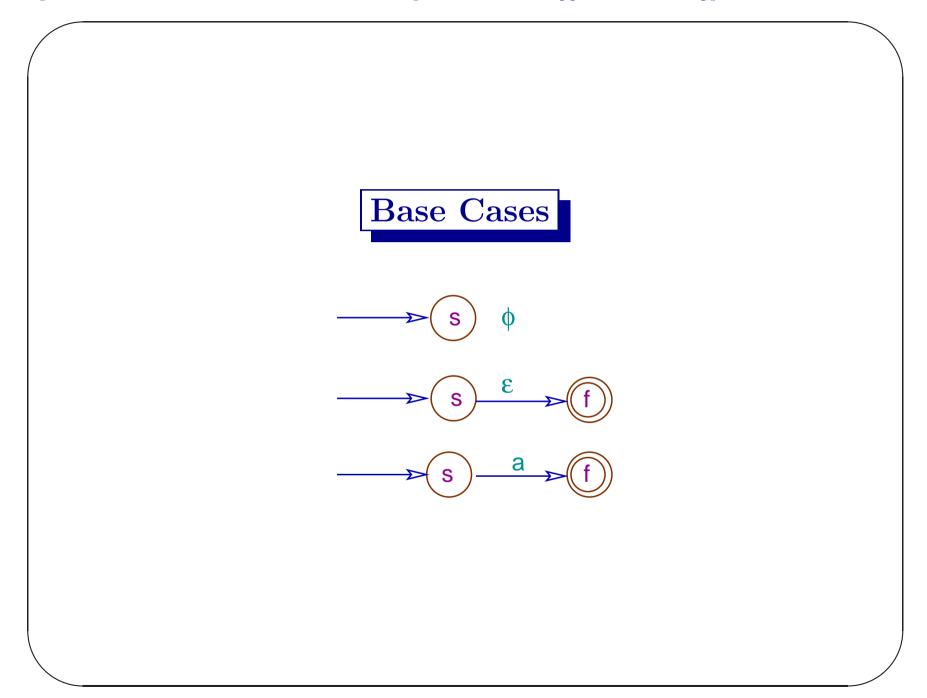
#### Example of a Regular Definition

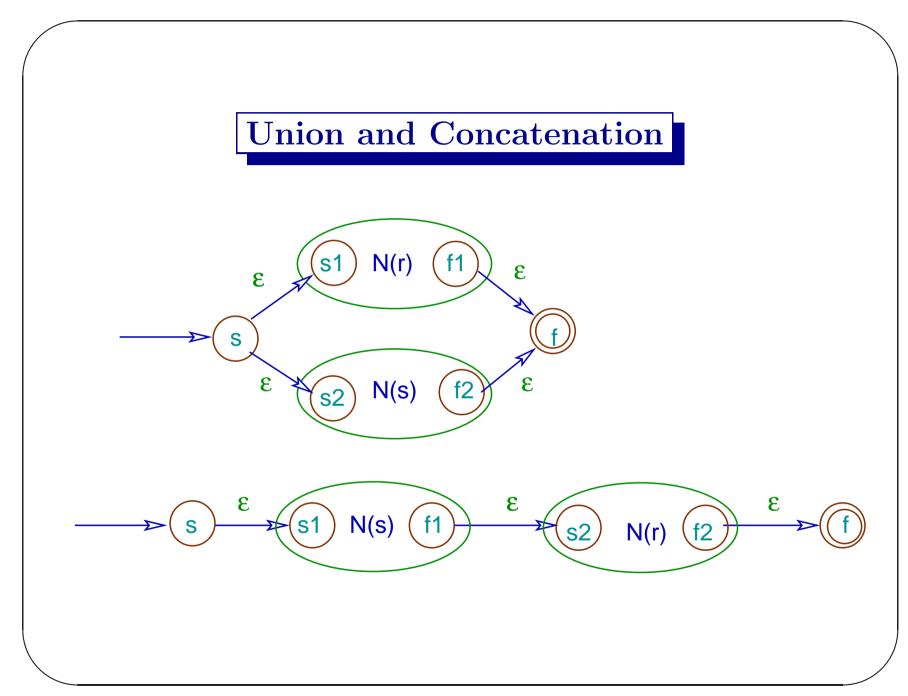
```
sign: + | - | \varepsilon
digit: [0-9]
digits: {digit}*
frac: \.{digits} | \varepsilon
frace: \.{digit}{digits}
expo: ((E \mid e)\{sign\}\{digit\}\{digit\}?) \mid \varepsilon
          {sign}(({digit}+ {frac} {expo}))
num:
           ({frace} {expo}))
```

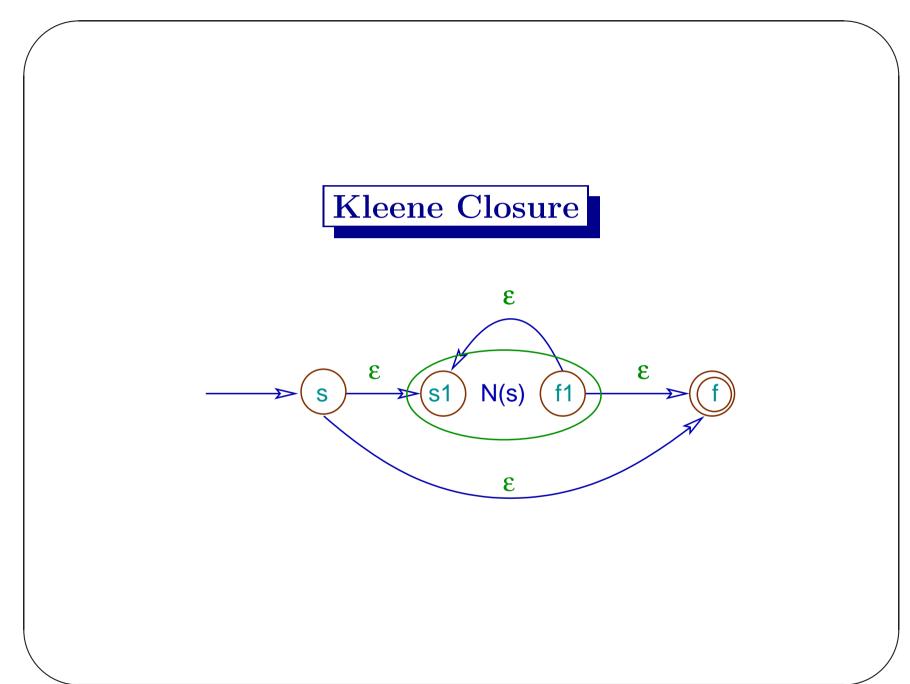
#### RE to NFA: Thompson's Construction

We can mechanically construct a non-deterministic finite automaton (NFA) with only one initial and only one final state from a given regular expression. The total number of states of the NFA is linear in the number of symbols of the regular expression<sup>a</sup>

 $<sup>^</sup>a$ The construction is on the inductive structure of the definition of the regular expression.





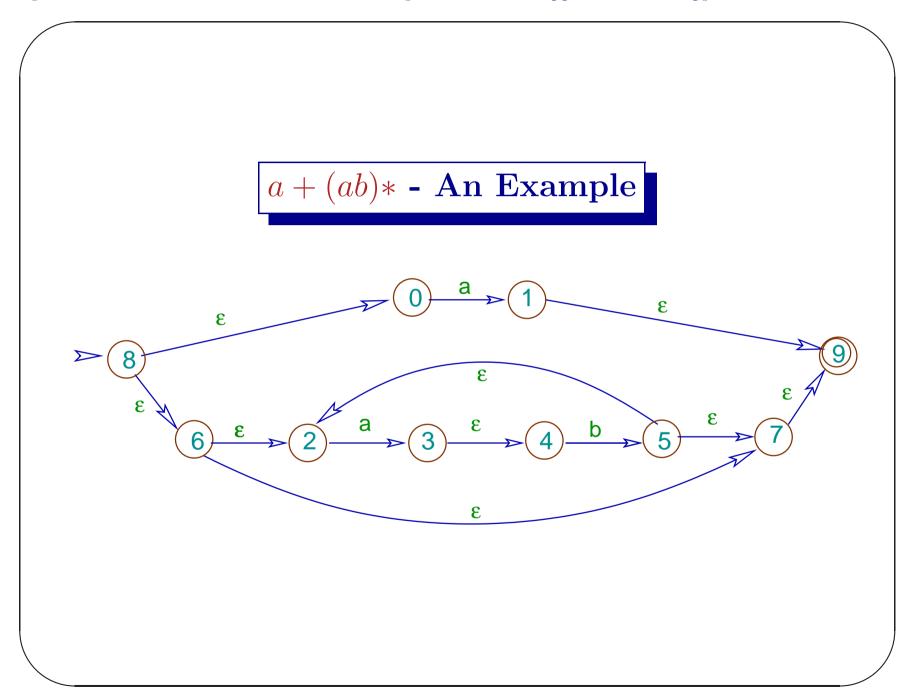


## Properties of Thompson's Construction

- $|Q| \leq 2 \text{length}(r)$ , where Q is the number of states of the NFA and length(r) is the number of alphabet and operator symbols in r.
- Only one initial and one final state. No incoming edge to the initial state and no outgoing edge from the final state.

## Properties of Thompson's Construction

• At most one incoming and one outgoing transition on a symbol of the alphabet. At most two incoming and two outgoing  $\epsilon$ —transitions.



## Context-Free Grammar of RE

The set of regular expression can be specified by a context-free grammar.

$$E \rightarrow \emptyset \mid \varepsilon \mid \sigma, \forall \sigma \in \Sigma$$

$$\rightarrow E.E \mid E + E \mid E * \mid (E)$$

We have put a '.' for concatenation to make it an *operator grammar* and have replaced '|' by '+' for clarity<sup>a</sup>.

<sup>&</sup>lt;sup>a</sup>This ambiguous grammar can be used with proper precedence and associativity rules.

## Syntax Directed Thompson's Construction

Rules of Thompson's construction can be associated with the production rules of the grammar. We assume the following data structures.

## Syntax Directed Thompson's Construction

- Global state counter S initialized to 0, and the state transition table: T[][].
- With every occurrence of the non-terminal E we associate two attributes E.ini and E.fin to store the initial and the final states of the NFA, corresponding to the regular expression generated by this occurrence of E.

## Some of the Rules: Basis

$$E \rightarrow \varepsilon$$
: {T[S][ $\varepsilon$ ] = S+1; E.ini = S;  
S = S+1; E.fin = S; S = S+1;}  
 $E \rightarrow a$ : {T[S][a] = S+1; E.ini = S;  
S = S+1; E.fin = S; S = S+1;}

The second rule depends on the symbol of the alphabet

### Concatenation Rules

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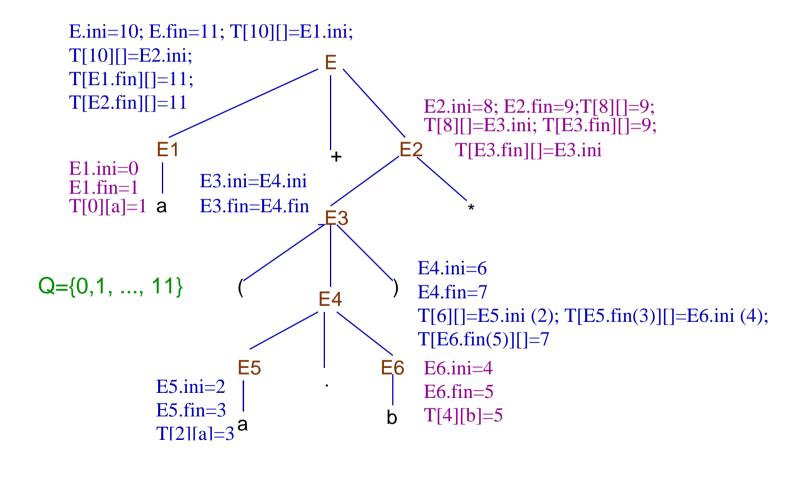
```
E \rightarrow E1.E2: \quad \{\text{E.ini} = \text{S}; \; \text{S} = \text{S+1}; \\ \text{E.fin} = \text{S+1}; \; \text{S} = \text{S+1}; \\ \text{T}[\text{E.ini}] [\varepsilon] = \text{E1.ini}; \\ \text{T}[\text{E1.fin}] [\varepsilon] = \text{E2.ini}; \\ \text{T}[\text{E2.fin}] [\varepsilon] = \text{E.fin}; \} \\ \text{Similarly other rules can be derived.}
```

#### The Final NFA

The states of the final NFA are  $\{0, 1, \dots, S-1\}$ . The *initial* state is in E.ini and the *final* state is in E.fin. The state transitions are in T[][].

## a + (a.b)\* - An Example

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## NFA to DFA

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Let the constructed  $\varepsilon$ -NFA be  $(N, \Sigma, \delta_n, n_0, n_F)$ . By taking  $\varepsilon$ -closure of states and doing the subset construction we can get an equivalent DFA  $(Q, \Sigma, \delta_d, q_0, Q_F)$ .

## ${f Algorithm}$

$$Q = L = \varepsilon\text{-}closure(\{q_0\})$$
  
 $\mathbf{while}(L \neq \emptyset)$   
 $q = removeElm(L)$   
 $\mathbf{for \ all} \ \sigma \in \Sigma$   
 $t = \varepsilon\text{-}closure(\delta_n(q, \sigma))$   
 $T[q][\sigma] = t$   
 $\mathbf{if} \ t \notin Q$   
 $Q = Q \cup \{t\}$   
 $L = L \cup \{t\}$ 

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## $\varepsilon$ -closure(T)

```
for all q \in T push(St, q)
\varepsilon T = T
while (isEmpty(St) == false)
t = pop(St)
for all u \in \delta(t, \varepsilon)
if u \not\in \varepsilon T
\varepsilon T = \varepsilon T \cup \{u\}
push(St, u)
```

Note

The time complexity of the  $\varepsilon$ -closure algorithm for each state is  $O(|M|) = O(|N| + |\delta|)$ .

#### Final State of the DFA

The set of final states of the equivalent DFA is  $Q_F = \{q \in Q : n_F \in q\}$ . It is to be noted that different final states will recognize different tokens. It is also possible that one final state identifies more than one tokens.

#### Time Complexity of Subset Construction

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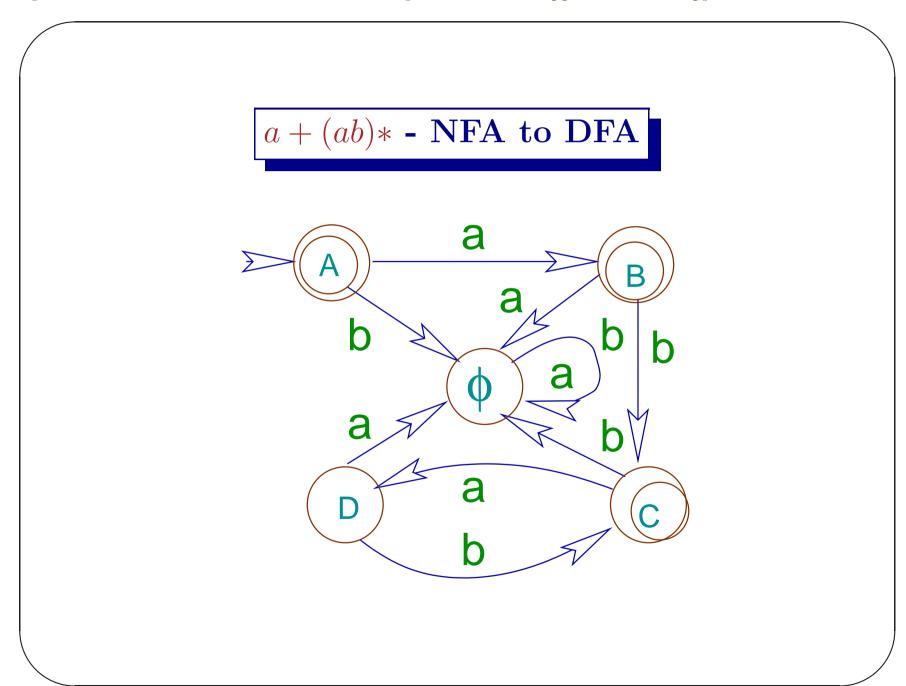
The size of Q is  $O(2^{|N|})$  and so the time complexity is also  $O(2^{|N|})$ , where N is the set of states of the NFA. But this is one time construction.

$$a + (ab)*$$
 - NFA to DFA

The state transition table of the DFA is

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Initial	Final State	
State	a	b
$A: \{0, 2, 6, 7, 8, 9\}$	$\{1, 3, 4, 9\}$	Ø
$B: \{1,3,4,9\}$	Ø	$\{2, 5, 7, 9\}$
$C: \{2, 5, 7, 9\}$	${3,4}$	Ø
$D: \{3,4\}$	Ø	$\{2, 5, 7, 9\}$
Ø	Ø	Ø



Note

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It may be of advantage to drop the transitions to  $\emptyset$  for designing a scanner. This makes the DFA incompletely specified. Absence of a transition from a final state may identify a token.

## **DFA State Minimization**

The constructed DFA may have set of equivalent states<sup>a</sup> and can be minimized. It is to be noted that the time complexity of a scanner of a DFA with a larger number of states is not different from the scanner of a DFA having a smaller number of states. Their code sizes are different and that may give rise to some difference in their speeds.

<sup>&</sup>lt;sup>a</sup>Let  $M=(Q,\Sigma,\delta,s,F)$  be a DFA. Two states  $p,q\in Q$  are said to be equivalent if there is no  $x\in \Sigma^*$  so that  $\delta(p,x)\neq \delta(q,x)$ .

## DFA State Minimization

We start with two non-equivalent partitions of Q: F and  $Q \setminus F$ .

If p, q belongs to the same initial partition P but there is some  $\sigma \in \Sigma$  so that  $\delta(p, \sigma) \in P_1$  and  $\delta(q, \sigma) \in P_2$ , where  $P_1$  and  $P_2$  are two distinct partitions, then p, q cannot remain in the same partition i.e. they are not equivalent.

#### DFA to Scanner

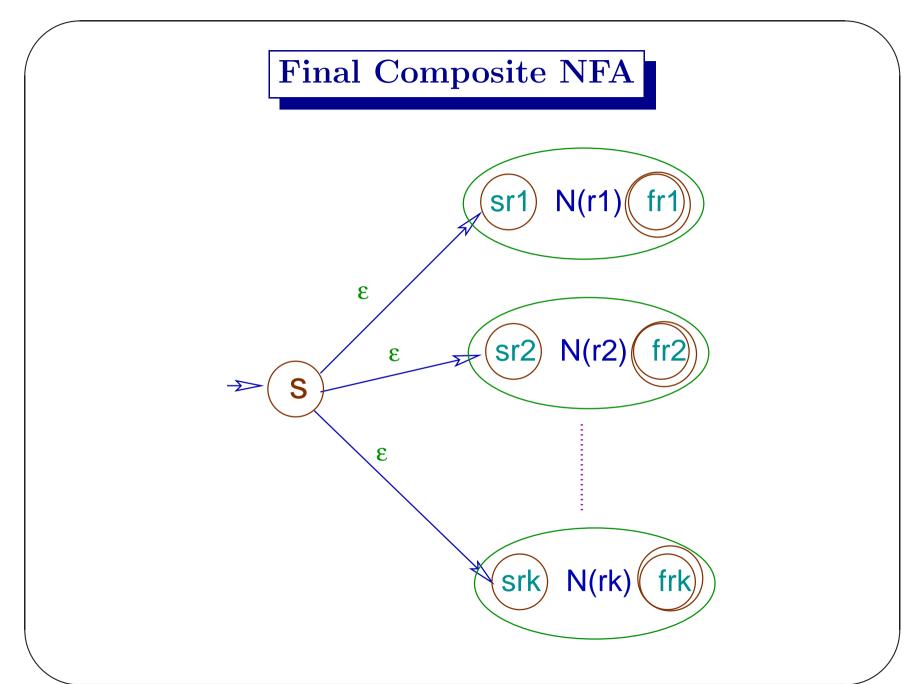
Given a regular expression r we can construct the recognizer of L(r). For every token class or syntactic category of a language we have a regular expression. Let  $\{r_1, r_2, \dots, r_k\}$  be the total collection of all regular expressions of a language. The regular expression  $r = r_1 | r_2 | \cdots | r_k$  represents objects of all syntactic categories.

## DFA to Scanner

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Give the NFAs of  $r_1, r_2, \dots, r_k$  we construct the NFA for  $r = r_1 | r_2 | \dots | r_k$  by introducing a new start state and adding  $\varepsilon$ -transitions from this state to the *initial states* of the component NFAs. But we keep different final states as they are to identify different token classes.

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## DFA to Scanner

The DFA corresponding to r can be constructed from the composite NFA. It can be implemented as a C program that will be used as a scanner of the language. But the following points are to be noted.

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A program is not a single word but a stream of words and the notion of acceptance of a scanner should be different from a simple DFA. The following questions are of importance:

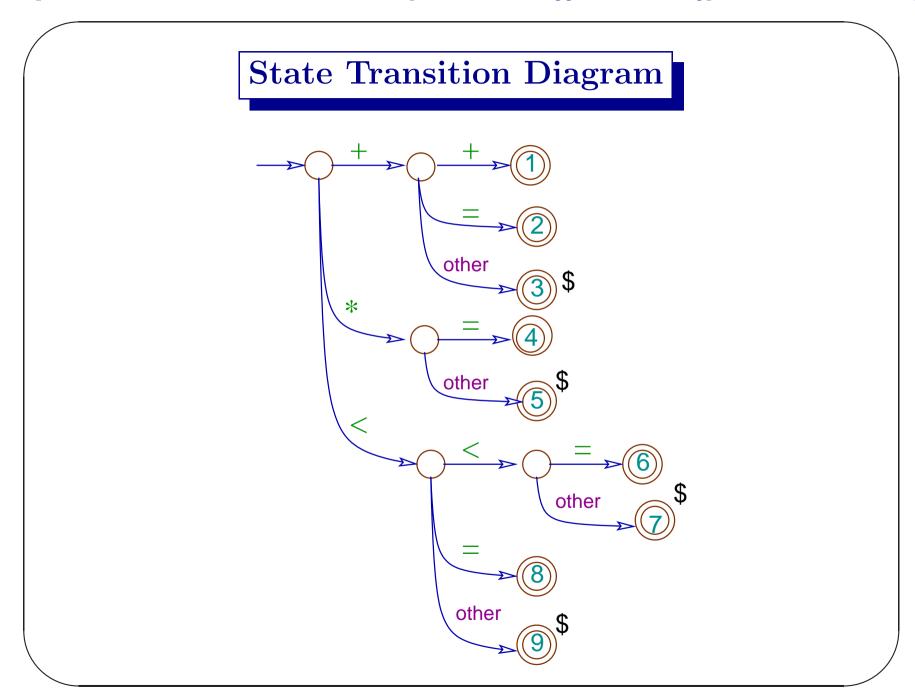
- when does the scanner report an acceptance?
- what does it do if the word (lexeme) matches with more than one regular expressions?

Example

Consider the following subset of C language operators: + ++ += \* \*= < << <= <<=

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At the final state 1 we know that we have "++". But we cannot decide whether it is *pre* or *post* increment operator. Though scanner can take that decision, but it is better to delay it for the parser.

Note

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At the final state 3 we know that we have '+'. But we do not know whether it is binary or unary. Again that decision is defered. Moreover the last consumed symbol is not part of the lexeme. It is a look-ahead symbol. We mark such a final state with the number of look-ahead symbols to un-read before going back to the start state. Here we have done that by one \$.

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• There are situations where there may be more than one look-ahead.

#### Fortran:

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D0 10 I = 1, 10 and D0 10 I = 1.10 The first one is a do-loop and the second one is an assignment D010I=1.10.

# PL/I:

IF ELSE THEN THEN = ELSE; ELSE ELSE = THEN IF THEN are not reserved as keyword.

## Maximum Word Length Matching

The scanner will go on reading input as long as there is a transition. Let there be no transitions for the current state q on the input  $\sigma$  (the machine is incompletely specified). The state q may or may not be final.

q is Final

If the final state q corresponds to only one regular expression  $r_i$ , the scanner returns the corresponding token<sup>a</sup>. But if it matches with more than one regular expressions then it is necessary to resolve the conflict. This is often done by specifying priority of expressions e.g. keyword over an identifier.

<sup>&</sup>lt;sup>a</sup>It is necessary to identify the final state with the regular expression  $r_i$ .

|q| is not Final

It is possible that while consuming symbols the scanner has crossed one or more final states. The decision may be to report the last final state. But then it is necessary to keep track of the final states and the position of the input.

# Specifying Actions

Once a final state is reached with no transition on the current input, the scanner returns a token and its attribute value. The question is whether to attach action only with a final state or with every transition. An action only at the final state may call for rescanning the already read input which may be inefficient.

# Components of a Scannar

- 1. The transition table of the DFA or NFA.
- 2. Set of actions corresponding to a final states.
- 3. Other essential functions.

## Maximum Prefix on NFA

- 1. Read input and keep track of the sequence of the set of states. Stop when no more transition is possible (maximum prefix).
- 2. Trace back the *last set of states* with a final state.
- 3. Push back the look-ahead symbols in the buffer and emit appropriate *token* along with attribute value(s).



It is possible that the last set of states has more than one final states corresponding to different patterns. Take action corresponding to a pattern with highest priority<sup>a</sup>.

<sup>&</sup>lt;sup>a</sup>A pattern specified earlier may have higher priority.

# Reading Characters: Input Buffer

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A scanner or lexical analyser reads the input character by character. The process will be very inefficient if it sends request to the OS for every caharacter read.

# Input Buffer

- OS reads a block of data, supplies the requesting process the required amount, and stored the remaining portion in a buffer called buffer cache. In subsequent calls, the actual IO does not take place as long as the data is available in the buffer.
- Requesting OS for single character is also costly due to context-switching overhead. So the scanner uses its own buffer.

# Input Buffer

- A buffer at its end may contain an initial portion of a lexeme. It creates problem in refilling the buffer. So a 2-buffer scheme is used. The buffers are filled alternatively.
- A sentinal-character is placed at the end-of-buffer to avoid two comparisons character and end-of-buffer.
- We may run out of buffer space for a long

character string or a comment.