

Unit 3 Test MDM4U

(K/U)

(1)

a) The group of plants grown using water with neutral pH serves as the control group. while each ~~of the~~ other group grown using water with increasingly acidic pH levels are the experimental groups.

b) Using a group of plants for each pH level allows the botanist to observe and account for variations in individual plant responses. It helps in obtaining more reliable and generalizable results by reducing the impact of outliers and providing a basis for comparison and statistical analysis.

(2)

Observation table

$$N = \sum f = 50$$

Distance (m)	frequency	Cumulative frequency
0-5	1	1
5-10	0	$1+0 = 1$
10-15	6	$1+6 = 7$
15-20	12	$7+12 = 19$
20-25	15	$19+15 = 34$
25-30	5	$34+5 = 39$
30-35	7	$39+7 = 46$
35-40	1	$46+1 = 47$
40-45	3	$47+3 = 50$

② The Median is given by

Median = The value of $(\frac{N+1}{2})^{\text{th}}$ observation.

= The value of $(\frac{50+1}{2})^{\text{th}}$ observation.

= The value of $(25.5)^{\text{th}}$ observation.

The median class is the class just greater than 25.5 which means the median class is 20-25

The formula is-

$$\text{Median} = L + \frac{(\frac{N}{2}) - CF}{f} * W$$

Where

L = Lower limit of median class = 20

CF = Cumulative frequency of previous of median class

CF = 19

f = frequency of median class = 15

W = Class width = 5 = ~~10~~

= Upper limit - Lower limit

$$\begin{aligned}\text{Median} &= L + \frac{(\frac{N}{2} - CF)}{f} W \\ &= 20 + \frac{(\frac{50}{2} - 19)}{15} * 5 \\ &= 20 + \frac{(25 - 19)}{3} * 5\end{aligned}$$

$$\begin{aligned}&= 20 + \frac{(6) * 5}{3} \\ &= 22\end{aligned}$$

$$\boxed{\text{Median} = 22}$$

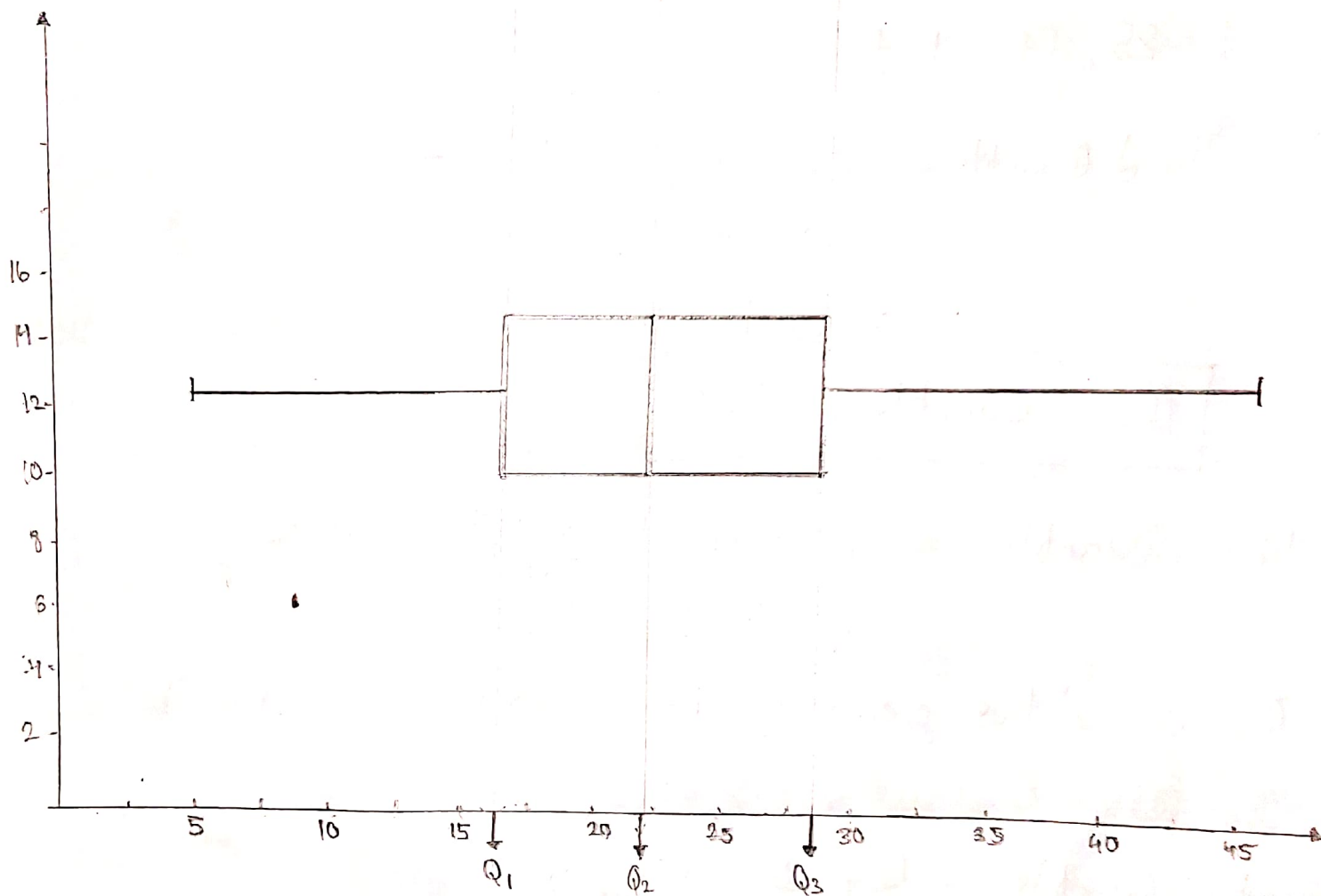
$$\begin{aligned}\text{Range} &= \text{Upper limit} - \text{Lower limit} \\ &= 45 - 0\end{aligned}$$

$$\boxed{\text{Range} = 45}$$

$$\begin{aligned}\text{Inter Quartile Range} &= Q_3 - Q_1 \\ &= 28.5 - 17.3 \\ &= 11.2\end{aligned}$$

$$\boxed{\text{Inter Quartile Range (IQR)} = 11.2}$$

Box and Whisker Plot



- ⑥ The whiskers would extend from 0 meters to 40 meters. This means the farthest any turtle travelled was 40m and the closest any ~~low~~ turtle traveled was 0m.
- The box covers the range of distance between 10m and 30m. This suggests that most turtle traveled between 10 and 30m in 15 minutes.

$$\text{Third Quartile} = Q_3 = \text{value of } 3\left(\frac{N+1}{4}\right)^{\text{th}} \text{ observation}$$

$$= Q_3 = \text{value of } (37.25)^{\text{th}} \text{ observation}$$

The cumulative frequency just greater than 37.25 is 39.

The Quartile class is 25-30.

$$\text{Third Quartile} = L + \frac{3\left(\frac{N}{4}\right) - CF}{f} \times W$$

$$L = 25, CF = 34, f = 5, W = 5$$

$$\text{Third Quartile} = 25 + \frac{3\left(\frac{50}{4}\right) - 34}{5} \times 5$$

$$= 25 + 3.5$$

$$\boxed{\text{Third Quartile} = 28.5}$$

$$\text{First Quartile} = \text{value of } 1\left(\frac{N+1}{4}\right)^{\text{th}} \text{ observation.}$$

$$= 12.75^{\text{th}} \text{ observation}$$

The cumulative frequency just greater 12.75 is 19.

The Quartile class is 15-20

$$\text{First Quartile} = L + \frac{\frac{N}{4} - CF}{f} \times W$$

$$= 15 + \frac{\frac{50}{4} - 9}{12} \times 5$$

$$= 17.3$$

$$\boxed{\text{First Quartile} = 17.3}$$

(K/U) Cont'd

Outliers of the data

$$\begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 28.5 - 17.3 \end{aligned}$$

$$\boxed{\text{IQR} = 11.2}$$

$$\begin{aligned} \text{Lower limit} &= Q_1 - 1.5 \text{IQR} \\ &= 17.3 - 1.5(11.2) \\ &= 17.3 - 16.8 \end{aligned}$$

$$\boxed{\text{Lower limit} = 0.5}$$

$$\begin{aligned} \text{Upper limit} &= Q_3 + 1.5 \text{IQR} \\ &= 28.5 + 1.5(11.2) \\ &= 28.5 + 16.8 \end{aligned}$$

$$\boxed{\text{Upper limit} = 45.3}$$

Any value outside the limits (0.5 - 45.3) is regarded as outliers

Yes, there are outliers in the dataset. They are values from the interval 0-5 and 40-45

(T/I)

(2)

- a) The type of sample in this scenario is a convenience sample. It's convenient because you're only surveying the people on your street, which might not represent the broader population of your town.
- b) The type of sample in this scenario is a stratified random sample. The university is dividing its student population into different strata based on department enrollment proportions and then randomly selecting students from each stratum to ensure representation from all departments.
- c) The type of sample in this case is a cluster sample. Swim Ontario is dividing the swim clubs into clusters (groups) and then randomly selecting a few clusters (10 swim clubs) to survey all members within each selected cluster. This method is more practical than surveying all members of all 139 swim clubs.
- d) The type of sample is called random sample. Each basketball player has an equal chance of being selected because their names are all placed in the hat and the coach randomly draws one name without ~~for~~ any bias or stratification.

Q cont'd

- e) The type of sample in this scenario is a **systematic sample**. The store is selecting every ninth person from an alphabetical list of credit card customers after choosing the first person randomly. This method ensures a systematic and organized approach to sampling while still providing representation from the customer list.
- f) The type of sample in this case is called **voluntary responsive sample**. The student council is inviting all students to provide ideas voluntarily. This method relies on individuals choosing to participate, so the sample may not be representative of all students, as those who participate might have different interests or ~~incentives~~ motivations.
- g) The type of sample in this scenario is a **multistage cluster sample**. The marketing firm first divides the city into neighbourhoods, then selects clusters of streets within each neighbourhood, and then finally randomly selects households within each street cluster. This method allows for efficient sampling while ensuring representation from different areas of the city.

(A)

Day	1	2	3	4	5	6	7
Temperature (°C)	27	29	32	29	45	29	31

Mean

$$\text{To find the mean} = \frac{\sum_{i=1}^n x_i}{n} = \frac{27 + 29 + 32 + 29 + 45 + 29 + 31}{7}$$

$$= \frac{222}{7}$$

$$= 31.714$$

Mean

$$\boxed{\text{Mean} = 31.71^\circ\text{C}}$$

Median

To find the median, arrange the temperature in ascending values to find the middle value

Arranged temperatures: 27, 29, 29, 29, 31, 32, 45

$$\boxed{\text{Median} = 29^\circ\text{C}}$$

Mode

The mode is the temperature that appears most frequently

$$\boxed{\text{Mode} = 29^\circ\text{C}} \rightarrow \text{occurs 3 times}$$

Comparing the predicted temperature of 36°C with the measures of central tendency

$$\text{Mean} = 31.71^\circ\text{C}, \text{ Mode} = 29^\circ\text{C}, \text{ Median} = 29^\circ\text{C}$$

The predicted temperature of 36°C is higher than all the means of central tendency. This suggests that the weather report may overestimate the temperature for the day of arrival.

c) Yes, there is an outlier in the data: 45°C . An outlier can skew the mean significantly, pulling it away from the center. In this case, it affects the mean more than the median and mode, making mean less representative of typical temperatures.

d) The median and mode would best represent temperature in this Mexican location. The median is less affected by outliers, making it a robust measure of central tendency. The mode also provides insight into the most common temperature experienced, which is valuable for understanding typical temperature conditions.

(C)

a) The question might introduce response bias, particularly if respondents feel pressured to provide a higher reading speed than they actually possess.

b) This situation could involve selection bias if only parents with strong opinions, either for or against bus safety laws, respond to the survey, rather than a representative.

© Cont'd

This could lead to non-response bias if the survey is ~~so~~ only sent to customers who have recently interacted with the company, potentially excluding those who are less engaged or dissatisfied with the services.

) This question is prone to framing bias, as it suggests a connection between the city debt and the mayor's chances of winning the next election, potentially influencing respondent opinions.