

Übung 3

$$① \lim_{x \rightarrow \infty} (x^2 + 5) = +\infty$$

$$② \lim_{x \rightarrow +\infty} (x^3 + 1855) = +\infty$$

$$③ \lim_{x \rightarrow +\infty} (x^2 + x + 6) = +\infty$$

$$④ \lim_{x \rightarrow +\infty} (3 - x) = -\infty$$

$$⑤ \lim_{x \rightarrow +\infty} (x^2 - x) = +\infty \neq (-\infty) = +\infty - \infty \text{ unbestimmt}$$

$$⑥ \lim_{x \rightarrow +\infty} (x^3 - x^2 - x + 1)$$

$$⑦ \lim_{x \rightarrow +\infty} (-x^4 + 7x^3 - x^2 + x + 1)$$

$$⑧ \lim_{x \rightarrow +\infty} (x^2 - x) = \lim_{x \rightarrow +\infty} \left[\underbrace{x^2}_{x^2} \left(\underbrace{1 - \frac{1}{x}}_{1} \right) \right] = \lim_{x \rightarrow +\infty} x^2 = +\infty$$

$$\textcircled{6} \lim_{x \rightarrow +\infty} \left[x^3 \left(1 - \frac{1}{x} - \frac{1}{x^2} + \frac{1}{x^3} \right) \right] = \lim_{x \rightarrow +\infty} x^3 = +\infty$$

$$\textcircled{7} \lim_{x \rightarrow +\infty} x^4 = +\infty$$

$$\textcircled{8} \lim_{x \rightarrow +\infty} -(x^4) = -\infty$$

$$\textcircled{9} \lim_{x \rightarrow +\infty} \frac{x+1}{x^2+1} = \frac{+\infty}{+\infty} \text{ indeterminação.}$$

$$\lim_{x \rightarrow +\infty} \frac{x \left(1 + \frac{1}{x} \right)}{x^2 \left(1 + \frac{1}{x^2} \right)} = \lim_{x \rightarrow +\infty} \frac{x}{x^2} = \frac{1}{x}$$

Símbolos de indeterminação: $\frac{0}{0}$; $+\infty - \infty$; $\frac{+\infty}{+\infty}$; $\frac{-\infty}{+\infty}$; $\frac{-\infty}{-\infty}$

$$\lim_{x \rightarrow +\infty} \frac{1}{x} = 0$$

Símbolos de indeterminação: $\frac{-\infty}{-\infty}$; $1 + \infty$; $0 \cdot \left(\frac{+\infty}{-\infty} \right)$; 0

$$\textcircled{10} \lim_{x \rightarrow -\infty} \frac{x^2 - 5x + 8}{x + 3} = \lim_{x \rightarrow -\infty} \frac{x^2}{x} = \lim_{x \rightarrow -\infty} \frac{x}{1}$$

$\lim_{x \rightarrow -\infty} x = -\infty$

$$\textcircled{11} \lim_{x \rightarrow +\infty} \frac{1 - x + x^2 + 5x^3}{4 + x^3} = \lim_{x \rightarrow +\infty} \frac{5x^3}{x^3} = \lim_{x \rightarrow +\infty} 5 = 5$$

$$\textcircled{12} \lim_{x \rightarrow +\infty} \frac{3 - x + 2x^2}{5 - 7x^2} = \lim_{x \rightarrow +\infty} \frac{2x^2}{-7x^2} = \lim_{x \rightarrow +\infty} \left(-\frac{2}{7} \right)$$

$$\textcircled{13} \lim_{x \rightarrow -\infty} \frac{1 - 4x^3}{5x^3 - 8} = \lim_{x \rightarrow -\infty} \frac{-4x^3}{5x^3}$$

$$= \lim_{x \rightarrow -\infty} \frac{-4}{5} = -\frac{4}{5}$$

$$(14) \lim_{x \rightarrow +\infty} \frac{2x^3 - 5x^2 + 3}{x^2 + 9x - 1} = \lim_{x \rightarrow +\infty} \frac{2x^3}{x^2} = \lim_{x \rightarrow +\infty} 2x = +\infty$$

$$(15) \lim_{x \rightarrow -\infty} \frac{5x^2 - 2x}{-3x^4 + 2x^3 - x^2} = \lim_{x \rightarrow -\infty} \frac{5x^2}{-3x^4} = \lim_{x \rightarrow -\infty} \left(-\frac{5}{3} \cdot \frac{1}{x^2} \right)$$

$\frac{+\infty}{-\infty} = 0$

$$(16) \lim_{x \rightarrow +\infty} (\lim_{x \rightarrow +\infty} x) = +\infty \Rightarrow \lim_{x \rightarrow +\infty} x = +\infty$$

$$(17) \lim_{x \rightarrow +\infty} \left[\lim_{x \rightarrow +\infty} \left(\frac{1}{x} \right) \right] = \lim_{x \rightarrow +\infty} 0 = 0$$

$\frac{1}{+\infty} = 0$

$$(18) \lim_{x \rightarrow -\infty} e^{1-x^2} = e^{-\infty} = 0$$

$\frac{1}{x^2} \rightarrow \frac{x^2}{x^4}$

$$(19) \lim_{x \rightarrow +\infty} (10 + e^{-x}) = 10 + 0 = 10$$