

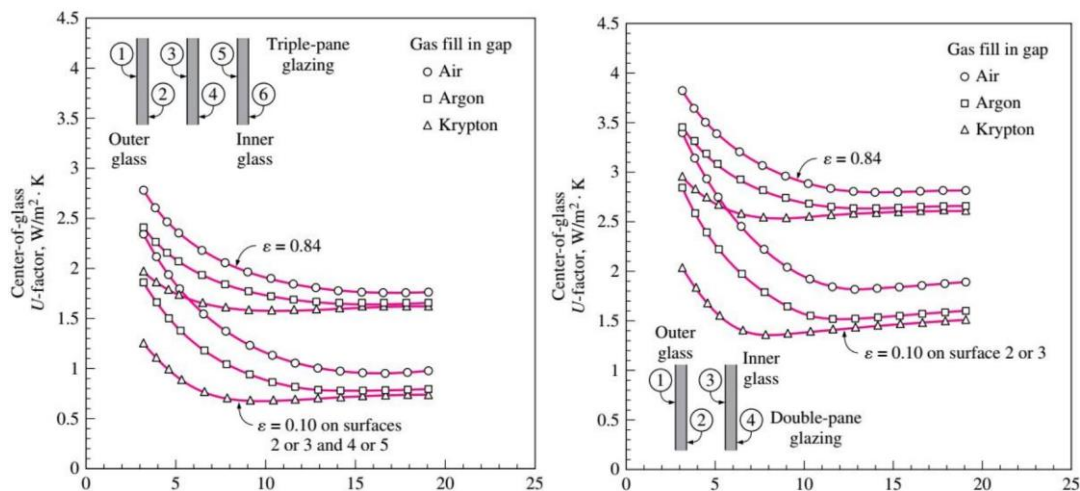
Week8 YU YUE

1. Using the diagrams given in the presentation calculate how much(%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickness to be 13 mm)

Benchmark:

with Double pane glazing ($\epsilon=0.84$) and gap thickness is 13mm filled with air

U value= $2.8\text{W/m}^2\text{K}$



Refer to the diagram:

	benchmark	1	2	3
ϵ	0.84	0.84	0.10	0.84
Pane number	2	2	2	3
Gas	air	krypton	air	air
U-value ($\text{W/m}^2\text{K}$)	2.8	2.6	1.8	1.8
Change (%)	100	93	64	64

$$\dot{Q}_{window1_{east}} = CF_{fenestration1_{east}} * A_{window1_{east}} = 132 * 14.4 = 1900.8W$$

Heating Load:

$$U_{window1_{east}} = 2.84W/m^2 K$$

$$HF_{window1_{east}} = U_{window1_{east}} * \Delta T_{cooling} = 2.84 * 24.8 = 70.44W/m^2$$

$$Q_{window1_{east}} = HF_{window1_{east}} * A_{window1_{east}} = 132 * 14.4 = 1014.2W$$

2Fixed window on West side:

$$A=14.4 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$CF_{window2_{west-heat}} = U_{window2_{west}} (\Delta T_{cooling} - 0.46 * DR)$$

$$= 2.84 * (7.9 - 0.46 * 11.9) = 6.9 \text{ W/m}^2$$

Irradiation part

$$E_D = 559$$

$$E_d = 188$$

West window of a detached house $-FF_s = 0.56$

$$SHGC = 0.54$$

$$PXI_{window2_{west}} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window2_{west-irr}} = PXI * SHGC * IAC * FF_s = 747 * 0.54 * 1 * 0.56 = 225.9$$

$$CF_{fenestration2_{west}} = CF_{window2_{west-heat}} + CF_{window2_{west-irr}} = 6.9 + 225.9 = 232.8W/m^2$$

$$\dot{Q}_{window2_{west}} = CF_{fenestration2_{west}} * A_{window2_{west}} = 232.8 * 14.4 = 3352.32W$$

Heating Load:

$$U_{window2_{west}} = 2.84W/m^2 K$$

$$HF_{window2_{west}} = U_{window2_{west}} * \Delta T_{cooling} = 2.84 * 24.8 = 70.44W/m^2$$

$$Q_{window2_{west}} = HF_{window2_{west}} * A_{window2_{west}} = 89.52 * 14.4 = 1014.2W$$

3Fixed window on south side:

$$A=3.6 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$CF_{window3_{south-heat}} = U_{window3_{south}} (\Delta T_{cooling} - 0.46 * DR)$$

$$= 2.84 * (7.9 - 0.46 * 11.9) = 6.9 \text{ W/m}^2$$

Irradiation part

$$E_D = 348$$

$$E_d = 209$$

south window of a detached house $-FF_s = 0.47$

$$SHGC = 0.54$$

$$PXI_{window3_{south}} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window3_{south-irr}} = PXI * SHGC * IAC * FF_s = 557 * 0.54 * 1 * 0.47 = 141.4$$

$$CF_{fenestration3_{south}} = CF_{window3_{south-heat}} + CF_{window3_{south-irr}} = 6.9 + 141.4 = 148.3 \text{ W/m}^2$$

$$\dot{Q}_{window3_{south}} = CF_{fenestration3_{south}} * A_{window3_{south}} = 148.3 * 3.6 = 533.88 \text{ W}$$

Heating Load:

$$U_{window3_{south}} = 2.84 \text{ W/m}^2 \text{ K}$$

$$HF_{window3_{south}} = U_{window3_{south}} * \Delta T_{cooling} = 2.84 * 24.8 = 70.44 \text{ W/m}^2$$

$$Q_{window3_{south}} = HF_{window3_{south}} * A_{window3_{south}} = 70.44 * 3.6 = 253.6 \text{ W}$$

4 Operable window on south side:

$$A = 3.6 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$CF_{window4_{south-heat}} = U_{window4_{south}} (\Delta T_{cooling} - 0.46 * DR)$$

$$= 2.87 * (7.9 - 0.46 * 11.9) = 6.96 \text{ W/m}^2$$

Irradiation part

$$E_D = 348$$

$$E_d = 209$$

south window of a detached house $-FF_s = 0.47$

$$SHGC = 0.46$$

$$PXI_{window4_{south}} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window4_{south-irr}} = PXI * SHGC * IAC * FF_s = 557 * 0.46 * 1 * 0.47 = 120.4$$

$$CF_{fenestration4_{south}} = CF_{window4_{south-heat}} + CF_{window4_{south-irr}} = 6.9 + 120.4 = 127.3 \text{ W/m}^2$$

$$\dot{Q}_{window4_{south}} = CF_{fenestration4_{south}} * A_{window4_{south}} = 127.3 * 3.6 = 458.28 \text{ W}$$

Heating Load:

$$U_{window4_{south}} = 2.87 \text{ W/m}^2 \text{ K}$$

$$HF_{window4_{south}} = U_{window4_{south}} * \Delta T_{cooling} = 2.87 * 24.8 = 71.17 \text{ W/m}^2$$

$$Q_{window4_{south}} = HF_{window4_{south}} * A_{window4_{south}} = 71.17 * 3.6 = 256.2 \text{ W}$$

$$\begin{aligned}\dot{Q}_{total_windows_cooling_woodframe} &= \dot{Q}_{window1_{east}} + \dot{Q}_{window2_{west}} + \dot{Q}_{window3_{south}} + \dot{Q}_{window4_{south}} \\ &= 1900.8 + 3352.32 + 533.8 + 458.28 = 6245.3W\end{aligned}$$

$$\begin{aligned}Q_{total_windows_heating_woodframe} &= Q_{window1_{east}} + Q_{window2_{west}} + Q_{window3_{south}} + Q_{window4_{south}} \\ &= 1014.2 + 1014.2 + 253.6 + 256.2 = 2538.2W\end{aligned}$$

ALUMINIUM FRAME:

1Fixed window on East side:

$$A=14.4 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$\begin{aligned}CF_{window1_{east-heat}} &= U_{window1_{east}} (\Delta T_{cooling} - 0.46 * DR) \\ &= 3.61 * (7.9 - 0.46 * 11.9) = 8.7W/m^2\end{aligned}$$

Irradiation part

$$E_D = 559$$

$$E_d = 188$$

$$\text{East window of a detached house } -FF_s = 0.31$$

$$SHGC = 0.56$$

$$PXI_{window1_{east}} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window1_{east-irr}} = PXI * SHGC * IAC * FF_s = 747 * 0.56 * 1 * 0.31 = 129.6$$

$$CF_{fenestration1_{east}} = CF_{window1_{east-heat}} + CF_{window1_{east-irr}} = 8.7 + 129.6 = 138.3W/m^2$$

$$\dot{Q}_{window1_{east}} = CF_{fenestration1_{east}} * A_{window1_{east}} = 138.3 * 14.4 = 1991.5W$$

Heating Load:

$$U_{window1_{east}} = 3.61W/m^2 K$$

$$HF_{window1_{east}} = U_{window1_{east}} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52W/m^2$$

$$Q_{window1_{east}} = HF_{window1_{east}} * A_{window1_{east}} = 89.52 * 14.4 = 1289.1W$$

2Fixed window on West side:

$$A=14.4 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$\begin{aligned}CF_{window2_{west-heat}} &= U_{window2_{west}} (\Delta T_{cooling} - 0.46 * DR) \\ &= 3.61 * (7.9 - 0.46 * 11.9) = 8.7 W/m^2\end{aligned}$$

Irradiation part

$$E_D = 559$$

$$E_d = 188$$

West window of a detached house $-FF_s = 0.56$

$$SHGC = 0.56$$

$$PXL_{window2_{west}} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window2_{west-irr}} = PXL * SHGC * IAC * FF_s = 747 * 0.56 * 1 * 0.56 = 234.26$$

$$CF_{fenestration2_{west}} = CF_{window2_{west-heat}} + CF_{window2_{west-irr}} = 8.7 + 234.26 = 242.96 \text{ W/m}^2$$

$$\dot{Q}_{window2_{west}} = CF_{fenestration2_{west}} * A_{window2_{west}} = 242.96 * 14.4 = 3498.6 \text{ W}$$

Heating Load:

$$U_{window2_{west}} = 3.61 \text{ W/m}^2 \text{ K}$$

$$HF_{window2_{west}} = U_{window2_{west}} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52 \text{ W/m}^2$$

$$Q_{window2_{west}} = HF_{window2_{west}} * A_{window2_{west}} = 89.52 * 14.4 = 1289.1 \text{ W}$$

3 Fixed window on south side:

$$A = 3.6 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$CF_{window3_{south-heat}} = U_{window3_{south}} (\Delta T_{cooling} - 0.46 * DR)$$

$$= 3.61 * (7.9 - 0.46 * 11.9) = 8.7 \text{ W/m}^2$$

Irradiation part

$$E_D = 348$$

$$E_d = 209$$

south window of a detached house $-FF_s = 0.47$

$$SHGC = 0.56$$

$$PXL_{window3_{south}} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window3_{south-irr}} = PXL * SHGC * IAC * FF_s = 557 * 0.56 * 1 * 0.47 = 146.6$$

$$CF_{fenestration3_{south}} = CF_{window3_{south-heat}} + CF_{window3_{south-irr}} = 8.7 + 146.6 = 155.3 \text{ W/m}^2$$

$$\dot{Q}_{window3_{south}} = CF_{fenestration3_{south}} * A_{window3_{south}} = 155.3 * 3.6 = 559.08 \text{ W}$$

Heating Load:

$$U_{window3_{south}} = 3.61 \text{ W/m}^2 \text{ K}$$

$$HF_{window3_{south}} = U_{window3_{south}} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52 \text{ W/m}^2$$

$$Q_{window3_{south}} = HF_{window3_{south}} * A_{window3_{south}} = 89.52 * 3.6 = 322.2 \text{ W}$$

4 Operable window on south side:

$$A = 3.6 \text{ m}^2$$

Cooling Load:

Heat transfer part

$$CF_{window4_{south-heat}} = U_{window4_{south}} (\Delta T_{cooling} - 0.46 * DR)$$

$$= 4.62 * (7.9 - 0.46 * 11.9) = 11.2 \text{ W/m}^2$$

Irradiation part

$$E_D = 348$$

$$E_d = 209$$

south window of a detached house $-FF_s = 0.47$

$$SHGC = 0.55$$

$$PXI_{window4_{south}} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window4_{south-irr}} = PXI * SHGC * IAC * FF_s = 557 * 0.55 * 1 * 0.47 = 143.98$$

$$CF_{fenestration4_{south}} = CF_{window4_{south-heat}} + CF_{window4_{south-irr}} = 11.2 + 143.98 \\ = 155.18 \text{ W/m}^2$$

$$\dot{Q}_{window4_{south}} = CF_{fenestration4_{south}} * A_{window4_{south}} = 155.18 * 3.6 = 558.65 \text{ W}$$

Heating Load:

$$U_{window4_{south}} = 4.62 \text{ W/m}^2 \text{ K}$$

$$HF_{window4_{south}} = U_{window4_{south}} * \Delta T_{cooling} = 4.62 * 24.8 = 114.57 \text{ W/m}^2$$

$$Q_{window4_{south}} = HF_{window4_{south}} * A_{window4_{south}} = 114.57 * 3.6 = 412.4 \text{ W}$$

$$\dot{Q}_{total_windows_cooling_aluminiumframe}$$

$$= \dot{Q}_{window1_{east}} + \dot{Q}_{window2_{west}} + \dot{Q}_{window3_{south}} + \dot{Q}_{window4_{south}} \\ = 1991.5 + 3498.6 + 559.08 + 558.65 = 6607.8 \text{ W}$$

$$Q_{total_windows_heating_aluminiumframe}$$

$$= Q_{window1_{east}} + Q_{window2_{west}} + Q_{window3_{south}} + Q_{window4_{south}} \\ = 1289.1 + 1289.1 + 322.2 + 412.4 = 3312.8 \text{ W}$$

Change:

$$\Delta \dot{Q}_{total_windows_cooling}$$

$$= \dot{Q}_{total_windows_cooling_aluminiumframe} - \dot{Q}_{total_windows_cooling_woodframe} \\ = 6607.8 - 6245.3 = 362.5 \text{ W}$$

$$Q_{total_windows_heating}$$

$$= Q_{total_windows_heating_aluminiumframe} - Q_{total_windows_heating_woodframe} \\ = 3312.8 - 2538.2 = 774.6 \text{ W}$$