

1.

The U_{value} of a window:

$$U_{window} = \frac{(U_{centre} * A_{centre}) + (U_{edge} * A_{edge}) + (U_{frame} * A_{frame})}{A_{window}}$$

$$\frac{1}{U_{double\ pane\ window}} = \frac{1}{h_i} + \frac{1}{h_{space}} + \frac{1}{h_o} ; h_{space} = h_{radiation} = h_{conv.\ space}$$

*U and h change according to the type of gas

According to the diagrams given in the presentation:

-Gap thickness is 13mm

-Gas type: Argon

-the U_{value} of the centre of the glass decreases from $2.8 \frac{W}{m^2K}$ to $2.65 \frac{W}{m^2K}$

-5.3%

-Gap thickness is 13mm

-Gas type: Krypton

-the U_{value} of the centre of the glass decreases from $2.8 \frac{W}{m^2K}$ to $2.6 \frac{W}{m^2K}$

-7.1%

*U and h changed when we added an extra pane

-Gap thickness is 13mm

-Gas type: air

-Extra pane

-the U_{value} decreases from $2.8 \frac{W}{m^2K}$ to $1.8 \frac{W}{m^2K}$

-35.7%

-Gap thickness is 13mm

-Gas type: air

-Extra pane +coating film with emissivity of 0.1

-the U_{value} decreases from $2.8 \frac{W}{m^2K}$ to $1.8 \frac{W}{m^2K}$

-35.7%

2.

Case 1. Fixed window on West:

A. Cooling Load:

Frame: Wood

$$Q_{window} = A * CF_{window} ; A = 14.4m^2$$

$$CF_{window \text{ with Heat Trans}} = U_{window}(\delta T_{cooling} - 0.46 DR) - 2.84(7.9 - 0.46 - 11.9) \\ = 6.89 \frac{W}{m^2}$$

$$PXI_{window} = ED + Ed = 559 + 188 = 747 ; SHGC = 0.54 ; IAC = 1 ; FFs = 0.56$$

$$CF_{window \text{ with Radiation}} = PXI * SHGC * IAC * FFs = 747 * 0.54 * 1 * 0.56 \\ = 225.9$$

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 14.4(6.89 + 225.9) \\ = 3352.17 W$$

B. Heating Load:

Frame: Aluminum

$$Q_{window} = A * HF_{window} = A * U_{window \text{ with } \delta T_{heating}} = 14.4(6.89 + 225.9) \\ = 253.56 W$$

$$U_{window} = 3.61 ; HSGC = 0.56$$

$$U_{window} = A * HF_{window} = A_{window}((\delta T_{cooling} - 0.46 DR) = 3.61(7.9 - 0.46 * 11.9)) \\ = 8.76 W/m^2$$

Cooling Load:

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 14.4(8.76 + 234.26) \\ = 3499.49 W$$

Heating Load

$$Q_{window} = A * HF_{window} = A * U_{window} * \delta T_{heating} = 14.4 * 3.61 * 24.8 \\ = 1289.2 W$$

Case 2. Fixed window on South:

A. Cooling Load:

Frame: Wood

$$Q_{window} = A * CF_{window} ; A = 14.4m^2$$

$$CF_{window \text{ with Heat Trans}} = U_{window}(\delta T_{cooling} - 0.46 DR) - 2.84(7.9 - 0.46 - 11.9) \\ = 6.89 \frac{W}{m^2}$$

$$CF_{window \text{ with Radiation}} = PXI * SHGC * IAC * FFs = 557 * 0.56 * 0.47 \\ = 146.60$$

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 3.6(6.89 + 146.60) \\ = 552.56 W$$

B. Heating Load:

Frame: Wood

$$Q_{window} = A * CF_{window} ; A = 14.4m^2$$

$$CF_{window \text{ with Heat Trans}} = U_{window}(\delta T_{cooling} - 0.46 DR) - 2.84(7.9 - 0.46 - 11.9) \\ = 6.89 \frac{W}{m^2}$$

$$PXI_{window} = ED + Ed = 559 + 188 = 747 ; SHGC = 0.54 ; IAC = 1 ; Ffs = 0.56 \\ CF_{window \text{ with Radiation}} = PXI * SHGC * IAC * Ffs = 747 * 0.54 * 1 * 0.56 \\ = 225.9$$

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 14.4(6.89 + 225.9) \\ = 3352.17 W$$

Frame: Aluminum

$$Q_{Window} = A * HF_{window} = A * U_{window \text{ with } \delta T_{heating}} = 3.6 * 2.84 * 24.8 \\ = 253.56 W$$

$$U_{window} = 3.61 ; HSGC = 0.56$$

$$U_{window} = A * HF_{window} = A_{window}((\delta T_{cooling} - 0.46 DR) = 3.61(7.9 - 0.46 * 11.9)) \\ = 8.76 W/m^2$$

Cooling Load:

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 3.6(8.76 + 146.60) \\ = 559.3 W$$

Heating Load:

$$Q_{window} = A * HF_{window} = A * U_{window} * \delta T_{heating} = 3.6 * 3.61 * 24.8 \\ Q_{window} = 322.3 W$$

Case 3. Operable window on South:

Cooling Load for the Operable Window:

$$Q_{window} = A * CF_{window} ; A = 3.6m^2 \\ CF_{window \text{ with Heat Trans}} = U_{window}(\delta T_{cooling} - 0.46 DR) - 2.87(7.9 - 0.46 - 11.9) \\ = 6.96 \frac{W}{m^2}$$

$$CF_{window \text{ with Radiation}} = PXI * SHGC * IAC * Ffs = 557 * 0.46 * 0.47 \\ = 120.42$$

$$Q_{window} = A * CF_{window} = A(CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 3.6(6.96 + 141.36) \\ = 553.97 W$$

Heating Load:

$$Q_{Window} = A * HF_{window} = A * U_{window \text{ with } \delta T_{heating}} = 3.6 * 2.84 * 24.8 \\ = 253.56 \text{ W}$$

Aluminum Frame:

$$U_{window} = 3.61 ; HSGC = 0.56$$

$$CF_{window \text{ with Heat Trans}} = U_{window}(\delta T_{cooling} - 0.46 DR) - 4.62(7.9 - 0.46 - 11.9) \\ = 11.21 \frac{W}{m^2}$$

Cooling Load:

$$Q_{window} = A * CF_{window} = A * (CF_{window \text{ Heat transfer}} + CF_{window \text{ Radiation}}) = 3.6(11.21 + 143.98) \\ = 558.7 \text{ W}$$

Heat Load:

$$Q_{Window} = A * HF_{window} = A * U_{window \text{ with } \delta T_{heating}} = 3.6 * 4.62 * 24.8 \\ = 412.47 \text{ W}$$