

EXAMPLE AND SUMMARY

EXAMPLE 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickness to be 13 mm)

$$U_{\text{window}} = \frac{U_{\text{center}}A_{\text{center}} + U_{\text{edge}}A_{\text{edge}} + U_{\text{fram}}U_{\text{fram}}}{A_{\text{window}}}$$

For double pan window, regardless of the thermal resistances of glass layers,

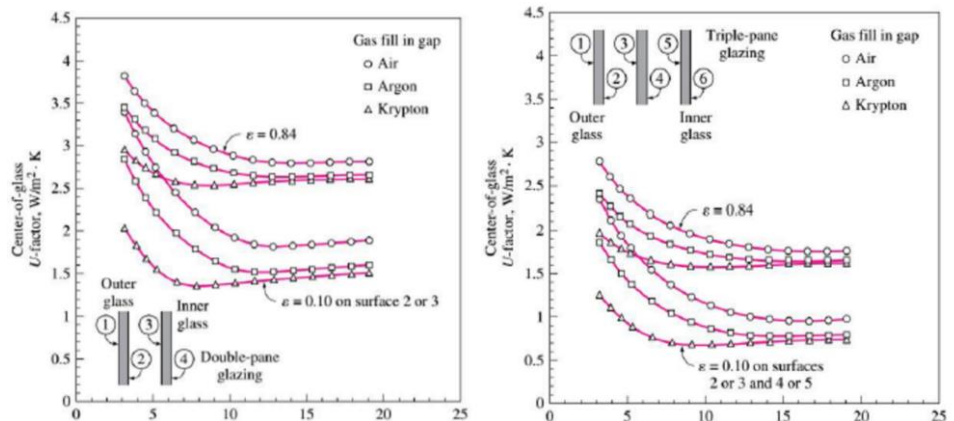
$$\frac{1}{U_{\text{double-pane(center region)}}} \approx \frac{1}{h_i} + \frac{1}{h_{\text{space}}} + \frac{1}{h_o}, \quad h_{\text{space}} = h_{\text{rad,space}} + h_{\text{conv,space}}$$

U_{center} , i.e. the h_{space} changes by changing the gas that fills the gap.

By adding an extra pane, the U value of the centre of the glass decreases from

$$2.8 \frac{\text{W}}{\text{m}^2\text{K}} \text{ to } 1.8 \frac{\text{W}}{\text{m}^2\text{K}}, \text{ which means the u value decreases about 55.6\%.$$

Another way to change the U_{center} , is to coat the glass surfaces with a film that has a low emissivity. From the diagram in the right we can see that: when the gap thickness is 13 mm, and the gas fills the gap is air, by coating the glass surfaces with a film that has the emissivity of 0.1, the U value of the centre of the glass decreases from $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$ to $1.8 \frac{\text{W}}{\text{m}^2\text{K}}$, which means the U value decreases about 55.6%



$$A = 14.4 \text{ m}^2$$

$$CF_{\text{windowwest}} = CF_{\text{windowwest_heattransfer}} + CF_{\text{windowwest_irradiation}}$$

$$CF_{\text{windowwest}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowwest_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 3.61$$

$$CF_{\text{windowwest_heattransfer}} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowwest_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 559 + 188 = 747$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_s = 0.56$$

$$CF_{\text{windowwest_irradiation}} = 747 \times 0.56 \times 1 \times 0.56 = 234.26 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowwest}} = 8.76 + 234.26 = 243.02 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}} = 14.4 \times 243.02 = 3499.47 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}}$$

$$A = 14.4 \text{ m}^2$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}}$$

$$U = 2.84$$

$$HF_{\text{windowwest}} = 2.84 \times 24.8 = 70.43 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 70.43 = 1014.22 \text{ W}$$

Heating Load: Aluminium Frame

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}}$$

$$A = 14.4 \text{ m}^2$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}}$$

$$U = 3.61$$

$$HF_{\text{windowwest}} = 3.61 \times 24.8 = 89.53 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 89.53 = 1289.20 \text{ W}$$

Difference:

$$\text{Cooling Load} = 147.4 \text{ W}$$

$$\text{Heating Load} = 274.98 \text{ W}$$

SOUTH WINDOW (FIXED)

Cooling Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 2.84$$

$$CF_{\text{windowssouth_heattransfer}} = 2.84 (7.9 - (0.46)(11.9)) = 6.89 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.54 \times 1 \times 0.47 = 141.37 \frac{W}{m^2}$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = 6.89 + 141.37 = 148.26 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 148.26 = 533.74 \text{ W}$$

Cooling Load: Aluminium Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 3.61$$

$$CF_{\text{windowssouth_heattransfer}} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{W}{m^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.56 \times 1 \times 0.47 = 146.60 \frac{W}{m^2}$$

$$CF_{\text{windowssouth}} = 8.76 + 146.60 = 155.36 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 155.36 = 559.30 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowssouth}} = U_{\text{windowssouth}} \times \Delta T_{\text{heating}}$$

$$U = 2.84$$

$$HF_{\text{windowssouth}} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}} = 3.6 \times 70.43 = 253.08 \text{ W}$$

Heating Load: Aluminium Frame

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowssouth}} = U_{\text{windowssouth}} \times \Delta T_{\text{heating}}$$

$$U = 3.61$$

$$HF_{\text{windowssouth}} = 3.61 \times 24.8 = 89.53 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}} = 3.6 \times 89.53 = 322.31 \text{ W}$$

Difference:

$$\text{Cooling Load} = 25.56 \text{ W}$$

$$\text{Heating Load} = 69.23 \text{ W}$$

SOUTH WINDOW (OPERABLE)

Cooling Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 2.87$$

$$CF_{\text{windowssouth_heattransfer}} = 2.87 (7.9 - (0.46)(11.9)) = 6.96 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.46$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.46 \times 1 \times 0.47 = 120.42 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = 6.96 + 120.42 = 127.38 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 127.38 = 458.57 \text{ W}$$

Cooling Load: Aluminium Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 4.62$$

$$CF_{\text{windowssouth_heattransfer}} = 4.62 (7.9 - (0.46)(11.9)) = 11.21 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.55$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.55 \times 1 \times 0.47 = 143.98 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth}} = 11.21 + 143.98 = 155.19 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 155.19 = 558.68 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowssouth}} = U_{\text{windowssouth}} \times \Delta T_{\text{heating}}$$

$$U = 2.87$$

$$HF_{\text{windowssouth}} = 2.87 \times 24.8 = 71.18 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}} = 3.6 \times 71.18 = 256.23 \text{ W}$$

Heating Load: Aluminium Frame

$$\dot{q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}}$$

$$A = 3.6 \text{ m}^2$$

$$\text{HF}_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}}$$

$$U = 4.62$$

$$\text{HF}_{\text{windowsouth}} = 4.62 \times 24.8 = 114.58 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}} = 3.6 \times 114.58 = 412.47 \text{ W}$$

Difference:

$$\text{Cooling Load} = 100.11 \text{ W}$$

$$\text{Heating Load} = 156.24 \text{ W}$$