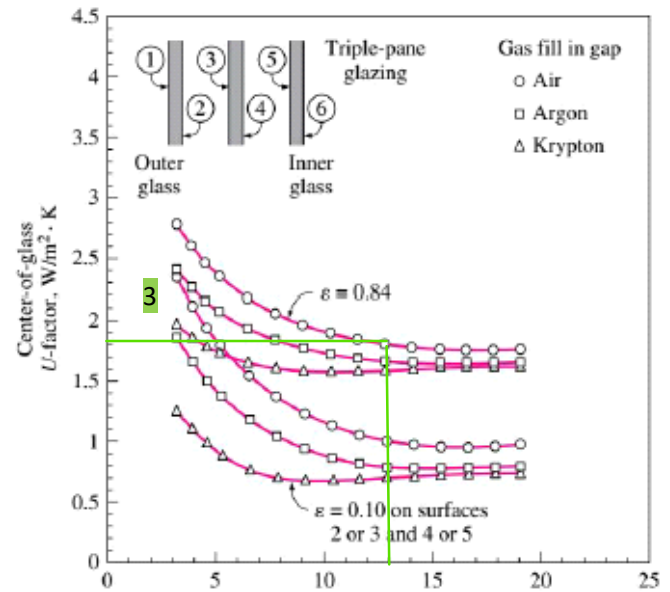
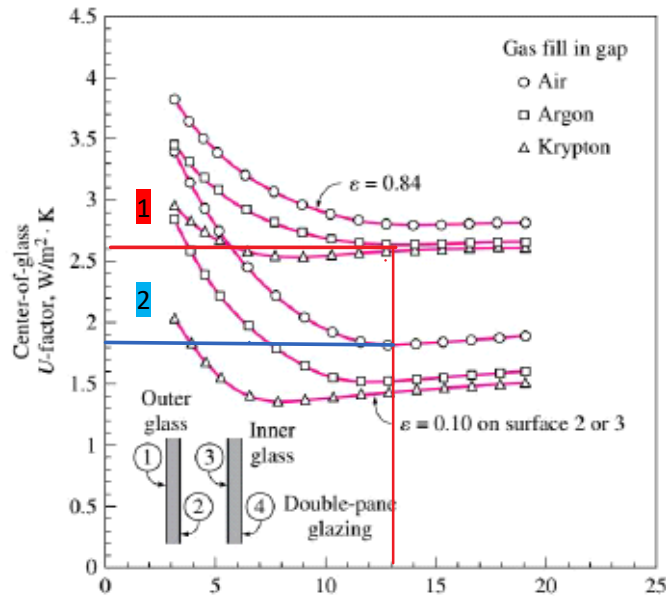


TASK 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? (keep the gap thickness to be 13 mm)



Benchmark cases;

Gap : 13 mm
 Pane number: 2
 Gas type : Air
 ε : 0.84
 U-factor : 2.8 W/m²K
 Result : 100%

Case 1 ;

Gap : 13 mm
 Pane number: 2
 Gas type : Argon
 ε : 0.84
 U-factor : 2.6 W/m²K
 Result : 93%

Case 2 ;

Gap : 13 mm
 Pane number: 2
 Gas type : Air
 ε : 0.10
 U-factor : 1.8 W/m²K
 Result : 64%

Case 3 ;

Gap : 13 mm
 Pane number: 3
 Gas type : Air
 ε : 0.84
 U-factor : 1.8 W/m²K
 Result : 64%

TASK 2

Consider the house that we analysed in the also two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m² on the west, fixed 3.6 m² on the south and an operable 3.6 m² on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium ?

AT PIACENZA :

Lat : 44,92 N,

Long : 9,73 E,

Elev : 138

T_{summer} : 24 °C

T_{winter} : 20 °C

Heating DB 99% : -4,8

Cooling DB 1% : 31,9

$\Delta T_{cooling} = 31,9 - 24 = 7,9$ °C

$\Delta T_{heating} = 20 - (-4,8) = 24,8$ °C

East side of the building 45° Latitude

No internal shading – AIC = 1

DR = 11,9

WOOD FRAME - WINDOW 1 : A_{w1east} = 14,4 m²

Heating

$$HF_{w1east} = U_{w1east} \times \Delta T_{cooling} \\ = 2.84 \times 24.8 = 70.44 \text{ W/m}^2$$

$$Q_{w1east} = HF_{w1east} \times A_{w1east} \\ = 70.44 \times 14.4 = 1014.2 \text{ W}$$

Cooling - Heat transfer part

$$CF_{w1east} = U_{w1east} \times (\Delta T_{cooling} - 0.46 \times DR) \\ = 2,84 (7,9 - 0,46 \times 11,9) = 6,9 \text{ W/m}^2$$

Cooling - Irradiation part

E_D = 559

E_d = 188

East window of a detached house - FFS = 0.31

SHGC = 0.54

$$P_{XI_{w1east}} = E_D + E_d \\ = 559 + 188 = 747$$

$$CF_{w1east} = P_{XI} \times SHGC \times IAC \times FF_s \\ = 747 \times 0.54 \times 1 \times 0.31 = 125.1$$

$$CF_{fenestration1east} = U_{w1east} \times (\Delta T_{cooling} - 0.46 \times DR) + P_{XI} \times SHGC \times IAC \times FF_s \\ = 6.9 + 125.1 = 132 \text{ W/m}^2$$

$$Q'_{w1east} = CF_{fenestration1east} \times A_{w1east} \\ = 132 \times 14.4 = 1900.8 \text{ W}$$

ALUMINIUM FRAME - WINDOW 1 : A_{w1east} = 14,4 m²

Heating

$$HF_{w1east} = U_{w1east} \times \Delta T_{cooling} \\ = 3.61 \times 24.8 = 89.52 \text{ W/m}^2$$

$$Q_{w1east} = HF_{w1east} \times A_{w1east} \\ = 89.52 \times 14.4 = 1289.1 \text{ W}$$

Cooling - Heat transfer part

$$CF_{w1east} = U_{w1east} \times (\Delta T_{cooling} - 0.46 \times DR) \\ = 3.61 (7.9 - 0.46 \times 11.9) = 8.7 \text{ W/m}^2$$

Cooling - Irradiation part

E_D = 559

E_d = 188

East window of a detached house - FFS = 0.31

SHGC = 0.56

$$P_{XI_{w1east}} = E_D + E_d \\ = 559 + 188 = 747$$

$$CF_{w1east} = P_{XI} \times SHGC \times IAC \times FF_s \\ = 747 \times 0.56 \times 1 \times 0.31 = 129.6$$

$$CF_{fenestration1east} = U_{w1east} \times (\Delta T_{cooling} - 0.46 \times DR) + P_{XI} \times SHGC \times IAC \times FF_s \\ = 8.7 + 129.6 = 138.3 \text{ W/m}^2$$

$$Q'_{w1east} = CF_{fenestration1east} \times A_{w1east} \\ = 138.3 \times 14.4 = 1991.5 \text{ W}$$

WOOD FRAME - WINDOW 2 : $A_{W2\text{south}} = 3.6 \text{ m}^2$

Heating

$$\begin{aligned} HF_{W2\text{south}} &= U_{W2\text{south}} \times \Delta T_{\text{cooling}} \\ &= 2.84 \times 24.8 = 70.44 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q_{W2\text{south}} &= HF_{W2\text{south}} \times A_{W2\text{south}} \\ &= 70.44 \times 3.6 = 253.6 \text{ W} \end{aligned}$$

Cooling - Heat transfer part

$$\begin{aligned} CF_{W2\text{south}} &= U_{W2\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR) \\ &= 2.84 (7.9 - 0.46 \times 11.9) = 6.9 \text{ W/m}^2 \end{aligned}$$

Cooling - Irradiation part

$$E_D = 348$$

$$E_d = 209$$

South window of a detached house - FFS = 0.31

$$SHGC = 0.54$$

$$\begin{aligned} PXI_{W2\text{south}} &= E_D + E_d \\ &= 348 + 209 = 557 \end{aligned}$$

$$\begin{aligned} CF_{W2\text{south}} &= PXI \times SHGC \times IAC \times FF_s \\ &= 557 \times 0.54 \times 1 \times 0.47 = 141.4 \end{aligned}$$

$$\begin{aligned} CF_{\text{fenestration1east}} &= U_{W2\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR) + PXI \times SHGC \times IAC \times FF_s \\ &= 6.9 + 141.4 = 148.3 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q'_{W2\text{south}} &= CF_{\text{fenestration1east}} \times A_{W2\text{south}} \\ &= 148.3 \times 3.6 = 533.88 \text{ W} \end{aligned}$$

ALUMINIUM FRAME - WINDOW 2 : $A_{W2\text{south}} = 3.6 \text{ m}^2$

Heating

$$\begin{aligned} HF_{W2\text{south}} &= U_{W2\text{south}} \times \Delta T_{\text{cooling}} \\ &= 3.61 \times 24.8 = 89.52 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q_{W2\text{south}} &= HF_{W2\text{south}} \times A_{W2\text{south}} \\ &= 89.52 \times 3.6 = 322.2 \text{ W} \end{aligned}$$

Cooling - Heat transfer part

$$\begin{aligned} CF_{W2\text{south}} &= U_{W2\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR) \\ &= 3.61 (7.9 - 0.46 \times 11.9) = 8.7 \text{ W/m}^2 \end{aligned}$$

Cooling - Irradiation part

$$E_D = 348$$

$$E_d = 209$$

South window of a detached house - FFS = 0.47

$$SHGC = 0.56$$

$$\begin{aligned} PXI_{W2\text{south}} &= E_D + E_d \\ &= 348 + 209 = 557 \end{aligned}$$

$$\begin{aligned} CF_{W2\text{south}} &= PXI \times SHGC \times IAC \times FF_s \\ &= 557 \times 0.56 \times 1 \times 0.47 = 146.6 \end{aligned}$$

$$\begin{aligned} CF_{\text{fenestration1east}} &= U_{W2\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR) + PXI \times SHGC \times IAC \times FF_s \\ &= 8.7 + 146.6 = 155.3 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q'_{W2\text{south}} &= CF_{\text{fenestration1east}} \times A_{W2\text{south}} \\ &= 155.3 \times 3.6 = 559.08 \text{ W} \end{aligned}$$

WOOD FRAME - WINDOW 3 : $A_{W3\text{south}} = 3.6 \text{ m}^2$

Heating

$$\begin{aligned} HF_{W3\text{south}} &= U_{W3\text{south}} \times \Delta T_{\text{cooling}} \\ &= 2.87 \times 24.8 = 71.17 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q_{W3\text{south}} &= HF_{W3\text{south}} \times A_{W3\text{south}} \\ &= 71.17 \times 3.6 = 256.2 \text{ W} \end{aligned}$$

Cooling - Heat transfer part

$$CF_{W3\text{south}} = U_{W3\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR)$$

ALUMINIUM FRAME - WINDOW 3 : $A_{W3\text{south}} = 3.6 \text{ m}^2$

Heating

$$\begin{aligned} HF_{W3\text{south}} &= U_{W3\text{south}} \times \Delta T_{\text{cooling}} \\ &= 4.62 \times 24.8 = 114.57 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q_{W3\text{south}} &= HF_{W3\text{south}} \times A_{W3\text{south}} \\ &= 114.57 \times 3.6 = 412.4 \text{ W} \end{aligned}$$

Cooling - Heat transfer part

$$CF_{W3\text{south}} = U_{W3\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times DR)$$

$$= 2,87 (7,9 - 0,46 \times 11,9) = 6,96 \text{ W/m}^2$$

Cooling - Irradiation part

$$E_D = 348$$

$$E_d = 209$$

South window of a detached house - FFS = 0.47

$$\text{SHGC} = 0.46$$

$$\begin{aligned} \text{PXi}_{W3\text{south}} &= E_D + E_d \\ &= 348 + 209 = 557 \end{aligned}$$

$$\begin{aligned} \text{CF}_{W3\text{south}} &= \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s \\ &= 557 \times 0.46 \times 1 \times 0.47 = 120.4 \end{aligned}$$

$$\begin{aligned} \text{CF}_{\text{fenestration1east}} &= U_{W3\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times \text{DR}) + \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s \\ &= 6.9 + 120.4 = 127.3 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q'_{W3\text{south}} &= \text{CF}_{\text{fenestration1east}} \times A_{W3\text{south}} \\ &= 127.3 \times 3.6 = 458.28 \text{ W} \end{aligned}$$

$$\begin{aligned} Q'_{\text{Total windows Heating wood frame}} \\ &= 1014.2 + 253.6 + 256.2 = 1524 \text{ W} \end{aligned}$$

$$\begin{aligned} Q'_{\text{Total windows Cooling wood frame}} \\ &= 1900.8 + 533.88 + 458.28 = 2892.96 \text{ W} \end{aligned}$$

$$Q_{\text{Total windows Heating Aluminium frame}} (2023.7 \text{ W}) > Q_{\text{Total windows Heating wood frame}} (1524 \text{ W})$$

$$Q_{\text{Total windows Cooling Aluminium frame}} (3109.2 \text{ W}) > Q_{\text{Total windows Cooling wood frame}} (2892.96 \text{ W})$$

$$= 4.62 (7,9 - 0,46 \times 11,9) = 11.2 \text{ W/m}^2$$

Cooling - Irradiation part

$$E_D = 348$$

$$E_d = 209$$

South window of a detached house - FFS = 0.47

$$\text{SHGC} = 0.55$$

$$\begin{aligned} \text{PXi}_{W3\text{south}} &= E_D + E_d \\ &= 348 + 209 = 557 \end{aligned}$$

$$\begin{aligned} \text{CF}_{W3\text{south}} &= \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s \\ &= 557 \times 0.55 \times 1 \times 0.47 = 143.95 \end{aligned}$$

$$\begin{aligned} \text{CF}_{\text{fenestration1east}} &= U_{W3\text{south}} \times (\Delta T_{\text{cooling}} - 0.46 \times \text{DR}) + \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s \\ &= 11.2 + 143.98 = 155.18 \text{ W/m}^2 \end{aligned}$$

$$\begin{aligned} Q'_{W3\text{south}} &= \text{CF}_{\text{fenestration1east}} \times A_{W3\text{south}} \\ &= 155.18 \times 3.6 = 558.65 \text{ W} \end{aligned}$$

$$\begin{aligned} Q'_{\text{Total windows Heating Aluminium frame}} \\ &= 1289.1 + 1289.1 + 322.2 + 412.4 = 2023.7 \text{ W} \end{aligned}$$

$$\begin{aligned} Q'_{\text{Total windows Cooling Aluminium frame}} \\ &= 1991.5 + 3498.6 + 559.08 + 558.65 = 3109.2 \text{ W} \end{aligned}$$