

Task 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickness to be 13 mm)

$$U_{\text{window}} = \frac{U_{\text{center}}A_{\text{center}} + U_{\text{edge}}A_{\text{edge}} + U_{\text{fram}}U_{\text{fram}}}{A_{\text{window}}}$$

For double pan window, regardless of the thermal resistances of glass layers,

$$\frac{1}{U_{\text{double-pane(center region)}}} \approx \frac{1}{h_i} + \frac{1}{h_{\text{space}}} + \frac{1}{h_o}, \quad h_{\text{space}} = h_{\text{rad,space}} + h_{\text{conv,space}}$$

U_{center} , i.e. the h_{space} changes by changing the gas that fills the gap.

By changing the gas that fills the gap from air to argon, the U-value of the center of the glass decreases from $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$ to $2.65 \frac{\text{W}}{\text{m}^2\text{K}}$, which means the u value decreases about 5.36%.

By changing the gas that fills the gap from air to Krypton, the U-value of the center of the glass decreases from $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$ to $2.6 \frac{\text{W}}{\text{m}^2\text{K}}$, which means the u value decreases about 7.14%.

By adding an extra pane, the u- value of the center of the glass decreases $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$ to $1.8 \frac{\text{W}}{\text{m}^2\text{K}}$, which means the u value decreases about 35.71%.

Another way to change the U_{center} , is to coat the glass surfaces with a film that has a low emissivity.

By coating the glass surfaces with a film that has the emissivity of 0.1, the U value of the center of the glass decreases from $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$ to $1.8 \frac{\text{W}}{\text{m}^2\text{K}}$, which means the U value decreases about 35.71%

ε value	0.84		0.10			0.84			0.10		
# of panes	2	2	2	2	2	3	3	3	3	3	3
Gas	Argon	Krypton	Air	Argon	Krypton	Air	Argon	Krypton	Air	Argon	krypton
U value	2.65	2.6	1.8	1.5	1.4	1.8	1.7	1.6	1	0.8	0.75
% of change	5.36	7.14	35.71	46.42	50	35.71	39.2	42.85	64.28	71.4	73.21

$$A = 14.4 \text{ m}^2$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}}$$

$$\begin{aligned} \text{So, } CF_{\text{windowwest}} &= CF_{\text{windowwest_heattransfer}} + CF_{\text{windowwest_irradiation}} \\ &= U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s \end{aligned}$$

$$\text{Here, } U = 2.84, DR = 11.9, \Delta T_{\text{cooling}} = 7.9, SHGC = 0.54, IAC = 1, FF_s = 0.56$$

$$PXI = E_D - E_d = 559 + 188 = 747$$

$$CF_{\text{windowwest}} = 2.84(7.9 - 0.46 \times 11.9) + 747 \times 0.54 \times 1 \times 0.56 = 232.78 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = 14.4 \times 232.78 = 3352.07 \text{ W}$$

Cooling Load: Aluminum Frame

$$A = 14.4 \text{ m}^2$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}}$$

$$\begin{aligned} \text{So, } CF_{\text{windowwest}} &= CF_{\text{windowwest_heattransfer}} + CF_{\text{windowwest_irradiation}} \\ &= U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s \end{aligned}$$

$$\text{Here, } U = 3.61, DR = 11.9, \Delta T_{\text{cooling}} = 7.9, SHGC = 0.56, IAC = 1, FF_s = 0.56$$

$$PXI = E_D - E_d = 559 + 188 = 747$$

$$CF_{\text{windowwest}} = 3.61(7.9 - 0.46 \times 11.9) + 747 \times 0.56 \times 1 \times 0.56 = 243.02 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = 14.4 \times 243.02 = 3499.47 \text{ W}$$

Heating Load: Wooden Frame

$$A = 14.4 \text{ m}^2$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}}$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}} = 2.84 \times 24.8 = 70.43 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 70.43 = 1014.22 \text{ W}$$

Heating Load: Aluminum Frame

$$A = 14.4 \text{ m}^2$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}}$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}} = 3.61 \times 24.8 = 89.53 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 89.53 = 1289.20 \text{ W}$$

So, The cooling load difference = $3499.47 - 3352.07 = 147.4 \text{ W}$
 The heating load difference = $1289.20 - 1014.22 = 274.98 \text{ W}$

SOUTH WINDOW (FIXED)

Cooling Load: Wooden Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{windowsouth}} = A \times CF_{\text{windowsouth}}$$

So,

$$CF_{\text{windowsouth}} = CF_{\text{windowsouth_heattransfer}} + CF_{\text{windowsouth_irradiation}}$$

$$= U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$\text{Here, } U = 2.84, DR = 11.9, \Delta T_{\text{cooling}} = 7.9, SHGC = 0.54, IAC = 1, FF_s = 0.47$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$CF_{\text{windowsouth}} = 2.84(7.9 - 0.46 \times 11.9) + 557 \times 0.54 \times 1 \times 0.47 = 148.26 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{windowsouth}} = 3.6 \times 148.26 = 533.74 \text{ W}$$

Cooling Load: Aluminum Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{windowsouth}} = A \times CF_{\text{windowsouth}}$$

So,

$$CF_{\text{windowsouth}} = CF_{\text{windowsouth_heattransfer}} + CF_{\text{windowsouth_irradiation}}$$

$$= U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$\text{Here, } U = 3.61, DR = 11.9, \Delta T_{\text{cooling}} = 7.9, SHGC = 0.56, IAC = 1, FF_s = 0.47$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$CF_{\text{windowsouth}} = 3.61(7.9 - 0.46 \times 11.9) + 557 \times 0.56 \times 1 \times 0.47 = 155.36 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{windowsouth}} = 3.6 \times 155.36 = 559.30 \text{ W}$$

Heating Load: Wooden Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}}$$

$$HF_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}} = 2.84 \times 24.8 = 70.43 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}} = 3.6 \times 70.43 = 253.08 \text{ W}$$

Heating Load: Aluminum Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{window south}} = A \times \text{HF}_{\text{window south}}$$

$$\text{HF}_{\text{window south}} = U_{\text{window south}} \times \Delta T_{\text{heating}} = 3.61 \times 24.8 = 89.53 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{window south}} = A \times \text{HF}_{\text{window south}} = 3.6 \times 89.53 = 322.31 \text{ W}$$

So, The cooling load difference = $559.30 - 533.74 = 25.56 \text{ W}$

The heating load difference = $322.31 - 253.08 = 69.23 \text{ W}$

SOUTH WINDOW (OPERABLE)

Cooling Load: Wooden Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{window south}} = A \times \text{CF}_{\text{window south}}$$

So,

$$\text{CF}_{\text{window south}} = \text{CF}_{\text{window south_heattransfer}} + \text{CF}_{\text{window south_irradiation}}$$

$$= U(\Delta T - 0.46\text{DR}) + \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s$$

Here, $U = 2.87$, $\text{DR} = 11.9$, $\Delta T_{\text{cooling}} = 7.9$, $\text{SHGC} = 0.46$, $\text{IAC} = 1$, $\text{FF}_s = 0.47$

$$\text{PXi} = E_D - E_d = 348 + 209 = 557$$

$$\text{CF}_{\text{window west}} = 2.87(7.9 - 0.46 \times 11.9) + 557 \times 0.46 \times 1 \times 0.47 = 127.38 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{window west}} = 3.6 \times 127.38 = 458.57 \text{ W}$$

Cooling Load: Aluminum Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{window south}} = A \times \text{CF}_{\text{window south}}$$

So,

$$\text{CF}_{\text{window south}} = \text{CF}_{\text{window south_heattransfer}} + \text{CF}_{\text{window south_irradiation}}$$

$$= U(\Delta T - 0.46\text{DR}) + \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FF}_s$$

Here, $U = 4.62$, $\text{DR} = 11.9$, $\Delta T_{\text{cooling}} = 7.9$, $\text{SHGC} = 0.55$, $\text{IAC} = 1$, $\text{FF}_s = 0.47$

$$\text{PXi} = E_D - E_d = 348 + 209 = 557$$

$$\text{CF}_{\text{window west}} = 4.62(7.9 - 0.46 \times 11.9) + 557 \times 0.55 \times 1 \times 0.47 = 155.19 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{window west}} = 3.6 \times 155.19 = 558.68 \text{ W}$$

Heating Load: Wooden Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}}$$

$$\text{HF}_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}} = 2.87 \times 24.8 = 71.18 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}} = 3.6 \times 71.18 = 256.23 \text{ W}$$

Heating Load: Aluminum Frame

$$A = 3.6 \text{ m}^2$$

$$\dot{Q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}}$$

$$\text{HF}_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}} = 4.62 \times 24.8 = 114.58 \frac{\text{W}}{\text{m}^2}$$

$$\dot{Q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}} = 3.6 \times 114.58 = 412.47 \text{ W}$$

So, The cooling load difference = $558.68 - 458.57 = 100.11 \text{ W}$

The heating load difference = $412.47 - 256.23 = 156.243 \text{ W}$