

Task 1** Considering the same example you solved in the previous assignment (radiative heat transfer between two parallel plates), how many shields with epsilon = 0.1 should you add in order to have the new heat transfer rate to be 1% of the case without shields ?

Question:

Find the net heat exchange between the surface 1 and 2 where $A_1 = 1.5 \text{ m}^2$, $F_{12} = 0.01$, $T_1 = 800 \text{ K}$, $= 500 \text{ K}$, $\epsilon_1 = 0.2$, $\epsilon_2 = 0.7$, $\sigma = 5.67 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}$, $q = 1035.81 \frac{\text{W}}{\text{m}^2}$

Solve the last example in the class (radiative heat exchange between two parallel plates) awhile considering the two emissivities to be 0.1, what can you conclude from the result?

Solution:

$$\frac{3625.37}{100} = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + \left(\frac{1}{\epsilon_{3,1}} + \frac{1}{\epsilon_{3,2}} - 1\right)(N \text{ of Shields})}$$

$$\frac{\sigma(T_1^4 - T_2^4)}{36,25} = \left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + \left(\frac{1}{\epsilon_{3,1}} + \frac{1}{\epsilon_{3,2}} - 1\right)(N)$$

$$\begin{aligned} N &= \left(\frac{\sigma(T_1^4 - T_2^4)}{36,25} - \left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right)\right) / \left(\frac{1}{\epsilon_{3,1}} + \frac{1}{\epsilon_{3,2}} - 1\right) = \\ &= \left(\frac{\sigma(800^4 - 500^4)}{36,25} - \left(\frac{1}{0,2} + \frac{1}{0,7} - 1\right)\right) / \left(\frac{1}{0,1} + \frac{1}{0,1} - 1\right) = \\ &= \left(\frac{5,67 \cdot 10^{-8}(800^4 - 500^4)}{36,25} - \left(\frac{1}{0,2} + \frac{1}{0,7} - 1\right)\right) / \left(\frac{1}{0,1} + \frac{1}{0,1} - 1\right) = 28 \text{ shields} \end{aligned}$$

$$\begin{aligned} q &= \frac{\sigma(800^4 - 500^4)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + \left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right)X(N)} \left(\frac{1}{0,1} + \frac{1}{0,1} - 1\right) = \\ &= \frac{\sigma(800^4 - 500^4)}{\left(\frac{1}{0,2} + \frac{1}{0,7} - 1\right) + \left(\frac{1}{0,1} + \frac{1}{0,1} - 1\right)X(28)} = 10,36 \frac{\text{W}}{\text{m}^2} \end{aligned}$$

1% of 1085,81

$$q_{N\text{shields}} = 1/(N+1) \Rightarrow N = (100\%/1\%) - 1 = 99$$

$$Q_{99 \text{ shields}} = \frac{\sigma(T_1^4 - T_2^4)}{(N+1) + \left(\frac{1}{\epsilon_{\square}} + \frac{1}{\epsilon_{\square}} - 1\right)} = 10,36 \text{ W/m}^2$$

** Task 2** You should create a pdf file with screenshots of all of the steps we went through (clearly from your own file) and explain briefly the reason behind the use of each step (in your own words!)



