

## Task 1:

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? ( keep the gap thickness to be 13 mm)

Answer

To calculate the U – value of a window,

$$U_{\text{window}} = \frac{U_{\text{center}}A_{\text{center}} + U_{\text{edge}}A_{\text{edge}} + U_{\text{fram}}A_{\text{fram}}}{A_{\text{window}}}$$

If it is a double – pane window, disregard the thermal resistances of glass layers,

$$\frac{1}{U_{\text{double-pane (center region)}}} \approx \frac{1}{h_i} + \frac{1}{h_{\text{space}}} + \frac{1}{h_o}, \quad h_{\text{space}} = h_{\text{rad, space}} + h_{\text{conv, space}}$$

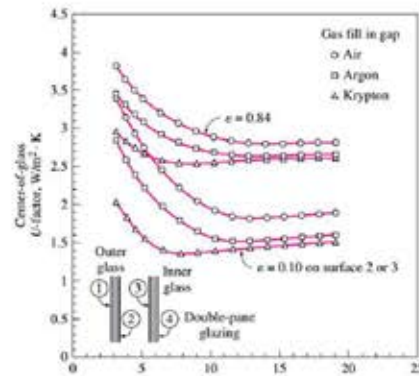
The  $U_{\text{center}}$ , i. e. the  $h_{\text{space}}$  changes by changing the gas that fills the gap.

From the diagram in the right side, we can see that:

When the gap thickness is 13 mm,

By changing the gas that fills the gap from air to argon, the U-value of the center of the glass decreases from  $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$  to  $2.65 \frac{\text{W}}{\text{m}^2\text{K}}$ , which means the U-value decreases about 5.36%;

By changing the gas that fills the gap from air to krypton, the U-value of the center of the glass decrease from  $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$  to  $2.6 \frac{\text{W}}{\text{m}^2\text{K}}$ , which means the U-value decreases about 7.14%.



The  $U_{\text{center}}$ , i. e. the  $h_{\text{space}}$  changes by adding an extra pane.

From the diagram in the right side, we can see that:

When the gap thickness is 13 mm, and the gas that fills the gap is air,

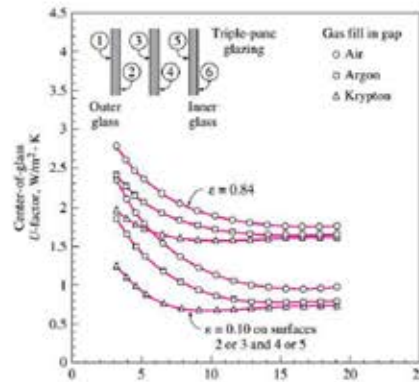
By adding an extra pane, the U-value of the center of the glass decreases from  $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$  to  $1.8 \frac{\text{W}}{\text{m}^2\text{K}}$ , which means the U-value decreases about 35.71%.

Another way to change the  $U_{\text{center}}$ , is to coat the glass surfaces with a film that has a low emissivity.

From the diagram in the right we can see that:

When the gap thickness is 13 mm, and the gas fills the gap is air,

By coating the glass surfaces with a film that has the emissivity of 0.1, the U-value of the center of the glass decreases from  $2.8 \frac{\text{W}}{\text{m}^2\text{K}}$  to  $1.8 \frac{\text{W}}{\text{m}^2\text{K}}$ , which means the U-value decreases about 35.71%.



## Task 2:

Consider the house that we analysed in the last two examples, calculate the heating and cooling load of the other windows which are fixed  $14.4 \text{ m}^2$  on the west, fixed  $3.6 \text{ m}^2$  on the south and an operable  $3.6 \text{ m}^2$  on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium?

(The questions exempt gratic).

- The net area of walls (excluding doors and windows) of a building located in Piacenza is  $105.8 \text{ m}^2$ , the calculated U value is  $0.438 \text{ W/m}^2\text{K}$  for the winter and  $0.435 \text{ W/m}^2\text{K}$  for the summer. Find the corresponding heating and cooling load.
- A fixed heat absorbing double layer glass (with a wooden frame) window at the east side of a building located in Piacenza has a surface of  $14.4 \text{ m}^2$ . In case there are no internal and external shading factors. Calculate the heating and cooling load of the corresponding to that window.)

PIACENZA, Italy														Version: 100040
Lat: 44.82N	Long: 9.72E	Elev: 126	Dist: 89.88	Time Zone: 1.00 (EUM)	Period: 88-10	Index: 99999								
General Heating and Cooling Load Data (continued)														
Calendar Month	Heating DB	Heating DB: 10°C and 18°C						Cooling DB: 24°C and 26°C				MOISTURE: 10°C and 18°C		
		DB	WB	DP	WB	MACDB	WB	MACDB	WB	MACDB	WB	MACDB	WB	MACDB
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	
1	-6.2	-4.8	-11.6	1.4	3.1	-8.9	1.8	1.8	8.6	5.6	7.7	6.2	2.1	
General Cooling Load Data														
Calendar Month	Cooling DB	Cooling DB: 24°C and 26°C				Cooling DB: 28°C and 30°C				MOISTURE: 24°C and 26°C				
		DB	WB	DP	WB	DB	WB	DP	WB	WB	MACDB	WB	MACDB	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	
8	11.8	22.5	22.7	21.9	22.4	20.3	21.8	24.6	20.2	23.7	28.2	22.8	28.3	

Answer:

First of all, define the cooling design temperature  $T_{\text{cooling}} = 24^\circ\text{C}$ , and heating design temperature  $T_{\text{heating}} = 20^\circ\text{C}$ , thus

$$\Delta T_{\text{cooling}} = 31.9^\circ\text{C} - 24^\circ\text{C} = 7.9^\circ\text{C} = 7.9\text{K}$$

$$\Delta T_{\text{heating}} = 20^\circ\text{C} - (-4.8^\circ\text{C}) = 24.8^\circ\text{C} = 24.8\text{K}$$

$$\text{From the table above, } DR = 11.9^\circ\text{C} = 11.9\text{K}$$

Calculating the cooling load of the fixed window on the west:

$$Q_{\text{window,cool}} = A \times CF_{\text{window,cool}}$$

$$A = 14.4 \text{ m}^2$$

$$CF_{\text{window,cool}} (\text{West Transf or Part}) = U_{\text{window,cool}} (\Delta T_{\text{cooling}} - 0.46 DR)$$

The window has a fixed heat absorbing double layer glass with a wooden frame,

$$U_{\text{window,cool}} = 2.04 \frac{\text{W}}{\text{m}^2\text{K}}$$

$$i. e., CF_{\text{window,cool}} (\text{West Transf or Part}) = 2.04 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9\text{K} - 0.46 \times 11.9\text{K}) = 6.09 \frac{\text{W}}{\text{m}^2}$$

$$PX_{\text{window,cool}} = E_D + E_g = 559 + 180 = 747$$

$$SHGC = 0.54$$

No internal shading, so IAC = 1

Table 13: Peak Heat Losses, W/m²													
Exposure	1	2	3	4	5	6	7	8	9	10	11	12	13
North	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
East	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
South	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
West	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
North	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
East	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
South	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
West	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
North	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
East	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
South	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
West	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
North	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
East	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
South	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
West	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0



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$$FF_s = 0.56$$

$$CF_{\text{window west (Irradiation Part)}} = PXI \times SHGC \times IAC \times FF_s$$

$$q_{\text{window west}} = A \times CF_{\text{window west}} = A \times (CF_{\text{window west (Heat Transfer Part)}} + CF_{\text{window west (Irradiation Part)}}) \\ \approx 14.4 \text{ m}^2 \times (6.89 + 747 \times 0.54 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} \approx 3352.07 \text{ W}$$

**Calculating the heating load of the fixed window on the west:**

$$q_{\text{window west}} = A \times HF_{\text{window west}} = A \times U_{\text{window west}} \Delta T_{\text{heating}} \\ = 14.4 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 1014.22 \text{ W}$$

**When the frame were to be aluminium,**  $U_{\text{window west}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}}, HSGC = 0.56$

$$CF'_{\text{window west (Heat Transfer Part)}} = U'_{\text{window west}} (\Delta T_{\text{cooling}} - 0.46 DR) \\ = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 8.76 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{window west}} = A \times CF'_{\text{window west}} \\ = A \times (CF'_{\text{window west (Heat Transfer Part)}} + CF'_{\text{window west (Irradiation Part)}}) \\ \approx 14.4 \text{ m}^2 \times (8.76 + 747 \times 0.56 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} \approx 3499.48 \text{ W}$$

$$\text{Heating load } q'_{\text{window west}} = A \times HF'_{\text{window west}} = A \times U'_{\text{window west}} \Delta T_{\text{heating}} \\ = 14.4 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 1289.20 \text{ W}$$

**Calculating the cooling load of the fixed window on the south:**

$$q_{\text{window south}} = A \times CF_{\text{window south}}$$

$$A = 3.6 \text{ m}^2,$$

$$CF_{\text{window south (Heat Transfer Part)}} = U_{\text{window south}} (\Delta T_{\text{cooling}} - 0.46 DR)$$

∴ The window has a fixed heat absorbing double layer glass with a wooden frame,

$$\therefore U_{\text{window south}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{i.e., } CF_{\text{window south (Heat Transfer Part)}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 6.89 \frac{\text{W}}{\text{m}^2}$$

$$PXI_{\text{window south}} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

No internal shading, so IAC = 1

$$FF_s = 0.47$$

$$CF_{\text{window south (Irradiation Part)}} = PXI \times SHGC \times IAC \times FF_s$$

$$q_{\text{window south}} = A \times CF_{\text{window south}} = A \times (CF_{\text{window south (Heat Transfer Part)}} + CF_{\text{window south (Irradiation Part)}}) \\ \approx 3.6 \text{ m}^2 \times (6.89 + 557 \times 0.54 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} \approx 553.72 \text{ W}$$

**Calculating the heating load of the fixed window on the south:**

$$q_{\text{window south}} = A \times HF_{\text{window south}} = A \times U_{\text{window south}} \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 253.56 \text{ W}$$

**When the frame were to be aluminium,**  $U_{\text{window south}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}}, HSGC = 0.56$

$$CF'_{\text{window south (Heat Transfer Part)}} = U'_{\text{window south}} (\Delta T_{\text{cooling}} - 0.46 DR) \\ = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 8.76 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{window south}} = A \times CF'_{\text{window south}} \\ = A \times (CF'_{\text{window south (Heat Transfer Part)}} + CF'_{\text{window south (Irradiation Part)}}) \\ = 3.6 \text{ m}^2 \times (8.76 + 557 \times 0.56 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} \approx 559.30 \text{ W}$$

$$\text{Heating load } q'_{\text{window south}} = A \times HF'_{\text{window south}} = A \times U'_{\text{window south}} \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 322.30 \text{ W}$$

**Calculating the cooling load of the operable window on the south:**

$$q_{\text{window south}} = A \times CF_{\text{window south}}$$

$$A = 3.6 \text{ m}^2,$$

$$CF_{\text{window south (Heat Transfer Part)}} = U_{\text{window south}} (\Delta T_{\text{cooling}} - 0.46 DR)$$

∴ The window has an operable heat absorbing double layer glass with a wooden frame,

$$\therefore U_{\text{window south}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{i.e., } CF_{\text{window south (Heat Transfer Part)}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 6.96 \frac{\text{W}}{\text{m}^2}$$

$$PXI_{\text{window south}} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.46$$

No internal shading, so IAC = 1

$$FF_s = 0.47$$

$$CF_{\text{window south (Irradiation Part)}} = PXI \times SHGC \times IAC \times FF_s$$

$$q_{\text{window south}} = A \times CF_{\text{window south}} = A \times (CF_{\text{window south (Heat Transfer Part)}} + CF_{\text{window south (Irradiation Part)}}) \\ \approx 3.6 \text{ m}^2 \times (6.96 + 557 \times 0.46 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} \approx 458.58 \text{ W}$$

**Calculating the heating load of the operable window on the south:**

$$q_{\text{window south}} = A \times HF_{\text{window south}} = A \times U_{\text{window south}} \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 2.87 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 256.23 \text{ W}$$

**When the frame were to be aluminium,**  $U_{\text{window south}} = 4.62 \frac{\text{W}}{\text{m}^2 \text{K}}, HSGC = 0.55$

$$CF'_{\text{window south (Heat Transfer Part)}} = U'_{\text{window south}} (\Delta T_{\text{cooling}} - 0.46 DR)$$

$$= 4.62 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 11.21 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{window south}} = A \times CF'_{\text{window south}} \\ = A \times (CF'_{\text{window south (Heat Transfer Part)}} + CF'_{\text{window south (Irradiation Part)}}) \\ \approx 3.6 \text{ m}^2 \times (11.21 + 557 \times 0.55 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} \approx 558.70 \text{ W}$$

$$\text{Heating load } q'_{\text{window south}} = A \times HF'_{\text{window south}} = A \times U'_{\text{window south}} \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 4.62 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 412.47 \text{ W}$$



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