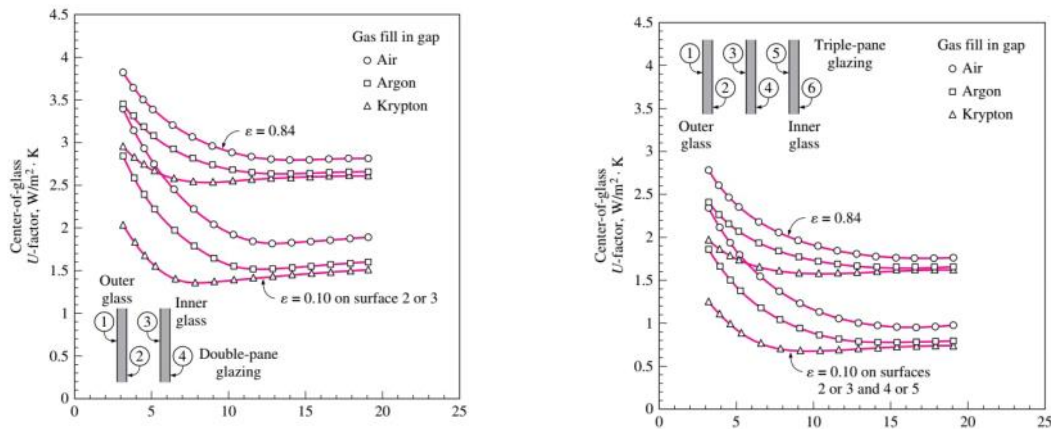


1 Using the diagrams given in the presentation about heat transfer through windows calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating (keep the gap thickness to be 13 mm).



| | BENCHMARK CASE | CASE 1 | CASE 2 | CASE 3 |
|-----------------|----------------|------------|------------|------------|
| GAP | 13 mm | 13 mm | 13 mm | 13 mm |
| ε | 0.84 | 0.84 | 0.84 | 0.10 |
| N PANE | 2 | 2 | 3 | 2 |
| GAS | air | krypton | air | air |
| U-factor | 2.8 W/m² K | 2.6 W/m² K | 1.8 W/m² K | 1.8 W/m² K |
| % | 100% | 93% | 64% | 64% |

CASE 1: the thermal performance of the window increases by 7%.

CASE 2: the thermal performance of the window increases by 36%.

CASE 3: the thermal performance of the window increases by 36%.

2 Consider the house that we analysed in the alst two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m² on the west, fixed 3.6 m² on the south and an operable 3.6 m² on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium?

| | | | | | | |
|-----------------|------|-------------|------------------------|------------------|------------|-------------------|
| WINDOW 1 | West | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Wood Frame | 14.4 surface area |
|-----------------|------|-------------|------------------------|------------------|------------|-------------------|

FENESTRATION HEATING

$$U_{window_{West}} = 2.84 \frac{W}{m^2 K}$$

$$\Delta T_{heating} = 20 - (-4.8) = 24.8 \text{ } ^\circ C$$

$$HF_{window_{West}} = U_{window_{West}} \times \Delta T_{heating} = 2.84 * 24.8 = 70.43 \frac{W}{m^2 K}$$

$$\dot{Q}_{window_{West} Heating} = HF_{window_{West}} \times A_{window_{West}} = 70.43 * 14.4 = 1014.22 \text{ W}$$

FENESTRATION COOLING

$$CF_{fen} = U (\Delta T - 0.46 DR) + PXI \times SHGC \times IAC \times FF_S$$

$$CF_{windowWestHeatTrasnferPart} = U_{windowWest} (\Delta T_{cooling} - 0.46 DR) = 2.84 (7.9 - 0.46 * 11.9) = 6.9 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 31.9 - 24 = 7.9 ^\circ C$$

$$DR = 11.9 ^\circ C$$

$$PXI_{windowWest} = E_D + E_d = 559 + 188 = 747 \quad (\text{no external shading})$$

$$SHGC = 0.54$$

$$IAC = 1 \quad (\text{no internal shading})$$

$$FF_S = 0.56 \quad (\text{Western window of a detached house})$$

$$CF_{windowWestIrradiationPart} = PXI \times SHGC \times IAC \times FF_S = 747 * 0.54 * 1 * 0.56 = 225.9$$

$$CF_{windowWest} = CF_{windowWestHeatTrasnferPart} + CF_{windowWestIrradiationPart} = 6.9 + 225.9 = 232.8 \frac{W}{m^2}$$

$$\dot{Q}_{windowWestCooling} = CF_{windowWest} \times A_{windowWest} = 232.8 * 14.4 = \mathbf{3352.32 W}$$

| | | | | | | |
|-----------------|------|-------------|------------------------|------------------|------------------|-------------------|
| WINDOW 1 | West | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Alluminium Frame | 14.4 surface area |
|-----------------|------|-------------|------------------------|------------------|------------------|-------------------|

FENESTRATION HEATING

$$U_{windowWest} = 3.61 \frac{W}{m^2 K}$$

$$\Delta T_{heating} = 24.8 ^\circ C$$

$$HF_{windowWest} = U_{windowWest} \times \Delta T_{heating} = 3.61 * 24.8 = 89.53 \frac{W}{m^2 K}$$

$$\dot{Q}_{windowWestHeating} = HF_{windowWest} \times A_{windowWest} = 89.53 * 14.4 = \mathbf{1289.23 W}$$

FENESTRATION COOLING

$$CF_{windowWestHeatTrasnferPart} = U_{windowWest} (\Delta T_{cooling} - 0.46 DR) = 3.61 (7.9 - 0.46 * 11.9) = 8.75 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 ^\circ C$$

$$DR = 11.9 ^\circ C$$

$$PXI_{windowWest} = 747$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_S = 0.56$$

$$CF_{windowWestIrradiationPart} = PXI \times SHGC \times IAC \times FF_S = 747 * 0.56 * 1 * 0.56 = 234.25$$

$$CF_{windowWest} = CF_{windowWestHeatTrasnferPart} + CF_{windowWestIrradiationPart} = 8.75 + 234.25 = 243 \frac{W}{m^2}$$

$$\dot{Q}_{windowWestCooling} = CF_{windowWest} \times A_{windowWest} = 243 * 14.4 = \mathbf{3499.2 W}$$

| | | | | | | |
|-----------------|-------|-------------|------------------------|------------------|------------|------------------|
| WINDOW 2 | South | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Wood Frame | 3.6 surface area |
|-----------------|-------|-------------|------------------------|------------------|------------|------------------|

FENESTRATION HEATING

$$U_{windowSouth} = 2.84 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 24.8 \text{ }^{\circ}C$$

$$HF_{windowSouth} = U_{windowSouth} \times \Delta T_{heating} = 2.84 * 24.8 = 70.43 \frac{W}{m^2K}$$

$$\dot{Q}_{windowSouthHeating} = HF_{windowSouth} \times A_{windowSouth} = 70.43 * 3.6 = \mathbf{253.55 \text{ W}}$$

FENESTRATION COOLING

$$CF_{windowSouthHeatTrasnferPart} = U_{windowSouth} (\Delta T_{cooling} - 0.46 DR) = 2.84 (7.9 - 0.46 * 11.9) = 6.9 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 \text{ }^{\circ}C$$

$$DR = 11.9 \text{ }^{\circ}C$$

$$PXI_{windowSouth} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FFs = 0.47$$

$$CF_{windowSouthIrradiationPart} = PXI \times SHGC \times IAC \times FFs = 557 * 0.54 * 1 * 0.47 = 141.37$$

$$CF_{windowSouth} = CF_{windowSouthHeatTrasnferPart} + CF_{windowSouthIrradiationPart} = 6.9 + 141.37 = 148.27 \frac{W}{m^2}$$

$$\dot{Q}_{windowSouthCooling} = CF_{windowSouth} \times A_{windowSouth} = 148.27 * 3.6 = \mathbf{533.77 \text{ W}}$$

| | | | | | | |
|-----------------|-------|-------------|------------------------|------------------|------------------|------------------|
| WINDOW 2 | South | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Alluminium Frame | 3.6 surface area |
|-----------------|-------|-------------|------------------------|------------------|------------------|------------------|

FENESTRATION HEATING

$$U_{windowSouth} = 3.61 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 24.8 \text{ }^{\circ}C$$

$$HF_{windowSouth} = U_{windowSouth} \times \Delta T_{heating} = 3.61 * 24.8 = 89.53 \frac{W}{m^2K}$$

$$\dot{Q}_{windowSouthHeating} = HF_{windowSouth} \times A_{windowSouth} = 89.53 * 3.6 = \mathbf{322.31 \text{ W}}$$

FENESTRATION COOLING

$$CF_{windowSouthHeatTrasnferPart} = U_{windowSouth} (\Delta T_{cooling} - 0.46 DR) = 3.61 (7.9 - 0.46 * 11.9) = 8.75 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 \text{ }^{\circ}C$$

$$DR = 11.9 \text{ }^{\circ}C$$

$$PXI_{windowSouth} = 557$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FFs = 0.47$$

$$CF_{windowSouthIrradiationPart} = PXI \times SHGC \times IAC \times FFs = 557 * 0.56 * 1 * 0.47 = 146.6$$

$$CF_{windowSouth} = CF_{windowSouthHeatTrasnferPart} + CF_{windowSouthIrradiationPart} = 8.75 + 146.6 = 155.35 \frac{W}{m^2}$$

$$\dot{Q}_{windowSouthCooling} = CF_{windowSouth} \times A_{windowSouth} = 155.35 * 3.6 = \mathbf{559.26 W}$$

| | | | | | | |
|-----------------|-------|----------------|------------------------|------------------|------------|------------------|
| WINDOW 3 | South | Operable Frame | Heat-absorbing glazing | 2 glazing layers | Wood Frame | 3.6 surface area |
|-----------------|-------|----------------|------------------------|------------------|------------|------------------|

FENESTRATION HEATING

$$U_{windowSouth} = 2.87 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 24.8 ^\circ C$$

$$HF_{windowSouth} = U_{windowSouth} \times \Delta T_{heating} = 2.87 * 24.8 = 71.18 \frac{W}{m^2K}$$

$$\dot{Q}_{windowSouthHeating} = HF_{windowSouth} \times A_{windowSouth} = 71.18 * 3.6 = \mathbf{256.25 W}$$

FENESTRATION COOLING

$$CF_{windowSouthHeatTrasnferPart} = U_{windowSouth} (\Delta T_{cooling} - 0.46 DR) = 2.87 (7.9 - 0.46 * 11.9) = 6.96 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 ^\circ C$$

$$DR = 11.9 ^\circ C$$

$$PXI_{windowSouth} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.46$$

$$IAC = 1$$

$$FFs = 0.47$$

$$CF_{windowSouthIrradiationPart} = PXI \times SHGC \times IAC \times FFs = 557 * 0.46 * 1 * 0.47 = 120.42$$

$$CF_{windowSouth} = CF_{windowSouthHeatTrasnferPart} + CF_{windowSouthIrradiationPart} = 6.96 + 120.42 = 127.38 \frac{W}{m^2}$$

$$\dot{Q}_{windowSouthCooling} = CF_{windowSouth} \times A_{windowSouth} = 127.38 * 3.6 = \mathbf{458.57 W}$$

| | | | | | | |
|-----------------|-------|----------------|------------------------|------------------|------------------|------------------|
| WINDOW 3 | South | Operable Frame | Heat-absorbing glazing | 2 glazing layers | Alluminium Frame | 3.6 surface area |
|-----------------|-------|----------------|------------------------|------------------|------------------|------------------|

FENESTRATION HEATING

$$U_{windowSouth} = 4.62 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 24.8 ^\circ C$$

$$HF_{windowSouth} = U_{windowSouth} \times \Delta T_{heating} = 4.62 * 24.8 = 144.58 \frac{W}{m^2K}$$

$$\dot{Q}_{windowSouthHeating} = HF_{windowSouth} \times A_{windowSouth} = 144.58 * 3.6 = \mathbf{412.49 \text{ W}}$$

FENESTRATION COOLING

$$CF_{windowSouthHeatTrasnferPart} = U_{windowSouth} (\Delta T_{cooling} - 0.46 DR) = 4.62 (7.9 - 0.46 * 11.9) \\ = 11.21 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 \text{ }^{\circ}\text{C}$$

$$DR = 11.9 \text{ }^{\circ}\text{C}$$

$$PXI_{windowSouth} = 557$$

$$SHGC = 0.55$$

$$IAC = 1$$

$$FFs = 0.47$$

$$CF_{windowSouthIrradiationPart} = PXI \times SHGC \times IAC \times FFs = 557 * 0.55 * 1 * 0.47 = 144$$

$$CF_{windowSouth} = CF_{windowSouthHeatTrasnferPart} + CF_{windowSouthIrradiationPart} = 11.21 + 144 = 155.21 \frac{W}{m^2}$$

$$\dot{Q}_{windowSouthCooling} = CF_{windowSouth} \times A_{windowSouth} = 155.21 * 3.6 = \mathbf{558.75 \text{ W}}$$

| | | | | | | |
|-----------------|------|-------------|------------------------|------------------|------------|-------------------|
| WINDOW 4 | East | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Wood Frame | 14.4 surface area |
|-----------------|------|-------------|------------------------|------------------|------------|-------------------|

FENESTRATION HEATING

$$U_{windowEast} = 2.84 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 20 - (-4.8) = 24.8 \text{ }^{\circ}\text{C}$$

$$HF_{windowEast} = U_{windowEast} \times \Delta T_{heating} = 2.84 * 24.8 = 70.43 \frac{W}{m^2K}$$

$$\dot{Q}_{windowEastHeating} = HF_{windowEast} \times A_{windowEast} = 70.43 * 14.4 = \mathbf{1014.22 \text{ W}}$$

FENESTRATION COOLING

$$CF_{windowEastHeatTrasnferPart} = U_{windowEast} (\Delta T_{cooling} - 0.46 DR) = 2.84 (7.9 - 0.46 * 11.9) = 6.9 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 \text{ }^{\circ}\text{C}$$

$$DR = 11.9 \text{ }^{\circ}\text{C}$$

$$PXI_{windowEast} = 747$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FFs = 0.31$$

$$CF_{windowEastIrradiationPart} = 747 * 0.54 * 1 * 0.31 = 125.1$$

$$CF_{windowWest} = CF_{windowWestHeatTrasnferPart} + CF_{windowWestIrradiationPart} = 6.9 + 125.1 = 132 \frac{W}{m^2}$$

$$\dot{Q}_{windowWestCooling} = CF_{windowWest} \times A_{windowWest} = 132 * 14.4 = \mathbf{1900.8 \text{ W}}$$

| | | | | | | |
|-----------------|------|-------------|------------------------|------------------|-----------------|-------------------|
| WINDOW 4 | East | Fixed Frame | Heat-absorbing glazing | 2 glazing layers | Aluminium Frame | 14.4 surface area |
|-----------------|------|-------------|------------------------|------------------|-----------------|-------------------|

FENESTRATION HEATING

$$U_{window\,East} = 3.61 \frac{W}{m^2K}$$

$$\Delta T_{heating} = 20 - (-4.8) = 24.8 \text{ }^{\circ}C$$

$$HF_{window\,East} = U_{window\,East} \times \Delta T_{heating} = 3.61 * 24.8 = 89.53 \frac{W}{m^2K}$$

$$\dot{Q}_{window\,East\,Heating} = HF_{window\,East} \times A_{window\,East} = 89.53 * 14.4 = \mathbf{1289.23 \text{ W}}$$

FENESTRATION COOLING

$$CF_{window\,East\,Heat\,Trasnfer\,Part} = U_{window\,East} (\Delta T_{cooling} - 0.46 DR) = 3.61 (7.9 - 0.46 * 11.9) = 8.76 \frac{W}{m^2}$$

$$\Delta T_{cooling} = 7.9 \text{ }^{\circ}C$$

$$DR = 11.9 \text{ }^{\circ}C$$

$$PXI_{window\,East} = 747$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FFs = 0.31$$

$$CF_{window\,East\,Irradiation\,Part} = 747 * 0.56 * 1 * 0.31 = 129.68$$

$$CF_{window\,West} = CF_{window\,West\,Heat\,Trasnfer\,Part} + CF_{window\,West\,Irradiation\,Part} = 8.76 + 129.68 = 138.44 \frac{W}{m^2}$$

$$\dot{Q}_{window\,West\,Cooling} = CF_{window\,West} \times A_{window\,West} = 138.44 * 14.4 = \mathbf{1993.54 \text{ W}}$$

Conclusions:

$$\dot{Q}_{total\,Windows\,Heating\,Woden\,Frame} = 1014.22 + 253.55 + 256.25 + 1014.22 = \mathbf{2538.24 \text{ W}}$$

$$\dot{Q}_{total\,Windows\,Cooling\,Woden\,Frame} = 3352.32 + 533.77 + 458.57 + 1900.8 = \mathbf{6245.46 \text{ W}}$$

$$\dot{Q}_{total\,Windows\,Heating\,Alluminium\,Frame} = 1289.23 + 322.31 + 412.49 + 1289.23 = \mathbf{3313.26 \text{ W}}$$

$$\dot{Q}_{total\,Windows\,Cooling\,Alluminium\,Frame} = 3499.2 + 559.26 + 558.75 + 1993.54 = \mathbf{6610.75 \text{ W}}$$

$$\Delta \dot{Q}_{total\,Windows\,Heating\,Woden\,Frame-Alluminium\,Frame} = 3313.26 - 2538.24 = \mathbf{775.02 \text{ W}}$$

$$\Delta \dot{Q}_{total\,Windows\,Cooling\,Woden\,Frame-Alluminium\,Frame} = 6610.75 - 6245.46 = \mathbf{364.29 \text{ W}}$$

From the results we can conclude that aluminum frame windows are worse than wooden frame windows because heat transfer is bigger in aluminum frame windows than in wooden frame windows.