

Task 1:

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? (keep the gap thickness to be 13 mm)

Answer

To calculate the U – value of a window,

$$U_{\text{window}} = \frac{U_{\text{center}}A_{\text{center}} + U_{\text{edge}}A_{\text{edge}} + U_{\text{fram}}A_{\text{fram}}}{A_{\text{window}}},$$

If it is a double – pane window, disregard the thermal resistances of glass layers,

$$\frac{1}{U_{\text{double-pane (center region)}}} \approx \frac{1}{h_i} + \frac{1}{h_{\text{space}}} + \frac{1}{h_o}, \quad h_{\text{space}} = h_{\text{rad, space}} + h_{\text{conv, space}}$$

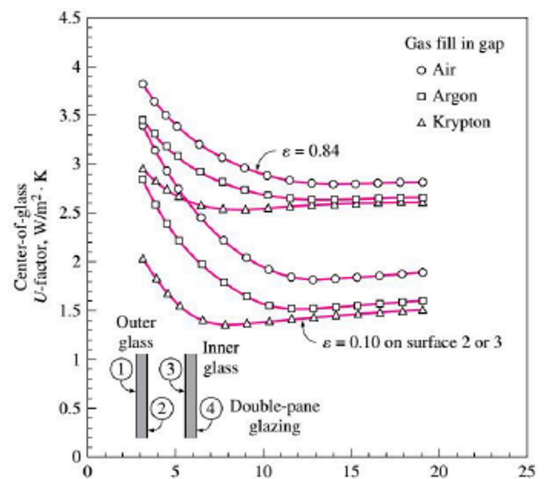
The U_{center} , i. e. the h_{space} changes by changing the gas that fills the gap.

From the diagram in the right side, we can see that:

When the gap thickness is 13 mm,

By changing the gas that fills the gap from air to argon, the U-value of the center of the glass decreases from $2.8 \frac{W}{m^2K}$ to $2.65 \frac{W}{m^2K}$, which means the U-value decreases about 5.36%;

By changing the gas that fills the gap from air to krypton, the U-value of the center of the glass decrease from $2.8 \frac{W}{m^2K}$ to $2.6 \frac{W}{m^2K}$, which means the U-value decreases about 7.14%.



The U_{center} , i. e. the h_{space} changes by adding an extra pane.

From the diagram in the right side, we can see that:

When the gap thickness is 13 mm, and the gas that fills the gap is air,

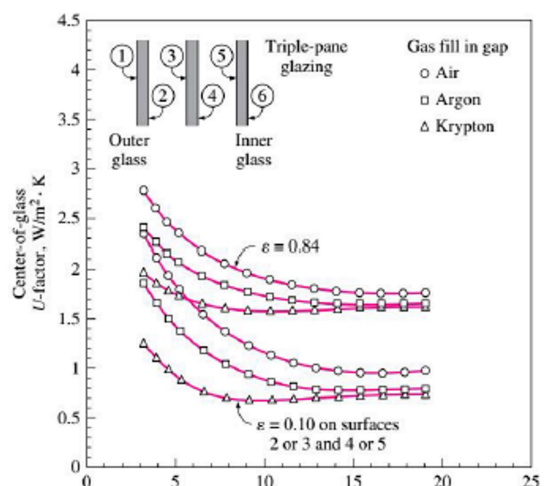
By adding an extra pane, the U-value of the center of the glass decreases from $2.8 \frac{W}{m^2K}$ to $1.8 \frac{W}{m^2K}$, which means the U-value decreases about 35.71%.

Another way to change the U_{center} , is to coat the glass surfaces with a film that has a low emissivity.

From the diagram in the right we can see that:

When the gap thickness is 13 mm, and the gas fills the gap is air,

By coating the glass surfaces with a film that has the emissivity of 0.1, the U-value of the center of the glass decreases from $2.8 \frac{W}{m^2K}$ to $1.8 \frac{W}{m^2K}$, which means the U-value decreases about 35.71%.



$$FF_s = 0.56$$

$$CF_{\text{window}_{\text{west}}(\text{Irradiation Part})} = PXI \times SHGC \times IAC \times FF_s$$

$$\begin{aligned} q_{\text{window}_{\text{west}}} &= A \times CF_{\text{window}_{\text{west}}} = A \times (CF_{\text{window}_{\text{west}}(\text{Heat Transfer Part})} + CF_{\text{window}_{\text{west}}(\text{Irradiation Part})}) \\ &\approx 14.4 \text{ m}^2 \times (6.89 + 747 \times 0.54 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} \approx 3352.07 \text{ W} \end{aligned}$$

Calculating the heating load of the fixed window on the west:

$$\begin{aligned} q_{\text{window}_{\text{west}}} &= A \times HF_{\text{window}_{\text{west}}} = A \times U_{\text{window}_{\text{west}}} \Delta T_{\text{heating}} \\ &= 14.4 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 1014.22 \text{ W} \end{aligned}$$

When the frame were to be aluminium, $U_{\text{window}_{\text{west}}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}},$ $SHGC = 0.56$

$$\begin{aligned} CF'_{\text{window}_{\text{west}}(\text{Heat Transfer Part})} &= U'_{\text{window}_{\text{west}}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR}) \\ &= 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 8.76 \frac{\text{W}}{\text{m}^2} \end{aligned}$$

$$\begin{aligned} \text{Cooling load } q'_{\text{window}_{\text{west}}} &= A \times CF'_{\text{window}_{\text{west}}} \\ &= A \times (CF'_{\text{window}_{\text{west}}(\text{Heat Transfer Part})} + CF'_{\text{window}_{\text{west}}(\text{Irradiation Part})}) \\ &\approx 14.4 \text{ m}^2 \times (8.76 + 747 \times 0.56 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} \approx 3499.48 \text{ W} \end{aligned}$$

$$\begin{aligned} \text{Heating load } q'_{\text{window}_{\text{west}}} &= A \times HF'_{\text{window}_{\text{west}}} = A \times U'_{\text{window}_{\text{west}}} \Delta T_{\text{heating}} \\ &= 14.4 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} \approx 1289.20 \text{ W} \end{aligned}$$

Calculating the cooling load of the fixed window on the south:

$$q_{\text{window}_{\text{south}}} = A \times CF_{\text{window}_{\text{south}}}$$

$$A = 3.6 \text{ m}^2,$$

$$CF_{\text{window}_{\text{south}}(\text{Heat Transfer Part})} = U_{\text{window}_{\text{south}}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

∴ The window has a fixed heat absorbing double layer glass with a wooden frame,

$$\therefore U_{\text{window}_{\text{south}}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{i.e., } CF_{\text{window}_{\text{south}}(\text{Heat Transfer Part})} = 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) \approx 6.89 \frac{\text{W}}{\text{m}^2}$$

$$PXI_{\text{window}_{\text{south}}} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

No internal shading, so $IAC = 1$

$$FF_s = 0.47$$

$$CF_{\text{window}_{\text{south}}(\text{Irradiation Part})} = PXI \times SHGC \times IAC \times FF_s$$

$$\begin{aligned} q_{\text{window}_{\text{south}}} &= A \times CF_{\text{window}_{\text{south}}} = A \times (CF_{\text{window}_{\text{south}}(\text{Heat Transfer Part})} + CF_{\text{window}_{\text{south}}(\text{Irradiation Part})}) \\ &\approx 3.6 \text{ m}^2 \times (6.89 + 557 \times 0.54 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} \approx 553.72 \text{ W} \end{aligned}$$

Calculating the heating load of the fixed window on the south:

$$q_{window\ south} = A \times HF_{window\ south} = A \times U_{window\ south} \Delta T_{heating}$$

$$= 3.6\ m^2 \times 2.84\ \frac{W}{m^2K} \times 24.8K \approx 253.56\ W$$

When the frame were to be aluminium, $U_{window\ south} = 3.61\ \frac{W}{m^2K}$, $HSGC = 0.56$

$$CF'_{window\ south(Heat\ Trasnfer\ Part)} = U'_{window\ south} (\Delta T_{cooling} - 0.46\ DR)$$

$$= 3.61\ \frac{W}{m^2K} \times (7.9\ K - 0.46 \times 11.9\ K) \approx 8.76\ \frac{W}{m^2}$$

$$Cooling\ load\ q'_{window\ south} = A \times CF'_{window\ south}$$

$$= A \times (CF'_{window\ south(Heat\ Trasnfer\ Part)} + CF'_{window\ south(Irradiation\ Part)})$$

$$\approx 3.6\ m^2 \times (8.76 + 557 \times 0.56 \times 1 \times 0.47)\ \frac{W}{m^2} \approx 559.30\ W$$

$$Heating\ load\ q'_{window\ south} = A \times HF'_{window\ south} = A \times U'_{window\ south} \Delta T_{heating}$$

$$= 3.6\ m^2 \times 3.61\ \frac{W}{m^2K} \times 24.8\ K \approx 322.30\ W$$

Calculating the cooling load of the operable window on the south:

$$q_{window\ south} = A \times CF_{window\ south}$$

$$A = 3.6\ m^2,$$

$$CF_{window\ south(Heat\ Trasnfer\ Part)} = U_{window\ south} (\Delta T_{cooling} - 0.46\ DR)$$

∴ The window has an operable heat absorbing double layer glass with a wooden frame,

$$\therefore U_{window\ south} = 2.87\ \frac{W}{m^2K}$$

$$i.e., CF_{window\ south(Heat\ Trasnfer\ Part)} = 2.87\ \frac{W}{m^2K} \times (7.9\ K - 0.46 \times 11.9\ K) \approx 6.96\ \frac{W}{m^2}$$

$$PXI_{window\ south} = E_D + E_d = 348 + 209 = 557$$

$$SHGC = 0.46$$

No internal shading, so IAC =1

$$FF_s = 0.47$$

$$CF_{window\ south(Irradiation\ Part)} = PXI \times SHGC \times IAC \times FF_s$$

$$q_{window\ south} = A \times CF_{window\ south} = A \times (CF_{window\ south(Heat\ Trasnfer\ Part)} + CF_{window\ south(Irradiation\ Part)})$$

$$\approx 3.6\ m^2 \times (6.96 + 557 \times 0.46 \times 1 \times 0.47)\ \frac{W}{m^2} \approx 458.58\ W$$

Calculating the heating load of the operable window on the south:

$$q_{window\ south} = A \times HF_{window\ south} = A \times U_{window\ south} \Delta T_{heating}$$

$$= 3.6\ m^2 \times 2.87\ \frac{W}{m^2K} \times 24.8K \approx 256.23\ W$$

When the frame were to be aluminium, $U_{window\ south} = 4.62\ \frac{W}{m^2K}$, $HSGC = 0.55$

$$CF'_{window\ south(Heat\ Trasnfer\ Part)} = U'_{window\ south} (\Delta T_{cooling} - 0.46\ DR)$$

$$= 4.62 \frac{W}{m^2 K} \times (7.9 K - 0.46 \times 11.9 K) \approx 11.21 \frac{W}{m^2}$$

$$\text{Cooling load } q'_{\text{window}_{\text{south}}} = A \times CF'_{\text{window}_{\text{south}}}$$

$$= A \times (CF'_{\text{window}_{\text{south}}}(\text{Heat Transfer Part}) + CF'_{\text{window}_{\text{south}}}(\text{Irradiation Part}))$$

$$\approx 3.6 m^2 \times (11.21 + 557 \times 0.55 \times 1 \times 0.47) \frac{W}{m^2} \approx 558.70 W$$

$$\text{Heating load } q'_{\text{window}_{\text{south}}} = A \times HF'_{\text{window}_{\text{south}}} = A \times U'_{\text{window}_{\text{south}}} \Delta T_{\text{heating}}$$

$$= 3.6 m^2 \times 4.62 \frac{W}{m^2 K} \times 24.8 K \approx 412.47 W$$