EXAMPLE AND SUMMARY

EXAMPLE 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickness to be 13 mm)

$$U_{window} = \frac{U_{center}A_{center} + U_{edge}A_{edge} + U_{fram}U_{fram}}{A_{window}}$$

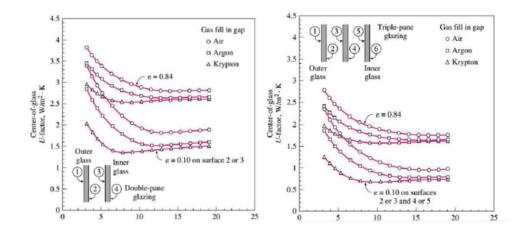
For double pan window, regardless of the thermal resistances of glass layers,

$$\frac{1}{U_{\text{double-pane(center region)}}} \approx \frac{1}{h_{\text{i}}} + \frac{1}{h_{\text{space}}} + \frac{1}{h_{\text{o}}} \text{ , } h_{\text{space}} = h_{\text{rad,space}} + h_{\text{conv,space}}$$

U_{center}, i.e. the h_{space} changes by changing the gas that fills the gap.

By adding an extra pane, the U value of the centre of the glass decreases from $2.8 \frac{W}{m^2 K}$ to $1.8 \frac{W}{m^2 K}$, which means the u value decreases about 55.6%.

Another way to change the U_{center} , is to coat the glass surfaces with a film that has a low emissivity. From the diagram in the right we can see that: when the gap thickness is 13 mm, and the gas fills the gap is air, by coating the glass surfaces with a film that has the emissivity of 0.1, the U value of the centre of the glass decreases from $2.8 \, \frac{W}{m^2 \, K}$ to $1.8 \, \frac{W}{m^2 \, K}$, which means the U value decreases about 55.6%



EXAMPLE 2

Considering the house that we analyzed in the last two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 sqm on the west, fixed 3.6 sqm on the south and an operable 3.6 sqm on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminum?

Temperature difference calculation

$$\Delta T_{cooling} = 31.9 - 24 = 7.9 \,^{\circ}\text{C}$$

 $\Delta T_{heating} = 20 - (-4.8) = 24.8 \,^{\circ}\text{C}$
DR = 11.9 $^{\circ}\text{C}$

						PIACENZA, Italy						WMO			160840	
Lat	44.92N	Long:	9.73E	Elev:	138	StdP:	99.68		Time Zone: 1.00 (EUV		N)	Period: 89-1		0 WBAN	99999)
nnual H	eating and H	umidification	on Design C	onditions												
Coldest Month	Heating DB		Humidification DP/MCDB and HR						Coldest month WS/MCDB			В	MCWS/PC			
			99.6%			99%			0.4%		1	1% to 99		6% DB		
	99.6%	99%	DP	HR	MCDB	DP	HR	MCDB	WS	MCDB	WS	MCDB	MCWS	PCWD		
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(1)	(m)	(n)	(0)		
1	-6.2	-4.8	-11.6	1.4	3.1	-8.8	1.8	1.8	8.8	5.6	7.7	6.2	2.1	250		
nnual C	ooling, Dehu	midificatio	n, and Enth	alpy Design	Conditions	E.										
Hottest Month	Hottest Month DB Range	Cooling DB/MCWB							Evaporation WB/MCDB					MCWS/PCWD		ľ
		0.4%		1%		2%		0.4%		1%		2%		to 0.4	6 DB	
		DB	MCWB	DB	MCWB	DB	MCWB	WB	MCDB	WB	MCDB	WB	MCDB	MCWS	PCWD	
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(1)	(m)	(n)	(0)	(P)	
8	11.9	33.1	22.7	31.9	22.4	30.3	21.8	24.6	30.2	23.7	29.2	22.9	28.3	2.4	90	-

WEST WINDOW (FIXED)

Cooling Load: Wooden Frame

$$\dot{q}_{windowwest} = A \times CF_{windowwest}$$

 $A = 14.4 \text{ m}^2$

$$CF_{windowwest} = CF_{windowwest_heattransfer} + CF_{windowwest_irridiation}$$

$$CF_{windowwest} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_{s}$$

$$CF_{windowwest_heattransfer} = U(\Delta T - 0.46DR)$$

U = 2.84

$$CF_{windowwest_heattransfer} = 2.84 (7.9 - (0.46)(11.9)) = 6.89 \frac{W}{m^2}$$

$$\text{CF}_{windowwest_irridiation} = \text{PXI x SHGC x IAC x FF}_s$$

$$PXI = E_D - E_d = 559 + 188 = 747$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FF_s = 0.56$$

$$CF_{windowwest_irridiation} = 747 \times 0.54 \times 1 \times 0.56 = 232.78 \frac{W}{m^2}$$

$$CF_{windowwest} = CF_{windowwest_heattransfer} + CF_{windowwest_irridiation}$$

$$CF_{windowwest} = 6.89 + 225.89 = 232.78 \frac{W}{m^2}$$

$$CF_{windowwest} = 6.89 + 225.89 = 232.78 \frac{w}{m^2}$$

$$\dot{q}_{windowwest} = A \times CF_{windowwest} = 14.4 \times 232.78 = 3352.07 \text{ W}$$

Cooling Load: Aluminium Frame

 $\dot{q}_{windowwest} = A \times CF_{windowwest}$

$$A = 14.4 \text{ m}^2$$

 $CF_{windowwest} = CF_{windowwest_heattransfer} + CF_{windowwest_irridiation}$

 $CF_{windowwest} = U(\Delta T - 0.46DR) + PXI x SHGC x IAC x FF_s$

 $CF_{windowwest_heattransfer} = U(\Delta T - 0.46DR)$

U = 3.61

 $CF_{windowwest_heattransfer} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{W}{m^2}$

 $CF_{windowwest_irridiation} = PXI x SHGC x IAC x FF_s$

 $PXI = E_D - E_d = 559 + 188 = 747$

SHGC = 0.56

IAC = 1

$$FF_s = 0.56$$

 $CF_{windowwest_irridiation} = 747 \times 0.56 \times 1 \times 0.56 = 234.26 \frac{W}{m^2}$

 $CF_{windowwest} = 8.76 + 234.26 = 243.02 \frac{W}{m^2}$

 $\dot{q}_{windowwest} = A x CF_{windowwest} = 14.4 x 243.02 = 3499.47 W$

Heating Load: Wooden Frame

 $\dot{q}_{windowwest} = A x HF_{windowwest}$

 $A = 14.4 \text{ m}^2$

 $HF_{windowwest} = U_{windowwest} \times \Delta T_{heating}$

U = 2.84

 $HF_{windowwest} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$

 $\dot{q}_{windowwest} = A x HF_{windowwest} = 14.4 x 70.43 = 1014.22 W$

Heating Load: Aluminium Frame

 $\dot{q}_{windowwest} = A x HF_{windowwest}$

 $A = 14.4 \text{ m}^2$

 $HF_{windowwest} = U_{windowwest} \times \Delta T_{heating}$

 $HF_{windowwest} = 3.61 \times 24.8 = 89.53 \frac{W}{m^2}$

 $\dot{q}_{windowwest} = A x HF_{windowwest} = 14.4 x 89.53 = 1289.20 W$

Difference:

Cooling Load = 147.4 W

Heating Load = 274.98 W

SOUTH WINDOW (FIXED)

Cooling Load: Wooden Frame

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$

 $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_{s}$

 $CF_{windowsouth\ heattransfer} = U(\Delta T - 0.46DR)$

U = 2.84

 $CF_{windowsouth_heattransfer} = 2.84 (7.9 - (0.46)(11.9)) = 6.89 \frac{W}{m^2}$

 $CF_{windowsouth_irridiation} = PXI x SHGC x IAC x FF_s$

$$PXI = E_D - E_d = 348 + 209 = 557$$

SHGC = 0.54
IAC = 1

$$FF_s = 0.47$$

$$CF_{windowsouth_irridiation} = 557 \times 0.54 \times 1 \times 0.47 = 141.37 \frac{W}{m^2}$$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$

$$CF_{\text{windowsouth}} = 6.89 + 141.37 = 148.26 \frac{W}{m^2}$$

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 148.26 = 533.74 \text{ W}$

Cooling Load: Aluminium Frame

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$

 $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$

 $CF_{windowsouth_heattransfer} = U(\Delta T - 0.46DR)$

U = 3.61

 $CF_{windowsouth_heattransfer} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{W}{m^2}$

 $CF_{windowsouth_irridiation} = PXI x SHGC x IAC x FF_s$

 $PXI = E_D - E_d = 348 + 209 = 557$

SHGC = 0.56

IAC = 1

$$FF_s = 0.47$$

 $CF_{windowsouth_irridiation} = 557 \times 0.56 \times 1 \times 0.47 = 146.60 \frac{W}{m^2}$

 $CF_{windowsouth} = 8.76 + 146.60 = 155.36 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 155.36 = 559.30 \text{ W}$

Heating Load: Wooden Frame

 $\dot{q}_{windowsouth} = A\,x\,HF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $HF_{windowsouth} = U_{windowsouth} \times \Delta T_{heating}$

U = 2.84

 $HF_{windowsouth} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A \times HF_{windowsouth} = 3.6 \times 70.43 = 253.08 \text{ W}$

Heating Load: Aluminium Frame

 $\dot{q}_{windowsouth} = A \times HF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $HF_{windowsouth} = U_{windowsouth} \times \Delta T_{heating}$

U = 3.61

 $HF_{windowsouth} = 3.61 \times 24.8 = 89.53 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A x HF_{windowsouth} = 3.6 x 89.53 = 322.31 W$

Difference:

Cooling Load = 25.56 W

Heating Load = 69.23 W

SOUTH WINDOW (OPERABLE)

Cooling Load: Wooden Frame

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$

 $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$

 $CF_{windowsouth_heattransfer} = U(\Delta T - 0.46DR)$

U = 2.87

 $CF_{windowsouth_heattransfer} = 2.87 (7.9 - (0.46)(11.9)) = 6.96 \frac{W}{m^2}$

 $CF_{windowsouth_irridiation} = PXI \ x \ SHGC \ x \ IAC \ x \ FF_s$

 $PXI = E_D - E_d = 348 + 209 = 557$

SHGC = 0.46

IAC = 1

 $FF_s = 0.47$

 $CF_{windowsouth_irridiation} = 557 \times 0.46 \times 1 \times 0.47 = 120.42 \frac{W}{m^2}$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$ $CF_{windowsouth} = 6.96 + 120.42 = 127.38 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 127.38 = 458.57 \text{ W}$

Cooling Load: Aluminium Frame

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $CF_{windowsouth} = CF_{windowsouth_heattransfer} + CF_{windowsouth_irridiation}$

 $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$

 $CF_{windowsouth\ heattransfer} = U(\Delta T - 0.46DR)$

U = 4.62

 $CF_{windowsouth_heattransfer} = 4.62 (7.9 - (0.46)(11.9)) = 11.21 \frac{W}{m^2}$

 $CF_{windowsouth_irridiation} = PXI x SHGC x IAC x FF_s$

 $PXI = E_D - E_d = 348 + 209 = 557$

SHGC = 0.55

IAC = 1

 $FF_s = 0.47$

 $CF_{windowsouth_irridiation} = 557 \times 0.55 \times 1 \times 0.47 = 143.98 \frac{W}{m^2}$

 $CF_{\text{windowsouth}} = 11.21 + 143.98 = 155.19 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 155.19 = 558.68 \text{ W}$

Heating Load: Wooden Frame

 $\dot{q}_{windowsouth} = A \times HF_{windowsouth}$

 $A = 3.6 \text{ m}^2$

 $HF_{windowsouth} = U_{windowsouth} \times \Delta T_{heating}$

U = 2.87

 $HF_{windowsouth} = 2.87 \times 24.8 = 71.18 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A x HF_{windowsouth} = 3.6 x 71.18 = 256.23 W$

Heating Load: Aluminium Frame

$$\begin{array}{l} \dot{q}_{windowsouth} \; = \; A \, x \, HF_{windowsouth} \\ A = 3.6 \, m^2 \\ HF_{windowsouth} = U_{windowsouth} \, x \, \Delta T_{heating} \\ U = 4.62 \\ HF_{windowsouth} = 4.62 \, x \, 24.8 = 114.58 \, \frac{W}{m^2} \\ \dot{q}_{windowsouth} = \; A \, x \, HF_{windowsouth} = 3.6 \, x \, 114.58 = 412.47 \, W \end{array}$$

Difference:

Cooling Load = 100.11 W Heating Load = 156.24 W