





Backtracking Striver sir lecture Notes

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|--|--|
|  | L14. N-Queens Leetcode Hard Backtracking
take U forward |
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~Thank you, Striver Sir, for your exceptional guidance in explaining the complex topic of backtracking. Your teaching has been incredibly effective and I would like to express my gratitude♥

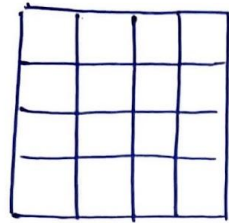
Playlist link

[Backtracking\(L14-L19\)](#)

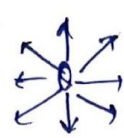
① $N=4$ Queen

N Queen problem

(Backtracking note)

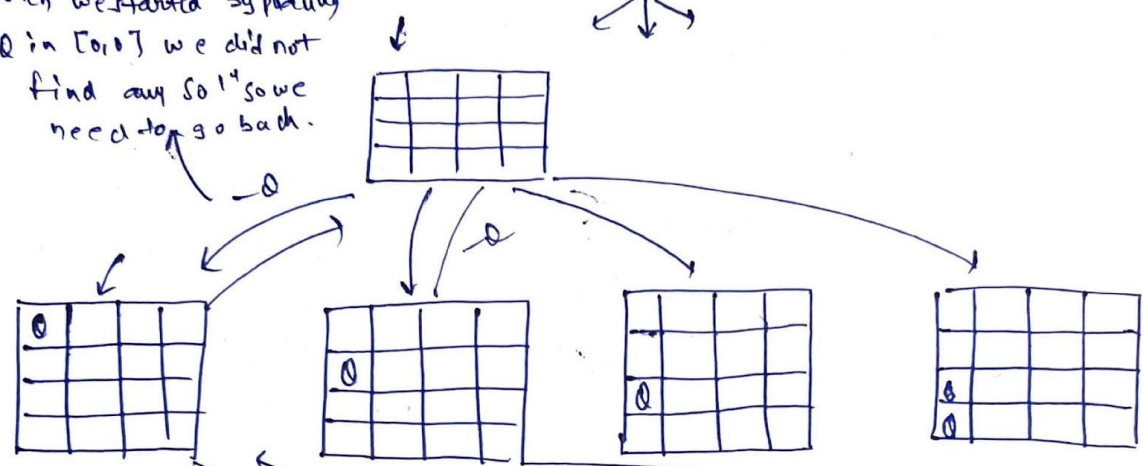


- Every row $\rightarrow 1Q$
- Every col $\rightarrow 1Q$
- Non of Queen should attack each other

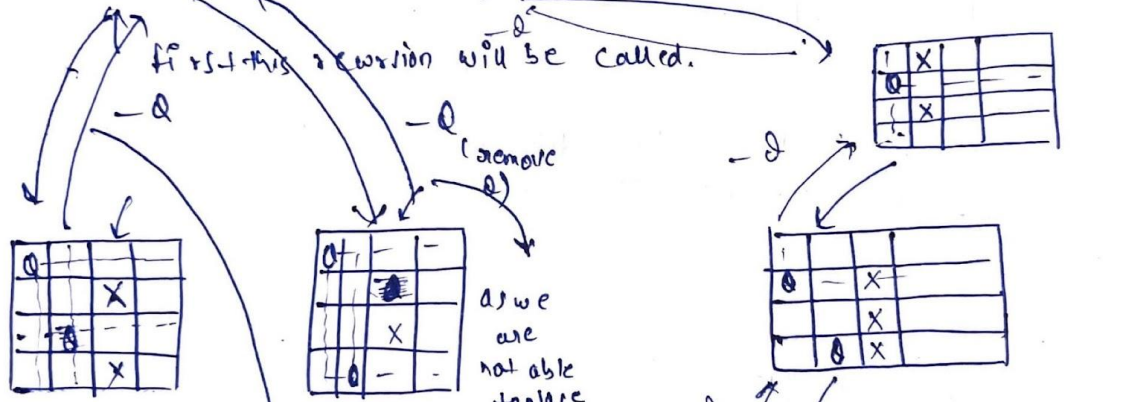


8 directions

when we started by placing Q in [0,0] we did not find any solⁿ so we need to go back.



first this recursion will be called.



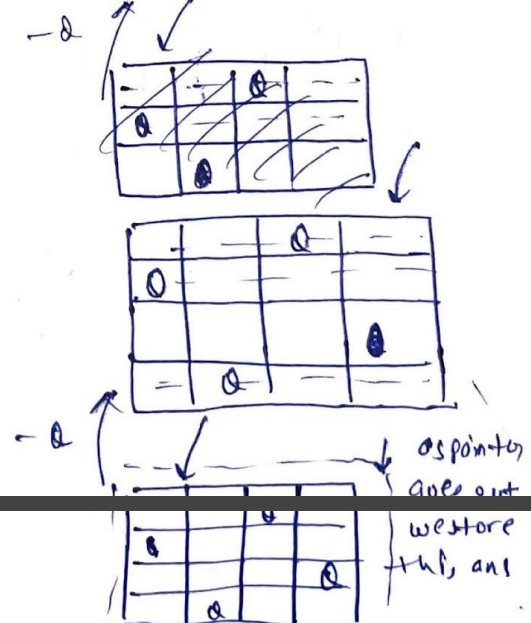
(if we follow this path we are not able to place the 3rd queen in any of 3rd column place)

as we are not able to place in 3rd column so col violate we go back.

while moving back we have to remove this Q

you can't place Queen anywhere in last column

back then and remove Q.



Structure of code

~~for~~
f(col)

```

{
  for (i = 0 → n-1)
    if (A[i] ✓)
      {
        make [new] [col] = 0
        f(col + 1)
        empty
      }
}

```

checking is it possible to find or not

(0 at abhi dena matrix at 1)

not find for first dot next col to move dot jte

when this recursion will be complete remove 0

q. 9 or woh safe na hua rite bank tak chad ke pick a paya jata hai to call karta shuru hua tha.

```

f(col)
{
  for (i = 0 → n-1)
    if (A[i])
      {
        make r jte 0
        f(col + 1)
        empty
      }
}

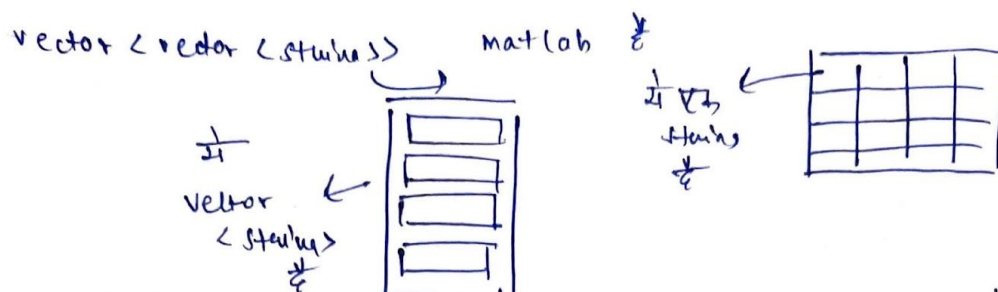
```

↑ it will return

as phir for loop next to jte chadke

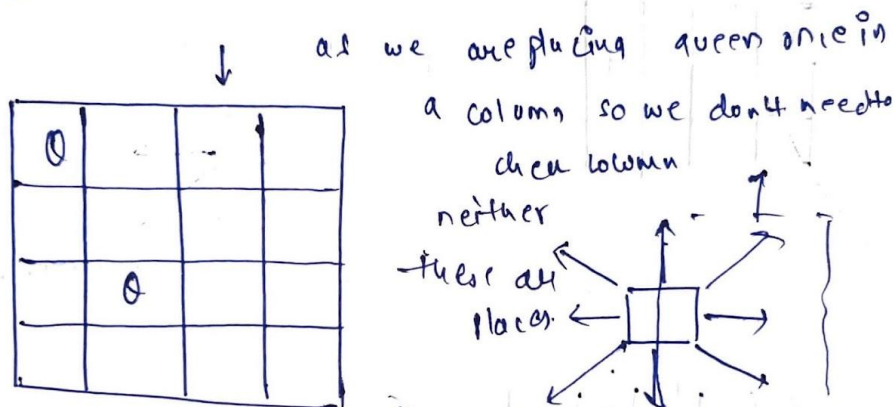
f(col) → f(col) → f(col) → base case

if (A[i]) → not exc



as in ~~it~~ store ~~data~~ make vector <vector<string>> honge
 it possible ans store ~~data~~

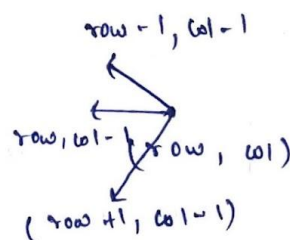
now we need to write the function to check
 whether it is safe to fill up or not.



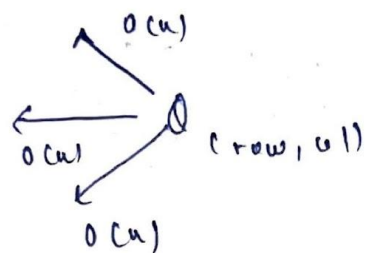
by checking in
 these three direction
 we can be sure about
 placing queen

Queen can attack any
 in this direction

So we won't just check in
 adjacent rather we will
 run loop till the end
 to check.

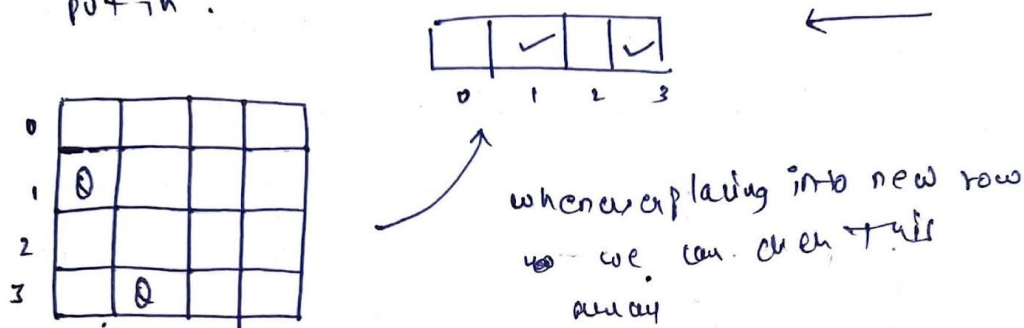


at last index start & set ~~start~~
 like we will run the loop.

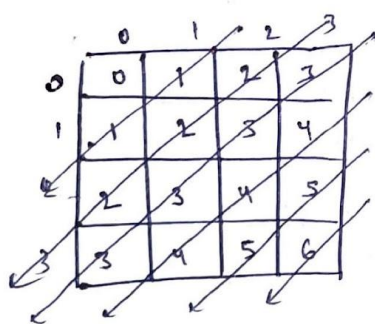


we can optimise this checking code using hashing

Now for case of row checking we can maintain a array mark it for all the row & have be put in.



for diagonal we need to observe pattern.



we can observe this pattern which will be in an $N \times N$ matrix
 $i + j = k$ for a diagonal,
 bcoz of $5n$.

* So we can make an array of size $2n-1$ and in that if at any index we place a Q we will mark $i+j$ with index.

0			

$n = 8$

0							

now we need to fill it
for

this diagonal

for that we will use

a formula

$$n-1 + \text{col} - \text{row}$$

$$8-1 + 7-0 = 14$$

$$8-1 + 6-0 = 13$$

$$8-1 + 7-1 = 13$$

So again this we will
make an array of $2n-1$
size and hash the values.

$(n-1 + j-i)$ should be marked 1 for
any index we place.

So now in recursion we pass left row, upper diagonal,
and lower diagonal and check if they are zero
put 'Q' in specified row and column and mark them
1 and then call recursion once recursion

returns on marking all and removing Q
replacing it with blank.

Sudoku Solver!

- ① The digit 1-9 only appears once in any row or col and in 3x3 matrix
- ② Traverse the matrix to figure out empty place
- ③ when empty place found try all possible combinations for it for each number call is valid function


```

if (is valid (board, i, j, c))
{
    board[i][j] = c;
    if (solve (board) == true)
        return true;
    else
        board[i][j] = '.';
}
return false;

```

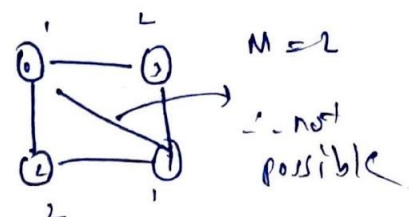
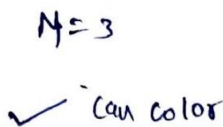
↗

જો 2 નું સ્થાન
આપે તો વાત
હાથ થઈ શકે છે
રેપ્લે કરો
ફરીથી
- ④ if there are never an empty cell, at least one is returned.

Ex $\text{board} [3 * (\text{row} / 3) + i / 3] [3 * (\text{col} / 3) + i / 3] = z$
to traverse in small matrix.

M Coloring of Graph!

You have to use max of m colours such a way that no 2 nodes in graph are having same colour.



We cannot color it with 1 or 2 as its adjacent are having the same color.

```

    graph TD
      f0["f(0)"] -- 1 --> f1["f(1)"]
      f1 -- 1 --> f2["f(2)"]
      f1 -- 2 --> f3["f(3)"]
      f2 -- 3 --> f4["f(4)"]
      f2 -- 2 --> f5["f(5)"]
      f3 -- 3 --> f6["f(6)"]
      f3 -- 2 --> f7["f(7)"]
      f4 --- X1["X"]
      f5 --- X2["X"]
      f6 --- X3["X"]
      f7 --- C1["✓"]
  
```

→ we have also possibility
at various nodes of
columning but as the question
is can we so. ∴ when
we reach at node $N = 4$
then we keep on
returning false.

* possible function में कुछ नई node दिया होगा and color ad uske adjacent में new way karo and ek bar ad jale में बिना का color vah node

f(node)

```
if (node == N) return true;
```

for $\omega = (1 \rightarrow m)$

a function to check if color has
node with that particular color
color possible or not

{ if (possible)

{ color [node] = col }

if (f(node+1) == T)

१८७१

```
else color [node] = 0
```

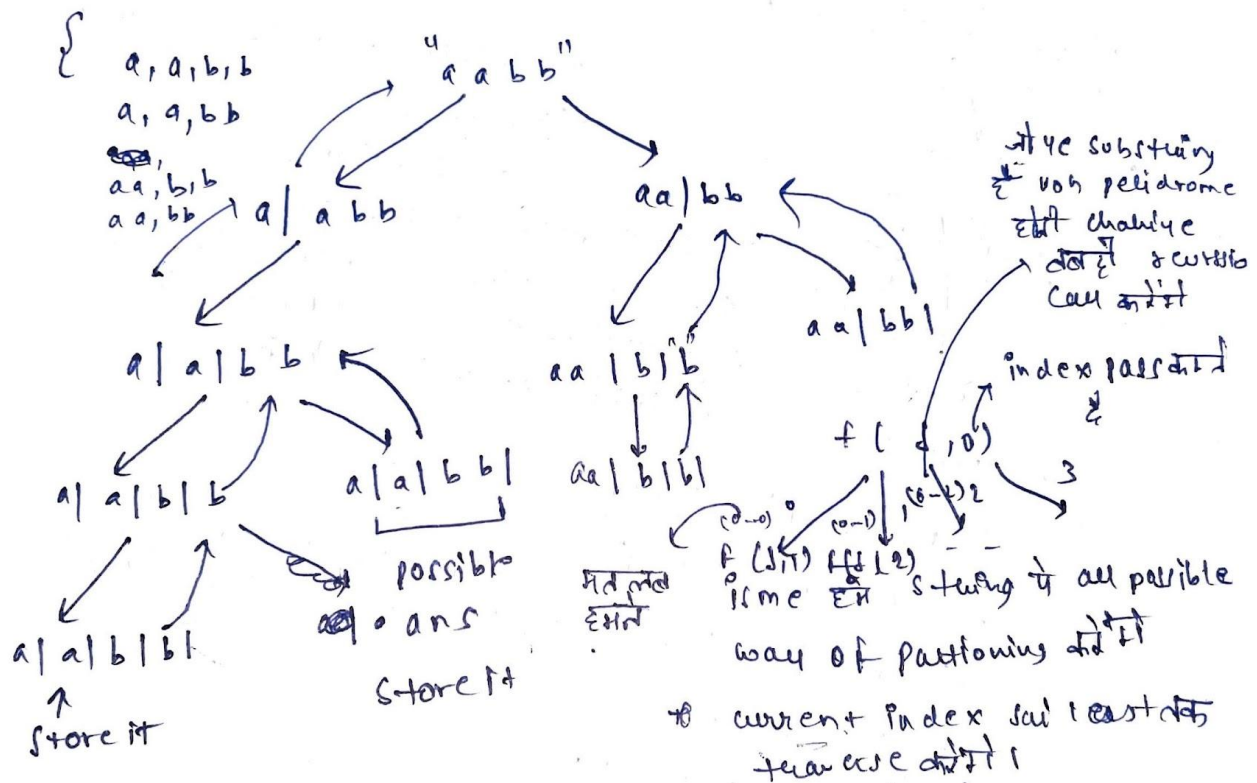
if it won't be possible
we return false.

$$T.C \rightarrow (N^m)$$

$$S.C \rightarrow O(N) + O(N)$$

Palindrome Partitioning

* whenever you reach the end your recursion call is over it means that you are able to partition then we backtrack.



* whenever we make tree diagram we try to make as per our given constraints and based on recursion we tell how the recursion would be called.

Rat in A Maze :

↓	0	0	0
↓	→	0	1
↓	→	0	0
0	↓	1	1

→ we will maintain a string in which we would keep adding the order

→ we would start traversing in DLRU fashion as we want lexicographical order

→ we also maintain a visited array bcz we don't want to visit same again and have row and col.

$f(0, 0, "", "")$

D L R U

	0	1	2	3
0	✓			
1	✗	✓		
2	✗	✓	✗	
3		✗	✗	

visited.

$f(0, 0, "", "")$

D L R U

$f(1, 0, "D")$

D L R U

$f(2, 0, "DD")$

only possible option
(U) while
backtr.
but
at (2,0)
we don't
go
upward
so
we
backtr.

$f(2, 1, "DDR")$

D L R U

$f(3, 1, "DDRD")$

D L R U

$f(3, 2, "DDRRD")$

D L R U

$f(3, 3, "DDRRDR")$

now for this as
we have gone through
Down so we will try
from L, R, U
always remember we'll
continue from where we
left & possible
 $f(1, 1, "DDRU")$
* is not possible
we get 1.

[Whenever u
back-track

pls ~~not~~ on mark
the visited.]

we possible ans & ... (print)

