

| Present State | X | Next State    | Y |
|---------------|---|---------------|---|
| $s_2 s_1 s_0$ |   | $n_2 n_1 n_0$ |   |
| 000           | 0 | 000           | 0 |
| 000           | 1 | 001           | 0 |
| 001           | 0 | 000           | 0 |
| 001           | 1 | 001           | 0 |
| 010           | 0 | 000           | 0 |
| 010           | 1 | 001           | 0 |
| 011           | 0 | 000           | 0 |
| 011           | 1 | 001           | 0 |
| 100           | 0 | 000           | 0 |
| 100           | 1 | 001           | 0 |
| 101           | 0 | 000           | 0 |
| 101           | 1 | 001           | 0 |
| 110           | 0 | 000           | 0 |
| 110           | 1 | 001           | 0 |
| 111           | 0 | 000           | 0 |
| 111           | 1 | 001           | 0 |

For  $n_2$

| $s_2 s_1$ | $s_0$ | X | $n_2$ |
|-----------|-------|---|-------|
| 00        | 0     | 0 | 0     |
| 00        | 1     | 0 | 0     |
| 01        | 0     | 0 | 0     |
| 01        | 1     | 0 | 0     |
| 10        | 0     | 0 | 0     |
| 10        | 1     | 0 | 0     |
| 11        | 0     | 0 | 0     |
| 11        | 1     | 0 | 0     |

$$\Rightarrow n_2 = s_2 s_1 s_0' X'$$

For  $n_1$

| $s_2 s_1$ | $s_0$ | X | $n_1$ |
|-----------|-------|---|-------|
| 00        | 0     | 0 | 0     |
| 00        | 1     | 0 | 0     |
| 01        | 0     | 0 | 0     |
| 01        | 1     | 0 | 0     |
| 10        | 0     | 0 | 0     |
| 10        | 1     | 0 | 0     |
| 11        | 0     | 0 | 0     |
| 11        | 1     | 0 | 0     |

$$\Rightarrow n_1 = s_2 s_1 s_0' + s_1 X + s_1 s_0$$

For  $n_0$

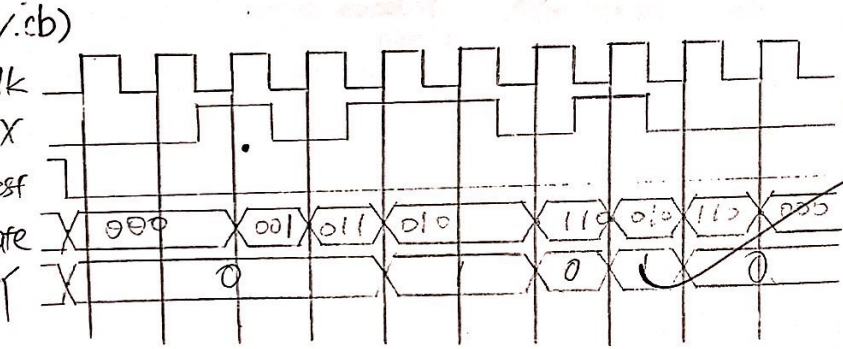
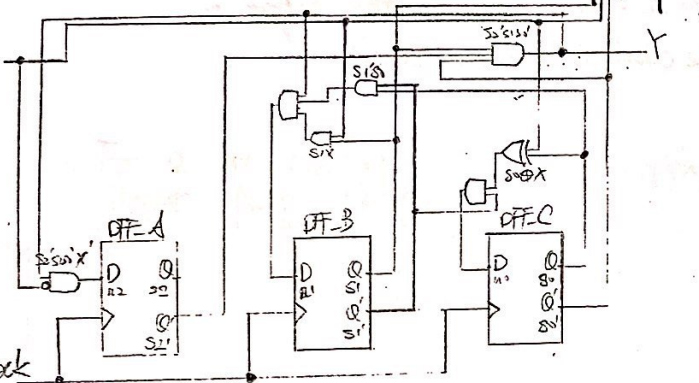
| $s_2 s_1$ | $s_0$ | X | $n_0$ |
|-----------|-------|---|-------|
| 00        | 0     | 0 | 0     |
| 00        | 1     | 0 | 0     |
| 01        | 0     | 0 | 0     |
| 01        | 1     | 0 | 0     |
| 10        | 0     | 0 | 0     |
| 10        | 1     | 0 | 0     |
| 11        | 0     | 0 | 0     |
| 11        | 1     | 0 | 0     |

$$\Rightarrow n_0 = s_1 s_0' X + s_1 s_0 X' = s_1 (s_0 \oplus X)$$

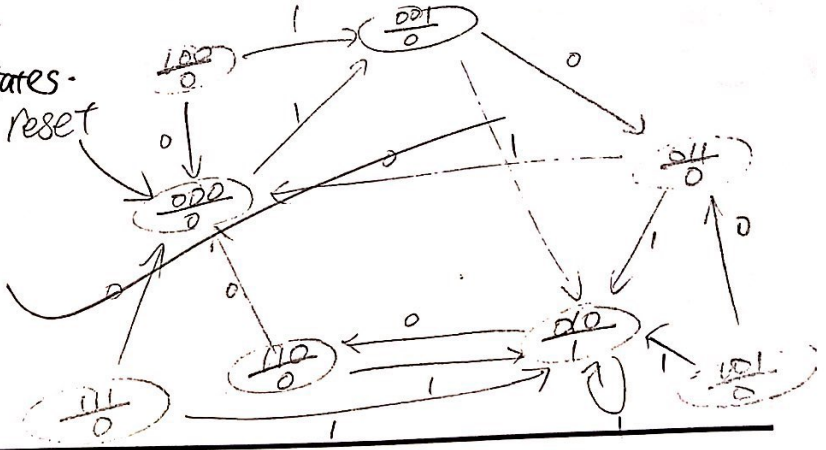
For Y

| $s_2 s_1$ | $s_0$ | X | Y |
|-----------|-------|---|---|
| 00        | 0     | 0 | 0 |
| 00        | 1     | 0 | 0 |
| 01        | 0     | 0 | 0 |
| 01        | 1     | 0 | 0 |
| 10        | 0     | 0 | 0 |
| 10        | 1     | 0 | 0 |
| 11        | 0     | 0 | 0 |
| 11        | 1     | 0 | 0 |

$$\Rightarrow Y = s_2 s_1 s_0'$$



It's not self-starting, since there are 3 unused states.



2/(a)

| Present State |    |    | X | Y | Next State |    |    |
|---------------|----|----|---|---|------------|----|----|
| s2            | s1 | s0 |   |   | n2         | n1 | n0 |
| 0             | 0  | 0  | 0 | 0 | 0          | 0  |    |
| 0             | 0  | 0  | 1 | 0 | 0          | 1  |    |
| 0             | 0  | 1  | 0 | 0 | 0          | 0  |    |
| 0             | 0  | 1  | 1 | 0 | 0          | 1  |    |
| 0             | 1  | 0  | 0 | 0 | 1          | 0  |    |
| 0             | 1  | 0  | 1 | 0 | 1          | 1  |    |
| 0             | 1  | 1  | 0 | 0 | 0          | 0  |    |
| 0             | 1  | 1  | 1 | 0 | 0          | 1  |    |
| 1             | 0  | 0  | 0 | 1 | 0          | 0  |    |
| 1             | 0  | 0  | 1 | 1 | 0          | 1  |    |
| 1             | 0  | 1  | 0 | 1 | 1          | 0  |    |
| 1             | 0  | 1  | 1 | 1 | 1          | 1  |    |
| 1             | 1  | 0  | 0 | 0 | 0          | 0  |    |
| 1             | 1  | 0  | 1 | 0 | 0          | 1  |    |
| 1             | 1  | 1  | 0 | 0 | 1          | 0  |    |
| 1             | 1  | 1  | 1 | 0 | 1          | 1  |    |

0 0 0 1 0

For  $n_2, n_1, n_0$  the equations are the same as those in the problem

$$n_2 = s_2 s_1 s_0' x'$$

$$n_1 = s_2 s_1 s_0' + s_1 x + s_1 s_0$$

$$n_0 = s_1 (s_0 \oplus x)$$

For Y

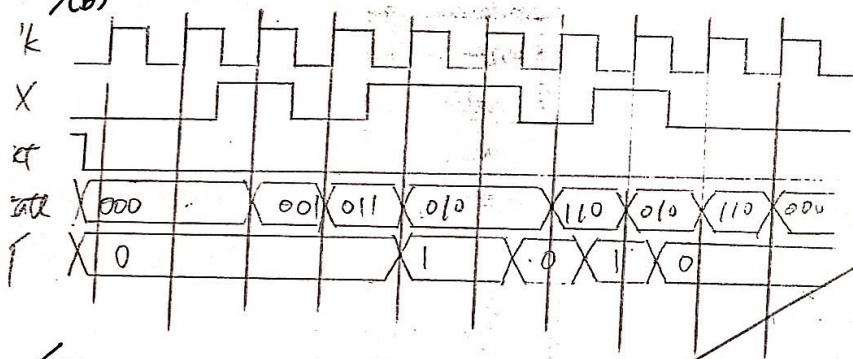
~~s2s1~~ s0x

| s2s1 | s0x | 00 | 01 | 11 | 10 |
|------|-----|----|----|----|----|
| 00   | 00  | 0  | 0  | 0  | 0  |
| 00   | 01  | 0  | 1  | 0  | x  |
| 00   | 11  | 0  | x  | x  | x  |
| 00   | 10  | x  | x  | x  | x  |

$$\Rightarrow Y = s_1 s_0' x$$

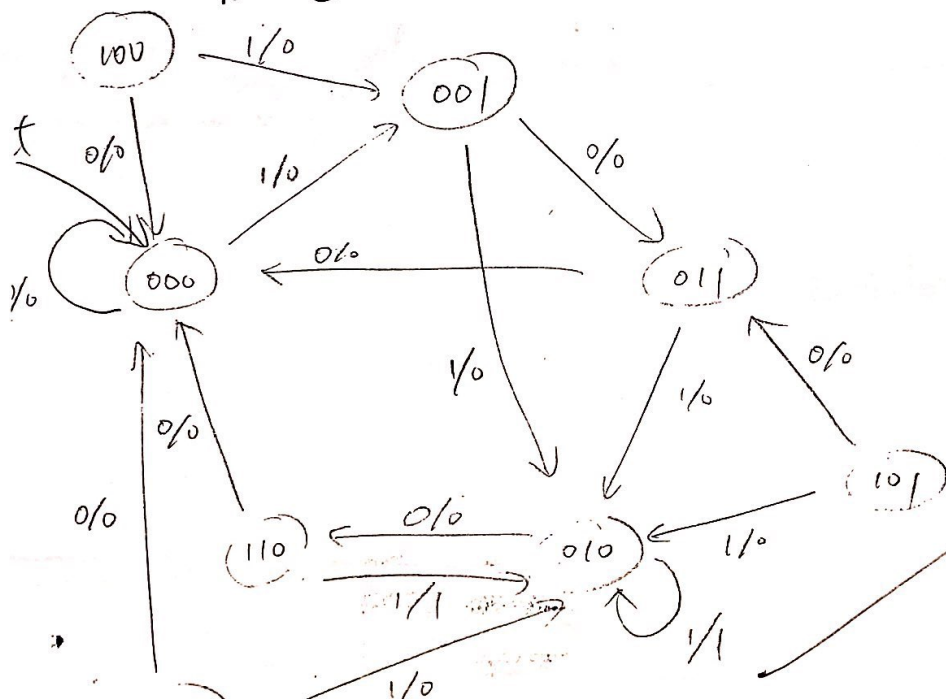
The circuit is exactly the same except the part for Y, so I add "Y new" as the output in this exercise to the previous circuit. (to delicately draw the circuit takes too much time)

(b)



(c)

It's not self-starting since there are unused states.





Date:

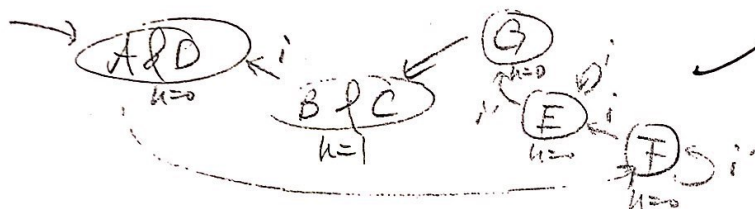
Next state

|   | A | B | C | D | E | F |
|---|---|---|---|---|---|---|
| A | X | X | X | X | X | X |
| B | X | X | X | X | X | X |
| C | X | X | X | X | X | X |
| D | X | X | X | X | X | X |
| E | X | X | X | X | X | X |
| F | X | X | X | X | X | X |

\* second

x third

Thus we find A & D, B & C are equivalent



After applying K-map, we get

| Present |    | Next |    | Output |   |
|---------|----|------|----|--------|---|
| S1      | S0 | K1   | K0 | W      | Y |
| 0       | 0  | 0    | 1  | 1      | 0 |
| 0       | 1  | 1    | 0  | 0      | 0 |
| 1       | 0  | 1    | 1  | 0      | 1 |
| 1       | 1  | 0    | 0  | 0      | 0 |

$u = s_0 s_1$   
 $u_0 = s_0$   
 $u_1 = s_1 s_0$   
 $u_2 = s_1 s_0 s_1$   
 $u_3 = s_1 s_0 s_1 s_0$

The number of zero inputs is 8  
The number of delays is 1

After applying K-map, we get

| Present |    |    | Next |   |    | Output |   |   |
|---------|----|----|------|---|----|--------|---|---|
| s2      | s1 | s0 | z    | x | h0 | w      | x | y |
| 1       | 0  | 0  | 0    | 1 | 0  | 1      | 0 | 0 |
| 0       | 1  | 0  | 0    | 0 | 1  | 0      | 1 | 0 |
| 0       | 0  | 1  | 0    | 0 | 0  | 0      | 0 | 1 |
| 0       | 0  | 0  | 1    | 0 | 0  | 0      | 0 | 0 |

After applying K-map, we get

$$\begin{aligned} W_2 &= S_1 S_1 S_1 \\ W_1 &= S_2 \\ W_0 &= S_1 \\ W &= S_2 \\ X &= S_1 \\ Y &= S_0 \end{aligned}$$

The number of gate inputs is 3  
The number of delays is 1

For one-hot encoding  
Present Next

| Fresh |    |    |    | New |     |     |     | Conf. |   |   |
|-------|----|----|----|-----|-----|-----|-----|-------|---|---|
| 13    | 12 | 81 | 50 | 113 | 112 | 111 | 110 | W     | X | Y |
| 1     | 0  | 0  | 0  | 0   | 1   | 0   | 0   | 1     | 0 | 0 |
| 0     | 1  | 0  | 0  | 0   | 0   | 1   | 0   | 0     | 1 | 0 |
| 0     | 0  | 1  | 0  | 0   | 0   | 0   | 1   | 0     | 0 | 1 |
| 0     | 0  | 0  | 1  | 1   | 0   | 0   | 0   | 0     | 0 | 0 |

After applying K-map, we get

$$\begin{aligned} V_1 &= 50 \\ V_2 &= 53 \\ V_3 &= 52 \\ V_4 &= 52 \\ V_5 &= 53 \\ V_6 &= 52 \\ V_7 &= 51 \end{aligned}$$

The number of gate inputs is  $D$   
The number of delays is  $0$



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