

VG101 — Introduction to Computer and Programming

Lab 2

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Goals of the lab

- Write clear algorithms
- Write MATLAB functions
- Use control statements in MATLAB

Ex. 1 — Algorithm, function, conditional statements, and loops

Given a continuous function f over an interval $[a, b]$ such that $\text{sign}(f(a)) \neq \text{sign}(f(b))$ find $r \in [a, b]$ such that $f(r) = 0$. The bisection method consists in dividing the interval $[a, b]$ into two sub-intervals $[a, c]$ and $[c, b]$ of equal size. Then either $f(a)$ and $f(c)$ or $f(c)$ and $f(b)$ will have different signs. In case $c = r$ we stop and return c , otherwise the process is repeated over the interval where the sign changes. The process of narrowing down the interval will only end when the error is smaller than a bound specified by the user.

1. Write a clear algorithm describing the bisection method
2. Implement the previous algorithm using a MATLAB function

Note: the degree of accuracy should be at least 0.001 (strictly positive and less than 0.001).

Ex. 2 — Input and output

Pascal's triangle is a triangular array composed of the binomial coefficients. Write a MATLAB function taking as input an integer n and which outputs n lines of Pascal's triangle in a text file. For instance in the case $n = 6$ the file should contain the following:

```
      1
     1 1
    1 2 1
   1 3 3 1
  1 4 6 4 1
 1 5 10 10 5 1
```

Hint: either generate it using the fact that each number in the triangle is the sum of the two numbers directly above it or using the functions `pascal`, `diag`, and `rot90`.

Ex. 3 — Basics on functions

Given a date Zeller's Congruence formula allows to determine the corresponding day of the week. The formula is as follows:

$$\text{day} = 1 + \left(d + \left\lfloor \frac{13m - 1}{5} \right\rfloor + y + \left\lfloor \frac{y}{4} \right\rfloor + \left\lfloor \frac{c}{4} \right\rfloor - 2c \right) \mod 7$$

where d is the day of the month (1–31), m the number of the month (from March=1 to February=12), y the year of the century (14 for 2014) and c the century minus one (20 for 2014); the value day is an integer between 1 and 7, with 1 representing Sunday. Assign January and February to previous year. Write a MATLAB function which takes as input a date in the format `[d m cy]` and returns the corresponding day of the week (e.g. on the input `[19 1 2012]` the function should return Thursday).