### **Core Maintenance**

This repository contains C++ codes and datasets for the paper.

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#### Introduction

We present efficient algorithms for maintaining  $(\alpha, \beta)$ -core (bi-core) over bipartite graphs. Our approach introduces the concept of bi-core numbers and uses them to narrow down the scope of updates caused by edge insertions and deletions. Based on this concept, we propose efficient algorithms for maintaining  $(\alpha, \beta)$ -core, for both edge insertion and edge deletion.

### **Environment**

The algorithms are implemented in C++ and compiled with the g++ compiler at -O3 optimization level. The development environment used for implementing and testing is:

• Linux version: Ubuntu 20.04.3 LTS

• Kernel version: 5.4.0-139-generic

• g++ version: 9.4.0

#### **Datasets**

We use eight large bipartite graphs, including seven real graphs (IMDB, WC, AR, DBLP, DE, DTI, WT) obtained from <u>KONECT</u> and one synthetic graph (PL) generated according to the bipartite network model[6], following the power-law distribution. You can generate PL by running the following command in the terminal:

```
    cd random
    g++ bigraph.cpp gephi.cpp main.cpp random.cpp utility.cpp -03 -o rand.o
    ./rand.o output_location 5000000 5000000 1000000000
```

Our paper contains the detailed statistics and original sources of the above datasets.

#### **Dataset format:**

- graph.meta file containing the number of vertices on each side and the number of edges.
- graph.e file containing all the edges.

#### Example:

```
graph.meta:
3 //number of vertices in U-side
3 //number of vertices in V-side
6 //number of edges

graph.e:
//U V
1 1
1 3
2 1
2 2
2 3
3 1
```

#### How to Run the Codes

#### A. Code Compilation

Both the insertion-maintenance and deletion-maintenance folders contain a Makefile. To compile the corresponding code:

```
    cd insertion-maintenance/ or cd deletion-maintenance/
    make
```

After compilation, an executable file named bicore will be generated.

### **B.** Experimentation

#### 1. Algorithms

- Recompute: the state-of-the-art bi-core decomposition algorithm.
- BiCore-Index-Ins\* (BII): the bi-core maintenance algorithm to handle an edge insertion [26].
- BiCore-Index-Rem\* (BIR): the bi-core maintenance algorithm to handle an edge deletion [26].
- Edge-Insert (EI): our proposed bi-core maintenance algorithm for handling an edge insertion.
- Edge-Delete (ED): our proposed bi-core maintenance algorithm for handling an edge deletion.
- BI-batch: the batch algorithm in [26].
- Edge-batch: our batch algorithm.

Parameter	Description
graph_path	The path of the graph.
vertex_1/vertex_2	(vertex_1, vertex_2) is the inserted or deleted edge.
insert_path/delete_path	The inserted/deleted edges list file.
edge_num	The total number of inserted and deleted edges.
U_num/V_num	The number of left/right side vertices in the graph.
α/β	(lpha,eta) is the given integer pair.
vertex	The given vertex.
is_left	Indicates whether the given vertex belongs to U or V. 1 (True) for U, 0 (False) for V.

#### 2. Preparation

Parameter of Command Line	Description	Command
BBI	Build BiCore-Index	sh BBI.sh graph_path
BBN	Compute all bi-core numbers	sh BBN.sh graph_path

### 3. Edge Insertions

3.1 Insert a specific edge ( $u_1, v_1$ )

Parameter of Command Line  Description Command
--

Parameter of Command Line	Description	Command
RCI	Recompute	sh RCI.sh graph_path vertex_1 vertex_2
BII	BiCore-Index-Ins* (BII)	sh BII.sh graph_path vertex_1 vertex_2
EI	Edge-Insert (EI)	sh EI.sh graph_path vertex_1 vertex_2

#### 3.2 Insert edges from an edge list file

Parameter of Command Line	Description	Command
RCIS	Recompute	sh RCIS.sh graph_path insert_path
BIIS	BiCore-Index-Ins* (BII)	sh BIIS.sh graph_path insert_path
(EIS)	Edge-Insert (EI)	sh EIS.sh graph_path insert_path

## 4. Edge Deletion

#### 4.1 Delete a specific edge ( $u_1,v_1$ )

Parameter of Command Line	Description	Command
RCR	Recompute	sh RCR.sh graph_path vertex_1 vertex_2
(BIR)	BiCore-Index-Rem* (BIR)	sh BIR.sh graph_path vertex_1 vertex_2
ED	Edge-Delete (ED)	sh ED.sh graph_path vertex_1 vertex_2

4.2 Delete edges from an edge list file.

Parameter of Command Line	Description	Command
RCRS	Recompute	sh RCRS.sh graph_path delete_path
BIRS	BiCore-Index-Rem* (BIR)	sh BIRS.sh graph_path delete_path
EDS	Edge-Delete (ED)	sh EDS.sh graph_path  delete_path

### 5. Batch Update

Parameter of Command Line	Description	Command
BBatch	BII-batch	sh BBatch.sh graph_path edge_num U_num V_num
EBatch	El-batch	sh EBatch.sh graph_path edge_num U_num V_num

## 6. Query

### 6.1 ( $\alpha$ , $\beta$ )-core query:

Parameter of Command Line	Description	Command
QCBI	BiCore-Index	sh QCBI.sh graph_path $\alpha$ $\beta$
QCBN	BiCore number	sh QCBN.sh graph_path $\alpha$ $\beta$

#### 6.2 community search:

Parameter of Command Line	Description	Command
QSBI	BiCore-Index	sh QSBI.sh graph_path $\alpha$ $\beta$ vertex is_left
QSBN	BiCore number	sh QSBN.sh graph_path $\alpha$ $\beta$ vertex is_left

#### 6.3 $\alpha/\beta$ -offsets query:

Parameter of Command Line	Description	Command
QOBI	BiCore-Index	sh QOBI.sh graph_path vertex is_left
QOBN	BiCore number	sh QOBN.sh graph_path vertex is_left

# **Running Example**

### 1. Toy Graph

- Number of vertices: 6, number of edges: 6
- Edge list:
  - $\circ$   $u_1$ - $v_1$
  - $\circ u_1$ - $v_3$
  - $\circ$   $u_2$ - $v_1$
  - $\circ$   $u_2$ - $v_2$
  - $\circ$   $u_2$ - $v_3$
  - $\circ u_3$ - $v_1$
- We can obtain the original bi-core numbers of all vertices:

U	V
<i>u</i> <sub>1</sub> : (1, 3), (2, 2)	v <sub>1</sub> : (1, 3), (2, 2), (3, 1)
<i>u</i> <sub>2</sub> : (1, 3), (2, 2), (3,1)	v <sub>2</sub> : (3, 1)
<i>u</i> <sub>3</sub> : (1, 3)	v <sub>3</sub> : (2, 2), (3, 1)

## 2. Edge Insertion

Suppose we want to insert edge ( $u_1, v_2$ ), we can run:

```
sh EI.sh ../data/example/ 1 2
```

The updated bi-core number of all vertices are stored in "bi-core number". The content is listed as follows:

U	V
<i>u</i> <sub>1</sub> : (1, 3), (3, 2)	<i>v</i> <sub>1</sub> :(1, 3), (3, 2)
<i>u</i> <sub>2</sub> : (1, 3), (3, 2)	v <sub>2</sub> : (3,2)
<i>u</i> <sub>3</sub> : (1, 3)	v <sub>3</sub> : (3, 2)

## 3. Edge Deletion

Suppose we want to delete edge ( $u_1, v_2$ ) after the edge insertion, we can run:

The updated bi-core number of all vertices are stored in "bi-core number". The content is listed as follows:

U	V
<i>u</i> <sub>1</sub> : (1, 3), (2, 2)	v <sub>1</sub> :(1, 3), (2, 2), (3,1)
<i>u</i> <sub>2</sub> : (1, 3), (2, 2), (3,1)	v <sub>2</sub> : (3,1)
<i>u</i> <sub>3</sub> : (1, 3)	v <sub>3</sub> : (2, 2), (3,1)