

$$\begin{aligned}
\varepsilon &\leq 8d \sqrt[2d]{\frac{\delta}{2}} \\
\Leftrightarrow \varepsilon &\leq 8d \left(\sqrt[2d]{\frac{2}{\delta}} \right)^{-1} \\
\Leftrightarrow \varepsilon &\leq 8d 2^{-\frac{1}{2d} \log(\frac{2}{\delta})} \\
\Leftrightarrow 2^{\frac{1}{2d} \log(\frac{2}{\delta})} &\geq \frac{8d}{\varepsilon} \\
\Leftrightarrow \frac{1}{2d} \log\left(\frac{2}{\delta}\right) &\geq \log\left(\frac{8d}{\varepsilon}\right) \\
\Leftrightarrow \frac{4}{\varepsilon} \log \frac{2}{\delta} &\leq \frac{8d}{\varepsilon} \log \frac{8d}{\varepsilon}
\end{aligned}$$

Then $|A| = \frac{8d}{\varepsilon} \log \frac{8d}{\varepsilon} = \max(\frac{4}{\varepsilon} \log \frac{2}{\delta}, \frac{8d}{\varepsilon} \log \frac{8d}{\varepsilon})$. Therefore, according to theorem ??, $\mathbb{P}(A \text{ is a } \varepsilon\text{-net}) \geq 1 - \delta$.

Let's denote the element of A by $a_1, a_2, \dots, a_{|A|}$. The probability that A is a subset of $MIS(G)$ is $P_A(\varepsilon)$.

$$P_A(\varepsilon) = \mathbb{P}(\forall a \in A, a \in MIS(G)) = \prod_{i=1}^{|A|} \mathbb{P}(a_i \in MIS(G)) = \prod_{i=1}^{|A|} \frac{|V(G)| \cdot c}{|V(G)|} \geq c^{|A|}.$$

Therefore the probability that A verify all the condition is $\mathbb{P}(A \subseteq MIS(G)) \mathbb{P}(A \text{ is a } \varepsilon\text{-net}) \geq (1 - \delta) c^{f(\frac{1}{\varepsilon})}$.