

Mid

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Ans. to the Ques. No : 01 :

Worst case of quick sort algorithm is  $O(n^2)$  when the picked pivot element is the smallest or largest element. The worst case time complexity of quick sort can be improved if the pivot element is the median element of the input array. The time complexity would be  $O(n \log n)$  in worst case.

Example : Let us take an array of ~~size~~ size 5

10 2

A [ 50 | 80 | 20 ]

~~A [ 50 | 40 | 30 | 20 | 10 ]~~

0 1 2 3 4

if we take last element as pivot  
ie. pivot = ~~10~~ 20

pe pseudo code for quicksort algo if

pivot is the last element of  
the array :

Partition (int arr[],

the partition process :

~~A F~~

Partition ( A, st, end)

{

if (~~i =~~

int pivot = A [end];

int i = st - 1; //index of f

for ( int j = st ; j <= end - 1 ; j++ )

{

if ( ~~A~~ [j] <= pivot )

{     i++;

swap ~~A~~ A[i] and A[j];

    i++

}

}

```
swap & A[i+1] and A[end];  
return (i+1);  
}
```

```
// quicksort algo  
quicksort (arr[], st, end).  
{ if (st < end)  
{ pi = partition (&A, st, end);  
quicksort (A, st, pi - 1);  
quicksort (A, pi + 1, end);
```

```
}
```

pseudocode for quicksort if

pivot is the median element  
of the array :

```
void quicksort (A, st, end, n)
{
    //n=size of array
    int i, j, pivot;
    if (st >= end)
        return;
    i = st;
    j = end;
    int mid = (st + end) / 2;
    pivot = A [mid];
    while (i <= j)
    {
        while (a [i] < pivot)
        {
            i++;
        }
        a [i] = a [j];
        a [j] = pivot;
        j--;
    }
}
```

```
while (a[j] > pivot) {
    j--;
}
if (i <= j)
{
    swap(a[i], a[j]);
    i++;
    j--;
}
}

← end of first while loop

// recursion
quicksort(A, st, j, n);
quicksort(A, i, end, n);
```

}

Simulation of quicksort using median as pivot element:

A	0	1	2
	50	30	20
	↑ st	↑ mid	↑ end
	↑ i		↑ ;

$$\text{pivot} = 30$$

20	30	50
↑ st	↑	↑ end
↑ i, j		

// you call quicksort for  $(A, st, i, n)$   
// call quicksort for  $(A, i, end, n)$ .

---

taking pivot as end element

A	50	30	20
	↓ st		↑ end
i = -1	↑	Pivot	
	↓ st		end pivot

swapping  $A[i+1], A[\text{end}]$

Ans. to the Ques No: 02:

Given a graph  $G$   
where  $m$  vertices,  
 $m$  edges,  
are present.

and degree of vertex  $v$  is  
 $\boxed{\deg(v)}$ .

property 1:

For an undirected graph

$$\sum \deg(v) = 2m$$

if there are  $v$  vertices in a  
graph, then ~~all~~ + summation  
of all degrees of all vertices  
is equal to the twice of  $m$ .

Proof : Each edge is counted  
twice.

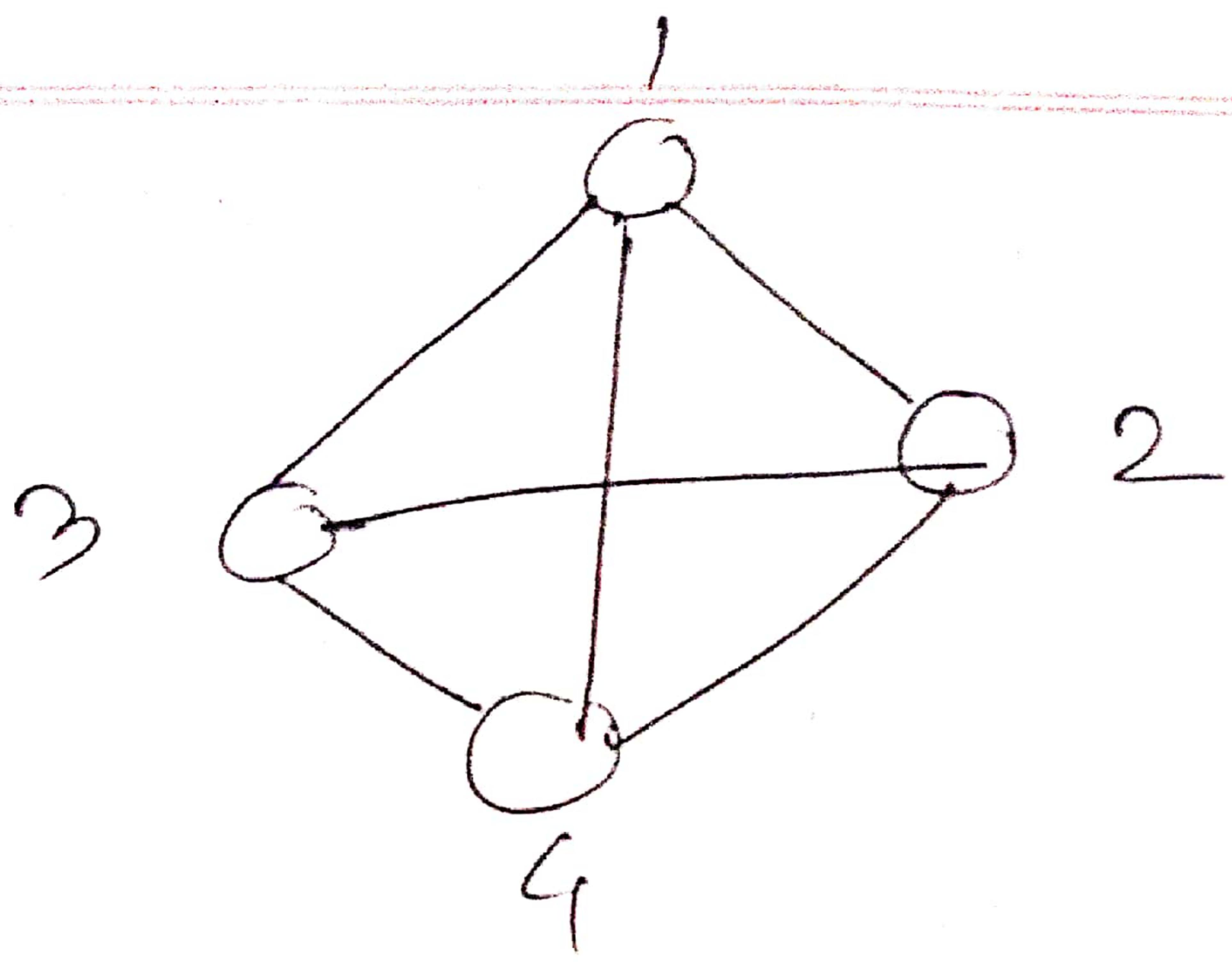


Fig 1

$$\begin{aligned}
 \deg(1) &= 2 \\
 \deg(2) &= 2 \\
 \deg(3) &= 2 \\
 \deg(4) &= 2 \\
 \text{total} &= 4 \times 2 = 8
 \end{aligned}$$

edges

$$= 2 \times m$$

$$= 2 \times 4$$

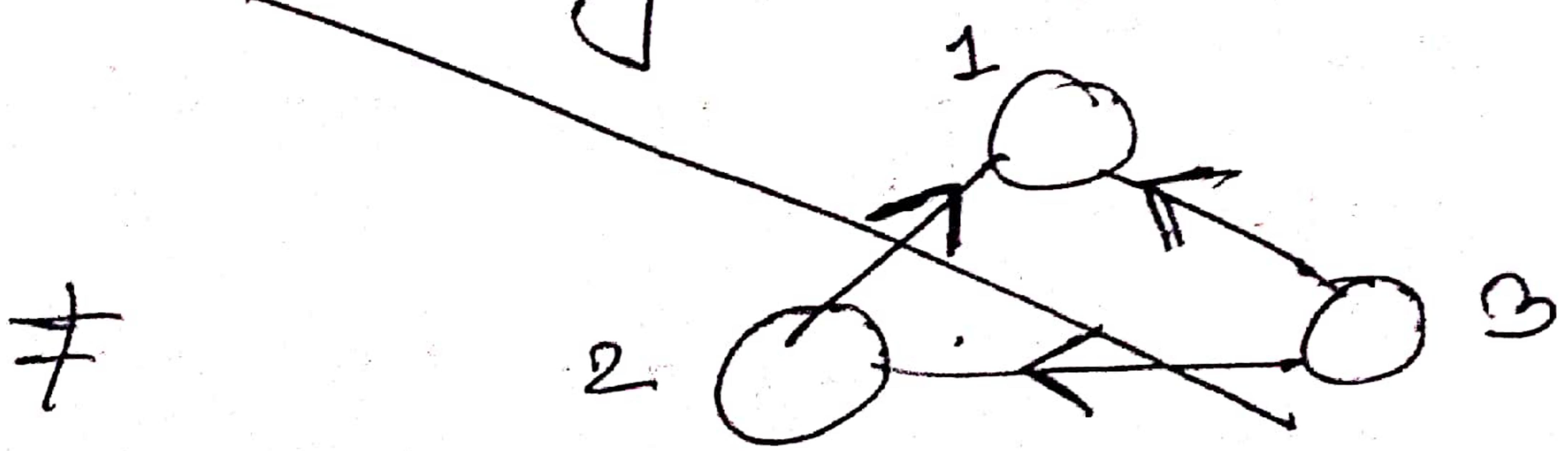
### Property 2 :

For a directed graph

$$\sum_v \text{indeg}(v) = \sum_v \text{outdeg}(v) = m$$

Proof : each edge is counted once  
for in-degree and once  
for out degree.

~~Ex: in degree of 1 in fig 1~~



Property 3 :

If  $G_i$  is a simple undirected graph, then then

$$m \leq n(n-1)/2$$

and

If  $G_i$  is a simple directed graph, then

$$m \leq n(n-1)$$

Proof : each vertex has degree at most  $(n-1)$ , then we can use property 1 & 2, to prove that.

#### Property 4 :

Let  $G_r$  be an undirected graph with  $n$  vertices and  $m$  edges.

- If  $G_r$  is connected then  $m \geq n-1$
- If  $G_r$  is a tree  $m = n-1$
- If  $G_r$  is a forest  $m \leq n-1$

Proof : Let  $G_r$  be a connected graph. Delete  $m$  edges

one by one from  $G_r$  keeping  $G_r$  connected. At last there will remain  $(m-1)$  edges.

### Ans. to the Ques. No: 03:

differences between adjacency matrix and adjacency list. here ~~suppose~~ there

<u>adjacency list</u>	<u>adjacency matrix</u>
① It is an one dimensional array, vector/linked list	① It is a 2D array. here
② takes less memory space than adjacency matrix. space complexity is $O(V+E)$	② takes more space. storage space is required in worst case is $O(V^2)$
③ To add an edge it requires $O(1)$ time	③ To add an edge it requires $O(1)$ time.
④ To remove an edge, we have traverse through all the edges in worst case. so, the time complexity is $O( E )$ .	④ To remove an edge say from $i$ to $j$ we need to make $\text{matrix}[i][j] = 0$ , which needs $O(1)$ time

⑤ time complexity for searching an edge in adj. list in  $O(|V|)$ .

⑤ time complexity for searching an element in matrix is  $O(1)$ . if we know the two vertices  $i$  and  $j$ , we can find  $\text{matrix}[i][j]$

⑥ Adding a vertex to adj list takes ~~maxt~~  $O(1)$  time

⑥ Adding a new vertex to adjacency matrix means creating a new array of  $V+1$  size. To do that we need to copy the whole matrix. So time complexity for this is  $O(|V|^2)$

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Ans. to the Ques. No: 04:

bet^n

diff., bubble sort, insertion sort, selection  
sort, merge sort and quick sort:

~~void~~

- ① time complexity of bubble sort (if not optimized), is  $O(n^2)$  in best case, worst case and average case. but if the algo is optimized, then the worst case complexity is improved by  $O(n)$ . Bubble sort can be used for small set of size of arrays.
- ② time complexity for insertion sort selection sort is  $O(n^2)$  in worst case, best case and average case.

~~time complexity of~~

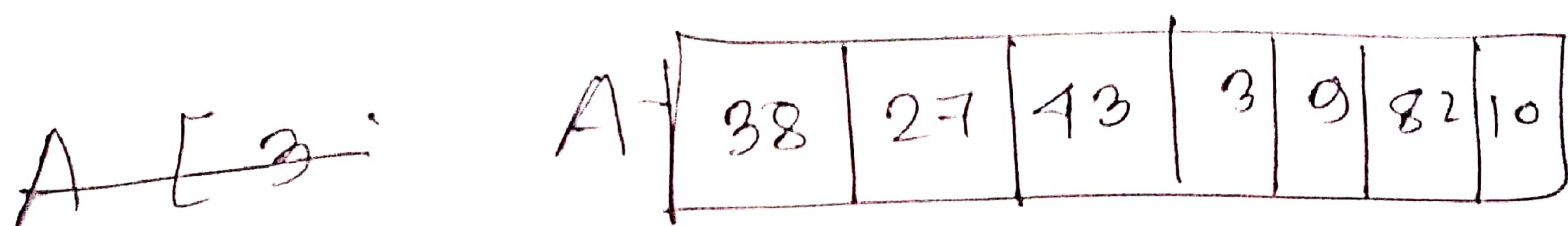
③ Insertion sort is  $O(n^2)$  is worst case. and in best case, time complexity is  $O(n)$

④ Time complexity of merge sort is  $O(n \log n)$  is best, worst and average case.

⑤ Time complexity of quick sort is  $O(n \log n)$  is best case. And in worst case, if the pivot is the end element, then the time complexity is  $O(n^2)$ . and if the pivot is median element, time complexity is  $O(n \log n)$

for large data sets, mergesort is used.

Ans. to the Ques. No: 05:



mergesort in A : n = size = 7

