Primitive Data Types

"Elementary Elements"

Prerequisite: None

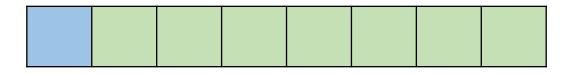
Primitive Data Types

- Char
- Integer
- Float
- Double

- Array
- Multidimensional Array

char Data Type

8 bit



1 sign bit

7 bit data

-128 to 127

Code	Char	Code	Char	Code	Char	Code	Char
0128	€	0160		0192	À	0224	à
0129	_	0161	i	0193	Á	0225	á
0130	,	0162	¢	0194	Â	0226	â
0131	f	0163	£	0195	Ã	0227	ã
0132	77	0164	×	0196	Ä	0228	ä
0133		0165	¥	0197	Å	0229	å
0134	†	0166	- 1	0198	Æ.	0230	æ
0135	‡	0167	§	0199	Ç	0231	Ç
0136	^	0168		0200	È	0232	è
0137	%。	0169	©	0201	É	0233	é
0138	_	0170	-	0202	Ê	0234	ê
0139	<	0171	«	0203	Ë	0235	ë
0140	Œ	0172	_	0204	Ì	0236	ì
0141	_	0173	-	0205	Í	0237	í
0142	_	0174	8	0206	Î	0238	î
0143	_	0175	-	0207	Ϊ	0239	ï
0144	_	0176	۰	0208	Ð	0240	ð

char Range

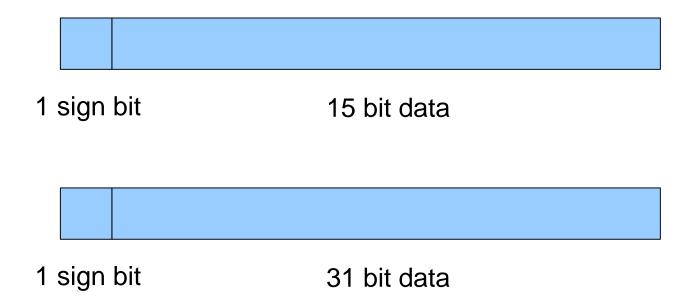
8 bit

8 bit data = 2^8 = 256 characters

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0135	‡	0167	§	0199	Ç	0231	Ç
0136	^	0168		0200	È	0232	è
0137	‰	0169	©	0201	É	0233	é
0138	_	0170	•	0202	Ê	0234	ê
0139	<	0171	«	0203	Ë	0235	ë
0140	Œ	0172	_	0204	Ì	0236	ì
0141	_	0173	-	0205	Í	0237	í
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Memory Allocation for int

16 or 32 bit



Memory Allocation for int

16 bit or 32 bit

16 bit range = -32,767 to 32,767



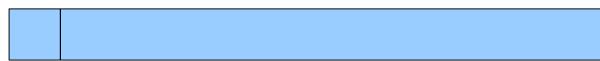


1 sign bit

15 bit data

32 bit range =
$$-2,14,74,83,647$$
 to $2,14,74,83,647$

31 30... ...0

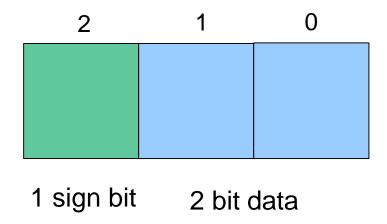


1 sign bit

31 bit data

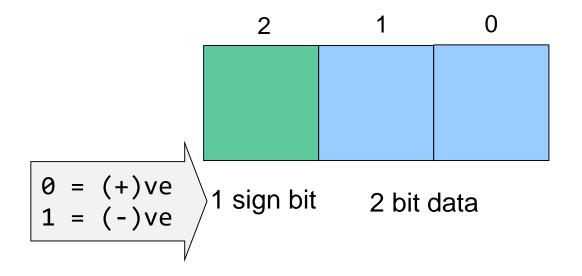
Where does this range come from?

Suppose int occupies only 3 bits



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Suppose int occupies only 3 bits



Understanding 2s complement

How to perform 2s complement

1.	Take binary representation	101
2.	Take 1s complement (Invert all bits)	010
3.	Add 1	011

Suppose int occupies only 3 bits

Suppose int occupies only 3 bits

- 1 00
- 1 01
- 1 10
- 1 11

Suppose int occupies only 3 bits

1 00

-4

1 01

-3

1 10

-2

1 11

-1

Suppose int occupies only 3 bits

Binary	/
--------	---

0 00

0 01

0 10

0 11

1 00

1 01

1 10

1 11

Decimal

+0

+1

+2

+3

-4

-3

-2

-1

3 bit = 2^3 = 8 numbers

When 2s complement is used:

4 positive: 0, 1, 2, 3

4 negative: -1, -2, -3, -4

Reviewing the ranges

Data-type	Size in bits	Range
int	16 or 32	-32,767 to 32,767
char	8	-127 to 127

Source: C++: The Complete Reference, 4th Edition (Herb Schldt, page 15)

Why do we use 2s complement instead of just flipping the sign bit?

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Because otherwise it would produce minus zero (-0)

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So the range of 16 bit int is from -32768 to 32767

32 bit memory

31 30...
 exponent mantissa
 1 bit 8 bit 23 bit

IEEE-754 floating-point standard

31	30	0
	exponent	mantissa
1 bit	8 bit	23 bit

IEEE-754 floating-point standard

31 30... ...0

exponent mantissa

1 bit 8 bit 23 bit

Suppose we have to store 10.375

1. Convert to Binary (=1010.011)

IEEE-754 floating-point standard

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[we had written e+3 because we have moved the point 3 times on the right]

IEEE-754 floating-point standard

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1 bit	8 bit	23 bit

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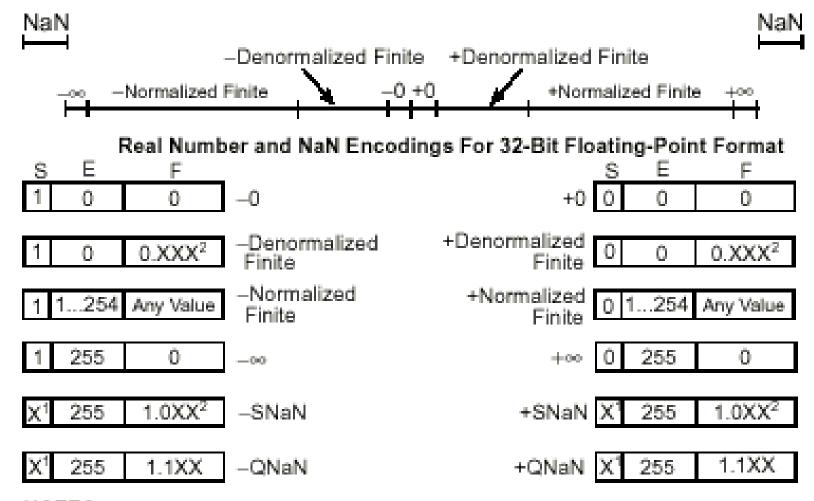
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	0	10000010	<u>010</u> 011and rest 17 zero
1 bit		8 bit	23 bit

Exercise

Convert 15.875 into IEEE-754 floating-point standard

Special Float Values



NOTES:

- Sign bit ignored.
- Fractions must be non-zero.

Memory Allocation of double

64 bit memory

63 62...

	exponent	mantissa
1 bit	11 bit	52 bit

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- 1.<u>010</u>011e+3
- 3. Now the value <u>after</u> the floating point is the mantissa (010011)
- 4. To find the exponent, add 1023 with 3 (=1026) and convert it to binary (=10000000010)
- 5. The sign bit is 0 for +

	0	10000000010	<u>010</u> 011and rest 46 zero
1 bit		11 bit	52 bit

Four modifers.

- 1. signed
- 2. unsigned
- 3. long
- 4. short

For char

For char

- 1. signed char (7 bit)
- 2. unsigned char (8 bit)

See Chapter 4.1 of Teach Yourself C, 3rd edition by Herb Schildt for size and range

For int

- 1. signed int
- 2. unsigned int
- 3. short int
- 4. long int
- 5. unsigned short int
- 6. unsigned long int

For float

No modifier

(Previously, long float was considered double. But it is obsolete in ANSI C)

See Chapter 4.1 of Teach Yourself C, 3rd edition by Herb Schildt for size and range

For double

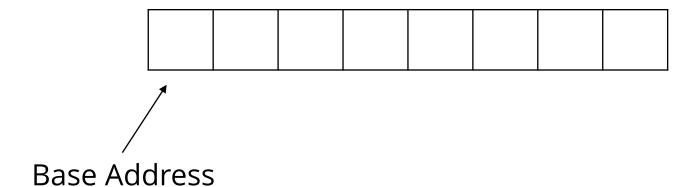
```
long double (10 byte: 1_sign+15_exp+64_man)*
short double (Same as double)
```

*In this case, exponent bias is 16383

See Chapter 4.1 of Teach Yourself C, 3rd edition by Herb Schildt for size and range

Array

Contagious memory location



Row-major order

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

Column-major order

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

- A 2D array is stored in the computer's memory one row following another.
- 2. The address of the first byte of memory is considered as the memory location of the entire 2D array.
- 3. Knowing the address of the first byte of memory, the compiler can easily compute to find the memory location of any other elements in the 2D array provided the number of columns in the array is known.

If each data value of the array requires B bytes of memory, and if the array has C columns, then the memory location of an element such as score[m][n] is (m*c+n)*B from the address of the first byte.

- 4. Note that to find the memory location of any element, there is no need to know the total number of rows in the array, i.e. the size of the first dimension. Of course the size of the first dimension is needed to prevent reading or storing data that is out of bounds.
- 5. Again one should not think of a 2D array as just an array with two indexes. You should think of it as an array of arrays.
- 6. Higher dimensional arrays should be similarly interpreted. For example a 3D array should be thought of as an array of arrays of arrays. To find the memory location of any element in the array relative to the address of the first byte, the sizes of all dimensions other than the first must be known.

int array1[3][2] = $\{\{0, 1\}, \{2, 3\}, \{4, 5\}\};$

In memory looks like this:

012345

exactly the same as:

int array2[6] = $\{0, 1, 2, 3, 4, 5\}$;

0	1
2	3
4	5

array1[0][][]: {{0, 1}, {2, 3}, {4, 5}};

array1[1][][]: {{6, 7}, {8, 9}, {10, 11}};

0	1
2	3
4	5

6	7
8	9
10	11