

Conflict Serializability Precedence Graph

T ₁	T ₂
read(<i>A</i>) $A := A - 50$ write(<i>A</i>)	read(<i>A</i>) $temp := A * 0.1$ $A := A - temp$ write(<i>A</i>)
read(<i>B</i>) $B := B + 50$ write(<i>B</i>)	read(<i>B</i>) $B := B + temp$ write(<i>B</i>)

Schedule-3

T_1	T_2
$\text{read}(A)$ $A := A - 50$ $\text{write}(A)$	$\text{read}(A)$ $\text{temp} := A * 0.1$ $A := A - \text{temp}$ $\text{write}(A)$
$\text{read}(B)$ $B := B + 50$ $\text{write}(B)$	$\text{read}(B)$ $B := B + \text{temp}$ $\text{write}(B)$

Schedule-3

T_1
 T_2

T_2
 T_1

Serial

T_1	T_2
$\text{read}(A)$ $A := A - 50$ $\text{write}(A)$	$\text{read}(A)$ $\text{temp} := A * 0.1$ $A := A - \text{temp}$ $\text{write}(A)$
$\text{read}(B)$ $B := B + 50$ $\text{write}(B)$	$\text{read}(B)$ $B := B + \text{temp}$ $\text{write}(B)$

Schedule-1

T ₁	T ₂
read(A) $A := A - 50$ write(A)	read(A) $temp := A * 0.1$ $A := A - temp$ write(A)
read(B) $B := B + 50$ write(B)	read(B) $B := B + temp$ write(B)

Schedule-3

T ₁	T ₂
	read(A) $temp := A * 0.1$ $A := A - temp$ write(A)
read(A) $A := A - 50$ write(A)	read(B) $B := B + temp$ write(B)
read(B) $B := B + 50$ write(B)	

Schedule-2

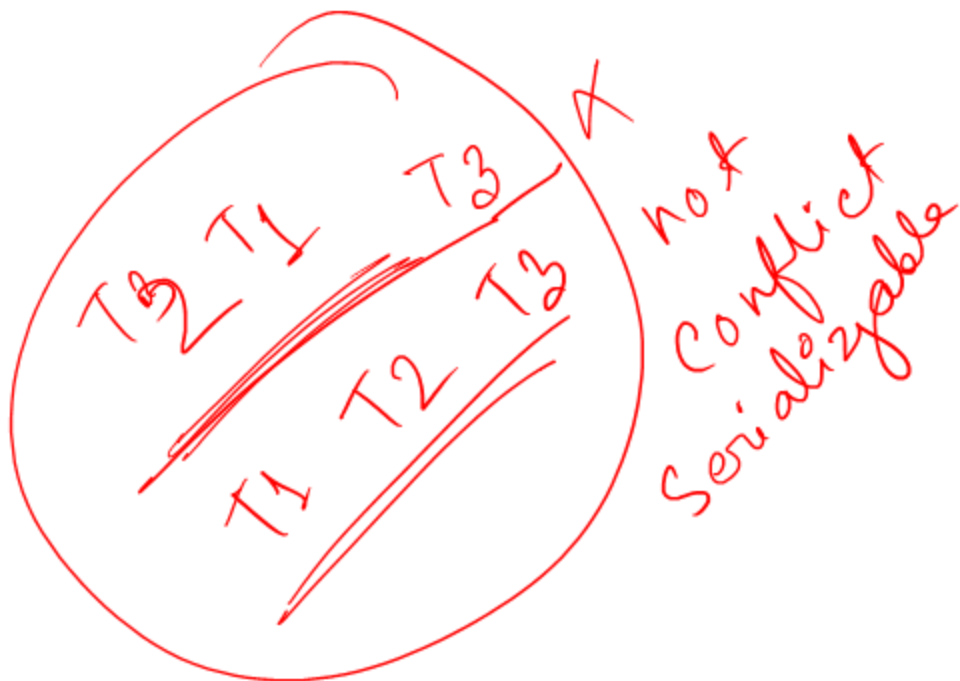
T_1	T_2
read(A) $A := A - 50$	read(A) $temp := A * 0.1$ $A := A - temp$ write(A) read(B)
write(A) read(B) $B := B + 50$ write(B)	$B := B + temp$ $write(B)$

Schedule-4

not conflict
 Serializable

T1	T2	T3
Read(A)		
	Read(B)	
	Write(A)	
Write(A)		
		Write(A)

Schedule-A



Testing of Serializability

The set of edges consists of all edges $T_i \rightarrow T_j$ for which one of three conditions holds:

1. T_i executes $\text{write}(Q)$ before T_j executes $\text{read}(Q)$.
2. T_i executes $\text{read}(Q)$ before T_j executes $\text{write}(Q)$.
3. T_i executes $\text{write}(Q)$ before T_j executes $\text{write}(Q)$.



Precedence graph — a direct graph where the vertices are the transactions.

Precedence Graph

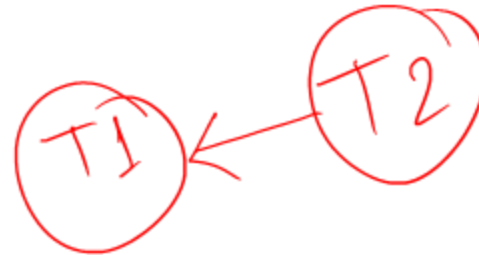
T_1	T_2
read(A) $A := A - 50$ write(A) read(B) $B := B + 50$ write(B)	read(A) $temp := A * 0.1$ $A := A - temp$ write(A) read(B) $B := B + temp$ write(B)



Schedule-1

Precedence Graph

T_1	T_2
read(A) $A := A - 50$ write(A) read(B) $B := B + 50$ write(B)	read(A) $temp := A * 0.1$ $A := A - temp$ write(A) read(B) $B := B + temp$ write(B)

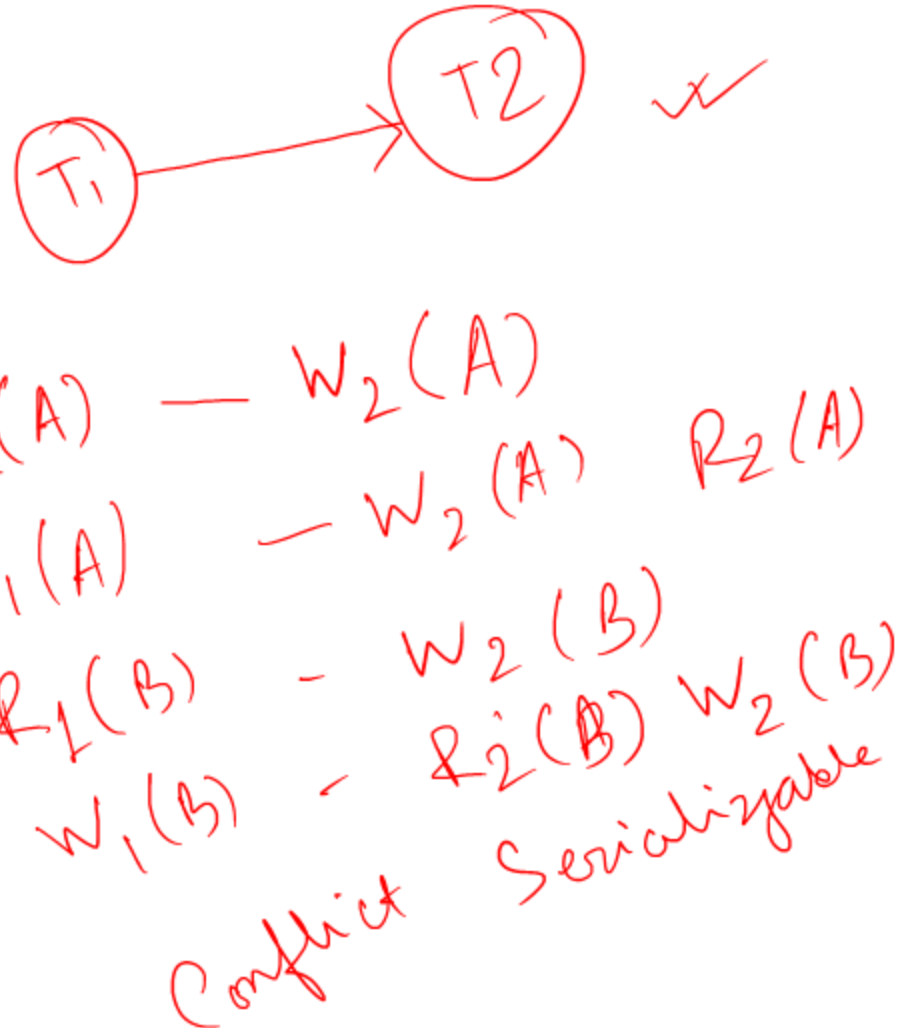


Schedule-2

Precedence Graph

T ₁	T ₂
read(A) A := A - 50 write(A) ✓	read(A) ✓ temp := A * 0.1 A := A - temp write(A) ✓
read(B) ✓ B := B + 50 write(B) ✓	read(B) B := B + temp write(B)

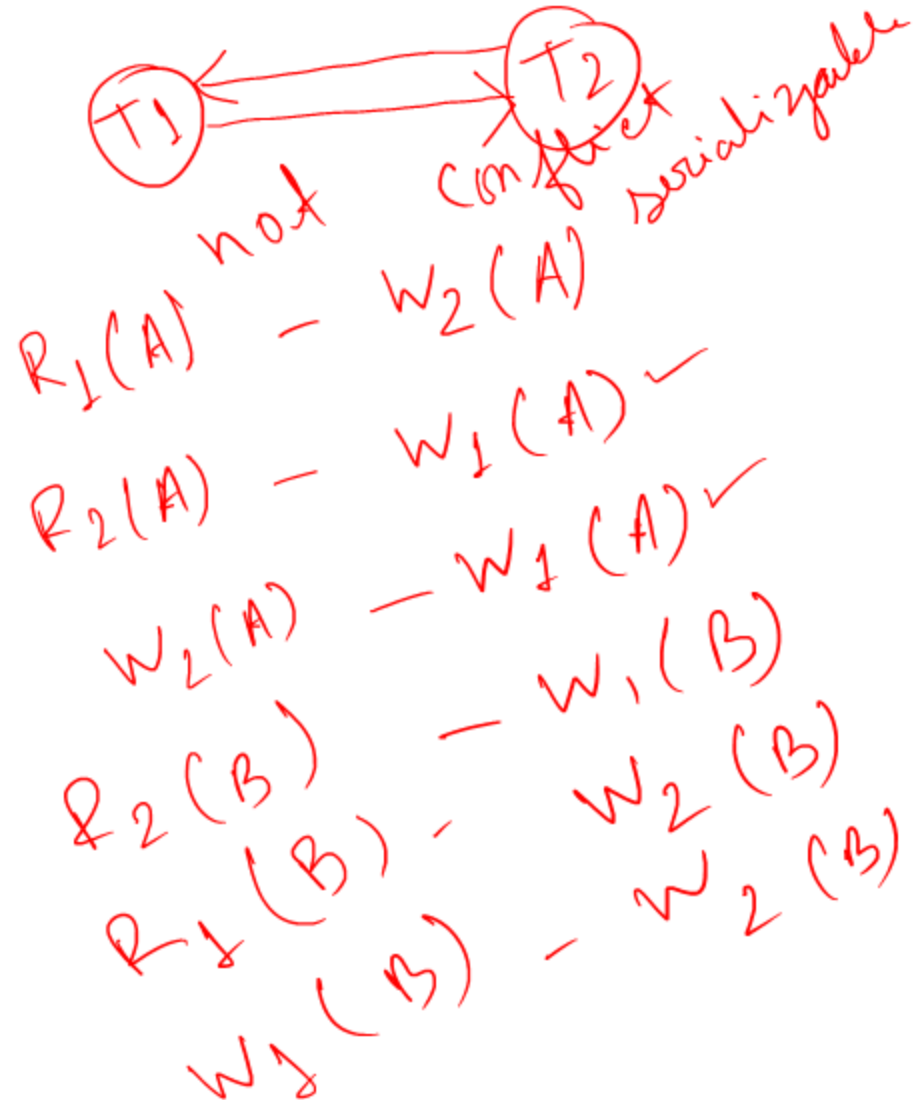
Schedule-3



Precedence Graph

T_1	T_2
$\text{read}(A)$ ✓ $A := A - 50$	$\text{read}(A)$ ✓ $\text{temp} := A * 0.1$ $A := A - \text{temp}$ $\text{write}(A)$ ✓ $\text{read}(B)$ ✓
$\text{write}(A)$ ✓ $\text{read}(B)$ ✓ $B := B + 50$ $\text{write}(B)$ ✓	$B := B + \text{temp}$ $\text{write}(B)$ ✓

Schedule-4

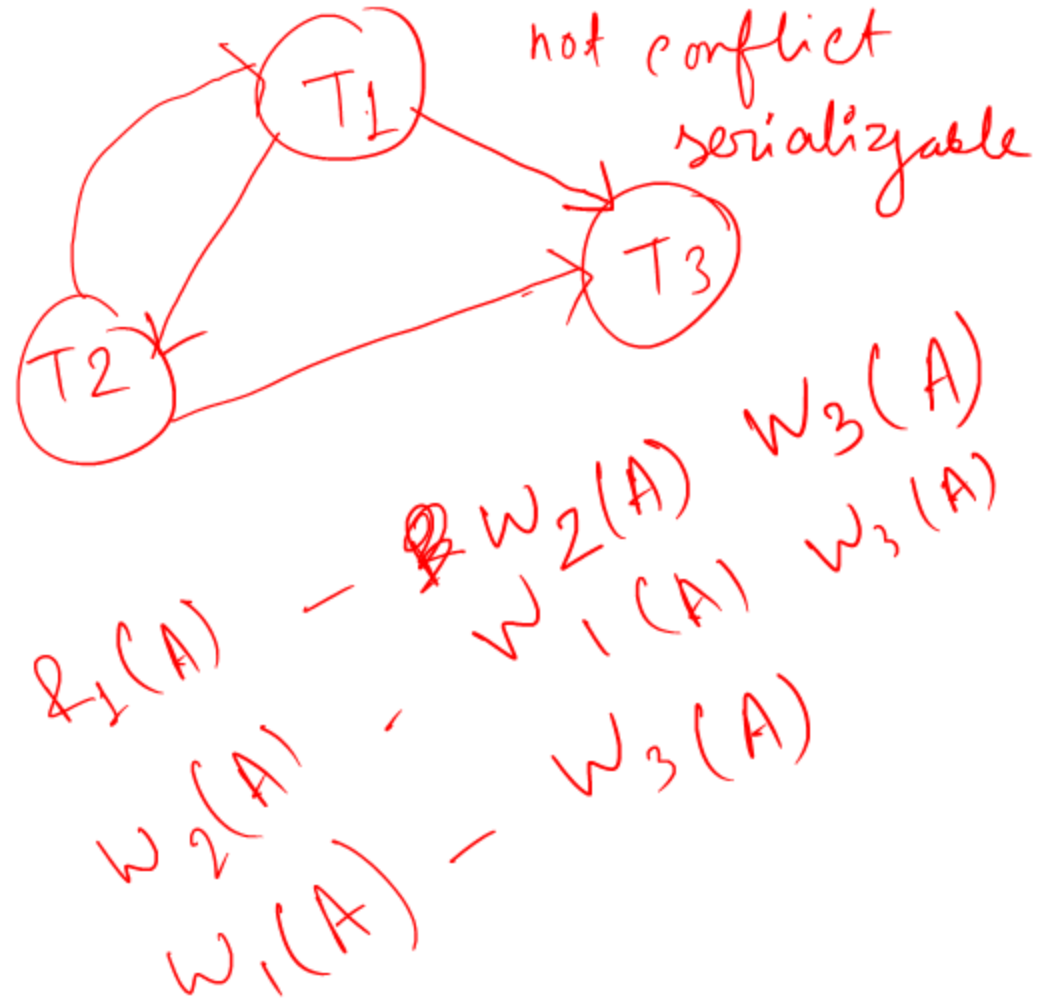


Precedence Graph

Cycle (DFS)

T1	T2	T3
Read(A)		
	Read(B)	
	Write(A)	
Write(A)		
		Write(A)

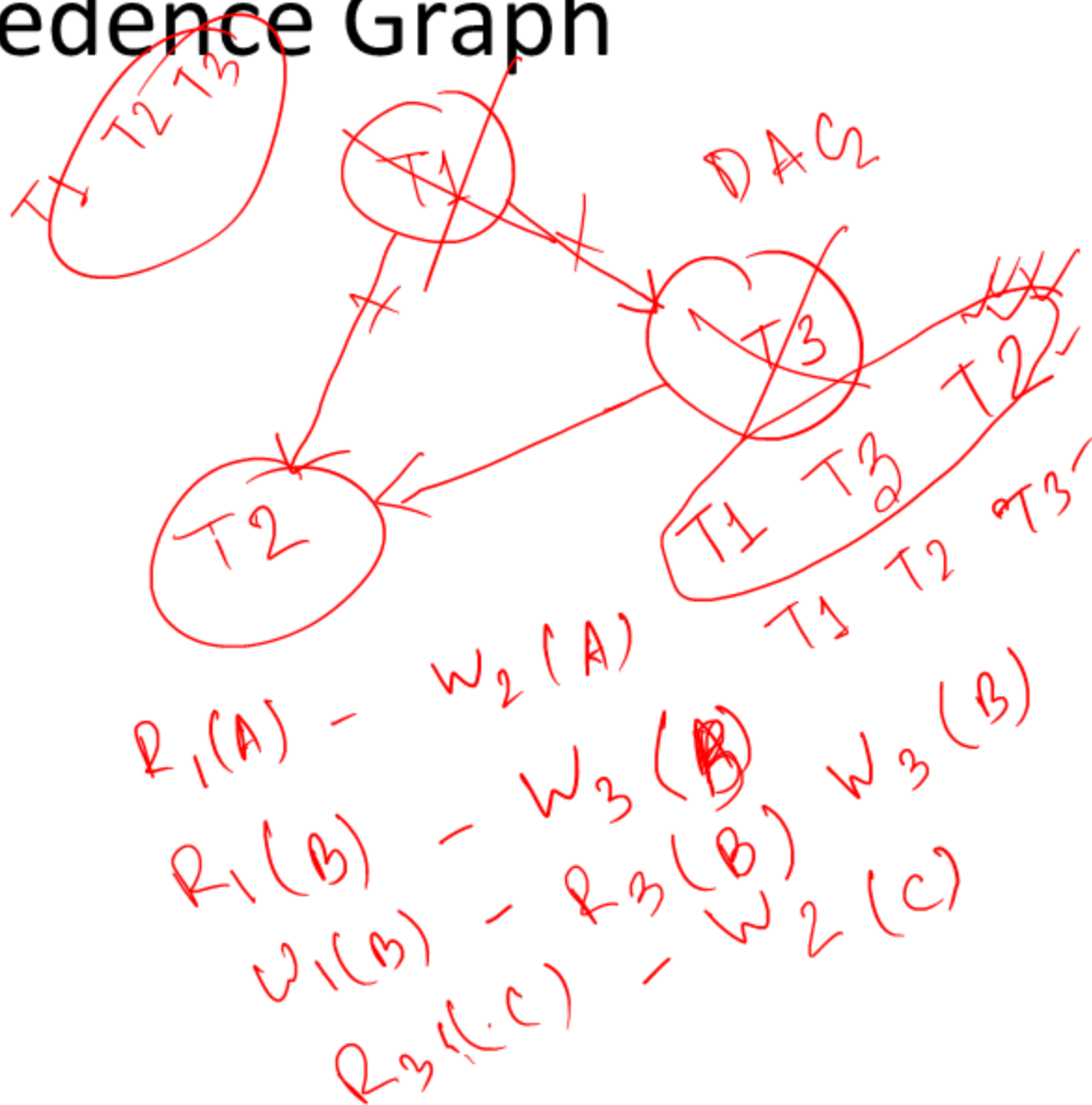
Schedule-A



Conflict
Serializable

T1	T2	T3
R(A)		
R(B)		
W(B)	R(A) R(C)	
		R(B) R(C) W(B)
	W(A)	
	W(C)	

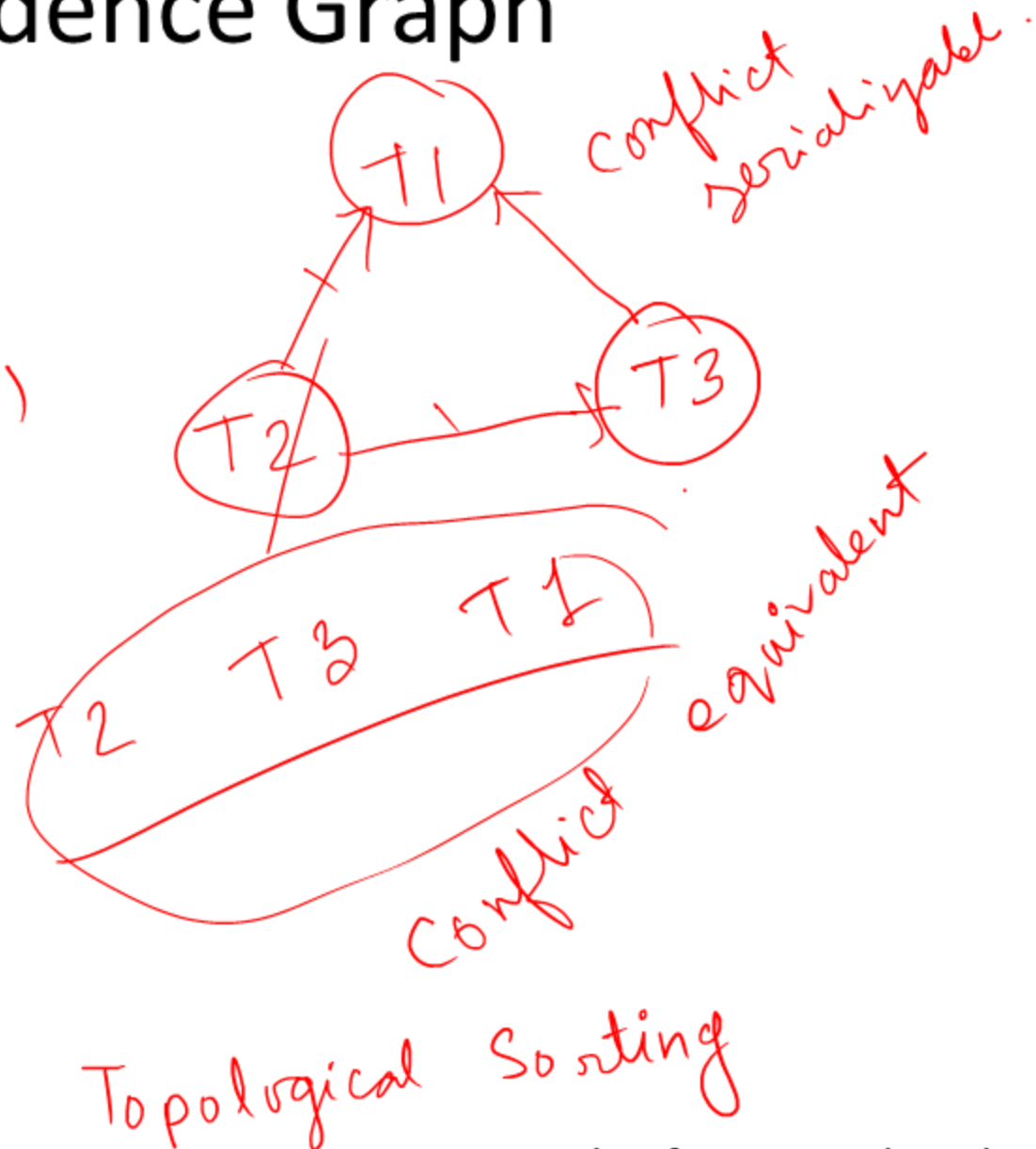
Schedule-B



Precedence Graph

T1	T2	T3
R(A)		
		R(B)
		R(A) - W₁(A)
	R(B) - W ₃ (B)	
	R(C) - W ₁ (C)	
		W(B)
	W(C) - W ₁ (A)	
R(C)		
W(A)		
W(C)		

Schedule-C



Thank You