

Suffix Array:

$S_1 = \overset{0}{B} \overset{1}{A} \overset{2}{N} \overset{3}{A} \overset{4}{N} \overset{5}{A}$

ABANAN

~~ANABAN~~

5	A	✓	→ (-)
3	ANA	✓	→ 1
1	ANANA	↔	3
0	BANANA	↔	0
4	NANA	✓	→ 0
2	NANA	✓	→ 2

$O(N^2 \log N)$

$O(N (\log N)^2)$

$O(N \cdot \log N)$

$O(N)$

$SA[] \rightarrow \{5, 3, 1, 0, 4, 2\}$

$LCP[] \rightarrow \{0, 1, 3, 0, 0, 2\}$

$LCP[i] = LCP \text{ of } (suf_i, suf_{i+1})$

P1: Given a string S , find the minimum cyclic shift.
that represents the lex... smallest string.

$S_1 = \textcircled{B}ANANA$

↳ ANANAB ✓

↳ NANABA ✓

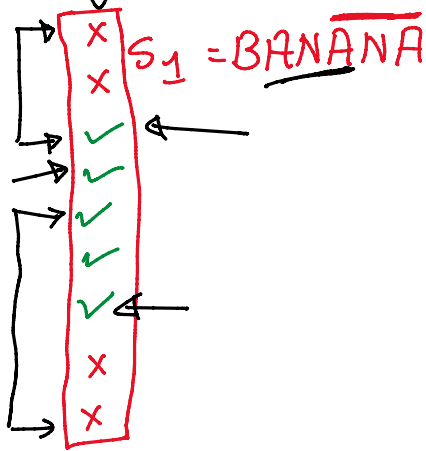
↳ ANABAN ✓

↳ NABANA ✓

↳ ABANAN ✓

P2: Given a string S of length N , and some query
... find out whether Q exists in S as a

P2 Given a string S and a set of strings Q_i , find out whether Q_i exists in S as a substring.



\checkmark ANA
 \checkmark ANANA
 \times BANANA
 \times NA
 \times NANA

$$|Q_i| \log |S|$$

$$\sum \text{len}(Q_i) \leq N$$

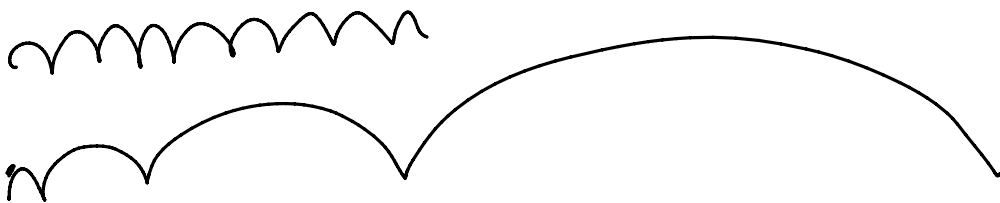
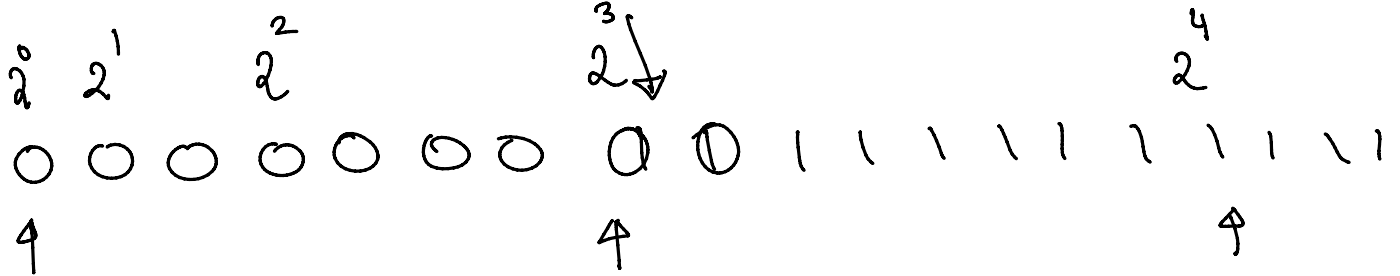
$$\text{len}(S) \leq N$$

$$1 \leq N \leq 10^6$$

$$|Q_i| \log |S|$$

$$\Rightarrow \log |S| \cdot (|Q_1| + |Q_2| + \dots + |Q_q|)$$

$$\Rightarrow N \log N$$



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P3 Find longest substring that occurs $\geq k$ times.

$S = \text{ABC}$ BANANA $\begin{matrix} B \\ A \end{matrix}$ $\begin{matrix} AN \\ NA \end{matrix}$ $k=3$ Leq

$S \rightarrow \overline{BANANA}$

$\frac{6 \times 7}{2} = 21 - (1 + 3 + 2)$
 $= 21 - 6$
 $= 15$

$K=3$

A
 A NA
 A NA NA
 BANANA
 NA
 NA NA

Lep
 0
 1
 3
 0
 0
 2

$k-1$

Monotonic Deque

$p4$

$ab \quad c \quad ab$

a ab
 b be
 c ca

1 ~ 2
 x
 z
 ad
 yy
 p
 ap

$26^1 + 26^2 - 6 = 696$

$\rightarrow L \quad R$
 $26 + \dots + 26 - x =$

$(x_1 \quad x_2 \quad \dots \quad x_p)$

$(y_1 \quad y_2 \quad \dots \quad y_q)$

$a + a + \dots + a$

a

$$\frac{1 \cdot n}{p}$$

$$\frac{1}{q}$$

$$O(pq) \rightarrow O(p \log q q)$$