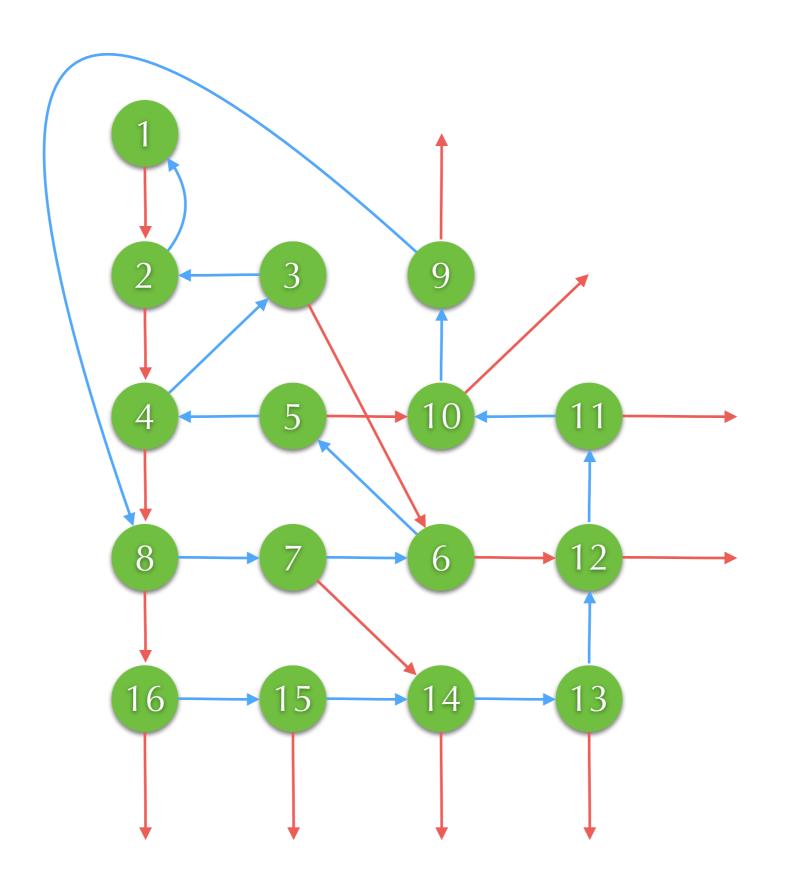
State Space Search

Learn from Example: CodeForces 520B

- ▶ A device initially displays an integer n>o.
- ▶ Red button doubles the displayed number
- ▶ Blue button decrease the number by 1
 - Cannot be clicked when the device displays 1.
- ▶ Question: given another integer m, how many clicks are required to change the displayed number into m?

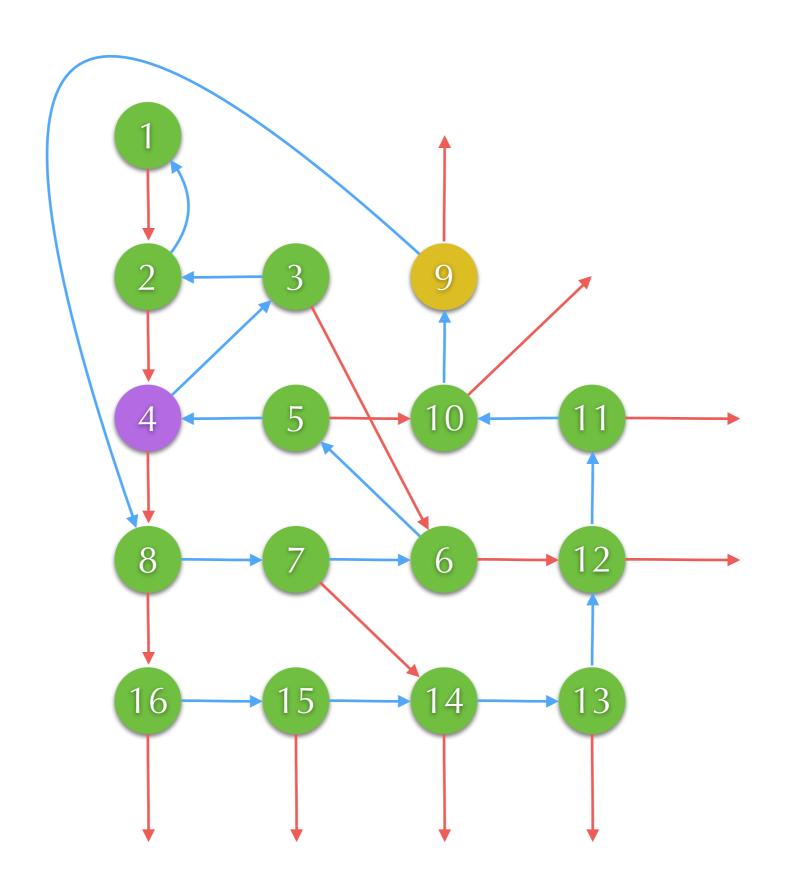
State Space

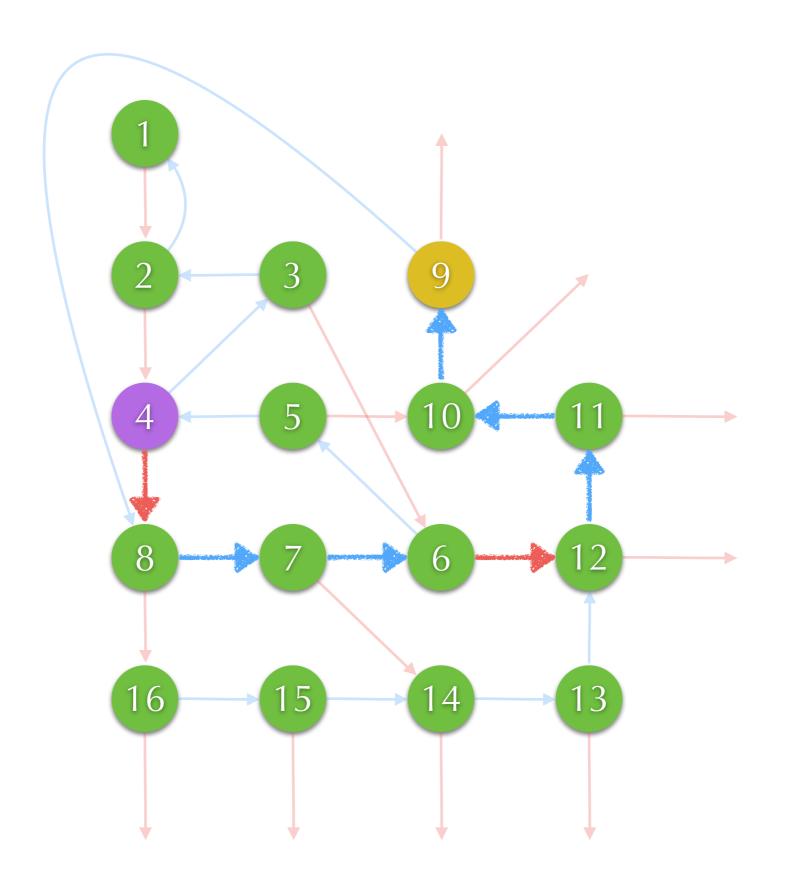
- ▶ State: the displayed number
- State space: set of all possible displayed numbers
 - Note: not necessarily finite!
- **▶** Transition
 - Action: clicking a button
 - Result: the new number
 - ▶ Cost: 1 (not necessarily uniform)

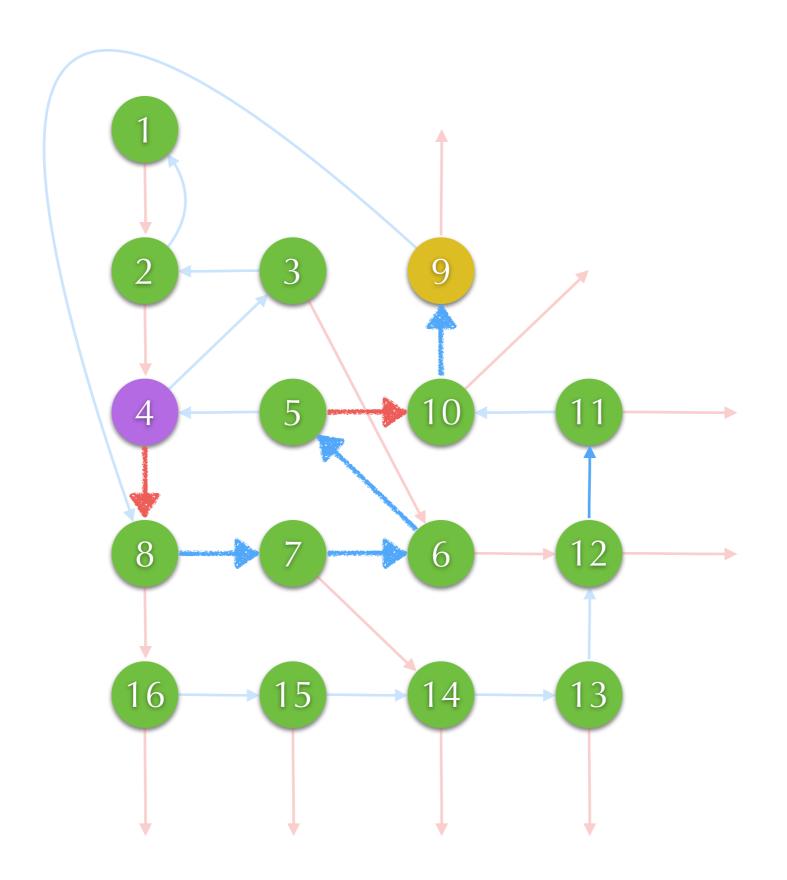


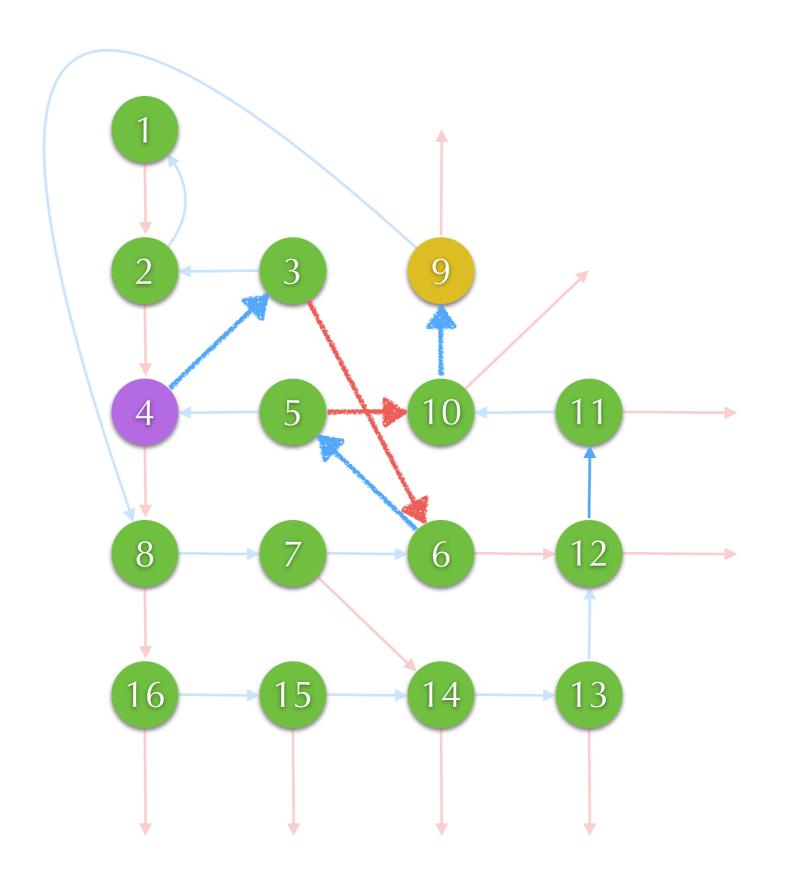
State Space Search

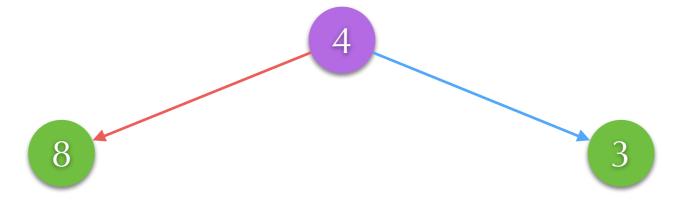
- Initial state
 - ▶ The initially displayed number n
- ▶ Goal state
 - ▶ The desired number m
- Find a sequence of transition from the initial state to the goal state.
- Sometimes there are many goal states
 - Ex: finding all states satisfying certain criteria.

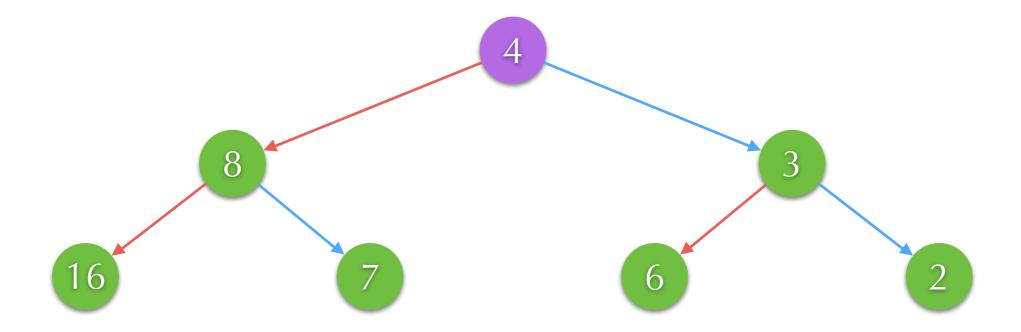


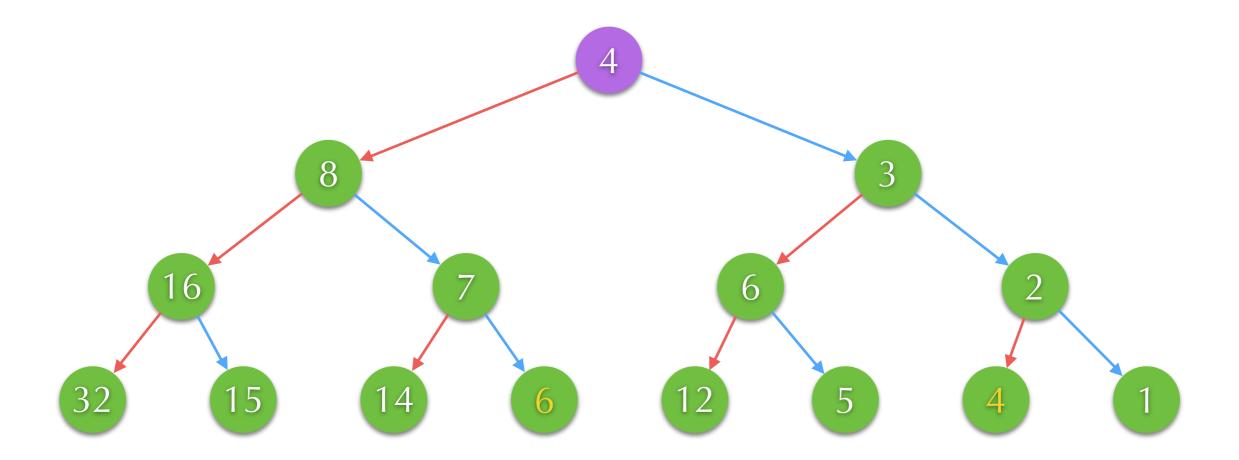


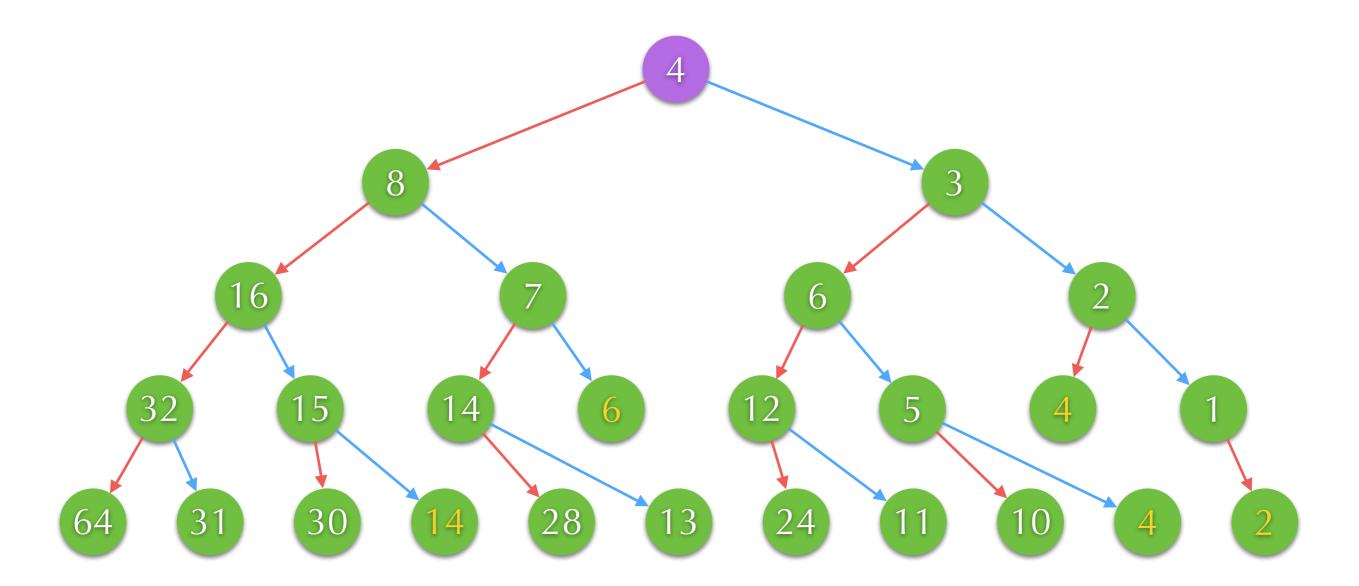


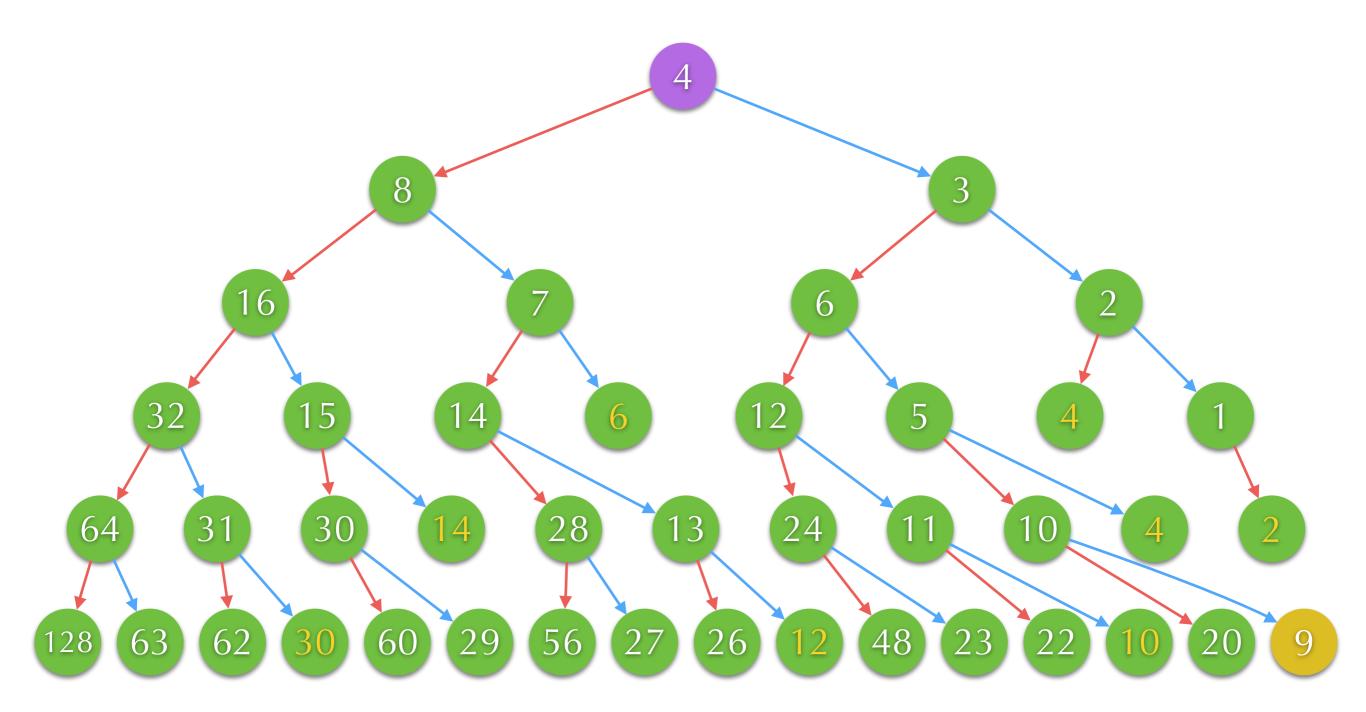




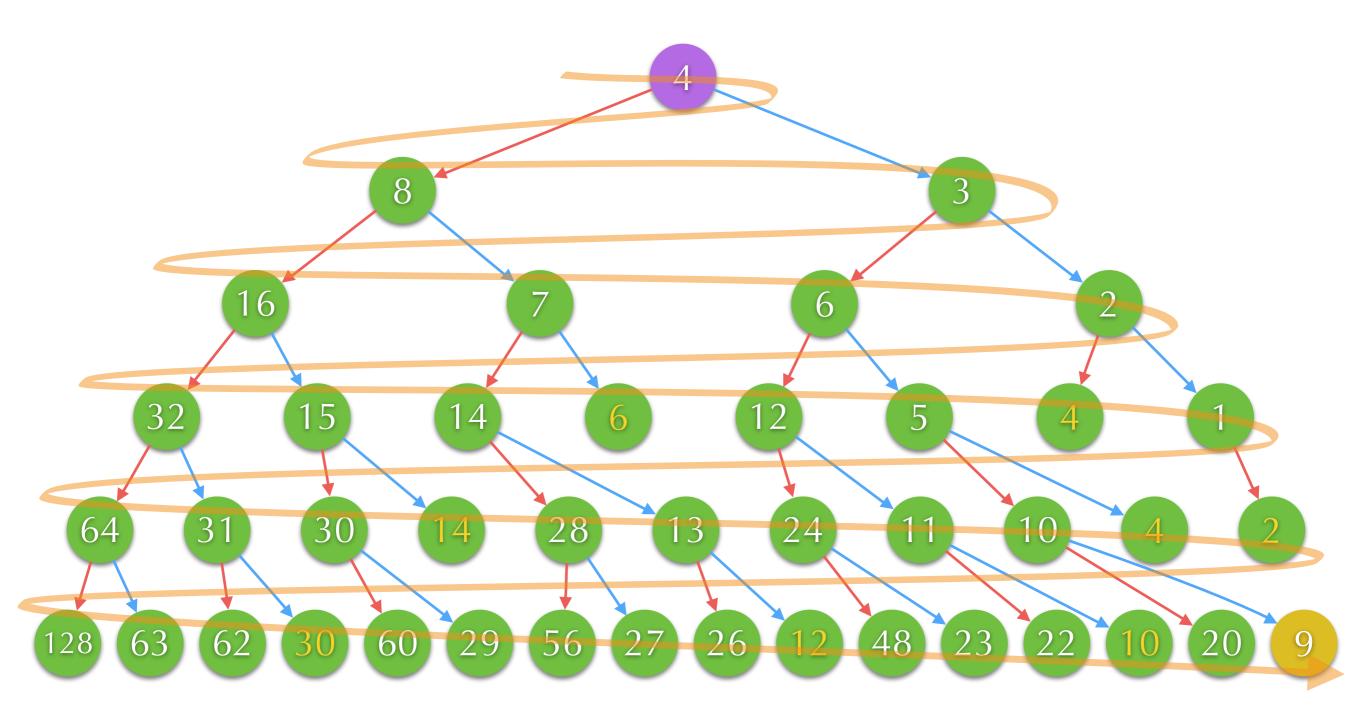








Breadth First Search

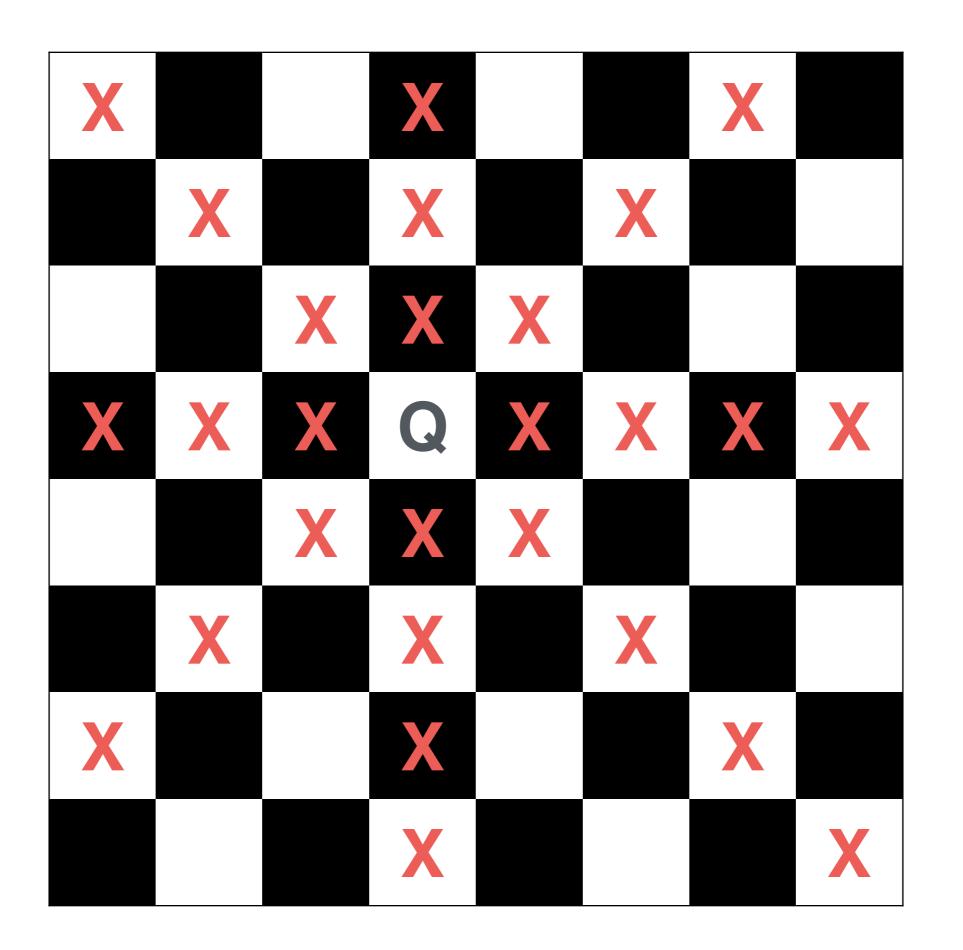


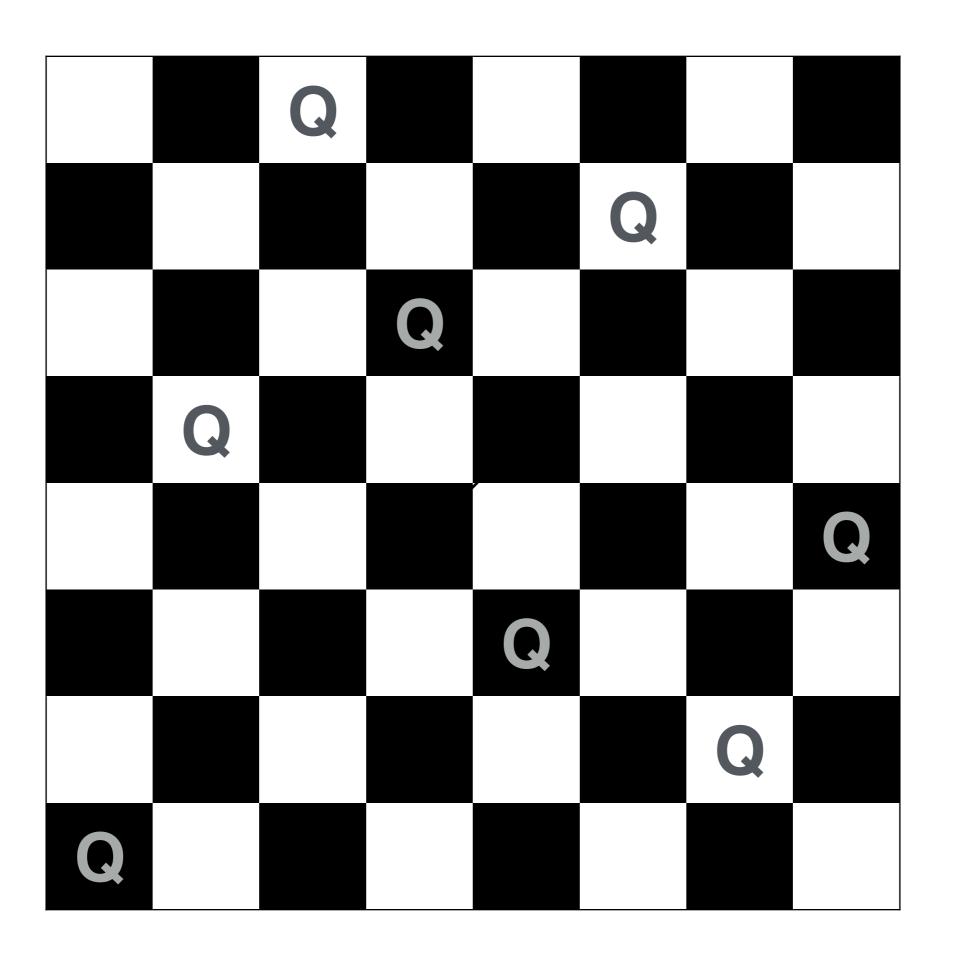
Breadth First Search

- Pros
 - Easy to implement
 - Can reach the goal state with minimum transitions
- **▶** Cons
 - May consume a lot of memory
 - May visit too many states

Learn from Example: n Queens Problem

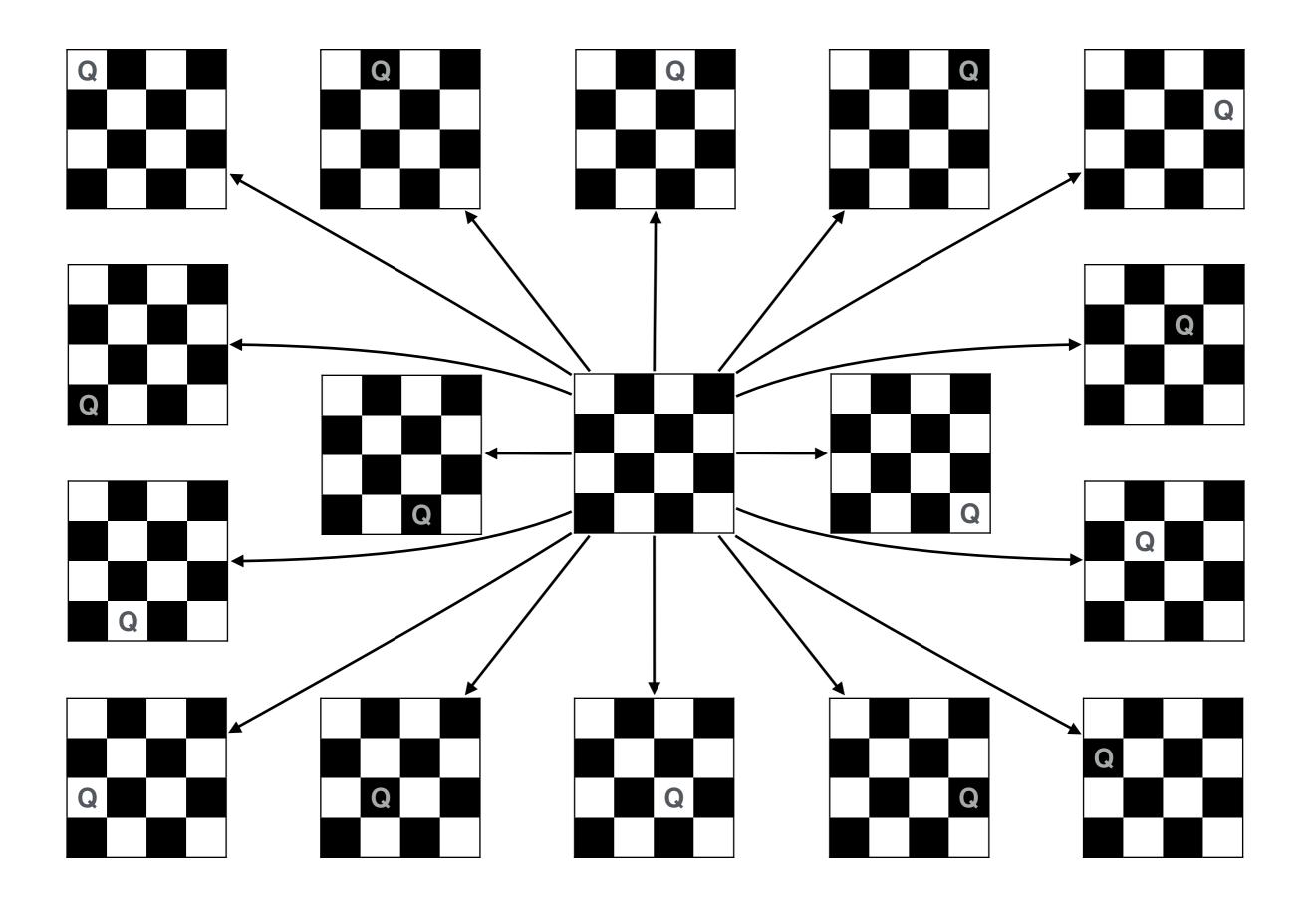
- Queen can move any number of squares vertically, horizontally, or diagonally.
- Place queens on an n-by-n chess board. No two queens can take one another.
- Various questions:
 - ▶ How many queens can be placed?
 - ▶ How many kinds of valid placements?

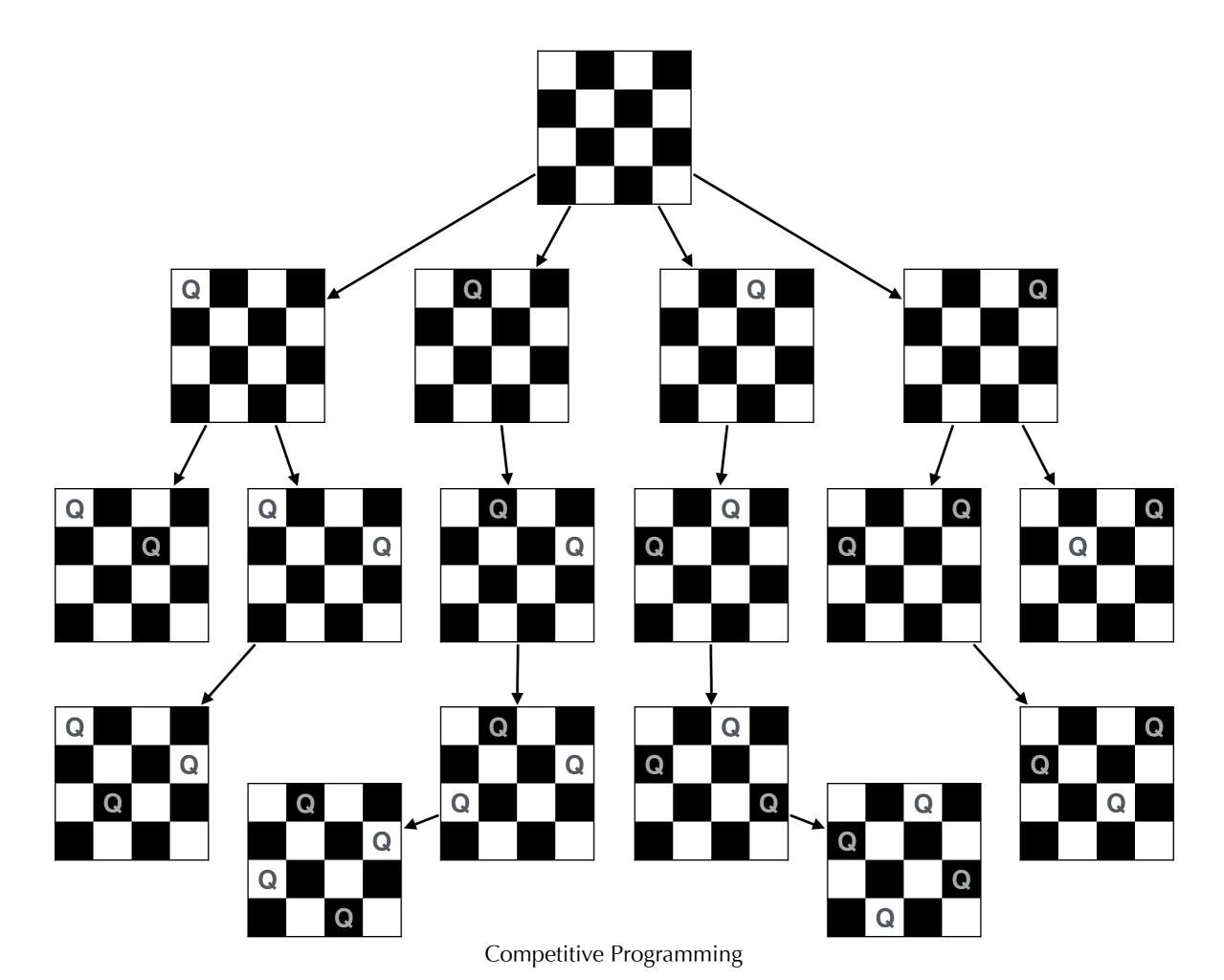


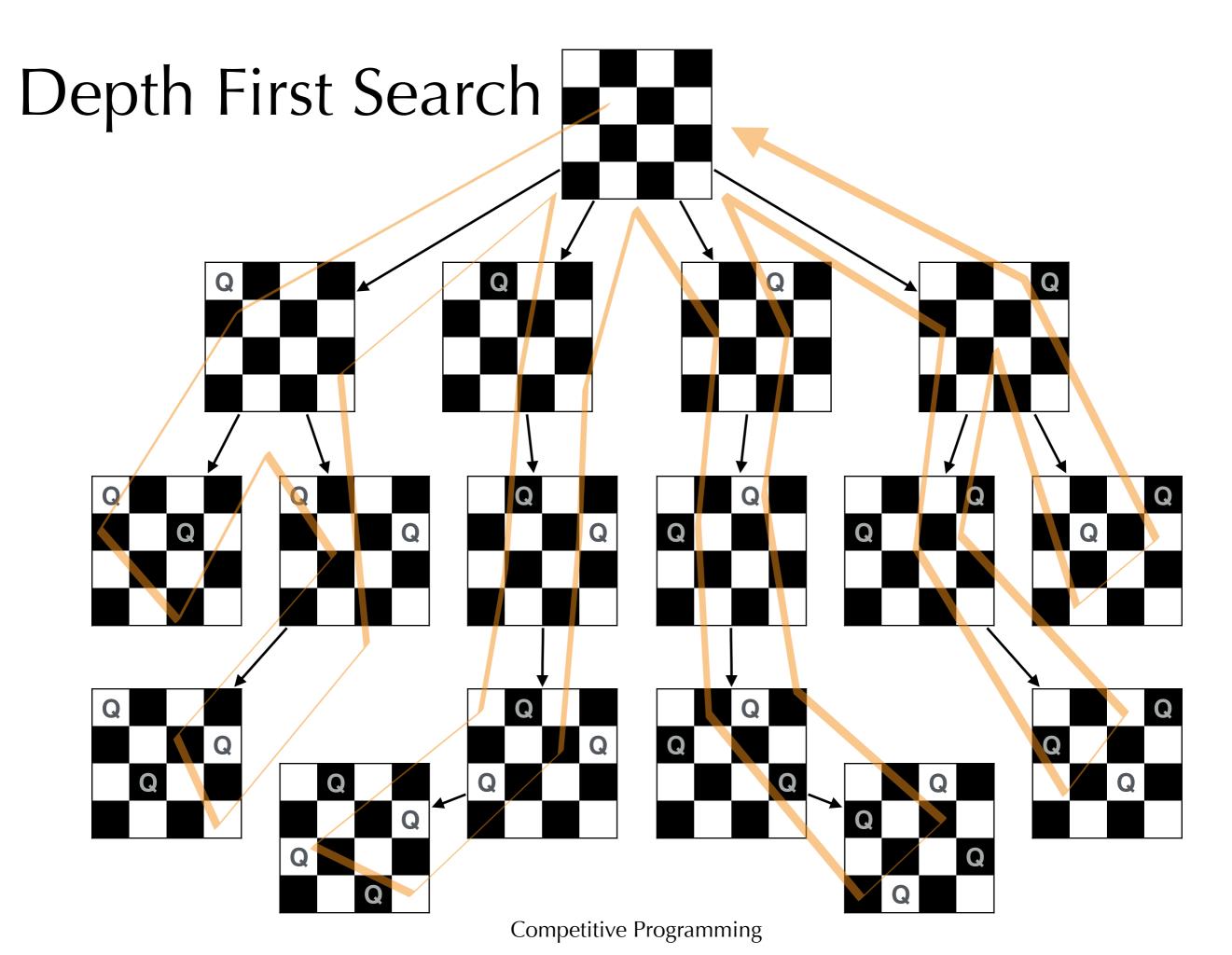


State Space

- State: a (valid) placement
- ▶ State space: set of all (valid) placement
 - ▶ This is finite but very large.
- **▶** Transition
 - Action: try to place a new queen on certain place (* add restriction)
 - Result: the new placement
 - Cost: 1 (* depends on the question)



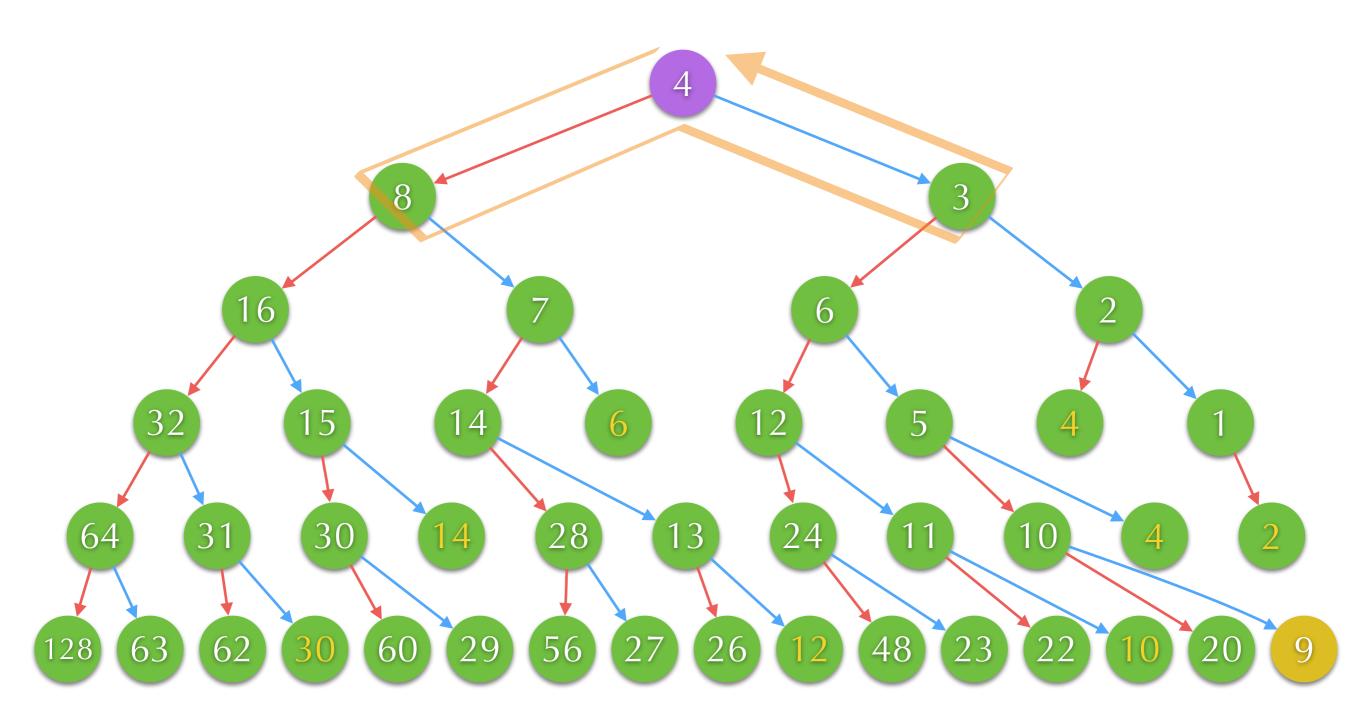


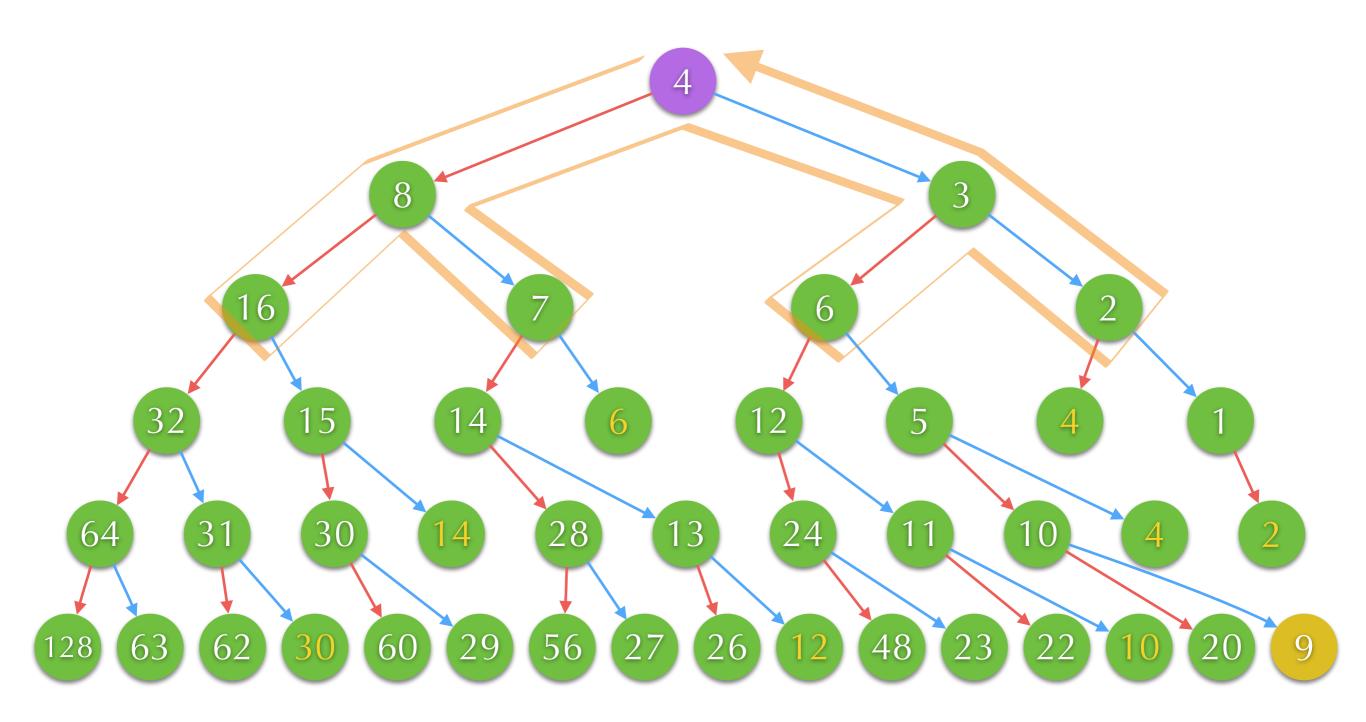


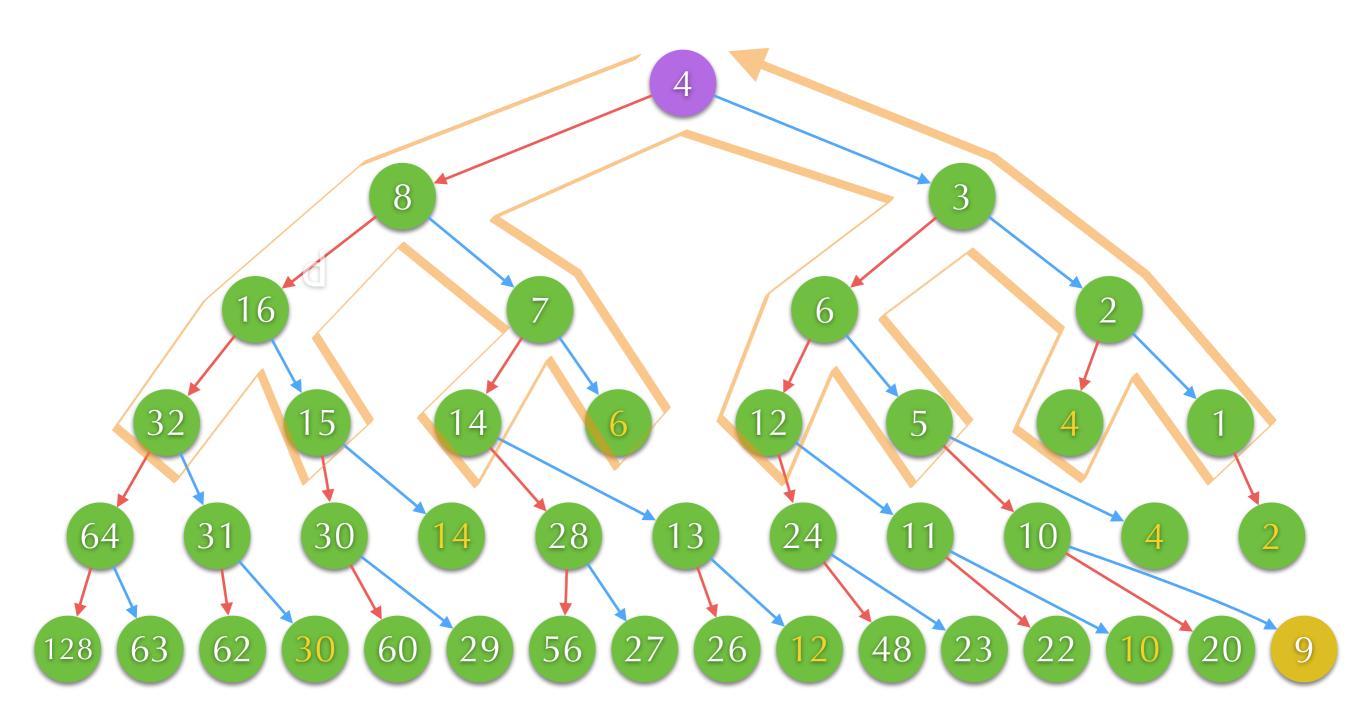
Depth First Search

- Pros
 - Easy to implement
 - Less memory consumption
 - Works for non-uniform costs
- Cons
 - Cannot reach the goal state with minimum transitions
 - ▶ May visit even more states than BFS

- Simulate BFS by multiple modified DFSs
- Pros
 - Still easy to implement
 - ▶ Less memory consumption than BFS
 - Works for non-uniform costs
- Cons
 - Slower than BFS & more complex than DFS

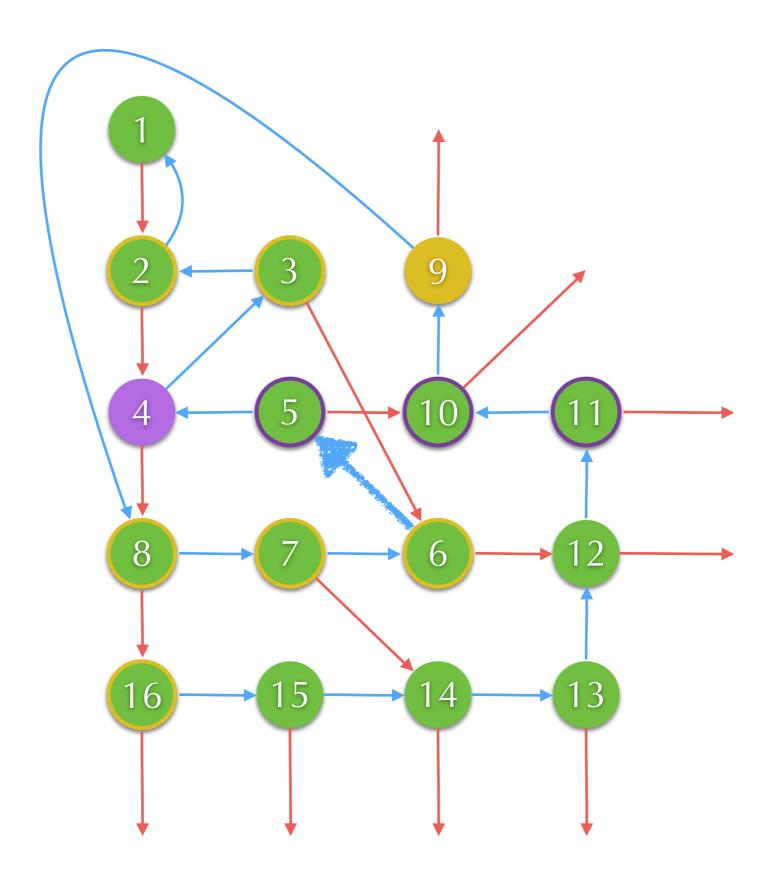






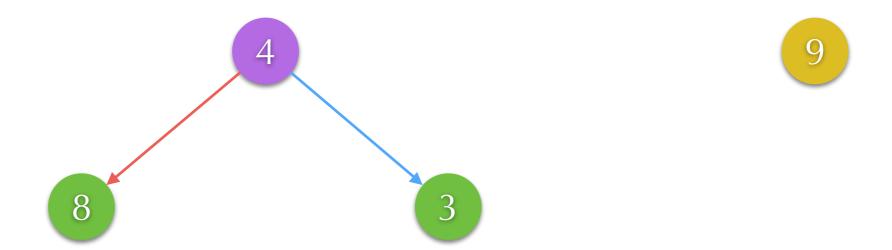
Assignment Week 2

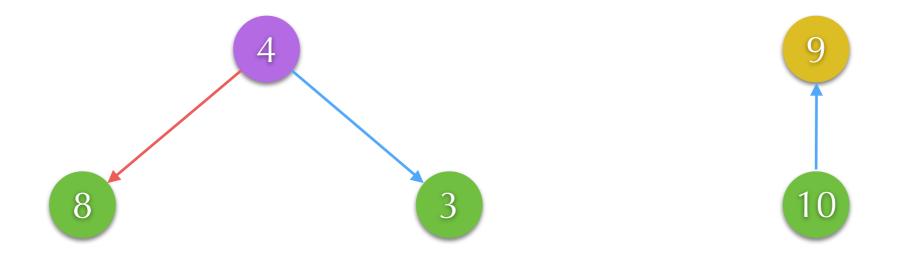
- UVa 11974
 - bitwise operators
 - stack overflow
 - Global variable (NG for SW development)
 - Static variable
 - vector (highly recommended)
 - Dynamic allocation
- ▶ UVa 167
 - ▶ format control: %5d

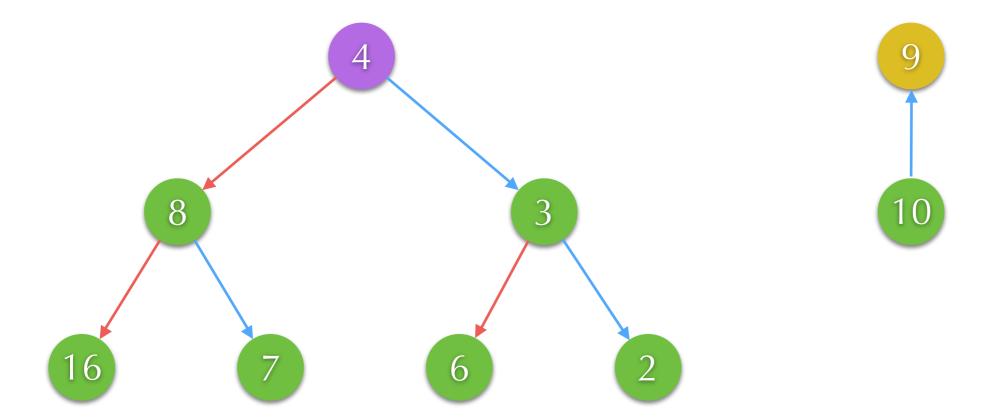


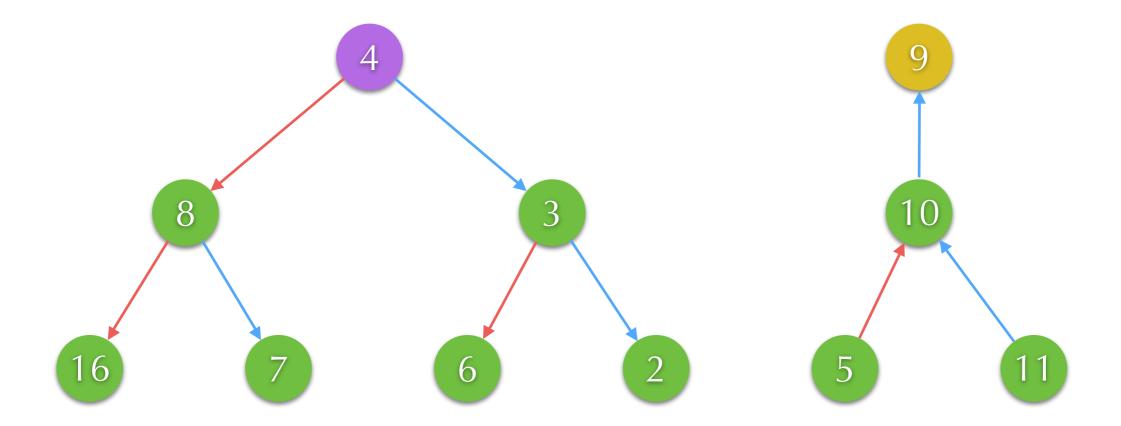


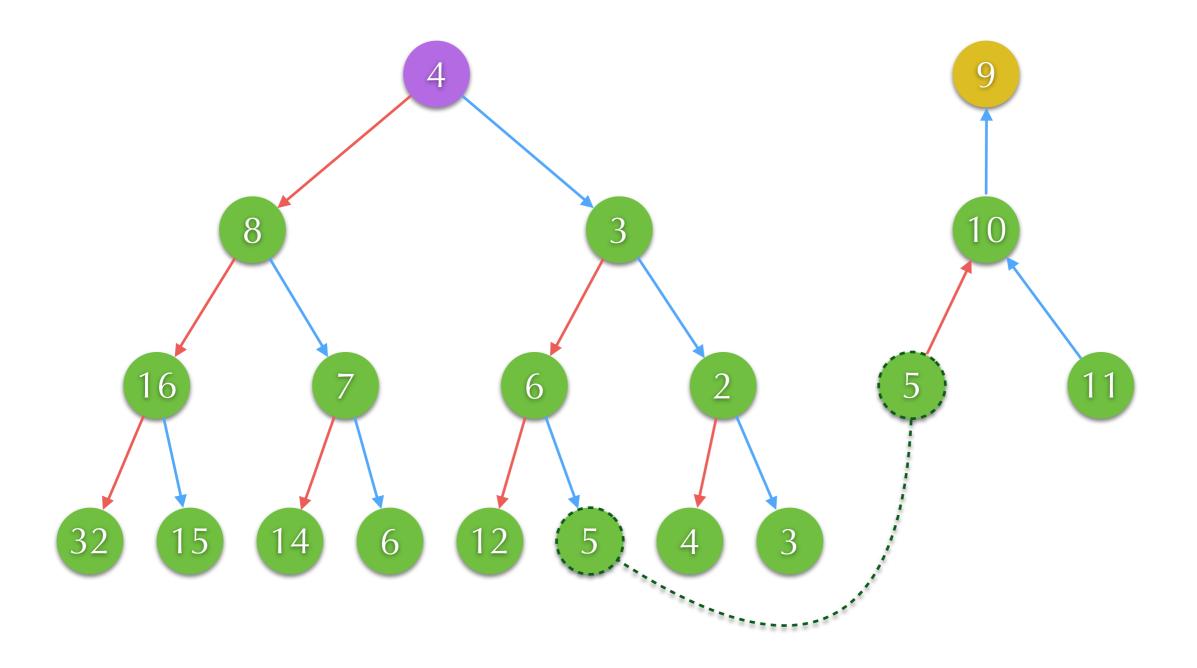




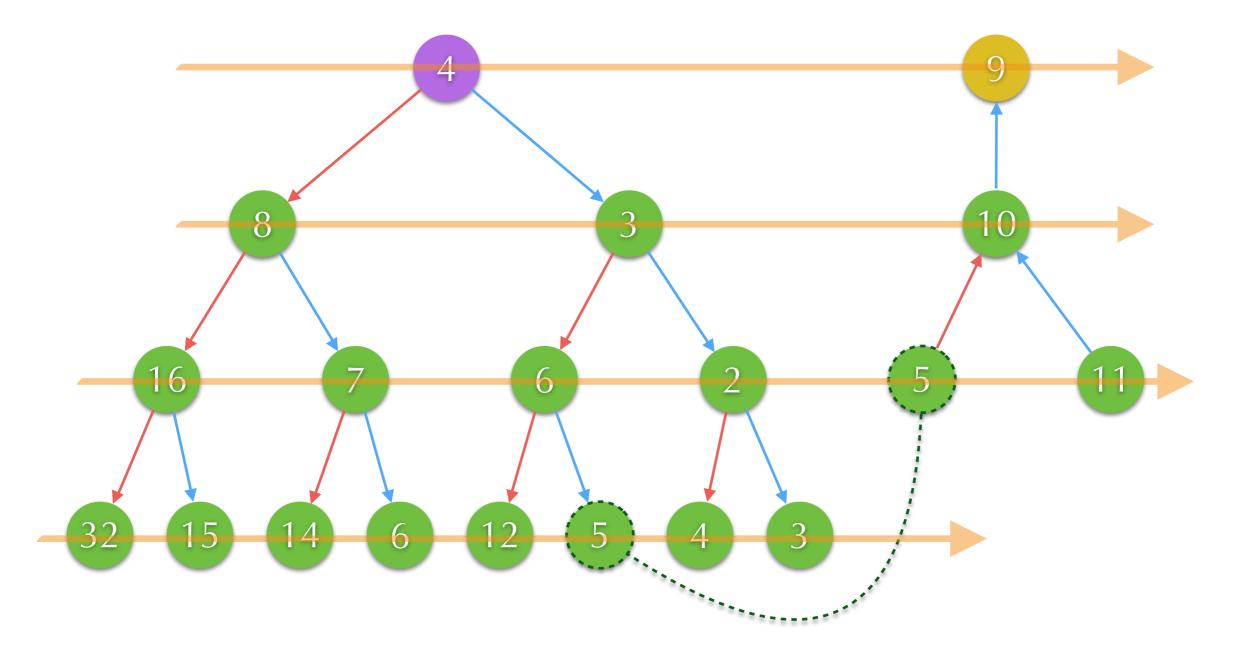








Meet in the Middle



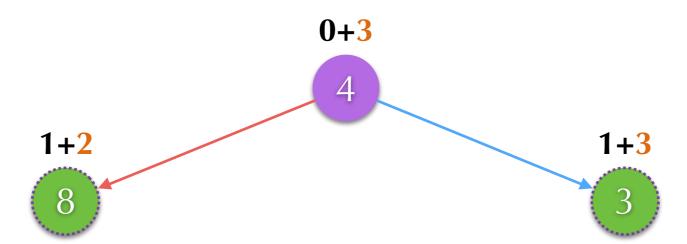
Meet in the Middle

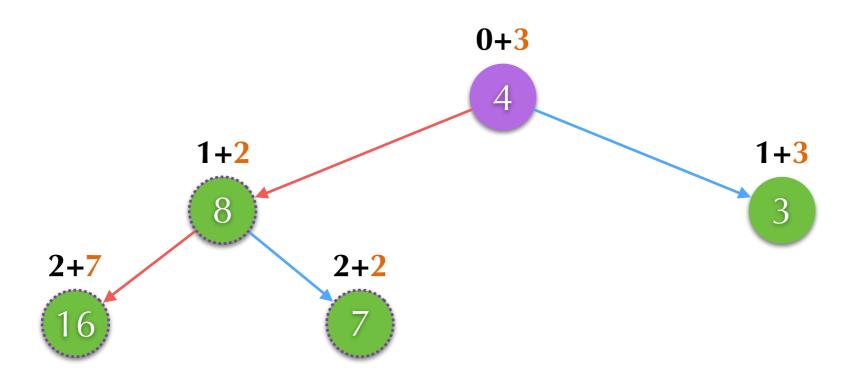
- Perform BFSs on both ends
- Pros
 - Still easy to implement
 - ▶ Less memory consumption than ordinary BFS
- Cons
 - ▶ More memory consumption than DFS
 - May visit too many states
 - ▶ Goal states must be specified

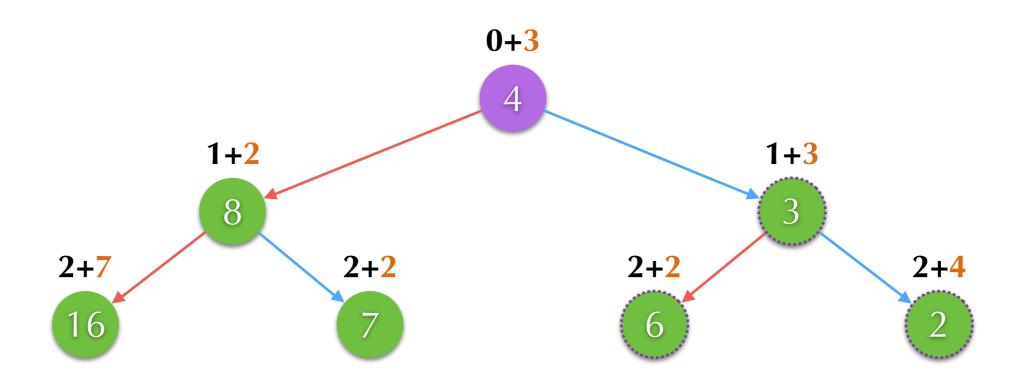
- Previous approaches do not exploit the COST.
- A-star is a greedy approach: pick the state x of minimum f(x)=g(x)+h(x) to branch
 - \triangleright g(x): accumulated cost from the initial to x
 - h(x): estimated cost from x to the goal
 - Heuristic function
- ▶ If h(x) is admissible (never overestimates), then A-star must find the optimal solution.

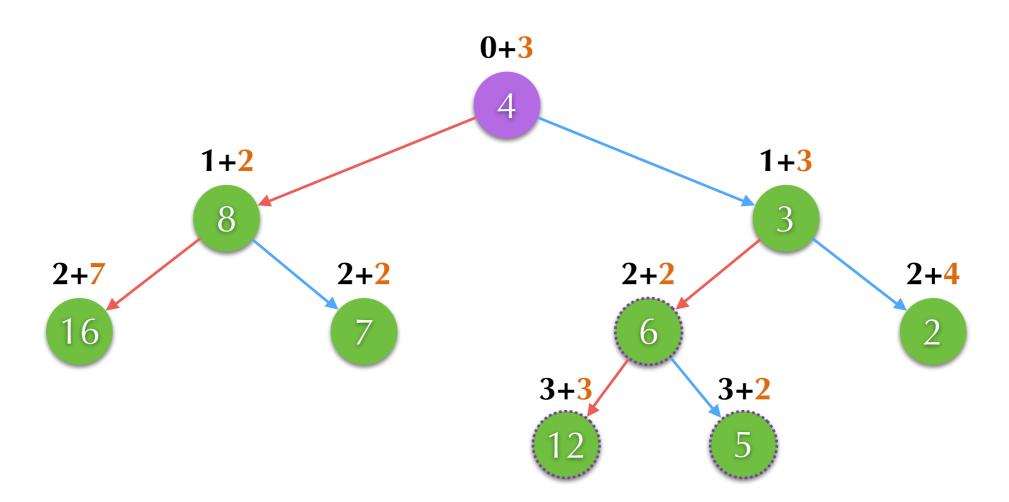
Heuristic for CF 520B

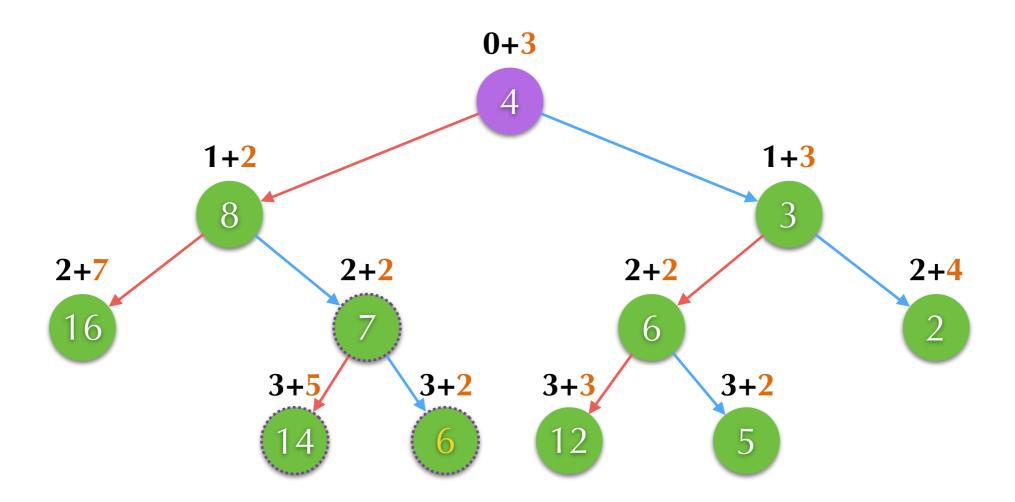
- x: the current displayed number
- ▶ m: the goal
- ▶ r: m/x
- ▶ $h(x)=x-m \text{ if } x \ge m.$
- $h(x) = \lceil \log_2 r \rceil + I[\log_2 r \notin Z] = 2\lceil \log_2 r \rceil \lfloor \log_2 r \rfloor \text{ if } x < m.$
 - \gt [log₂r] doubling clicks
 - ▶ ≥1 minus click if log₂r is not integral
- Never overestimate!

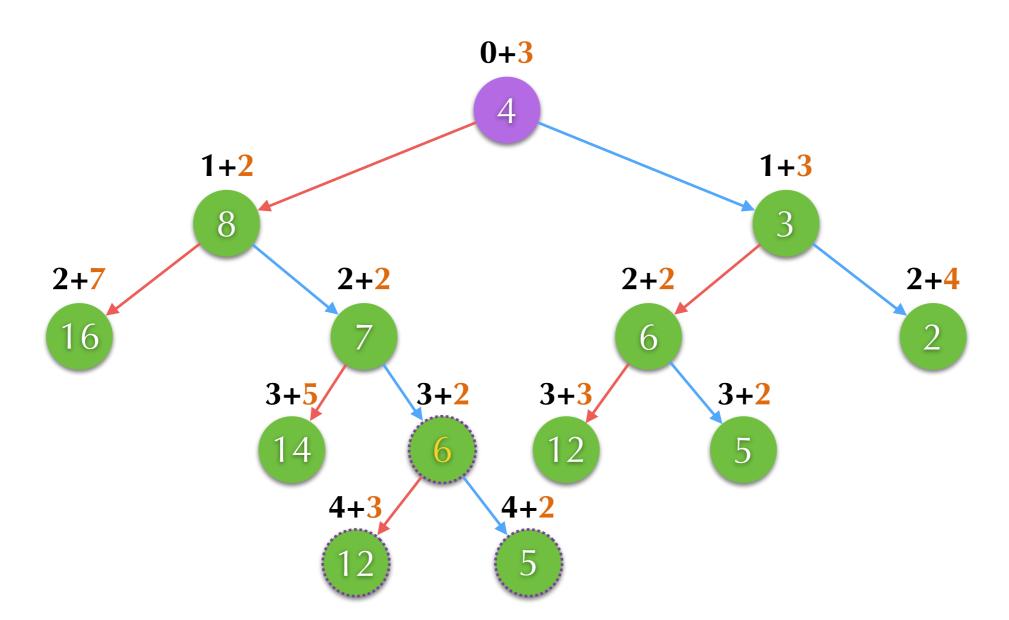


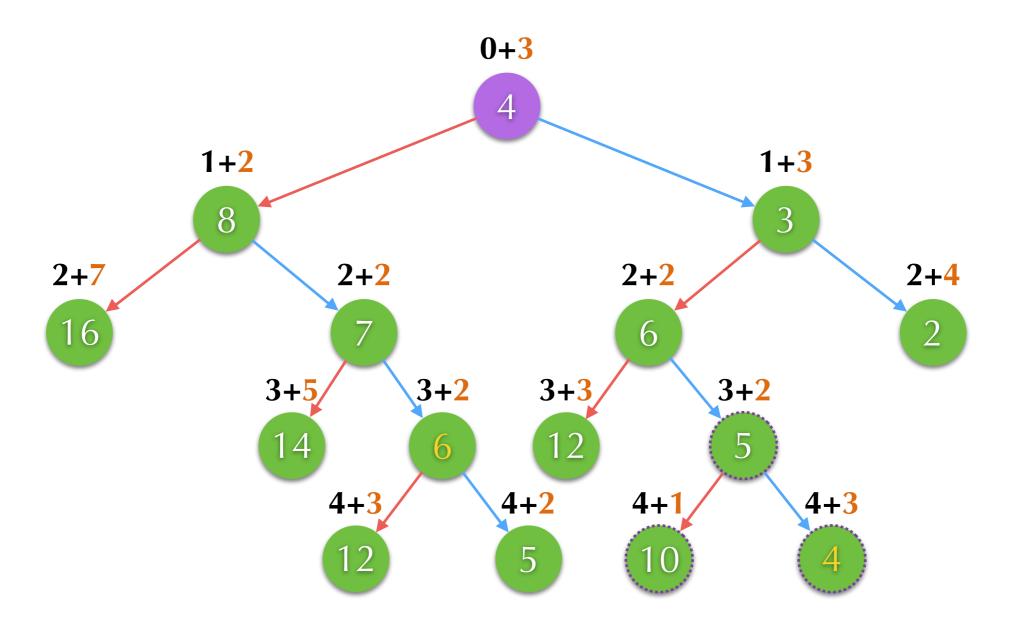


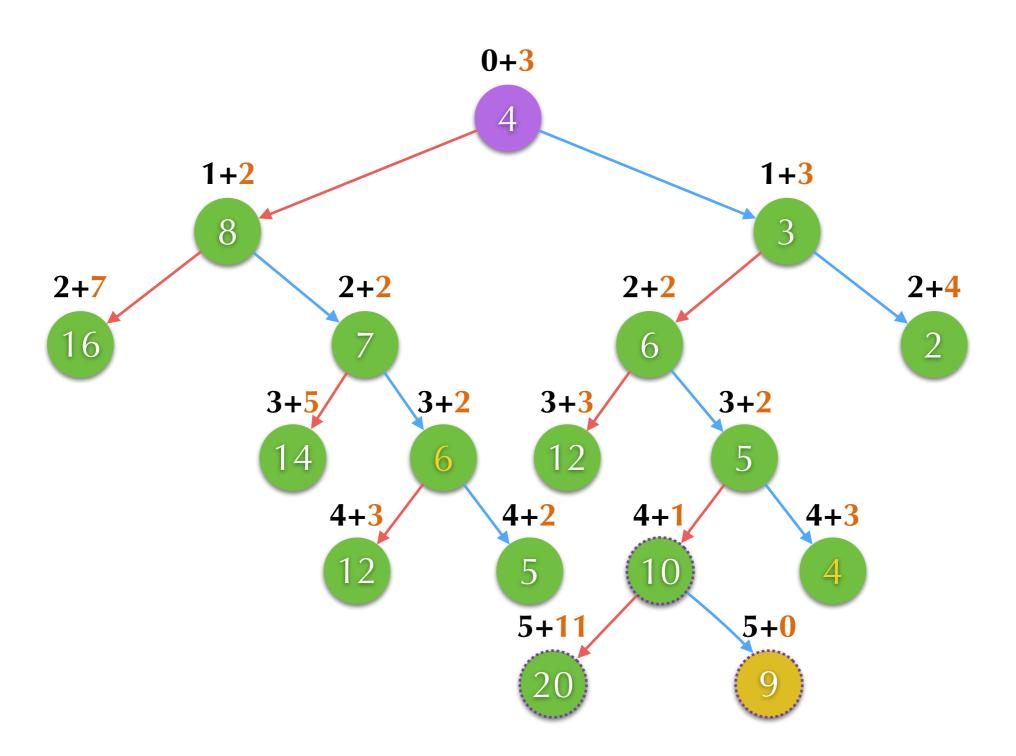




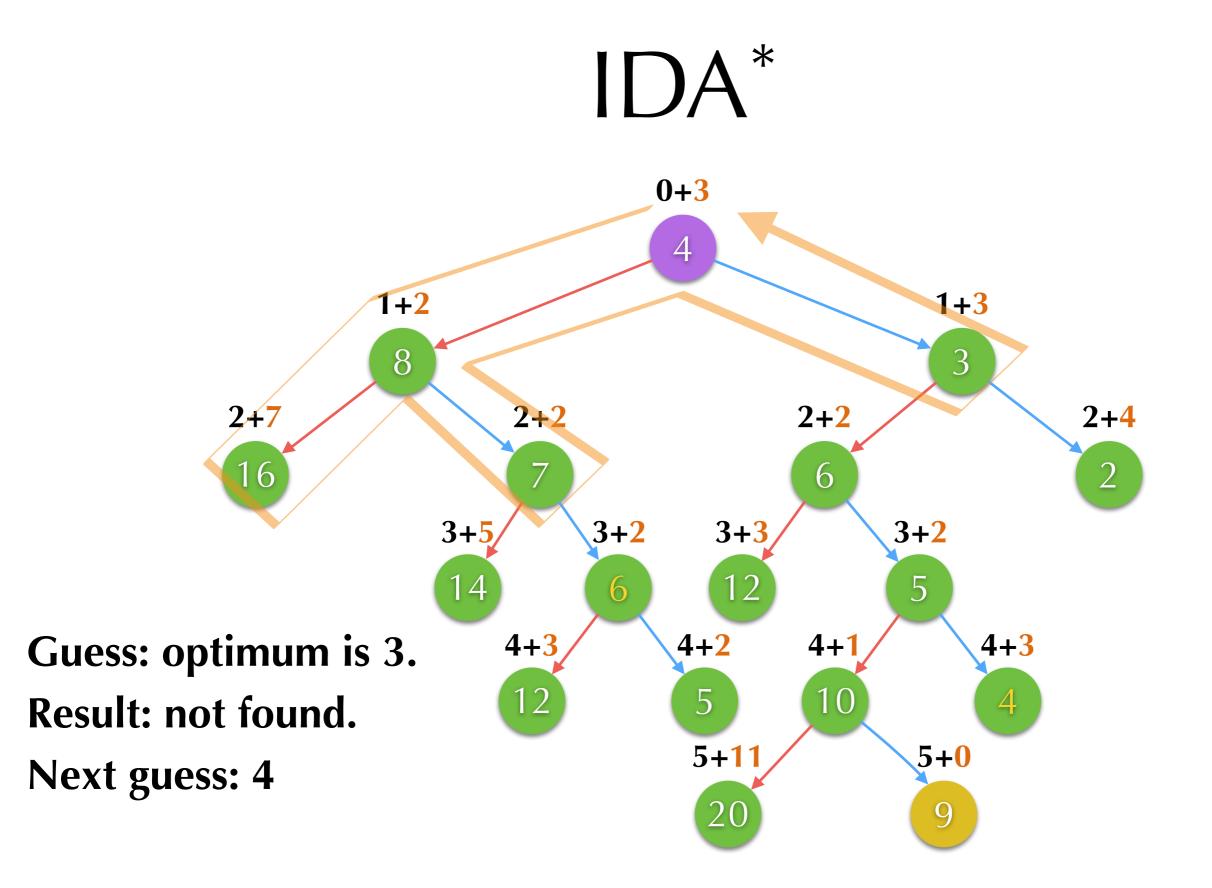


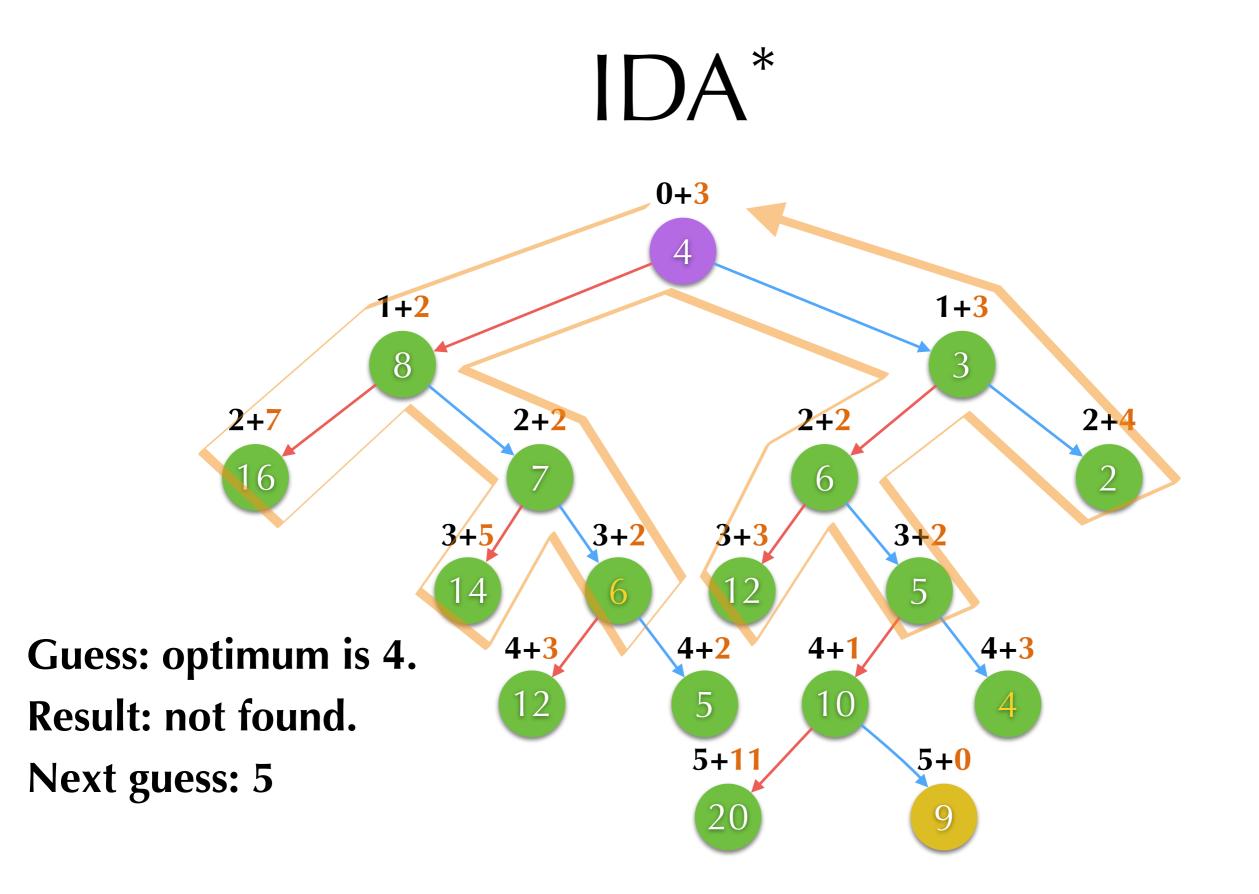


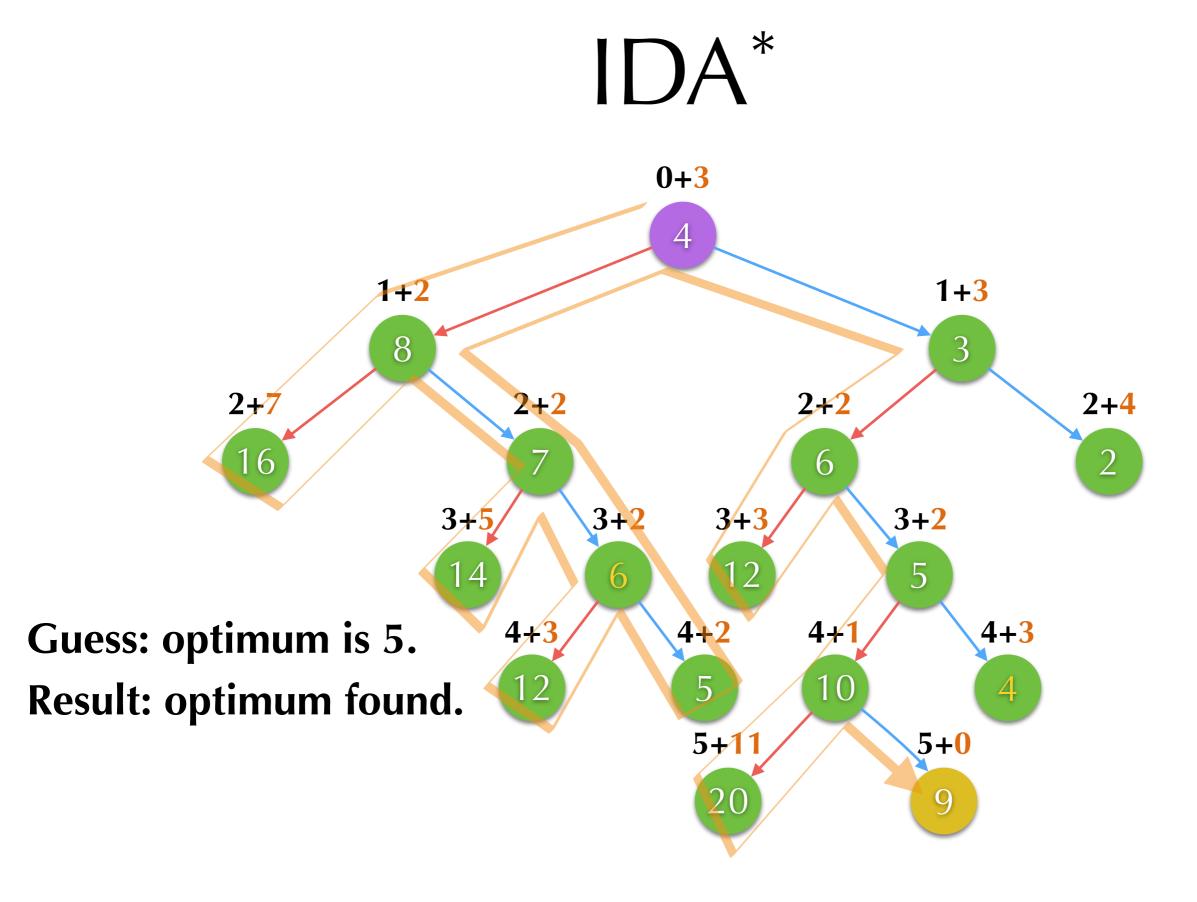




- ▶ Concept: best first search
 - Use priority queue
- Pros
 - Still easy to implement
 - Less memory consumption than ordinary BFS
- Cons
 - More memory consumption than DFS
 - Might be too large
 - ▶ Hard to design an admissible heuristic







IDA*

- Simulate best first by iterative deepening
- Pros
 - Still easy to implement (no priority queue required)
 - Memory usage can be very low (close to DFS)
- Cons
 - Might visit a state for many times
 - ▶ Hard to design an admissible heuristic
 - Can appear in your midterm

Assignment Week 3

- UVa 10422
 - bitwise operations on long long variables
 - ▶ Meet in the middle? A*? IDA*?
- UVa 11212
 - Still bitwise operations on long long variables
 - ▶ Breadth first search is too slow?