

(Theory of Computation)

Check whether the following languages are DCFL, CFL or not ?

$$L_1 = \{a^n b^n \mid n \geq 0\} \Rightarrow \text{DCFL}$$

$$L_2 = \{a^n b^{2n} \mid n \geq 0\} \quad \text{CPL}$$

$$L_3 = \{a^{2n} b^n \mid n \geq 0\}$$

$$L_4 = \{a^m b^m c^n d^n \mid m, n \geq 0\}$$

$$L_5 = \{a^m b^n c^n d^m \mid m, n \geq 0\}$$

DCFL

$$L_6 = \{a^m b^n c^m d^n \mid m, n \geq 0\}$$

CPL

$$L_7 = \{a^m b^{m+n} d^n \mid m, n \geq 0\}$$

$$= \{a^m b^m - b^n d^n\}$$

DCFL

$$L_8 = \{a^{m+n} b^m c^n \mid m, n \geq 0\}$$

DCFL

$$= \{a^m a^n b^m c^n \mid$$



(Theory of Computation)

$$L = \{ \underline{a^m b^m} \underline{c^n d^n} \underline{a^K b^K} \mid m, n, k \geq 1 \} \text{ DFLC}$$

$$L = \{ \underline{a^m b^m} \underline{c^n d^n} \mid m \geq n \geq 0 \} \rightarrow \text{not DFLC}$$

~~a⁵b⁵ c⁴d⁴~~

$$L = \{ \underline{a^{2n}} \underline{b^{3n}} \mid n \geq 0 \} \Rightarrow \text{not DFLC}$$

~~aa → aaaa~~

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$L = \{ a^{kn} b^{pn} \mid k, p \text{ are Constant}, n \geq 0 \}$ \Rightarrow DCLC

$a^{5n} b^{7n}$

for every k a 's push p a 's in the stack

~~Push~~

$\uparrow S \rightarrow \uparrow^a$
pop

DCLC
=

(Theory of Computation)

$$L = \{a^m b^n \mid m > n \geq 0\}$$

$$m < n$$

$$m \neq n$$

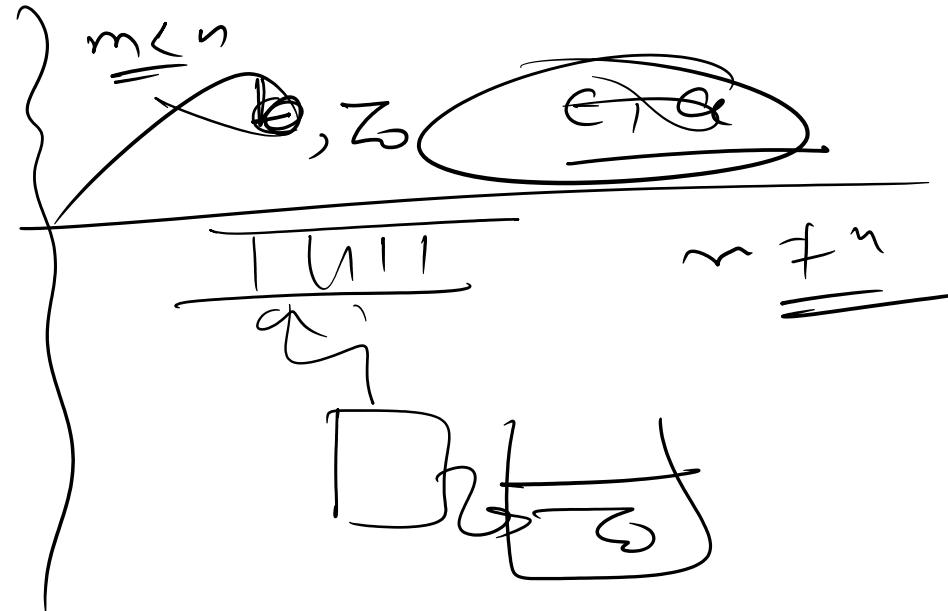
$$m = n$$

$$m \leq n$$

$$m \geq n$$

$$m = 2n + 1$$

$$m =$$



(Theory of Computation)

$$L = \{a^m b^n c^{m+n} \mid m, n \geq 1\}$$

CSL

$$L = \{a^{n^2} \mid n \geq 1\}$$

CSL

$$L = \{a^m b^n c^{m-n} \mid m, n \geq 1\}$$

$$= \{a^{nx} b^n c^x \mid \frac{m}{n} = x\}$$

CSL

$$n'$$

$$n = O(n^3)$$

notes $m = n^x$ $L = \{a^{n!} \mid n' \neq n = n^2\}$

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$$L = \{ a^{m-n} b^m c^n \mid m, n \geq 1 \}$$



- a) DCFL
- b) CFL
- c) Regular
- d) None.

$$a^{6-2} b^6 c^2$$

$$a^4 b^6 c^2$$

$$\Rightarrow a^m b^{m+n} c^n$$

$a^m b^m$

b^{n+c}

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$$L = \{ \underline{a^n b^n} \mid n \geq 0 \} \cup \{ a^{2m} b^{2m} \mid m \geq 0 \}$$



$$L = \{ a^n b^n \mid n \geq 0 \} \cup \{ a^m b^{2m} \mid m \geq 0 \}$$

~~HDCM~~

- a) DFA
b) NDFA
c) ~~Reguler~~
d) None

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$$L = \{ a^i b^j c^k \mid i=j \text{ or } j=1, i, j, k > 0 \}$$

\Rightarrow NDFA

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$$L = \{ w \in \omega^R \mid$$

$$w \in (a, b)^* \}$$

$|w| \geq 0$

\Rightarrow DFA

DFA but
not Regular

$$\checkmark L = \{ w x \in \omega^R \mid \cancel{w, x \in (a, b)^*} \}$$

\Rightarrow Regular

DFA but not
DFA

None

$$\cancel{\sum_{x \in \{a, b\}} \cancel{abbaabbbg} \wedge \omega^T}$$

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$$L = \{ \omega x \omega^R \mid \omega, x \in \{a, b\}^*, |x| = 2 \}$$

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$\omega \in \{a+a+b+a+b\}^*$

\rightarrow HDUH

$L = \{ \omega c \omega \mid \omega \in \{a, b\}^* \}$



$$L = \{ \omega (a+b) \omega^R \mid \omega \in \{a, b\}^* \}$$

abb a bba



$D_{ave} = 28 \text{ m/s} \rightarrow 28 \text{ cm}$

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$$\begin{aligned}
 L &= \{\omega x \omega \mid \omega, x \in a, b\}^* \Rightarrow \{\text{rexxxxxx}\}^* \rightarrow R \rightarrow DCL \\
 &= \sum \text{abs } b \text{ abs } b \\
 &\quad \nearrow \qquad \searrow \qquad \wedge \\
 &\quad RIL \Rightarrow Bee \Rightarrow CSC \subseteq DCL \quad Z
 \end{aligned}$$

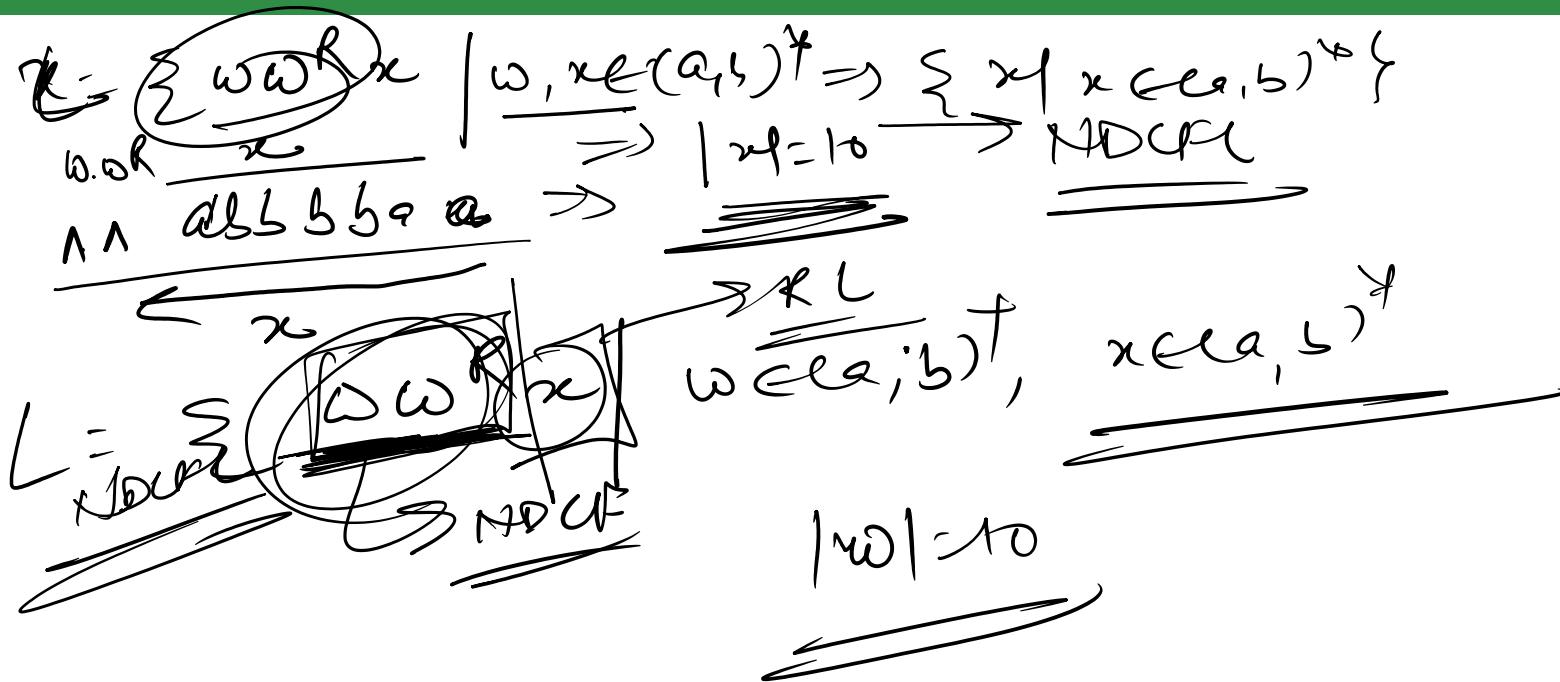
$$L = \{ \overline{\omega x \omega^R} \mid \underbrace{\omega \in (a,b)^*, \quad x \in (a,b)^*}_{\text{SRL}} \} \Rightarrow D$$

~~L = a(a+b)^* + b(a+b)^*~~

$$\frac{abb \ ab}{x} \quad \frac{bab}{\omega^R} \quad L = \frac{a(a+b)^* + b(a+b)^*}{S_{RL}}$$

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$$L = \{ w @ w \mid w \in (a,b)^*, x \in (a,b)^* \}$$

$$|w| = 10$$



CSL



(Theory of Computation)

$$L_1 = \{ \underline{a^n b^n} | (a+b)^* | n > 0 \}$$

$$L_2 = \{ \underline{(a+b)^* b^n} | a^n | n > 0 \}$$

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→ Revs

DFA

→ NDCFL

~~ab b b bbaa~~

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(Theory of Computation)



(Theory of Computation)



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(Theory of Computation)

$$L = \{a^m b^n c^k d^l \mid m, n, k, l \geq 1\} \quad \underline{m+n = n+l}$$

2018

DPL

~~a a (b b b) b c) d e f g~~

~~1 2 3 4 5 6 7 8 9 10~~

~~FSC~~

~~1 2 3 4 5 6 7 8 9 10~~

~~S C~~

~~TM~~

$$L = \{a^m b^n c^k d^l \mid m, n, k, l \geq 1\}$$

DPL

$a^4 b^2 c^1 d^3$

DPL 10

$a^2 b^4 c^3 d^1$
 $a a b b b b c c c d$

a
a
30

b 6-7

7-8
m-p

26

3:30

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Properties of CFL & DCFL

DCFL are not closed Under:

- Union
- Intersection
- Set Difference
- Homomorphism
- Kleen's closure
- Reversal
- Concatenation

$$L_1 = \{a^n b^n \mid n \geq 0\}$$

No CS

$$L_2 = \{a^n b^{2n} \mid n \geq 0\}$$

$$L_1 = \{a^n b^m c^m \mid m, n \geq 0\}$$

$$L_2 = \{a^m b^m c^n \mid m, n \geq 0\}$$

$$L_1 \cap L_2 = \{a^m b^m c^m \mid m \geq 0\}$$

CS

DCL are closed Under:-

- Compliment ✓
- Inverse Homomorphism ✓
- Prefix ✓
- Suffix ✓
- Quotient ✓
- Union with regular ✓
- Intersection with regular ✓
- Set difference with regular ✓

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Context free Language (CFL) are closed Under:

- Union ✓ CFL
- Concatenation
- Homomorphism ✓
- Inverse Homomorphism

- Union with regular ✓ CFL
- Intersection with regular → CFL
- Set difference with regular → CFL

- Kleen closure
- Positive closure
- Quotient $S \rightarrow S_1 S_2$
- Prefix
- Suffix
- Reversal
- Cycle

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CFL are not closed Under:

- Intersection
- Complement
- Set difference
- Subset
- Superset
- Infinik Union
- Infinik Intersection
- Infinite set difference
- max
- min
- ALT
- HALF



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Ex:- Let L_1 is CFL, L_2 is DCFL and L_3 is Regular

(i) $L_1 - L_3$? $\Leftrightarrow \text{CFL} \cap \overline{\text{Reg}} \Rightarrow \text{CFL} \cap \text{Reg} \Rightarrow \text{CFL}$

(ii) $L_3 - L_1$? $L_3 - L_1 \Rightarrow L_3 \cap \overline{L_1} \Rightarrow \text{Reg} \cap \overline{\text{CFL}} \Rightarrow \text{CSL}$

(iii) $L_2 - L_3$? $\overline{\text{DCFL} \cap \text{Regular}} \Rightarrow \text{Reg} \cap \overline{\text{DCFL}}$

(iv) $L_3 - L_2$? $\overline{\text{Regular} \cap \text{DCFL}} \Rightarrow \text{Reg} \cap \overline{\text{DCFL}} \Rightarrow \text{DFA}$

(v) $\text{CFL} \cap \text{Regular}$? CFL

(vi) $\text{CFL} \cup \text{Regular}$? CFL

Operations	RL	CFL	DCFL	CSL	Rec	REL
Union	✓	✓	✗	✓	✓	✓
Intersection	✓	✗	✗	✓	✓	✓
Set Difference	✓	✗	✗	✓	✓	✗
Complementation	✓	✗	✓	✓	✓	✗
Intersection with Regular	✓	✓	✗	✓	✓	✓
Concatenation	✓	✓	✗	✓	✓	✓
Kleen Closure	✓	✓	✗	✓	✓	✓
Kleen Plus	✓	✓	✗	✓	✓	✓
Reversal	✓	✓	✗	✓	✓	✓
Homomorphism	✓	✓	✗	✗	✗	✓
ϵ -free Homomorphism	✓	✓	✗	✓	✓	✓
Inverse Homomorphism	✓	✓	✓	✓	✓	✓
Substitution	✓	✓	✗	✗	✗	✓
ϵ -free Substitution	✓	✓	✗	✓	✓	✓
Quotient with Regular	✓	✓	✓	✗	✗	✓



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