

Compiler Design

Today's Class Topics

- CLR(1) Parsing ✓
- LALR(1) Parsing ✓
- S/R and R/R Conflict
- How to Test CLR(1) and LALR(1) Grammar etc. ✓
- Relationship amongst LL(1), LR(0), SLR(1), CLR(1) and LALR(1)
- YACC Tool ✓



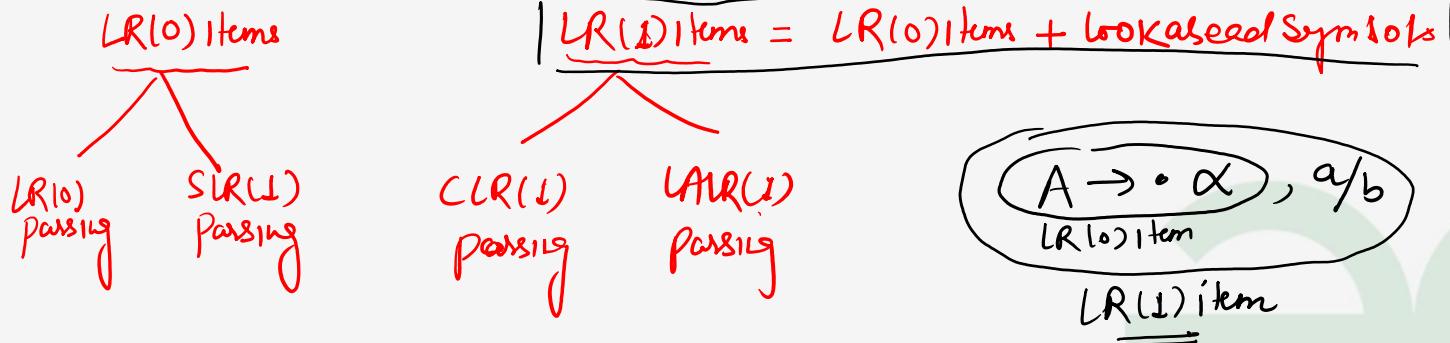
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CLR(1) or LR(1) Parsing :- It can be divided into two Parts

- 1 - Construction of Canonical Set of items or LR(1) items
- 2 - Construction of Parsing Table
 - Action Part
 - Goto part

Closure operation

Goto operation



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Construction of closure operation:



1- Initially we add $S' \rightarrow \cdot S, \$$ ✓

2- if $A \rightarrow \alpha \cdot B \boxed{B, a}$, is in I_i and if $B \rightarrow r$ is a production then Add $B \rightarrow \cdot r, \underline{x}$ in I_i where $x \in \text{first}(\beta a)$

Ex: $G = \{ S \rightarrow AB, A \rightarrow aA | a, B \rightarrow \underline{b} \}$

$$I_i \left| \begin{array}{l} A \rightarrow \alpha \cdot B \boxed{B, a}, B \rightarrow r \\ B \rightarrow \cdot r, \underline{x} \end{array} \right. \\ x = \text{first}(\beta a)$$

To $\left\{ \begin{array}{l} S' \rightarrow \cdot S, \$ \\ S \rightarrow \cdot A \boxed{B, \$} \\ A \rightarrow \cdot aA, b \\ A \rightarrow \cdot a, b \end{array} \right\}$

$\text{first}(\in \$) = \text{first}(\$) = \$$
 $\text{first}(\underline{B} \$) = \text{first}(CB) = \{ b \}$
 $\text{first}(a)$

$I'_i \xrightarrow{\text{Goto}(I_i, X)} I_j \boxed{A \rightarrow \alpha x \cdot \beta, a}$

Construction of Goto operation:-

1) if $\boxed{A \rightarrow \alpha \cdot X \beta, a}$ is in I_i then $\boxed{\text{Goto}(I_i, X) = A \rightarrow \alpha X \cdot \beta, a}$

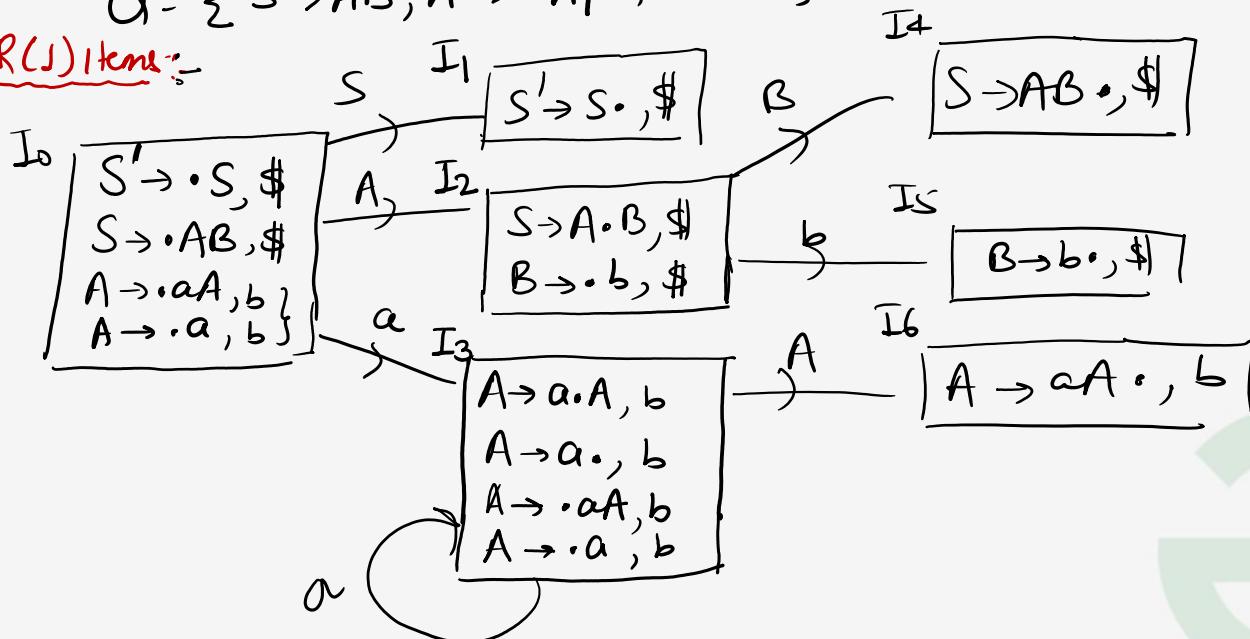
Here X can be either a terminal or non-terminal

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Ex:- Construct LR(1) items for the following Grammar

$$G = \{ S \rightarrow AB, A \rightarrow aA/a, B \rightarrow b \}$$

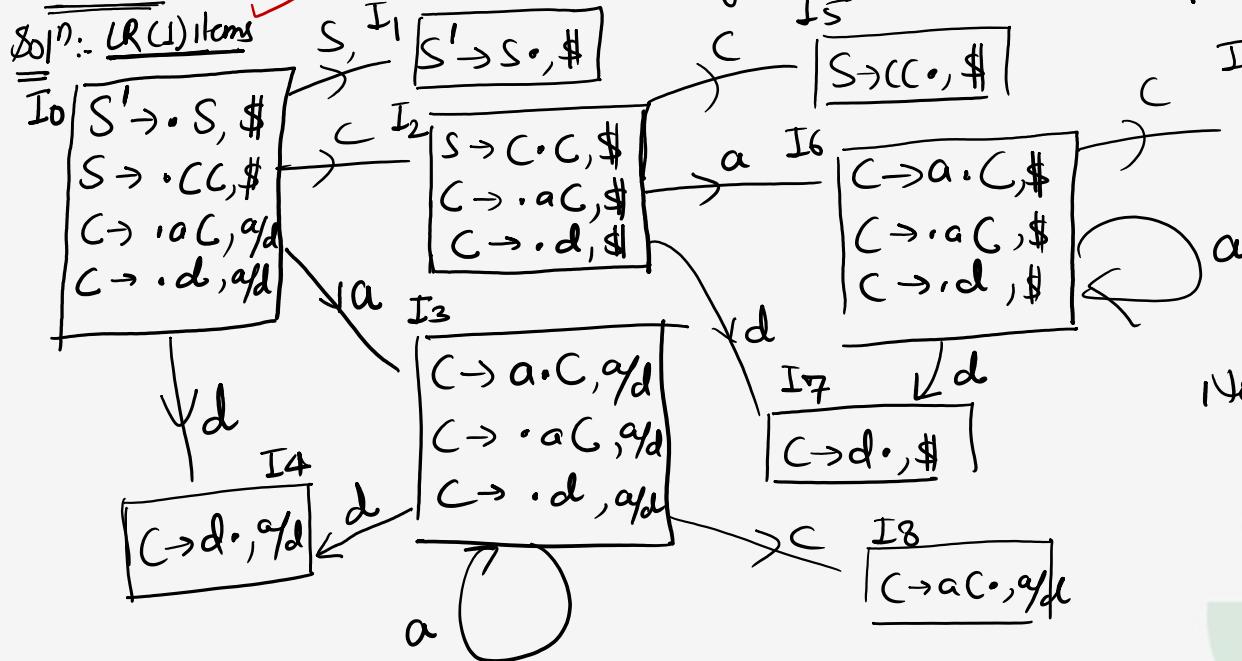
LR(1) Items :-



LR(1) items \Rightarrow States = ?

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Question: Construct CLR(1) Parsing Table for the following Grammar



$$G: \begin{cases} S \rightarrow CC \\ C \rightarrow aC/d \end{cases}$$

- 1) $S \rightarrow CC$
- 2) $C \rightarrow aC$
- 3) $C \rightarrow d$

No of States = 10

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Action Part

Goto part

CLR(1) Parsing Table Construction: It has 2 parts

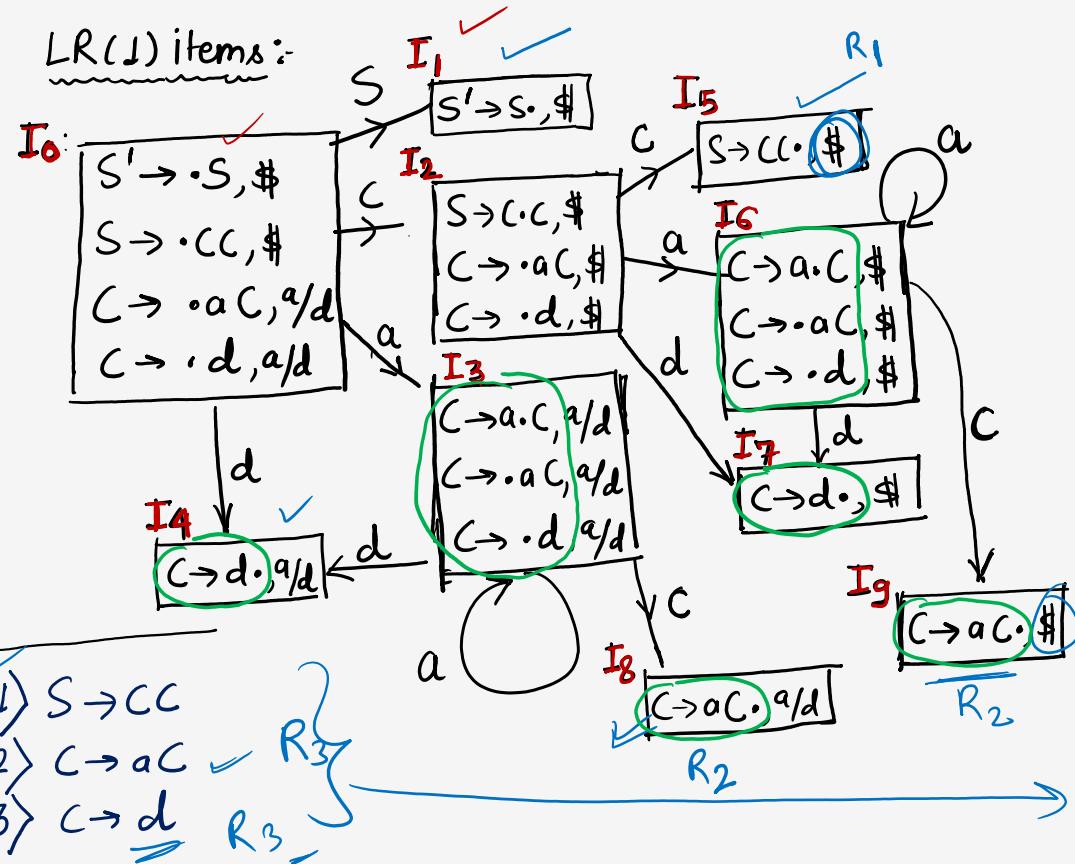
The Action Part of the Table will be filled as follows:

- i) if $A \rightarrow \alpha \cdot a \beta$, a is in I_i and if $\text{Goto}(I_i, a) = I_j$ Then Set Action $[i, a] = S_j$ (shift-J)
- ii) if $A \rightarrow \alpha \cdot a$ is in I_i then set Action $[i, a] = \text{Reduce by } A \rightarrow \alpha$, Here $A \rightarrow \alpha$ must not be an Augmented Production
- iii) if $S' \rightarrow S \cdot, \$$ is in I_i then set Action $[i, \$] = \text{Accept}$

The Goto Part of the Table will be filled as follows:

- i) if $A \rightarrow \alpha \cdot B \beta$, a is in I_i and if $\text{Goto}(I_i, B) = I_j$ Then
 I_i Set goto $[i, B] = j$ $[i, B] = j$

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CLR(1) Parsing Table

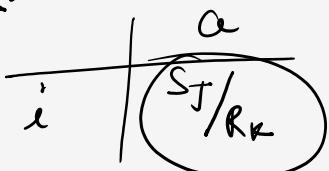
States	Action Part			Go to part	
	a	d	\$	S	C
0	S_3	S_4		1	2
1				Accept	
2	S_6	S_7			5
3	S_3	S_4			8
4	R_3	R_3			
5				R_1	
6	S_6	S_7			9
7				R_3	
8	R_2	R_2			
9				R_2	

CLR(1) Grammar.

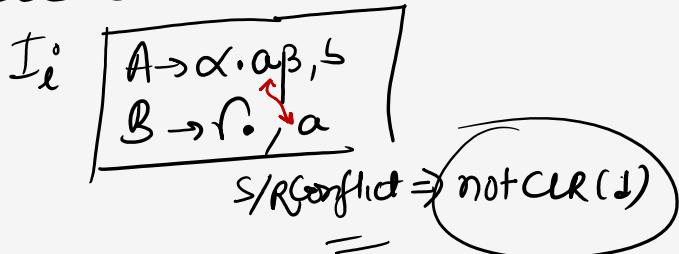
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Conflict in CLR(1) :-

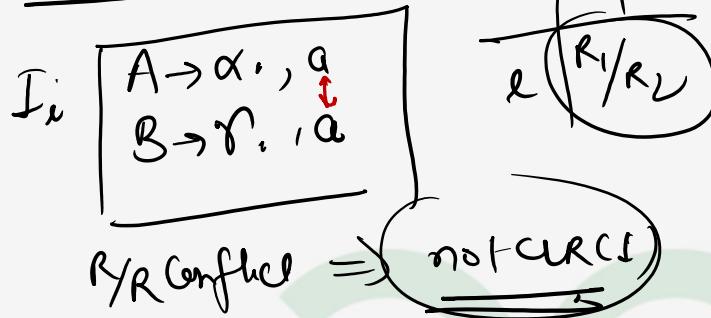
- S/R Conflict
- R/R Conflict



S/R Conflict:



R/R Conflict:

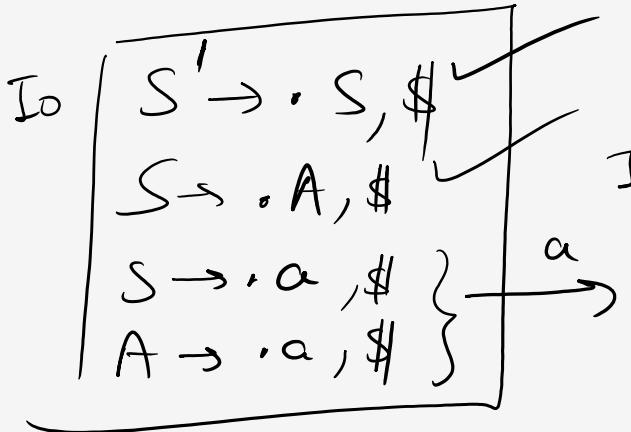


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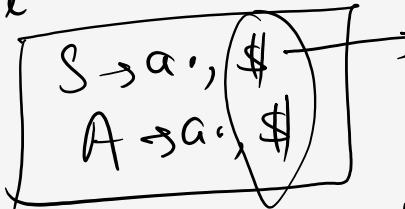
Ques:- Check whether the following grammar is CLR(1) or not?

$$G = \{ S \rightarrow A \mid a, A \rightarrow a \}$$

Solⁿ:



I_i



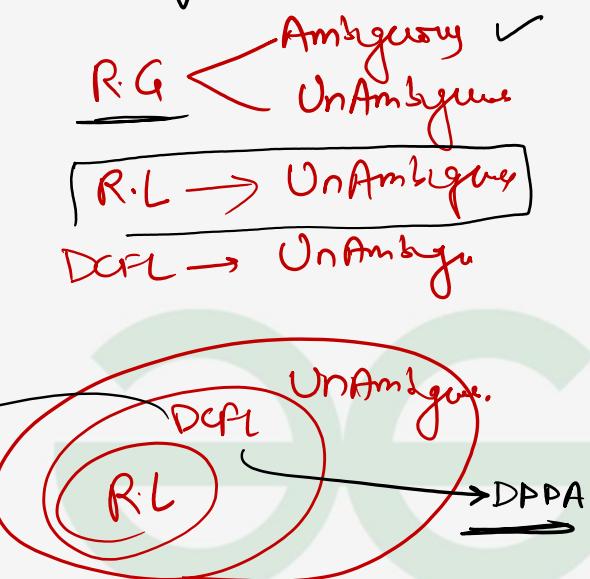
$R_F R$ Conflic not CLR(1)

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NOTE :-

- 1) An Ambiguous Grammar can never be LR(K) for any K
- 2) Every LR(K) Grammar is Unambiguous but every UnAmbiguous Grammar is not LR(K)
- 3) Every LR(1) Grammar has an equivalent DPDA
→ UnAmbig.
- 4) Every Regular Language has a LR(1) grammar
- 5) Every Regular Grammar can not be LR(1) grammar

DPDA



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Question: $G = \{ S \rightarrow Aa, A \rightarrow Ba/b, B \rightarrow b \}$ CLR(1) = ?

Solⁿ:

I₀

$S' \rightarrow \cdot S, \$$	x
$S \rightarrow \cdot A(a, \$)$	x
$A \rightarrow \cdot B(b, a)$	x
$A \rightarrow \cdot b, a$	-
$B \rightarrow \cdot L, a$	{

- 1) $S \rightarrow Aa$
- 2) $A \rightarrow Ba$
- 3) $A \rightarrow b$
- 4) $B \rightarrow L$

I₅

$A \rightarrow b \cdot , a$	$\rightarrow R_3$
$B \rightarrow b \cdot , a$	$\rightarrow R_4$

R_3/R_4

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Question: $G = \{ S \rightarrow aSa | Aa, A \rightarrow aA | b \}$



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LR(1) Items :-

LALR(1) Parsing :- minimized form of CLR(1)

Ex:- $G = \{ S \rightarrow CC, C \rightarrow aC/d \}$

I_3 \Rightarrow $C \rightarrow a \cdot C, a/d$
 $C \rightarrow \cdot aC, a/d$
 $C \rightarrow \cdot d, a/d$

I_6 \Rightarrow $C \rightarrow a \cdot C, \$$
 $C \rightarrow \cdot aC, \$$
 $C \rightarrow \cdot d, \$$

$\Rightarrow I_{36}$ \Rightarrow $C \rightarrow a \cdot C, a/d | \$$
 $C \rightarrow \cdot aC, a/d | \$$
 $C \rightarrow \cdot d, a/d | \$$

I_4 \Rightarrow $C \rightarrow d \cdot, a/d$

I_7 \Rightarrow $C \rightarrow d \cdot, \$$

$\Rightarrow I_{47}$ \Rightarrow $C \rightarrow d \cdot, a/d | \$$

I_8 : \Rightarrow $C \rightarrow aC \cdot, a/d$

I_9 \Rightarrow $C \rightarrow aC \cdot, \$$

$\Rightarrow I_{89}$ \Rightarrow $C \rightarrow aC \cdot, a/d | \$$

LALR(1) Parsing Table

States	Action Part			Goto Part	
	a	d	\$	S	C
0	S_3	S_4		J	2
1				Accept	
2	S_6	S_7			5
36	S_{36}	S_{47}			89
47	R_3	R_3	R_3		
5				R_1	
89	R_2	R_2	R_2		89
117	R_3	R_3	R_3		
89	R_2	R_2	R_2		
117	R_3	R_3	R_3		

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Conflicts in LALR(1) :-

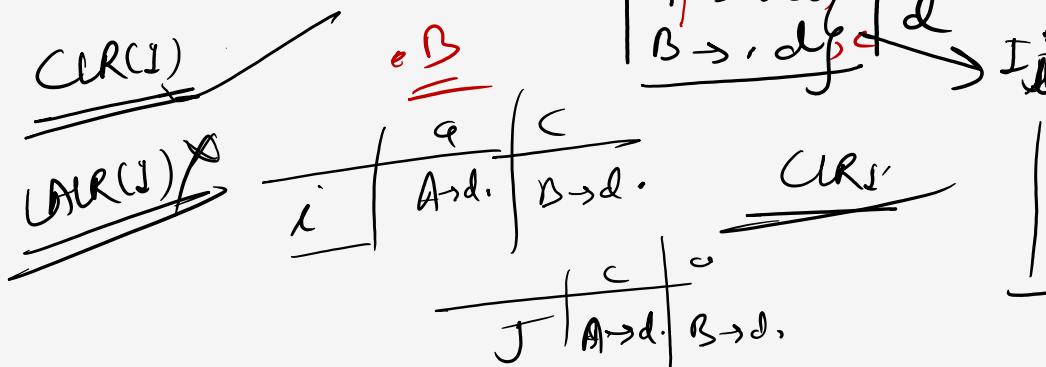
- S/R Conflict } \Rightarrow similar to CLR(1)
- R/R Conflict }



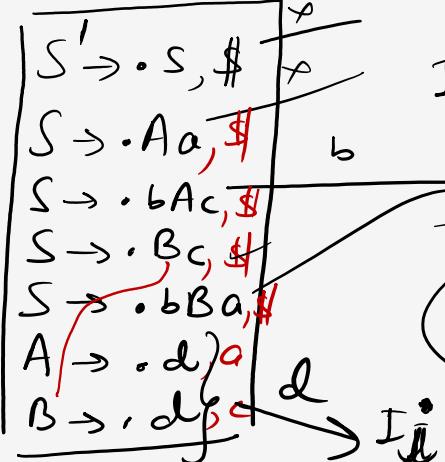
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Question: The following Grammar is $G = \{ S \rightarrow Aa | bAc | Bc | bBa, A \rightarrow d, B \rightarrow d \}$

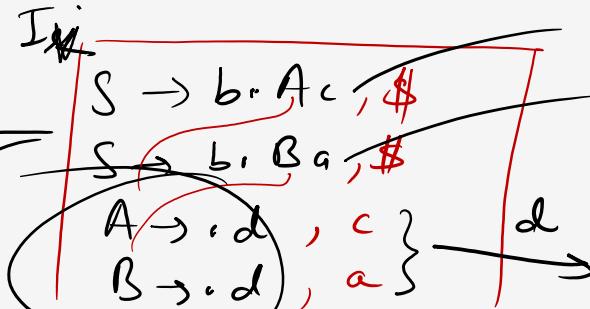
- a) LALR(1) but not CLR(1)
- b) LR(1) but not LALR(1)
- c) Both LALR(1) & LR(1)
- d) Neither LALR(1) nor LR(1)



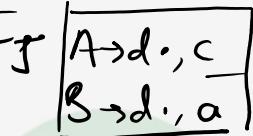
Io



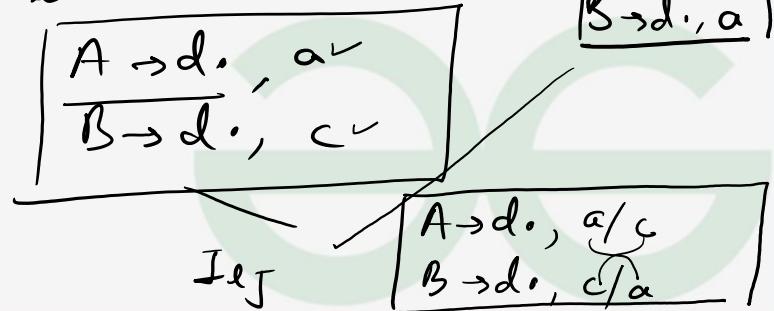
Ir



Ir



CLR'



IrJ

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NOTE:

	<u>CUR(I)</u>	<u>LALR(J)</u>
S/R Conflict	No	No
	Yes	Yes
R/R Conflict	Yes	Yes
	No	Yes/No

$$x \rightarrow y \cong \underline{y \rightarrow x}$$

~~$$Tx \rightarrow y \neq y \rightarrow n$$~~

$$\checkmark (A\text{LR}(1) \Rightarrow C\text{UR}(1))$$

$$C\text{UR}(1) \Rightarrow A\text{LR}(1)$$

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Ex:-

I_e^i

$$\boxed{A \rightarrow \alpha \cdot a\beta, b}$$

No S/R

I_j^j

$$\boxed{A \rightarrow \alpha \cdot a\beta, a}$$

No S/R

I_{ij}^j

$$\boxed{A \rightarrow \alpha \cdot a\beta, b/a}$$

$$\boxed{B \rightarrow r_1 \cdot , c/d}$$

No S/R Conflict.

Ex:

$$\boxed{A \rightarrow \alpha \cdot a\beta, b}$$

No S/R

$$\boxed{A \rightarrow \alpha \cdot a\beta, a}$$

S/R Conflict

$$\boxed{A \rightarrow \alpha \cdot a\beta, b/a}$$

S/R Conflict.

Ex:

I_e^i

$$\boxed{A \rightarrow \alpha \cdot , a/c}$$

No R/R

I_j^j

$$\boxed{A \rightarrow \alpha \cdot , c}$$

R/R Conflict

I_{ij}^j

$$\boxed{A \rightarrow \alpha \cdot , a/c}$$

R/R Conflict

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I_e

$$\boxed{A \rightarrow \alpha \cdot, a \\ B \rightarrow r \cdot, b}$$

No R/R

I_J

$$\boxed{A \rightarrow \alpha \cdot, c \\ B \rightarrow r \cdot, d}$$

No R/R

I_y

$$\boxed{A \rightarrow \alpha \cdot, a/c \\ B \rightarrow r \cdot, b/d}$$

No R/R

I_e

$$\boxed{A \rightarrow \alpha \cdot, a \\ B \rightarrow r \cdot, b}$$

No R/R

I_J

$$\boxed{A \rightarrow \alpha \cdot, c \\ B \rightarrow r \cdot, a}$$

No R/R

I_y

$$\boxed{A \rightarrow \alpha \cdot, a/c \\ B \rightarrow r \cdot, b/a}$$

R/R Conflic.

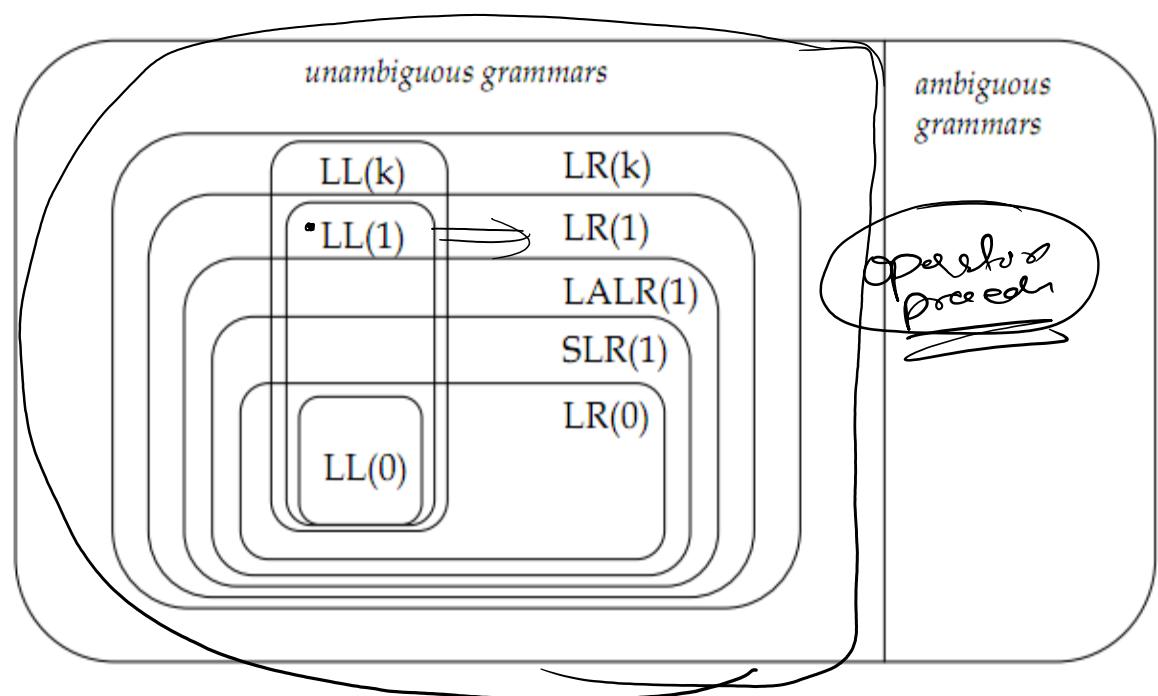


\approx

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LL(1) versus LR(k)

A picture is worth a thousand words:



$$\boxed{LL(K) \Rightarrow LR(K)}$$

$$LL(0) \Rightarrow LR(0)$$

$$LL(1) \Rightarrow LR(1)$$

$$\boxed{LL(2) \Rightarrow LR(2)}$$

$$\cancel{\boxed{LL(1) \Rightarrow LR(0)}}$$

$$LL(0) \Rightarrow LR(0)$$

$$= LR(0)$$

$$\Rightarrow SLR(1)$$

$$\Rightarrow LALR(1)$$

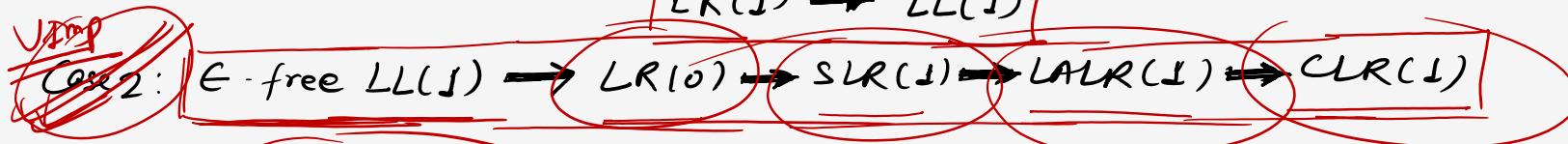
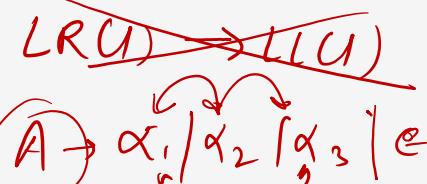
$$\Rightarrow CLR(1)$$

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LL(1) Vs LR(1) :-

Case 1: LL(1) With No Conditions

$$\begin{array}{l} \text{LL}(1) \rightarrow \text{LR}(1) \\ \text{LR}'(1) \rightarrow \text{LL}'(1) \end{array}$$



Question: G: $S \rightarrow CC$
 $C \rightarrow cC | d$

~~a) LL(1)~~

~~b) LL(1) but not LR(0)~~

~~c) LR(0) but not SLR(1)~~

~~d) SLR(1) but not LALR(1)~~

LL(1):

$$\begin{aligned} & \text{first}(CC) \cap \text{first}(d) \\ &= C \cap d = \emptyset \end{aligned}$$

∅

Break

5 mins

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NOTE:-

$$1) \boxed{n_1 = n_2 = n_3 \leq n_4}$$

$$2) |S_1| = |S_2| = |S_3| \leq |S_4|$$

3) ~~Shift entry rule is same for all LR(k) Tables~~

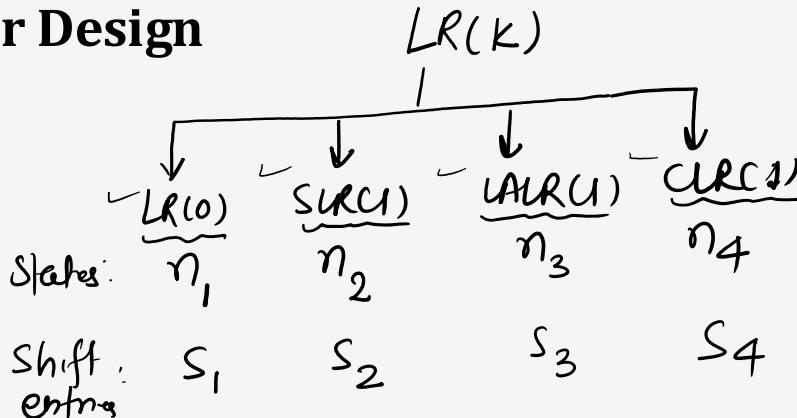
4) Reduce entry rule is different for all LR(k)

5) ~~No. of Reduce entries~~ $|LR(0) \geq SLR(1) \geq LALR(1) \geq CLR(1)|$

6) ~~Power of~~ $|LR(0) < SLR(1) < LALR(1) < CLR(1)|$

7) $|LL(K) = LR(K)|$

8) Among SLR(1), LALR(1) & CLR(1) the most easy method is SLR(1) and the most powerful method is CLR(1)



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YACC Tool :- Yet Another Compiler Compiler (YACC)

YACC is tool which is used to generate LALR Parser

YACC specification

file.y

YACC

y.tab.c

q4.q10/w

y.tab.c

C Compiler

a.out

LALR parser

Syntax Analyzer

1

LS

=>

Recursive Descent
Parsing

Tokens

a.out

Parse tree

NOTE :-

S/R

→ S/~~R~~

⇒ R to L

X	X

R to L

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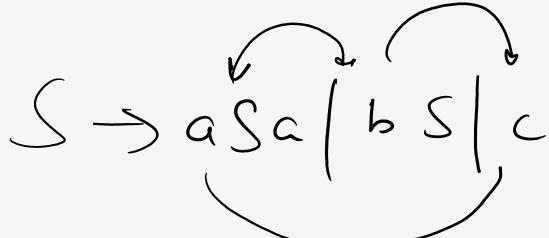
~~4~~
The grammar $S \rightarrow aSa \mid bS \mid c$ is

LL(1) but not LR(1)

LR(1) but not LR(1)

Both LL(1) and LR(1)

Neither LL(1) nor LR(1)



LL(1) \Rightarrow LR(1)



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An LALR(1) parser for a grammar G can have shift-reduce (S-R) conflicts if and only if

- the SLR(1) parser for G has S-R conflicts
- the LR(1) parser for G has S-R conflicts
- the LR(0) parser for G has S-R conflicts
- the LALR(1) parser for G has reduce-reduce conflicts



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Consider the following two statements:

- P: Every regular grammar is LL(1) false
Q: Every regular set has a LR(1) grammar TRUE

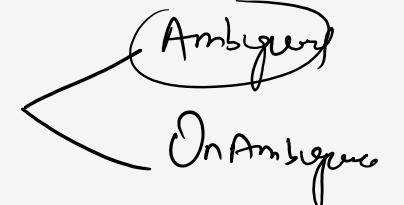
Which of the following is TRUE?

- Both P and Q are true
- P is true and Q is false
- P is false and Q is true
- Both P and Q are false

LL(1) Rule
→ Non left Rec
→ left factored
→ Unr

Regular Grammar

Regular Set or language



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Consider the grammar

$$S \rightarrow (S) \mid a$$

LR(0) items

$$n_1 \quad n_2 \quad n_3$$

Let the number of states in SLR(1), LR(1) and LALR(1) parsers for the grammar be n_1 , n_2 and n_3 respectively. The following relationship holds good

- $n_1 < n_2 < n_3$
- $n_1 = n_3 < n_2$
- $n_1 = n_2 = n_3$
- $n_1 \geq n_3 \geq n_2$

$$\boxed{n_1 = n_3 \leq n_2}$$



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Consider the grammar shown below.

$$\begin{array}{l} S \rightarrow C\ C \\ C \rightarrow c\ C \mid d \end{array}$$

The grammar is

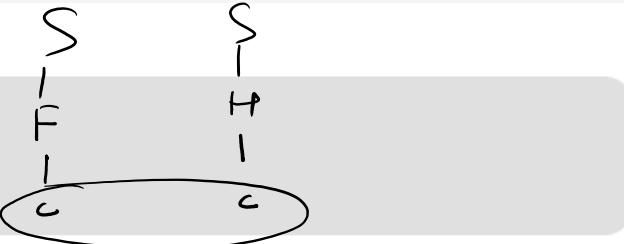
- LL(1)
- SLR(1) but not LL(1)
- LALR(1) but not SLR(1)
- LR(1) but not LALR(1)



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Consider the following grammar G.

$$G' : \left\{ \begin{array}{l} S \rightarrow F \mid H \\ F \rightarrow p \mid c \\ H \rightarrow d \mid c \end{array} \right. \quad \left. \right\}$$



Where S, F and H are non-terminal symbols, p, d and c are terminal symbols. Which of the following statement(s) is/are correct?

- S1: LL(1) can parse all strings that are generated using grammar G. X
- S2: LR(1) can parse all strings that are generated using grammar G. X

- Only S1
- Only S2
- Both S1 and S2
- Neither S1 and S2



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Which is True about SR and RR-conflict:

- If there is no SR-conflict in CLR(1) then definitely there will be no SR-conflict in LALR(1).
- RR-conflict might occur if lookahead for final items(reduce-moves) is same.
- Known that CLR(1) has no RR-conflict, still RR-conflict might occur in LALR(1).
- All of the above.

Ans



1)

$$\begin{array}{r} \underline{\underline{4 - 8}} \\ 6 \end{array}$$

Thank You !

(SDT)
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