

# AI1103: Assignment 6

Chitneedi Geetha Sowmya  
CS20BTECH11011

Download all latex codes from

<https://github.com/Geetha495/Assignment6/blob/main/Assignment6.tex>

Download all python codes from

<https://github.com/Geetha495/Assignment6/blob/main/Assignment6.py>

## 1 PROBLEM

A coin is tossed 4 times. What is the probability of getting heads exactly three times ?

- 1)  $\frac{1}{4}$       2)  $\frac{3}{8}$       3)  $\frac{1}{2}$       4)  $\frac{3}{4}$

## 2 SOLUTION

In an experiment of tossing a coin  $n(=4)$  times, random variable  $X \in \{0, 1, 2, 3\}$  follows binomial distribution.

The binomial distribution formula is:

$$\Pr(X = k) = {}^nC_k \times p^k \times (1 - p)^{n-k} \quad (2.0.1)$$

Where:

$k$	total number of “successes”
$p$	probability of a success on an individual trial
$n$	number of trials = 3

TABLE 0: The binomial distribution formula

Let  $X$  denote the number of heads

$$\Pr(X = 3) = {}^4C_3 \times \left(\frac{1}{2}\right)^3 \times \left(1 - \frac{1}{2}\right)^{4-3} \quad (2.0.2)$$

$$= \frac{1}{4} \quad (2.0.3)$$

Correct option is 1.