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**QUESTION 1:**

Total nylon sheet = 5000sqft

Total working time =  $35 \times 40 \times 60 = 84000$  minutes = 1400 hours

**a) Decision Variables:**

Y1= produced collegiate backpacks per week

Y2= produced Mini Backpacks per week

**b) Objective Function:**

$Z = 32Y1 + 24Y2$  (maximize profit)

**c) Constraints:**

Constrain 1:  $3Y1 + 2Y2 \leq 5000$  (square feet of material nylon to be shipped per week)

Constrain 2:  $Y1 \leq 1000$

Constrain 3:  $Y2 \leq 1200$

Constrain 4:  $45Y1 + 40Y2 \leq 84000 = (45/60) Y1 + (40/60) Y2 \leq 1400$  (converting minutes into hours that is converting 45 minutes into hours by dividing them with 60 (as 1 hour = 60 minutes) and the same case with the 40 minutes and 84000 hours)

**d) Mathematical formulation:**

Max  $Z = 32Y1 + 24Y2$

Subject to the restrictions

$3Y1 + 2Y2 \leq 5000$  (Material)

$Y1 \leq 1000$

$Y2 \leq 1200$

$(3/4) Y1 + (2/3) Y2 \leq 1400$  (Time)

45mins =  $3/4$  hour

40 mins =  $2/3$  hour

where  $Y1, Y2 \geq 0$

## QUESTION 2:

### a) Decision variables

Let A1, B1, and C1 be the quantities of products with large, medium, and small sizes of Plant 1.

Let A2, B2, and C2 be the quantities of products with large, medium, and small sizes of Plant 2.

Let A3, B3, and C3 be the quantities of products with large, medium, and small sizes of Plant 3.

### b) Linear programming model:

i) Decision variables  $\rightarrow A_x, B_x, C_x$

ii) Objective function :

$$Z = 420A1 + 420A2 + 420A3 + 360B1 + 360B2 + 360B3 + 300C1 + 300C2 + 300C3 \text{ (Maximize profit)}$$

### Subject to Constraints:

$$A1 + B1 + C1 \leq 750 \text{ (plant 1 spare capacity)}$$

$$A2 + B2 + C2 \leq 900 \text{ (plant 2 spare capacity)}$$

$$A3 + B3 + C3 \leq 450 \text{ (plant 3 spare capacity)}$$

$$A1 + A2 + A3 \leq 900 \text{ (sales forecast of Large)}$$

$$B1 + B2 + B3 \leq 1200 \text{ (sales forecast of Medium)}$$

$$C1 + C2 + C3 \leq 750 \text{ (sales forecast of Small)}$$

$$20A1 + 15B1 + 12C1 \leq 13000 \text{ (storage space in plant 1)}$$

$$20A2 + 15B2 + 12C2 \leq 12000 \text{ (storage space in plant 2)}$$

$$20A3 + 15B3 + 12C3 \leq 5000 \text{ (storage space in plant 3)}$$

$$A_x, B_x, C_x \geq 0$$

Given that each plant should use equal percentage of its production units

$$900*(A1+B1+C1) = 750*(A2+B2+C3)$$

$$450*(A2+B2+C2) = 900*(A3+B3+C3)$$

$$450*(A1 + B1 + C1) = 750*(A3 + B3 + C3)$$

### Non-Negativity

Where A1, A2, A3, B1, B2, B3, C1, C2, C3  $\geq 0$