

CC

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APCO

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Q Given three integers n , a and b return n^{th} magical no. since the ans may be very large returns a mod modulo. $10^9 + 7$.

A magical no. if no is divisible by either a or b

$$n=1 \quad a=2 \quad b=3$$

$$\text{Out} = 2$$

Approach

- (1) Creating a modulo with value $10^9 + 7$
- (2) calculating sum of a and b with the help of GCD relation

$$\text{lcm} \times \text{gcd} = a \times b$$

- (3) Performing binary search

$$s = \min(a, b) \quad (\text{start})$$

$$e = n \times \min(a, b) \quad (\text{end})$$

$$\text{mid} = \frac{s+e}{2}$$

- (4) Counting magical no $\leq \text{mid}$

$$\text{count} = \frac{\text{mid}}{a} + \frac{\text{mid}}{b} - \frac{\text{mid}}{\text{lcm}}$$

if count $< n$ then $s = \text{mid} + 1$

else $e = \text{mid}$

- (5) return $s \bmod$

Code

```
long long gcd (long long a, long b) {
```

```
    if (b == 0) return 0;
```

```
    return gcd (b, a % b); }
```

```
long long lcm (long long a, long long b) {
```

```
    return (a * b) / gcd (a, b); }
```

```
}
```

```
int nthMagicalNumber (int n, int a, int b) {
```

```
    int mod = 100000000007;
```

```
    long long low = min (a, b);
```

```
    long long high = n * min (a, b);
```

```
    long long L = lcm (a, b);
```

```
    while (low < high) {
```

```
        long long mid = low + (high - low) / 2;
```

```
        long long count = mid / a + mid / b - mid / c;
```

```
        if (count < n)
```

```
            low = mid + 1;
```

```
        else
```

```
            high = mid;
```

```
}
```

```
    return low % MOD;
```

```
}
```

```
int main () {
```

```
    cout << nthMagicalNumber (1, 2, 3);
```

```
}
```

Output = 2