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# **PyREx Documentation**

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## INTRODUCTION

PyREx (**P**ython package for an IceCube **R**adio **E**xtension) is, as its name suggests, a python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas, as in the ARA and ARIANA collaborations.

The most basic simulation can be produced as follows:

First, import the package:

```
import pyrex
```

Then, create a particle generator object that will produce random particles in a cube of 1 km on each side with a fixed energy of 100 PeV:

```
particle_generator = pyrex.ShadowGenerator(dx=1000, dy=1000, dz=1000,  
                                           energy_generator=lambda: 1e8)
```

An array of antennas that represent the detector is also needed. The base `Antenna` class provides a basic antenna with a flat frequency response and no trigger condition. Here we make a single vertical “string” of four antennas with no noise:

```
antenna_array = []  
for z in [-100, -150, -200, -250]:  
    antenna_array.append(  
        pyrex.Antenna(position=(0,0,z), noisy=False)  
    )
```

Finally, we want to pass these into the `EventKernel` and produce an event:

```
kernel = pyrex.EventKernel(generator=particle_generator,  
                           ice_model=pyrex.IceModel, antennas=antenna_array)  
kernel.event()
```

Now the signals received by each antenna can be accessed by their `waveforms` parameter:

```
import matplotlib.pyplot as plt  
for ant in kernel.ant_array:  
    for wave in ant.waveforms:  
        plt.figure()  
        plt.plot(wave.times, wave.values)  
        plt.show()
```



## CODE EXAMPLES

The following code examples assume these imports:

```
import numpy as np
import matplotlib.pyplot as plt
import pyrex
```

All of the following examples can also be found (and quickly run) in the Code Examples python notebook.

### 2.1 Working with Signal Objects

The base `Signal` class is simply an array of times and an array of signal values, and is instantiated with these two arrays. The `times` array is assumed to be in units of seconds, but there are no general units for the `values` array (though it is commonly assumed to be in volts or volts per meter). It is worth noting that the `Signal` object stores shallow copies of the passed arrays, so changing the original arrays will not affect the `Signal` object.

```
time_array = np.linspace(0, 10)
value_array = np.sin(time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)
```

Plotting the `Signal` object is as simple as plotting the times vs the values:

```
plt.plot(my_signal.times, my_signal.values)
```

`Signal` objects can be added as long as they have the same time array, and also support the python `sum` function:

```
time_array = np.linspace(0, 10)
values1 = np.sin(time_array)
values2 = np.cos(time_array)
signal1 = pyrex.Signal(time_array, values1)
plt.plot(signal1.times, signal1.values, label="signal1")
signal2 = pyrex.Signal(time_array, values2)
plt.plot(signal2.times, signal2.values, label="signal2")
signal3 = signal1 + signal2
plt.plot(signal3.times, signal3.values, label="signal3")
all_signals = [signal1, signal2, signal3]
signal4 = sum(all_signals)
plt.plot(signal4.times, signal4.values, label="signal4")
plt.legend()
```

The `Signal` class provides many convenience attributes for dealing with signals:

```
my_signal.dt == my_signal.times[1] - my_signal.times[0]
my_signal.spectrum == scipy.fftpack.fft(my_signal.values)
my_signal.frequencies == scipy.fftpack.fftfreq(n=len(my_signal.values),
                                              d=my_signal.dt)
my_signal.envelope == np.abs(scipy.signal.hilbert(my_signal.values))
```

The `Signal` class also provides functions for manipulating the signal. The `resample` function will resample the times and values arrays to the given number of points (with the same endpoints):

```
my_signal.resample(1001)
len(my_signal.times) == len(my_signal.values) == 1001
my_signal.times[0] == 0
my_signal.times[-1] == 10
```

The `filter_frequencies` function will apply a frequency-domain filter to the values array based on the passed frequency response function:

```
def lowpass_filter(frequency):
    if frequency < 1:
        return 1
    else:
        return 0

time_array = np.linspace(0, 10, 1001)
value_array = np.sin(0.1*2*np.pi*time_array) + np.sin(2*2*np.pi*time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)

plt.plot(my_signal.times, my_signal.values)
my_signal.filter_frequencies(lowpass_filter)
plt.plot(my_signal.times, my_signal.values)
```

A number of classes which inherit from the `Signal` class are included in PyREx: `EmptySignal`, `FunctionSignal`, `AskaryanSignal`, and `ThermalNoise`. `EmptySignal` is simply a signal whose values are all zero:

```
time_array = np.linspace(0,10)
empty = pyrex.EmptySignal(times=time_array)
plt.plot(empty.times, empty.values)
```

`FunctionSignal` takes a function of time and creates a signal based on that function:

```
time_array = np.linspace(0,10)
def square_wave(time):
    if int(time)%2==0:
        return 1
    else:
        return -1
square_signal = pyrex.FunctionSignal(times=time_array, function=square_wave)
plt.plot(square_signal.times, square_signal.values)
```

`AskaryanSignal` produces an Askaryan pulse on a time array due to a neutrino of given energy observed at a given angle from the shower axis:

```
time_array = np.linspace(-10e-9, 40e-9, 1001)
neutrino_energy = 1e5 # TeV
observation_angle = 45 * np.pi/180 # radians
askaryan = pyrex.AskaryanSignal(times=time_array, energy=neutrino_energy,
```



```

                                theta=observation_angle)
plt.plot(askaryan.times, askaryan.values)

```

ThermalNoise produces Rayleigh noise at a given temperature and resistance which has been passed through a bandpass filter of the given frequency range:

```

time_array = np.linspace(-10e-9, 40e-9, 1001)
noise_temp = 300 # K
system_resistance = 1000 # ohm
frequency_range = (550e6, 750e6) # Hz
noise = pyrex.ThermalNoise(times=time_array, temperature=noise_temp,
                           resistance=system_resistance,
                           f_band=frequency_range)
plt.plot(noise.times, noise.values)

```

## 2.2 Antenna Class and Subclasses

The base Antenna class provided by PyREx is designed to be inherited from to match the needs of each project. At its core, an Antenna object is initialized with a position, a temperature, and a frequency range, as well as optionally a resistance for noise calculations and a boolean dictating whether or not noise should be added to the antenna's signals (note that if noise is to be added, a resistance must be specified).

```

position = (0, 0, -100) # m
temperature = 300 # K
resistance = 1 # ohm
frequency_range = (0, 1e3) # Hz
basic_antenna = pyrex.Antenna(position=position, temperature=temperature,
                              resistance=resistance,
                              freq_range=frequency_range)
noiseless_antenna = pyrex.Antenna(position=position, noisy=False)

```

The basic properties of an Antenna object are `is_hit` and `waveforms`. `is_hit` specifies whether or not the antenna has been triggered by an event. `waveforms` is a list of all the waveforms which have triggered the antenna. The antenna also defines `signals`, which is a list of all signals the antenna has received, and `all_waveforms` which is a list of all waveforms (signal plus noise) the antenna has received including those which didn't trigger.

```

basic_antenna.is_hit == False
basic_antenna.waveforms == []

```

The Antenna class defines three methods which are expected to be overwritten: `trigger`, `response`, and `receive`. `trigger` takes a `Signal` object as an argument and returns a boolean of whether or not the antenna would trigger on that signal (default always returns `True`). `response` takes a frequency or list of frequencies (in Hz) and returns the frequency response of the antenna at each frequency given (default always returns 1).

```

basic_antenna.trigger(pyrex.Signal([0],[0])) == True
freqs = [1, 2, 3, 4, 5]
basic_antenna.response(freqs) == [1, 1, 1, 1, 1]

```

The `receive` method is a bit different in that it contains some default functionality:

```

def receive(self, signal):
    copy = Signal(signal.times, signal.values)
    copy.filter_frequencies(self.response)
    self.signals.append(copy)

```

In this sense, the `receive` function is intended to be extended instead of overwritten. In derived classes, it is recommended that a newly defined `receive` function call `super().receive(signal)`. For example, if a polarization is to be applied, the following `receive` function could be implemented:

```
def receive(self, signal, signal_polarization):
    polarization_factor = np.vdot(self.polarization, signal_polarization)
    polarized_signal = Signal(signal.times,
                              signal.values * polarization_factor)
    super().receive(polarized_signal)
```

To use the `receive` function, simply pass it the `Signal` object the antenna sees, and the `Antenna` class will handle the rest:

```
incoming_signal = pyrex.FunctionSignal(np.linspace(0,10), np.sin)
basic_antenna.receive(incoming_signal)
basic_antenna.is_hit == True
for wave in basic_antenna.waveforms:
    plt.figure()
    plt.plot(wave.times, wave.values)
    plt.show()
for pure_signal in basic_antenna.signals:
    plt.figure()
    plt.plot(pure_signal.times, pure_signal.values)
    plt.show()
```

The `Antenna` class also defines a `clear` method which will reset the antenna to a state of having received no signals:

```
basic_antenna.clear()
basic_antenna.is_hit == False
len(basic_antenna.waveforms) == 0
```

To create a custom antenna, simply inherit from the `Antenna` class:

```
class NoiselessThresholdAntenna(pyrex.Antenna):
    def __init__(self, position, threshold):
        super().__init__(position=position, noisy=False)
        self.threshold = threshold

    def trigger(self, signal):
        if max(np.abs(signal.values)) > self.threshold:
            return True
        else:
            return False
```

Our custom `NoiselessThresholdAntenna` should only trigger when the amplitude of a signal exceeds its threshold value:

```
my_antenna = NoiselessThresholdAntenna(position=(0, 0, 0), threshold=2)

incoming_signal = pyrex.FunctionSignal(np.linspace(0,10), np.sin)
my_antenna.receive(incoming_signal)
my_antenna.is_hit == False
len(my_antenna.waveforms) == 0
len(my_antenna.all_waveforms) == 1

incoming_signal = pyrex.Signal(incoming_signal.times,
                               5*incoming_signal.values)
my_antenna.receive(incoming_signal)
```

```

my_antenna.is_hit == True
len(my_antenna.waveforms) == 1
len(my_antenna.all_waveforms) == 2

for wave in my_antenna.waveforms:
    plt.figure()
    plt.plot(wave.times, wave.values)
    plt.show()

```

PyREx defines `DipoleAntenna` which as a subclass of `Antenna`, which provides a basic threshold trigger, a basic bandpass filter, and a polarization effect on the reception of a signal. A `DipoleAntenna` object is created as follows:

```

antenna_identifier = "antenna 1"
position = (0, 0, -100)
center_frequency = 250 # MHz
bandwidth = 200 # MHz
resistance = 1000 # ohm
antenna_length = 1 # m
polarization_direction = (0, 0, 1)
trigger_threshold = 1e-5 # V
dipole = pyrex.DipoleAntenna(name=antenna_identifier, position=position,
                             center_frequency=center_frequency,
                             bandwidth=bandwidth, resistance=resistance,
                             effective_height=antenna_length,
                             polarization=polarization_direction,
                             trigger_threshold=trigger_threshold)

```

## 2.3 Ice and Earth Models

PyREx provides a class `IceModel`, which is an alias for whichever south pole ice model class is the preferred (currently just the basic `AntarcticIce`). The `IceModel` class provides class methods for calculating characteristics of the ice at different depths and frequencies outlined below:

```

depth = -1000 # m
pyrex.IceModel.temperature(depth)
pyrex.IceModel.index(depth)
pyrex.IceModel.gradient(depth)
frequency = 100 # MHz
pyrex.IceModel.attenuation_length(depth, frequency)

```

PyREx also provides two functions related to its earth model: `prem_density` and `slant_depth`. `prem_density` calculates the density in grams per cubic centimeter of the earth at a given radius:

```

radius = 6360000 # m
pyrex.prem_density(radius)

```

`slant_depth` calculates the material thickness in grams per square centimeter of a chord cutting through the earth at a given nadir angle, starting from a given depth:

```

nadir_angle = 60 * np.pi/180 # radians
depth = 1000 # m
pyrex.slant_depth(nadir_angle, depth)

```

## 2.4 Particle Generation

PyREx includes `Particle` as a container for information about neutrinos which are generated to produce Askaryan pulses. `Particle` contains three attributes: `vertex`, `direction`, and `energy`:

```
initial_position = (0,0,0) # m
direction_vector = (0,0,-1)
particle_energy = 1e8 # GeV
pyrex.Particle(vertex=initial_position, direction=direction_vector,
               energy=particle_energy)
```

PyREx also includes a `ShadowGenerator` class for generating random neutrinos, taking into account some Earth shadowing. The neutrinos are generated in a box of given size, and with an energy given by an energy generation function:

```
box_width = 1000 # m
box_depth = 500 # m
const_energy_generator = lambda: 1e8 # GeV
my_generator = pyrex.ShadowGenerator(dx=box_width, dy=box_width,
                                     dz=box_depth,
                                     energy_generator=const_energy_generator)
my_generator.create_particle()
```

## 2.5 Ray Tracing

While PyREx does not currently support full ray tracing, it does provide a `PathFinder` class which implements some basic ray analysis by Snell's law. `PathFinder` takes an ice model and two points as arguments and provides a number of properties and methods regarding the path between the points.

```
start = (0, 0, -100) # m
finish = (0, 0, -250) # m
my_path = pyrex.PathFinder(ice_model=pyrex.IceModel,
                          from_point=start, to_point=finish)
```

`PathFinder.exists` is a boolean value of whether or not the path between the points is traversable according to the indices of refraction. `PathFinder.emitted_ray` is a unit vector giving the direction from `from_point` to `to_point`. `PathFinder.path_length` is the length in meters of the straight line path between the two points.

```
my_path.exists
my_path.emitted_ray
my_path.path_length
```

`PathFinder.time_of_flight()` calculates the time it takes for light to traverse the path, with an optional parameter `n_steps` defining the precision used. `PathFinder.tof` is a convenience property set to the time of flight using the default value of `n_steps`.

```
my_path.time_of_flight(n_steps=100)
my_path.time_of_flight() == my_path.tof
```

`PathFinder.attenuation()` calculates the attenuation factor along the path for a signal of given frequency. Here again there is an optional parameter `n_steps` defining the precision used.

```
frequency = 1e9 # Hz
my_path.attenuation(f=frequency, n_steps=100)
```

Finally, `PathFinder.propagate()` propagates a `Signal` object from `from_point` to `to_point` by applying a `1/PathFinder.path_length` factor, applying the frequency attenuation of `PathFinder.attenuation()`, and shifting the signal times by `PathFinder.tof`:

```
time_array = np.linspace(0, 5e-9, 1001)
my_signal = (pyrex.FunctionSignal(time_array, lambda t: np.sin(1e9*2*np.pi*t))
             + pyrex.FunctionSignal(time_array, lambda t: np.sin(1e10*2*np.pi*t)))
plt.plot(my_signal.times, my_signal.values)
plt.show()

my_path.propagate(my_signal)
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

## 2.6 Full Simulation

PyREx provides the `EventKernel` class to control a basic simulation including the creation of neutrinos, the propagation of their pulses to the antennas, and the triggering of the antennas:

```
particle_generator = pyrex.ShadowGenerator(dx=1000, dy=1000, dz=500,
                                           energy_generator=lambda: 1e8)

detector = []
for i, z in enumerate([-100, -150, -200, -250]):
    detector.append(
        pyrex.DipoleAntenna(name="antenna_"+str(i), position=(0, 0, z),
                           center_frequency=500, bandwidth=500,
                           resistance=0, effective_height=1,
                           trigger_threshold=0, noisy=False)
    )
kernel = pyrex.EventKernel(generator=particle_generator,
                          ice_model=pyrex.IceModel,
                          antennas=detector)

triggered = False
while not triggered:
    kernel.event()
    for antenna in detector:
        if antenna.is_hit:
            triggered = True
            break

for antenna in detector:
    for i, wave in enumerate(antenna.waveforms):
        plt.plot(wave.times * 1e9, wave.values)
        plt.xlabel("Time (ns)")
        plt.ylabel("Voltage (V)")
        plt.title(antenna.name + " - waveform " + str(i))
```

## 2.7 More Examples

For more code examples, see the [PyREx Demo python notebook](#).



## 3.1 Package contents

**class** `pyrex.Signal` (*times, values*)

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

**dt**

Returns the spacing of the time array, or None if invalid.

**envelope**

Calculates envelope of the signal by Hilbert transform.

**resample** (*n*)

Resamples the signal into n points in the same time range.

**spectrum**

Returns the FFT spectrum of the signal.

**frequencies**

Returns the FFT frequencies of the signal.

**filter\_frequencies** (*freq\_response*)

Applies the given frequency response function to the signal.

**class** `pyrex.EmptySignal` (*times*)

Bases: `pyrex.signals.Signal`

Class for signal with no amplitude (all values = 0)

**class** `pyrex.FunctionSignal` (*times, function*)

Bases: `pyrex.signals.Signal`

Class for signals generated by a function

`pyrex.AskaryanSignal`

alias of `FastAskaryanSignal`

**class** `pyrex.signals.FastAskaryanSignal` (*times, energy, theta, n=1.78, t0=0*)

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

**vector\_potential**

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

**RAC** (*time*)

Calculates  $R * \text{vector potential (A)}$  at the Cherenkov angle in Vs at the given time (s).

**charge\_profile** (*z, density=0.92, crit\_energy=7.86e-05, rad\_length=36.08*)

Calculates the longitudinal charge profile in the EM shower at distance  $z$  (m) with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

**max\_length** (*density=0.92, crit\_energy=7.86e-05, rad\_length=36.08*)

Calculates the maximum length (m) of an EM shower with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

**class** `pyrex.ThermalNoise` (*times, temperature, resistance, f\_band, f\_amplitude=1, n\_freqs=0*)

Bases: `pyrex.signals.Signal`

Thermal Rayleigh noise at a given temperature (K) and resistance (ohms) in the frequency band `f_band=[f_min,f_max]` (Hz). Optional parameters are `f_amplitude` (default 1) which can be a number or a function designating the amplitudes at each frequency, and `n_freqs` which is the number of frequencies to use (in `f_band`) for the calculation (default is based on the FFT bin size of given times array). Returned signal values are voltages (V).

**class** `pyrex.Antenna` (*position, temperature=None, freq\_range=None, resistance=None, noisy=True*)

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

**is\_hit**

Test for whether the antenna has received a signal.

**isHit** ()

Deprecated. Replaced by `is_hit` property.

**clear** ()

Reset the antenna to a state of having received no signals.

**waveforms**

Signal + noise (if noisy) at each triggered antenna hit.

**all\_waveforms**

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

**trigger** (*signal*)

Function to determine whether or not the antenna is triggered by the given Signal object.

**response** (*frequencies*)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

**receive** (*signal, polarization=[0, 0, 1]*)

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this function, but should end with `super().receive(signal)`.

**class** `pyrex.DipoleAntenna` (*name, position, center\_frequency, bandwidth, resistance, effective\_height, polarization=[0, 0, 1], trigger\_threshold=0, noisy=True*)

Bases: `pyrex.antenna.Antenna`

Antenna with a given name, position (m), center frequency (MHz), bandwidth (MHz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).



**trigger** (*signal*)

Trigger on the signal if the maximum signal value is above the given threshold.

**response** (*frequencies*)

Butterworth filter response for the antenna's frequency range.

**receive** (*signal, polarization=[0, 0, 1]*)

Apply polarization effect to signal, then proceed with usual antenna reception.

`pyrex.IceModel`

alias of `AntarcticIce`

**class** `pyrex.ice_model.AntarcticIce`

Bases: `object`

Class containing characteristics of ice at the south pole.

**k = 0.438**

**a = 0.0132**

**n0 = 1.32**

**thickness = 2850**

**classmethod** `gradient` (*z*)

Returns the gradient of the index of refraction at depth *z* (m).

**classmethod** `index` (*z*)

Returns the medium's index of refraction, *n*, at depth *z* (m).

**static** `temperature` (*z*)

Returns the temperature (K) of the ice at depth *z* (m)

**classmethod** `attenuation_length` (*z, f*)

Returns the attenuation length at depth *z* (m) and frequency *f* (MHz). Supports passing a list of frequencies with a single depth.

`pyrex.prem_density` (*r*)

Returns the earth's density (g/cm<sup>3</sup>) for a given radius *r* (m). Calculated by the Preliminary Earth Model (PREM).

`pyrex.slant_depth` (*angle, depth, step=5000*)

Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth (m).

**class** `pyrex.Particle`

Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy (GeV).

**direction**

**energy**

**vertex**

**class** `pyrex.ShadowGenerator` (*dx, dy, dz, energy\_generator*)

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into account Earth shadowing (sort of). `energy_generator` should be a function that returns a particle energy in GeV.

**create\_particle** ()

Creates a particle with random vertex in cube and random direction.

**class** `pyrex.PathFinder` (*ice\_model, from\_point, to\_point*)

Class for ray tracking.

**exists**

Boolean of whether path exists.

**emitted\_ray**

Direction in which ray is emitted.

**path\_length**

Length of the path (m).

**tof**

Time of flight (s) for a particle along the path. Calculated using default values of `self.time_of_flight()`

**time\_of\_flight** (*n\_steps=10*)

Time of flight (s) for a particle along the path.

**attenuation** (*f, n\_steps=10*)

Returns the attenuation factor for a signal of frequency *f* (Hz) traveling along the path. Supports passing a list of frequencies.

**propagate** (*signal*)

Applies attenuation to the signal along the path.

**class** `pyrex.EventKernel` (*generator, ice\_model, antennas*)

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

**event** ()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

## 3.2 Submodules

### 3.2.1 `pyrex.signals` module

Module containing classes for digital signal processing

**class** `pyrex.signals.Signal` (*times, values*)

Bases: `object`

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

**dt**

Returns the spacing of the time array, or `None` if invalid.

**envelope**

Calculates envelope of the signal by Hilbert transform.

**resample** (*n*)

Resamples the signal into *n* points in the same time range.

**spectrum**

Returns the FFT spectrum of the signal.

**frequencies**

Returns the FFT frequencies of the signal.

**filter\_frequencies** (*freq\_response*)

Applies the given frequency response function to the signal.

```
class pyrex.signals.EmptySignal(times)
```

Bases: `pyrex.signals.Signal`

Class for signal with no amplitude (all values = 0)

```
class pyrex.signals.FunctionSignal(times,function)
```

Bases: `pyrex.signals.Signal`

Class for signals generated by a function

```
class pyrex.signals.SlowAskaryanSignal(times,energy,theta,n=1.78,t0=0)
```

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as  $1/R$ , where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

**RAC** (time)

Calculates  $R * \text{vector potential}$  at the Cherenkov angle in Vs at the given time (s).

**charge\_profile** (z,density=0.92,crit\_energy=7.86e-05,rad\_length=36.08)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

**max\_length** (density=0.92,crit\_energy=7.86e-05,rad\_length=36.08)

Calculates the maximum length (m) of an EM shower with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

```
class pyrex.signals.FastAskaryanSignal(times,energy,theta,n=1.78,t0=0)
```

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as  $1/R$ , where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

**vector\_potential**

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

**RAC** (time)

Calculates  $R * \text{vector potential}$  (A) at the Cherenkov angle in Vs at the given time (s).

**charge\_profile** (z,density=0.92,crit\_energy=7.86e-05,rad\_length=36.08)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

**max\_length** (density=0.92,crit\_energy=7.86e-05,rad\_length=36.08)

Calculates the maximum length (m) of an EM shower with parameters for the density ( $\text{g/cm}^3$ ), critical energy (TeV), and electron radiation length ( $\text{g/cm}^2$ ) in ice.

```
pyrex.signals.AskaryanSignal
```

alias of `FastAskaryanSignal`

```
class pyrex.signals.GaussianNoise(times,sigma)
```

Bases: `pyrex.signals.FunctionSignal`

Gaussian noise signal with standard deviation sigma

```
class pyrex.signals.ThermalNoise(times, temperature, resistance, f_band, f_amplitude=1,
                                n_freqs=0)
```

Bases: `pyrex.signals.Signal`

Thermal Rayleigh noise at a given temperature (K) and resistance (ohms) in the frequency band `f_band=[f_min,f_max]` (Hz). Optional parameters are `f_amplitude` (default 1) which can be a number or a function designating the amplitudes at each frequency, and `n_freqs` which is the number of frequencies to use (in `f_band`) for the calculation (default is based on the FFT bin size of given times array). Returned signal values are voltages (V).

### 3.2.2 pyrex.antenna module

Module containing antenna class capable of receiving signals

```
class pyrex.antenna.Antenna(position, temperature=None, freq_range=None, resistance=None,
                             noisy=True)
```

Bases: `object`

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

**is\_hit**

Test for whether the antenna has received a signal.

**isHit ()**

Deprecated. Replaced by `is_hit` property.

**clear ()**

Reset the antenna to a state of having received no signals.

**waveforms**

Signal + noise (if noisy) at each triggered antenna hit.

**all\_waveforms**

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

**trigger (signal)**

Function to determine whether or not the antenna is triggered by the given `Signal` object.

**response (frequencies)**

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

**receive (signal, polarization=[0, 0, 1])**

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should end with `super().receive(signal)`.

```
class pyrex.antenna.DipoleAntenna(name, position, center_frequency, bandwidth, resistance, ef-
                                  fective_height, polarization=[0, 0, 1], trigger_threshold=0,
                                  noisy=True)
```

Bases: `pyrex.antenna.Antenna`

Antenna with a given name, position (m), center frequency (MHz), bandwidth (MHz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

**trigger (signal)**

Trigger on the signal if the maximum signal value is above the given threshold.

**response** (*frequencies*)

Butterworth filter response for the antenna's frequency range.

**receive** (*signal, polarization=[0, 0, 1]*)

Apply polarization effect to signal, then proceed with usual antenna reception.

### 3.2.3 pyrex.ice\_model module

Module containing ice model. AntarcticIce class contains static and class methods for easy swapping of models. IceModel class is set to the preferred ice model.

**class** `pyrex.ice_model.AntarcticIce`

Bases: `object`

Class containing characteristics of ice at the south pole.

**k** = 0.438

**a** = 0.0132

**n0** = 1.32

**thickness** = 2850

**classmethod** `gradient` (*z*)

Returns the gradient of the index of refraction at depth *z* (m).

**classmethod** `index` (*z*)

Returns the medium's index of refraction, *n*, at depth *z* (m).

**static** `temperature` (*z*)

Returns the temperature (K) of the ice at depth *z* (m)

**classmethod** `attenuation_length` (*z, f*)

Returns the attenuation length at depth *z* (m) and frequency *f* (MHz). Supports passing a list of frequencies with a single depth.

**class** `pyrex.ice_model.NewcombIce`

Bases: `pyrex.ice_model.AntarcticIce`

Class inheriting from AntarcticIce, with new `attenuation_length` function based on Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE ANTARCTICICE).

**classmethod** `attenuation_length` (*z, f*)

Returns the attenuation length at depth *z* (m) and frequency *f* (MHz) by Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE BOGORODSKY).

`pyrex.ice_model.IceModel`

alias of `AntarcticIce`

### 3.2.4 pyrex.earth\_model module

Module containing earth model. Uses PREM for density as a function of radius and a simple integrator for calculation of the slant depth as a function of nadir angle.

`pyrex.earth_model.prem_density` (*r*)

Returns the earth's density (g/cm<sup>3</sup>) for a given radius *r* (m). Calculated by the Preliminary Earth Model (PREM).

`pyrex.earth_model.slant_depth` (*angle, depth, step=5000*)

Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth (m).

### 3.2.5 `pyrex.particle` module

Module for particles (namely neutrinos) and neutrino interactions in the ice. Interactions include Earth shadowing (absorption) effect.

**class** `pyrex.particle.NeutrinoInteraction` (*c, p*)

Bases: `object`

Class for neutrino interaction attributes.

**cross\_section** (*E*)

Return the cross section at a given energy *E* (GeV).

**interaction\_length** (*E*)

Return the interaction length at a given energy *E* (GeV).

**class** `pyrex.particle.Particle`

Bases: `tuple`

Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy (GeV).

**direction**

**energy**

**vertex**

`pyrex.particle.random_direction` ()

Generate an arbitrary 3D unit vector.

**class** `pyrex.particle.ShadowGenerator` (*dx, dy, dz, energy\_generator*)

Bases: `object`

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into account Earth shadowing (sort of). `energy_generator` should be a function that returns a particle energy in GeV.

**create\_particle** ()

Creates a particle with random vertex in cube and random direction.

### 3.2.6 `pyrex.ray_tracing` module

Module containing class for ray tracking through the ice. Ray tracing not yet implemented.

**class** `pyrex.ray_tracing.PathFinder` (*ice\_model, from\_point, to\_point*)

Bases: `object`

Class for ray tracking.

**exists**

Boolean of whether path exists.

**emitted\_ray**

Direction in which ray is emitted.

**path\_length**

Length of the path (m).

**tof**

Time of flight (s) for a particle along the path. Calculated using default values of `self.time_of_flight()`

**time\_of\_flight** (*n\_steps=10*)

Time of flight (s) for a particle along the path.

**attenuation** (*f, n\_steps=10*)

Returns the attenuation factor for a signal of frequency *f* (Hz) traveling along the path. Supports passing a list of frequencies.

**propagate** (*signal*)

Applies attenuation to the signal along the path.

### 3.2.7 pyrex.kernel module

Module for the simulation kernel. Includes neutrino generation, ray tracking (no raytracing yet), and hit generation.

**class** `pyrex.kernel.EventKernel` (*generator, ice\_model, antennas*)

Bases: `object`

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

**event** ()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.





## VERSION HISTORY

### 4.1 Version 1.0.2

- Performance improvements:
  - Allow for `IceModel` to calculate many attenuation lengths at once. Improves speed of `PathFinder.propagate()`.

### 4.2 Version 1.0.1

- Fixed bugs in `AskaryanSignal` that caused the convolution to fail.
- Changed `Antenna` not require a temperature and frequency range if no noise is produced.
- Fixed bugs resulting from converting `IceModel.temperature()` from Celsius to Kelvin.

### 4.3 Version 1.0.0

- Created `PyREx` package based on original notebook.
- Added all signal classes to produce full-waveform Askaryan pulses and thermal noise.
- Changed `Antenna` class to `DipoleAntenna` to allow `Antenna` to be a base class.
- Changed `Antenna.isHit()` method to `Antenna.is_hit` property.
- Introduced `IceModel` alias for `AntarcticIce` (or any future preferred ice model).
- Moved `AntarcticIce.attenuationLengthMN` to its own `NewcombIce` class inheriting from `AntarcticIce`.
- Added `PathFinder.propagate()` to propagate a `Signal` object in a customizable way.
- Changed naming conventions to be more consistent, verbose, and “pythonic”:
  - `AntarcticIce.attenuationLength()` becomes `AntarcticIce.attenuation_length()`.
  - In `pyrex.earth_model`, `RE` becomes `EARTH_RADIUS`.
  - In `pyrex.particle`, `neutrino_interaction` becomes `NeutrinoInteraction`.
  - In `pyrex.particle`, `NA` becomes `AVOGADRO_NUMBER`.
  - `particle` class becomes `Particle` namedtuple.

- \* `Particle.vtx` becomes `Particle.vertex`.
- \* `Particle.dir` becomes `Particle.direction`.
- \* `Particle.E` becomes `Particle.energy`.
- In `pyrex.particle`, `next_direction()` becomes `random_direction()`.
- `shadow_generator` becomes `ShadowGenerator`.
- `PathFinder` methods become properties where reasonable:
  - \* `PathFinder.exists()` becomes `PathFinder.exists`.
  - \* `PathFinder.getEmittedRay()` becomes `PathFinder.emitted_ray`.
  - \* `PathFinder.getPathLength()` becomes `PathFinder.path_length`.
- `PathFinder.propagateRay()` split into `PathFinder.time_of_flight()` (with corresponding `PathFinder.tof` property) and `PathFinder.attenuation()`.

## 4.4 Version 0.0.0

Original PyREx python notebook written by Kael Hanson:

<https://gist.github.com/physkael/898a64e6fbf5f0917584c6d31edf7940>

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