PyREx Documentation

Release 1.5.0

Ben Hokanson-Fasig

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CHAPTER

ONE

ABOUT PYREX

PyREx (**Py**thon package for an IceCube **R**adio **Ex**tension) is, as its name suggests, a Python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas (e.g. the ARA and ARIANA collaborations).

1.1 Installation

The easiest way to get the PyREx package is using pip as follows:

```
pip install git+https://github.com/bhokansonfasig/pyrex#egg=pyrex
```

PyREx requires python version 3.6+ as well as numpy version 1.13+ and scipy version 0.19+, which should be automatically installed when installing via pip.

Alternatively, you can download the code from https://github.com/bhokansonfasig/pyrex and then either include the pyrex directory (the one containing the python modules) in your PYTHON_PATH, or just copy the pyrex directory into your working directory. PyREx is not currently available on PyPI, so a simple pip install pyrex will not have the intended effect.

1.2 Quick Code Example

The most basic simulation can be produced as follows:

First, import the package:

```
import pryex
```

Then, create a particle generator object that will produce random particles in a cube of 1 km on each side with a fixed energy of 100 PeV:

An array of antennas that represent the detector is also needed. The base Antenna class provides a basic antenna with a flat frequency response and no trigger condition. Here we make a single vertical "string" of four antennas with no noise:

```
antenna_array = []
for z in [-100, -150, -200, -250]:
    antenna_array.append(
```

```
pyrex.Antenna(position=(0,0,z), noisy=False)
)
```

Finally, we want to pass these into the EventKernel and produce an event:

Now the signals received by each antenna can be accessed by their waveforms parameter:

```
import matplotlib.pyplot as plt
for ant in kernel.ant_array:
    for wave in ant.waveforms:
        plt.figure()
        plt.plot(wave.times, wave.values)
        plt.show()
```

1.3 Units

For ease of use, PyREx tries to use consistent units in all classes and functions. The units used are mostly SI with a few exceptions listed in bold below:

Metric	Unit
time	seconds (s)
frequency	hertz (Hz)
distance	meters (m)
density	grams per cubic centimeter (g/cm^3)
material thickness	grams per square centimeter (g/cm^2)
temperature	kelvin (K)
energy	gigaelectronvolts (GeV)
resistance	ohms (Ω)
voltage	volts (V)
electric field	volts per meter (V/m)

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CHAPTER

TWO

CODE EXAMPLES

The following code examples assume these imports:

```
import numpy as np
import matplotlib.pyplot as plt
import scipy.fftpack
import pyrex
```

All of the following examples can also be found (and quickly run) in the Code Examples python notebook.

2.1 Working with Signal Objects

The base Signal class is simply an array of times and an array of signal values, and is instantiated with these two arrays. The times array is assumed to be in units of seconds, but there are no general units for the values array. It is worth noting that the Signal object stores shallow copies of the passed arrays, so changing the original arrays will not affect the Signal object.

```
time_array = np.linspace(0, 10)
value_array = np.sin(time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)
```

Plotting the Signal object is as simple as plotting the times vs the values:

```
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

While there are no specified units for a Signal.values, there is the option to specify the value_type of the values. This is done using the Signal.ValueTypes enum. By default, a Signal object has value_type=ValueTypes.unknown. However, if the signal represents a voltage, electric field, or electric power; value_type can be set to Signal.ValueTypes.voltage, Signal.ValueTypes.field, or Signal.ValueTypes.power respectively:

Signal objects can be added as long as they have the same time array and value_type. Signal objects also support the python sum function:

```
time_array = np.linspace(0, 10)
values1 = np.sin(time_array)
values2 = np.cos(time_array)
signal1 = pyrex.Signal(time_array, values1)
```

```
plt.plot(signal1.times, signal1.values, label="signal1 = sin(t)")
signal2 = pyrex.Signal(time_array, values2)
plt.plot(signal2.times, signal2.values, label="signal2 = cos(t)")
signal3 = signal1 + signal2
plt.plot(signal3.times, signal3.values, label="signal3 = sin(t)+cos(t)")
all_signals = [signal1, signal2, signal3]
signal4 = sum(all_signals)
plt.plot(signal4.times, signal4.values, label="signal4 = 2*(sin(t)+cos(t))")
plt.legend()
plt.show()
```

The Signal class provides many convenience attributes for dealing with signals:

The Signal class also provides functions for manipulating the signal. The resample function will resample the times and values arrays to the given number of points (with the same endpoints):

```
my_signal.resample(1001)
len(my_signal.times) == len(my_signal.values) == 1001
my_signal.times[0] == 0
my_signal.times[-1] == 10
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

The with_times function will interpolate/extrapolate the signal's values onto a new times array:

```
new_times = np.linspace(-5, 15)
new_signal = my_signal.with_times(new_times)
plt.plot(new_signal.times, new_signal.values, label="new signal")
plt.plot(my_signal.times, my_signal.values, label="original signal")
plt.legend()
plt.show()
```

The filter_frequencies function will apply a frequency-domain filter to the values array based on the passed frequency response function:

```
def lowpass_filter(frequency):
    if frequency < 1:
        return 1
    else:
        return 0

time_array = np.linspace(0, 10, 1001)
value_array = np.sin(0.1*2*np.pi*time_array) + np.sin(2*2*np.pi*time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)

plt.plot(my_signal.times, my_signal.values)
my_signal.filter_frequencies(lowpass_filter)
plt.plot(my_signal.times, my_signal.values)
plt.show()</pre>
```

A number of classes which inherit from the Signal class are included in PyREx: EmptySignal,

FunctionSignal, AskaryanSignal, and ThermalNoise. EmptySignal is simply a signal whose values are all zero:

```
time_array = np.linspace(0,10)
empty = pyrex.EmptySignal(times=time_array)
plt.plot(empty.times, empty.values)
plt.show()
```

FunctionSignal takes a function of time and creates a signal based on that function:

```
time_array = np.linspace(0, 10, num=101)
def square_wave(time):
    if int(time)%2==0:
        return 1
    else:
        return -1
square_signal = pyrex.FunctionSignal(times=time_array, function=square_wave)
plt.plot(square_signal.times, square_signal.values)
plt.show()
```

Additionally, FunctionSignal leverages its knowledge of the function to more accurately interpolate and extrapolate values for the with times function:

```
new_times = np.linspace(0, 20, num=201)
long_square_signal = square_signal.with_times(new_times)
plt.plot(long_square_signal.times, long_square_signal.values, label="new signal")
plt.plot(square_signal.times, square_signal.values, label="original signal")
plt.legend()
plt.show()
```

AskaryanSignal produces an Askaryan pulse (in V/m) on a time array due to a neutrino of given energy observed at a given angle from the shower axis:

ThermalNoise produces Rayleigh noise (in V) at a given temperature and resistance which has been passed through a bandpass filter of the given frequency range:

Note that since ThermalNoise inherits from FunctionSignal, it can be extrapolated nicely to new times. It may be highly periodic outside of its original time range however, unless a large number of frequencies is requested

on initialization.

2.2 Antenna Class and Subclasses

The base Antenna class provided by PyREx is designed to be inherited from to match the needs of each project. At its core, an Antenna object is initialized with a position, a temperature, and a frequency range, as well as optionally a resistance for noise calculations and a boolean dictating whether or not noise should be added to the antenna's signals (note that if noise is to be added, a resistance must be specified).

The basic properties of an Antenna object are is_hit and waveforms. is_hit specifies whether or not the antenna has been triggered by an event. waveforms is a list of all the waveforms which have triggered the antenna. The antenna also defines signals, which is a list of all signals the antenna has received, and all_waveforms which is a list of all waveforms (signal plus noise) the antenna has received including those which didn't trigger.

```
basic_antenna.is_hit == False
basic_antenna.waveforms == []
```

The Antenna class contains two attributes and three methods which represent characteristics of the antenna as they relate to signal processing. The attributes are efficiency and antenna_factor, and the methods are response, directional_gain, and polarization_gain. The attributes are to be set and the methods overwritten in order to custmoize the way the antenna responds to incoming signals. efficiency is simply a scalar which multiplies the signal the antenna receives (default value is 1). antenna_factor is a factor used in converting received electric fields into voltages (antenna_factor = E / V; default value is 1). response takes a frequency or list of frequencies (in Hz) and returns the frequency response of the antenna at each frequency given (default always returns 1). directional_gain takes angles theta and phi in the antenna's coordinates and returns the antenna's gain for a signal coming from that direction (default always returns 1). directional_gain is dependent on the antenna's orientation, which is defined by its z_axis and x_axis attributes. To change the antenna's orientation, use the set_orientation method which takes z_axis and x_axis arguments. Finally, polarization_gain takes a polarization vector and returns the antenna's gain for a signal with that polarization (default always returns 1).

```
basic_antenna.efficiency == 1
basic_antenna.antenna_factor == 1
freqs = [1, 2, 3, 4, 5]
basic_antenna.response(freqs) == [1, 1, 1, 1, 1]
```

```
basic_antenna.directional_gain(theta=np.pi/2, phi=0) == 1
basic_antenna.polarization_gain([0,0,1]) == 1
```

The Antenna class defines a trigger method which is also expected to be overwritten. trigger takes a Signal object as an argument and returns a boolean of whether or not the antenna would trigger on that signal (default always returns True).

```
basic_antenna.trigger(pyrex.Signal([0],[0])) == True
```

The Antenna class also defines a receive method which takes a Signal object and processes the signal according to the antenna's attributes (efficiency, antenna_factor, response, directional_gain, and polarization_gain as described above). To use the receive function, simply pass it the Signal object the antenna sees, and the Antenna class will handle the rest. You can also optionally specify the origin point of the signal (used in directional_gain calculation) and the polarization direction of the signal (used in polarization_gain calculation). If either of these is unspecified, the corresponding gain will simply be set to 1.

Beyond Antenna.waveforms, the Antenna object also provides methods for checking the waveform and trigger status for arbitrary times: full_waveform and is_hit_during. Both of these methods take a time array as an argument and return the waveform Signal object for those times and whether said waveform triggered the antenna, respectively.

```
total_waveform = basic_antenna.full_waveform(np.linspace(0,20))
plt.plot(total_waveform.times, total_waveform.values, label="Total Waveform")
plt.plot(incoming_signal_1.times, incoming_signal_1.values, label="Pure Signals")
plt.plot(incoming_signal_2.times, incoming_signal_2.values, color="C1")
plt.legend()
plt.show()
basic_antenna.is_hit_during(np.linspace(0, 200e-9)) == True
```

Finally, the Antenna class defines a clear method which will reset the antenna to a state of having received no signals:

```
basic_antenna.clear()
basic_antenna.is_hit == False
len(basic_antenna.waveforms) == 0
```

To create a custom antenna, simply inherit from the Antenna class:

```
class NoiselessThresholdAntenna(pyrex.Antenna):
    def __init__(self, position, threshold):
        super().__init__(position=position, noisy=False)
```

```
def trigger(self, signal):
    if max(np.abs(signal.values)) > self.threshold:
        return True
    else:
        return False
```

Our custom NoiselessThresholdAntenna should only trigger when the amplitude of a signal exceeds its threshold value:

```
my_antenna = NoiselessThresholdAntenna(position=(0, 0, 0), threshold=2)
incoming_signal = pyrex.FunctionSignal(np.linspace(0,10), np.sin,
                                       value_type=pyrex.Signal.ValueTypes.voltage)
my_antenna.receive(incoming_signal)
my_antenna.is_hit == False
len(my_antenna.waveforms) == 0
len(my_antenna.all_waveforms) == 1
incoming_signal = pyrex.Signal(incoming_signal.times,
                               5*incoming_signal.values,
                               incoming_signal.value_type)
my_antenna.receive(incoming_signal)
my_antenna.is_hit == True
len(my_antenna.waveforms) == 1
len(my_antenna.all_waveforms) == 2
for wave in my_antenna.waveforms:
   plt.figure()
   plt.plot(wave.times, wave.values)
   plt.show()
```

For more on customizing PyREx, see the Custom Sub-Package section.

PyREx defines DipoleAntenna which as a subclass of Antenna, which provides a basic threshold trigger, a basic bandpass filter frequency response, a sine-function directional gain, and a typical dot-product polarization effect. A DipoleAntenna object is created as follows:

2.3 AntennaSystem and Detector Classes

The AntennaSystem class is designed to bridge the gap between the basic antenna classes and realistic antenna systems including front-end processing of the antenna's signals. It is designed to be subclassed, but by default it takes as an argument the Antenna class or subclass it is extending, or an object of that class. It provides an interface nearly identical to that of the Antenna class, but where a front_end method (which by default does nothing) is applied to the extended antenna's signals.

To extend an Antenna class or subclass into a full antenna system, subclass the AntennaSystem class and define the front_end method. Optionally a trigger can be defined for the antenna system (by default it uses the antenna's trigger):

Objects of this class can then, for the most part, be interacted with as though they were regular antenna objects:

```
position = (0, 0, -100) \# m
temperature = 300 # K
resistance = 1e17 # ohm
frequency_range = (0, 5) \# Hz
basic_antenna_system = PowerAntennaSystem(position=position,
                                          temperature=temperature,
                                          resistance=resistance,
                                          frequency_range=frequency_range)
basic_antenna_system.trigger(pyrex.Signal([0],[0])) == True
incoming_signal_1 = pyrex.FunctionSignal(np.linspace(0,2*np.pi), np.sin,
                                         value_type=pyrex.Signal.ValueTypes.voltage)
incoming_signal_2 = pyrex.FunctionSignal(np.linspace(4*np.pi,6*np.pi), np.sin,
                                         value_type=pyrex.Signal.ValueTypes.voltage)
basic_antenna_system.receive(incoming_signal_1)
basic_antenna_system.receive(incoming_signal_2, origin=[0,0,-300],
                             polarization=[1,0,0])
basic_antenna_system.is_hit == True
for waveform, pure_signal in zip(basic_antenna_system.waveforms,
                                 basic_antenna_system.signals):
   plt.figure()
   plt.plot(waveform.times, waveform.values, label="Waveform")
   plt.plot(pure_signal.times, pure_signal.values, label="Pure Signal")
   plt.legend()
   plt.show()
```

```
total_waveform = basic_antenna_system.full_waveform(np.linspace(0,20))
plt.plot(total_waveform.times, total_waveform.values, label="Total Waveform")
plt.plot(incoming_signal_1.times, incoming_signal_1.values, label="Pure Signals")
plt.plot(incoming_signal_2.times, incoming_signal_2.values, color="C1")
plt.legend()
plt.show()

basic_antenna_system.is_hit_during(np.linspace(0, 200e-9)) == True

basic_antenna_system.clear()
basic_antenna_system.is_hit == False
len(basic_antenna_system.waveforms) == 0
```

The Detector class is another convenience class meant to be subclassed. It is useful for automatically generating many antennas (as would be used to build a detector). Subclasses must define a set_positions method to assign vector positions to the self.antenna_positions attribute. By default set_positions will raise a NotImplementedError. Additionally subclasses may extend the default build_antennas method which by default simply builds antennas of a passed antenna class using any keyword arguments passed to the method. In addition to simply generating many antennas at desired positions, another convenience of the Detector class is that once the build_antennas method is run, it can be iterated directly as though the object were a list of the antennas it generated. An example of subclassing the Detector class is shown below:

```
class AntennaGrid(pyrex.Detector):
    """A detector composed of a plane of antennas in a rectangular grid layout
    some distance below the ice."""
    def set_positions(self, number, separation=10, depth=-50):
        self.antenna_positions = []
        n_x = int(np.sqrt(number))
        n_y = int(number/n_x)
        dx = separation
        dy = separation
        for i in range(n_x):
            x = -dx * n_x/2 + dx/2 + dx * i
            for j in range(n_y):
                y = -dy*n_y/2 + dy/2 + dy*j
                self.antenna_positions.append((x, y, depth))
grid_detector = AntennaGrid(9)
# Build the antennas
temperature = 300 # K
resistance = 1e17 # ohm
frequency_range = (0, 5) \# Hz
grid_detector.build_antennas(pyrex.Antenna, temperature=temperature,
                             resistance=resistance,
                             freq_range=frequency_range)
plt.figure(figsize=(6,6))
for antenna in grid_detector:
   x = antenna.position[0]
   y = antenna.position[1]
   plt.plot(x, y, "kD")
plt.ylim(plt.xlim())
plt.show()
```

Due to the parallels between Antenna and AntennaSystem, an antenna system may also be used in the custom detector class. Note however, that the antenna positions must be accessed as antenna.antenna.position since

we didn't define a position attribute for the PowerAntennaSystem:

2.4 Ice and Earth Models

PyREx provides a class IceModel, which is an alias for whichever south pole ice model class is the preferred (currently just the basic AntarcticIce). The IceModel class provides class methods for calculating characteristics of the ice at different depths and frequencies outlined below:

```
depth = -1000 # m
pyrex.IceModel.temperature(depth)
pyrex.IceModel.index(depth)
pyrex.IceModel.gradient(depth)
frequency = 1e8 # HZ
pyrex.IceModel.attenuation_length(depth, frequency)
```

PyREx also provides two functions realted to its earth model: prem_density and slant_depth. prem_density calculates the density in grams per cubic centimeter of the earth at a given radius:

```
radius = 6360000 # m
pyrex.prem_density(radius)
```

slant_depth calculates the material thickness in grams per square centimeter of a chord cutting through the earth at a given nadir angle, starting from a given depth:

```
nadir_angle = 60 * np.pi/180 # radians
depth = 1000 # m
pyrex.slant_depth(nadir_angle, depth)
```

2.5 Particle Generation

PyREx includes Particle as a container for information about neutrinos which are generated to produce Askaryan pulses. Particle contains three attributes: vertex, direction, and energy:

```
initial_position = (0,0,0) # m
direction_vector = (0,0,-1)
particle_energy = 1e8 # GeV
```

PyREx also includes a ShadowGenerator class for generating random neutrinos, taking into account some Earth shadowing. The neutrinos are generated in a box of given size, and with an energy given by an energy generation function:

Lastly, PyREx includes ListGenerator and FileGenerator classes which can be used to reproduce pregenerated particles from either a list or from numpy files, respectively.

2.6 Ray Tracing

PyREx provides ray tracing in the RayTracer and RayTracerPath classes. RayTracer takes a launch point and receiving point as arguments (and optionally an ice model and z-step), and will solve for the paths between the points (as RayTracerPath objects).

```
start = (0, 0, -250) # m
finish = (100, 0, -100) # m
my_ray_tracer = pyrex.RayTracer(from_point=start, to_point=finish)
```

The two most useful properties of RayTracer are RayTracer.exists and RayTracer.solutions. RayTracer.exists is a boolean value of whether or not path solutions exist between the launch and receiving points. RayTracer.solutions is the list of (zero or two) RayTracerPath objects which exist between the launch and receiving points. There are many other properties available in RayTracer, outlined in the *PyREx API* section, which are mostly used internally and maybe not interesting otherwise.

```
my_ray_tracer.exists
my_ray_tracer.solutions
```

The RayTracerPath class contains the attributes of the paths between points. The most useful properties of RayTracerPath are RayTracerPath.tof, RayTracerPath.path_length, RayTracerPath.emitted_direction, and RayTracerPath.received_direction. These properties provide the time of flight, path length, and direction of rays at the launch and receiving points respectively.

```
my_path = my_ray_tracer.solutions[0]
my_path.tof
my_path.path_length
my_path.emitted_direction
my_path.received_direction
```

RayTracePath also provides the RayTracePath.attenuation() method which gives the attenuation of the signal at a given frequency (or frequencies), and the RayTracePath.coordinates property which gives the x, y, and z coordinates of the path (useful mostly for plotting, and are not garuanteed to be accurate for other purposes).

```
frequency = 500e6 # Hz
my_path.attenuation(100e6)
```

2.6. Ray Tracing

```
my_path.attenuation(np.linspace(1e8, 1e9, 11))
plt.plot(my_path.coordinates[0], my_path.coordinates[2])
plt.show()
```

Finally, RayTracePath.propagate() propagates a Signal object from the launch point to the receiving point by applying the frequency-dependent attenuation of RayTracePath.attenuation(), and shifting the signal times by RayTracePath.tof. Note that it does not apply a 1/R effect based on the path length. If needed, this effect should be added in manually.

2.7 Full Simulation

PyREx provides the EventKernel class to control a basic simulation including the creation of neutrinos, the propagation of their pulses to the antennas, and the triggering of the antennas:

```
particle_generator = pyrex.ShadowGenerator(dx=1000, dy=1000, dz=500,
                                           energy_generator=lambda: 1e8)
detector = []
for i, z in enumerate([-100, -150, -200, -250]):
   detector.append(
        pyrex.DipoleAntenna(name="antenna_"+str(i), position=(0, 0, z),
                            center_frequency=250e6, bandwidth=300e6,
                            resistance=0, effective_height=0.6,
                            trigger_threshold=0, noisy=False)
kernel = pyrex.EventKernel(generator=particle_generator,
                           ice_model=pyrex.IceModel,
                           antennas=detector)
triggered = False
while not triggered:
   kernel.event()
    for antenna in detector:
        if antenna.is_hit:
            triggered = True
           break
for antenna in detector:
    for i, wave in enumerate(antenna.waveforms):
       plt.plot(wave.times * 1e9, wave.values)
        plt.xlabel("Time (ns)")
        plt.ylabel("Voltage (V)")
        plt.title(antenna.name + " - waveform "+str(i))
```

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2.8 More Examples

For more code examples, see the PyREx Demo python notebook.

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CHAPTER

THREE

CUSTOM SUB-PACKAGE

While the PyREx package provides a basis for simulation, the real benefits come in customizing the analysis for different purposes. To this end the custom sub-package allows for plug-in style modules to be distributed for different collaborations.

By default PyREx comes with a custom module for IREX (IceCube Radio Extension) accessible at pyrex.custom. irex. This module includes a more thorough IREXAntennaSystem class inheriting from the AntennaSystem class which adds a front-end for amplifying the signal, processing signal envelopes, and downsampling the result. It also includes an IREXDetector class designed to easily produce different geometries of IREXAntennaSystem objects.

Other institutions and research groups are encouraged to create their own custom modules to integrate with PyREx. These modules have full access to PyREx as if they were a native part of the package. When PyREx is loaded it automatically scans for these custom modules in certain parts of the filesystem and includes any modules that it can find. The first place searched is the custom directory in the PyREx package itself. Next, if a .pyrex-custom directory exists in the user's home directory (note the leading .), its subdirectories are searched for custom directories and any modules in these directories are included. Finally, if a pyrex-custom directory exists in the current working directory (this time without the leading .), its subdirectories are similarly scanned for modules inside custom directories. Note that if any name-clashing occurs, the first result found takes precedence (without warning). Additionally, none of these custom directories should contain an __init__.py file, or else the plug-in system may not work (For more information on the implementation, see PEP 420 and/or David Beazley's 2015 PyCon talk on Modules and Packages at https://youtu.be/0oTh1CXRaQ0?t=1h25m45s).

As an example, in the following filesystem layout available custom modules are pyrex.custom. pyspice, pyrex.custom.irex, pyrex.custom.ara, pyrex.custom.ariana, and pyrex.custom.my_analysis:

```
/path/to/site-packages/pyrex/
|-- __init__.py
|-- signals.py
|-- antenna.py
|-- ...
|-- custom/
| |-- pyspice.py
| |-- irex/
| | |-- antenna.py
 | |-- ...
/path/to/home_dir/.pyrex-custom/
|-- ara/
| |-- custom/
| |-- ara/
| | | |-- antenna.py
| | | |-- ...
|-- ariana/
| |-- custom/
| | |-- ariana.py
/path/to/cwd/pyrex-custom/
|-- my_analysis_module/
| |-- custom/
| |-- my_analysis.py
```

FOUR

PYREX API

The API documentation here is split into three sections. First, the *Package contents* section documents all classes and functions that are imported by PyREx under a from pyrex import * command. Next, the *Submodules* section is a full documentation of all the modules which make up the base PyREx package. And finally, the *PyREx Custom Subpackage* section documents the custom subpackages contained in PyREx by default.

4.1 Package contents

```
class pyrex.Signal (times, values, value_type=<ValueTypes.undefined: 0>)
```

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

class ValueTypes

Enum containing possible types (units) for signal values.

```
undefined = 0
voltage = 1
field = 2
power = 3
```

dt

Returns the spacing of the time array, or None if invalid.

envelope

Calculates envelope of the signal by Hilbert transform.

$\verb"resample"\,(n)$

Resamples the signal into n points in the same time range.

with_times (new_times)

Returns a signal object representing this signal with a different times array. Uses numpy.iterp on values by default.

spectrum

Returns the FFT spectrum of the signal.

frequencies

Returns the FFT frequencies of the signal.

filter frequencies (freq response)

Applies the given frequency response function to the signal.

```
class pyrex.EmptySignal (times, value_type=<ValueTypes.undefined: 0>)
```

Bases: pyrex.signals.Signal

Class for signal with no amplitude (all values = 0)

```
with times (new times)
```

Returns a signal object representing this signal with a different times array. Returns EmptySignal for new times.

```
class pyrex.FunctionSignal (times, function, value_type=<ValueTypes.undefined: 0>)
```

```
Bases: pyrex.signals.Signal
```

Class for signals generated by a function

```
with times (new times)
```

Returns a signal object representing this signal with a different times array. Leverages knowledge of the function to properly interpolate and extrapolate.

pyrex.AskaryanSignal

alias of FastAskaryanSignal

```
class pyrex.signals.FastAskaryanSignal (times, energy, theta, n=1.78, t0=0)
```

```
Bases: pyrex.signals.Signal
```

Askaryan pulse binned to times from a particle shower with given energy (GeV) observed at angle theta (radians) from the shower axis. Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

vector_potential

Recover the vector_potential from the electric field. Mostly just for testing purposes.

RAC (time)

Calculates R * vector potential (A) at the Cherenkov angle in Vs at the given time (s).

```
charge_profile (z, density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

```
max_length (density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

```
class pyrex. ThermalNoise (times, f_band, f_amplitude=1, rms_voltage=None, temperature=None, resistance=None, n_break=0)
```

```
Bases: pyrex.signals.FunctionSignal
```

Thermal Rayleigh noise in the frequency band f_band=[f_min,f_max] (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are f_amplitude (default 1) which can be a number or a function designating the amplitudes at each frequency, and n_freqs which is the number of frequencies to use (in f_band) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

set_orientation (*z_axis=[0, 0, 1], x_axis=[1, 0, 0]*)

is hit

Test for whether the antenna has been triggered.

is_hit_during(times)

Test for whether the antenna has been triggered during the given times array.

clear()

Reset the antenna to a state of having received no signals.

waveforms

Signal + noise (if noisy) at each triggered antenna hit.

all waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

full_waveform(times)

Signal + noise (if noisy) for the given times array.

make_noise (times)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

directional_gain (theta, phi)

Function to calculate the directive electric field gain of the antenna at given angles theta (polar) and phi (azimuthal) relative to the antenna's orientation.

polarization_gain (polarization)

Function to calculate the electric field gain due to polarization for a given polarization direction.

response (frequencies)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

receive (signal, origin=None, polarization=None)

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should likely end with super().receive(signal).

class pyrex.**DipoleAntenna** (name, position, center_frequency, bandwidth, resistance, orientation=[0, 0,

```
1], trigger_threshold=0, effective_height=None, noisy=True)
```

Bases: pyrex.antenna.Antenna

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

trigger (signal)

Trigger on the signal if the maximum signal value is above the given threshold.

response (frequencies)

Butterworth filter response for the antenna's frequency range.

directional_gain (theta, phi)

Power gain of dipole antenna goes as sin(theta)^2, so electric field gain goes as sin(theta).

polarization_gain (polarization)

Polarization gain is simply the dot product of the polarization with the antenna's z-axis.

class pyrex.AntennaSystem(antenna)

Base class for an antenna system consisting of an antenna and some front-end processes.

```
setup_antenna(*args, **kwargs)
```

Setup the antenna by passing along its init arguments. This function can be overwritten if desired, just make sure to assign the self.antenna attribute in the function.

front_end(signal)

This function should take the signal passed (from the antenna) and return the resulting signal after all processing by the antenna system's front-end. By default it just returns the given signal.

```
is_hit
is_hit_during(times)
signals
waveforms
all_waveforms
full_waveform(times)
```

receive (signal, origin=None, polarization=None)

clear()

Reset the antenna system to a state of having received no signals.

```
trigger (signal)
```

Antenna system trigger. Should return True or False for whether the passed signal triggers the antenna system. By default just matches the antenna's trigger.

```
class pyrex.Detector(*args, **kwargs)
```

Class for automatically generating antenna positions based on geometry criteria. The set_positions method creates a list of antenna positions and the build_antennas method is responsible for actually placing antennas at the generated positions. Once antennas are placed, the class can be directly iterated over to iterate over the antennas (as if it were just a list of antennas itself).

```
test_antenna_positions = True
```

```
set_positions (*args, **kwargs)
```

Not implemented. Should generate positions for the antennas based on the given arguments and assign those positions to the antenna_positions attribute.

```
build_antennas(*args, **kwargs)
```

Sets up antenna objects at the positions stored in the class. By default takes an antenna class and passes a position to the 'position' argument, followed by any other arguments to be passed to this class.

```
triggered(*args, **kwargs)
```

Test for whether the detector is triggered based on the current state of the antennas.

```
clear()
```

Convenience method for clearing all antennas in the detector.

```
pyrex.IceModel
```

alias of ArasimIce

```
class pyrex.ice_model.ArasimIce
```

```
Bases: pyrex.ice_model.AntarcticIce
```

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice. Ice model index is the same as used in the ARA collaboration's arasim package.

k = 0.43

a = 0.0132

```
n0 = 1.78
```

```
pyrex.prem_density(r)
```

Returns the earth's density (g/cm³) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

```
pyrex.slant_depth (angle, depth, step=5000)
```

Returns the material thickness (g/cm²) for a chord cutting through earth at Nadir angle and starting at depth (m).

```
class pyrex.Particle (vertex, direction, energy)
```

Class for storing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector (automatically normalized), and an energy (GeV).

```
class pyrex.ShadowGenerator (dx, dy, dz, energy_generator)
```

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing (sort of). energy_generator should be a function that returns a particle energy in GeV. Note that the x and y ranges are (-dx/2, dx/2) and (-dy/2, dy/2) while the z range is (-dz, 0).

```
create_particle()
```

Creates a particle with random vertex in cube with a random direction.

```
pyrex.RayTracer
```

alias of SpecializedRayTracer

Bases: pyrex.ray_tracing.BasicRayTracer

Ray tracer specifically for ice model with index of refraction n(z) = n0 - k*exp(a*z). Calculations performed using true integral evaluation. Ice model must use methods inherited from pyrex. Antarctic Ice

```
solution_class
```

alias of SpecializedRayTracePath

```
valid_ice_model
z uniform
```

direct_r_max

peak_angle

pyrex.RayTracePath

alias of SpecializedRayTracePath

```
class pyrex.ray_tracing.SpecializedRayTracePath(parent_tracer, launch_angle, direct)
```

Bases: pyrex.ray_tracing.BasicRayTracePath

Class for storing a single ray-trace solution betwen points, specifically for ice model with index of refraction n(z) = n0 - k*exp(a*z). Calculations performed using true integral evaluation (except attenuation). Ice model must use methods inherited from pyrex.AntarcticIce

```
uniformity_factor = 0.99999
```

 $beta_tolerance = 0.005$

valid ice model

z uniform

z_integral (*integrand*, *numerical=False*, *x_func=<function SpecializedRayTracePath*.<*lambda>>*)
Function for integrating a given integrand along the depths of the path.

path_length

tof

attenuation(f)

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a list of frequencies.

coordinates

```
class pyrex.EventKernel (generator, ice_model, antennas)
```

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

```
event()
```

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

4.2 Submodules

4.2.1 pyrex.signals module

Module containing classes for digital signal processing

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

class ValueTypes

Bases: enum. Enum

Enum containing possible types (units) for signal values.

```
undefined = 0
voltage = 1
field = 2
power = 3
```

dt

Returns the spacing of the time array, or None if invalid.

envelope

Calculates envelope of the signal by Hilbert transform.

```
resample(n)
```

Resamples the signal into n points in the same time range.

```
with times (new times)
```

Returns a signal object representing this signal with a different times array. Uses numpy iterp on values by default.

spectrum

Returns the FFT spectrum of the signal.

frequencies

Returns the FFT frequencies of the signal.

filter frequencies (freq response)

Applies the given frequency response function to the signal.

class pyrex.signals.EmptySignal(times, value_type=<ValueTypes.undefined: 0>)

Bases: pyrex.signals.Signal

Class for signal with no amplitude (all values = 0)

with_times (new_times)

Returns a signal object representing this signal with a different times array. Returns EmptySignal for new times

class pyrex.signals.FunctionSignal (times, function, value_type=<ValueTypes.undefined: 0>)

Bases: pyrex.signals.Signal

Class for signals generated by a function

with_times (new_times)

Returns a signal object representing this signal with a different times array. Leverages knowledge of the function to properly interpolate and extrapolate.

class pyrex.signals.SlowAskaryanSignal (times, energy, theta, n=1.78, t0=0)

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from a particle shower with given energy (GeV) observed at angle theta (radians) from the shower axis. Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

RAC (time)

Calculates R * vector potential at the Cherenkov angle in Vs at the given time (s).

```
charge_profile (z, density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

```
max_length (density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

class pyrex.signals.FastAskaryanSignal (times, energy, theta, n=1.78, t0=0)

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from a particle shower with given energy (GeV) observed at angle theta (radians) from the shower axis. Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

vector_potential

Recover the vector_potential from the electric field. Mostly just for testing purposes.

RAC (time)

Calculates R * vector potential (A) at the Cherenkov angle in Vs at the given time (s).

```
charge_profile (z, density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

```
max length (density=0.92, crit energy=0.0786, rad length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

```
pyrex.signals.AskaryanSignal
```

alias of FastAskaryanSignal

class pyrex.signals.GaussianNoise (times, sigma)

Bases: pyrex.signals.Signal

Gaussian noise signal with standard deviation sigma

class pyrex.signals.ThermalNoise(times, f_band, f_amplitude=1, rms_voltage=None, temperature=None, resistance=None, n_freqs=0)

Bases: pyrex.signals.FunctionSignal

Thermal Rayleigh noise in the frequency band f_band=[f_min,f_max] (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are f_amplitude (default 1) which can be a number or a function designating the amplitudes at each frequency, and n_freqs which is the number of frequencies to use (in f_band) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

4.2.2 pyrex.antenna module

Module containing antenna class capable of receiving signals

```
class pyrex.antenna.Antenna (position, z_axis=[0, 0, 1], x_axis=[1, 0, 0], antenna_factor=1, effi-
ciency=1, freq_range=None, noise_rms=None, temperature=None, re-
sistance=None, noisy=True)
```

Bases: object

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

```
set_orientation (z_axis=[0, 0, 1], x_axis=[1, 0, 0])
```

is_hit

Test for whether the antenna has been triggered.

is_hit_during(times)

Test for whether the antenna has been triggered during the given times array.

clear()

Reset the antenna to a state of having received no signals.

waveforms

Signal + noise (if noisy) at each triggered antenna hit.

all waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

full waveform(times)

Signal + noise (if noisy) for the given times array.

make_noise (times)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

directional_gain (theta, phi)

Function to calculate the directive electric field gain of the antenna at given angles theta (polar) and phi (azimuthal) relative to the antenna's orientation.

polarization gain (polarization)

Function to calculate the electric field gain due to polarization for a given polarization direction.

response (frequencies)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

```
receive (signal, origin=None, polarization=None)
```

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should likely end with super().receive(signal).

class pyrex.antenna.DipoleAntenna (name, position, center_frequency, bandwidth, resistance, orientation=[0, 0, 1], trigger_threshold=0, effective_height=None,
noisy=True)

```
Bases: pyrex.antenna.Antenna
```

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

```
trigger (signal)
```

Trigger on the signal if the maximum signal value is above the given threshold.

```
response (frequencies)
```

Butterworth filter response for the antenna's frequency range.

```
directional_gain (theta, phi)
```

Power gain of dipole antenna goes as sin(theta)^2, so electric field gain goes as sin(theta).

```
polarization_gain (polarization)
```

Polarization gain is simply the dot product of the polarization with the antenna's z-axis.

4.2.3 pyrex.detector module

Module containing higher-level AntennaSystem and Detector classes

```
class pyrex.detector.AntennaSystem(antenna)
     Bases: object
```

Base class for an antenna system consisting of an antenna and some front-end processes.

```
setup_antenna(*args, **kwargs)
```

Setup the antenna by passing along its init arguments. This function can be overwritten if desired, just make sure to assign the self.antenna attribute in the function.

```
front_end(signal)
```

This function should take the signal passed (from the antenna) and return the resulting signal after all processing by the antenna system's front-end. By default it just returns the given signal.

```
is_hit
is_hit_during(times)
signals
```

```
waveforms
all_waveforms
full_waveform(times)
receive(signal, origin=None, polarization=None)
```

Reset the antenna system to a state of having received no signals.

```
trigger(signal)
```

clear()

Antenna system trigger. Should return True or False for whether the passed signal triggers the antenna system. By default just matches the antenna's trigger.

```
class pyrex.detector.Detector(*args, **kwargs)
    Bases: object
```

Class for automatically generating antenna positions based on geometry criteria. The set_positions method creates a list of antenna positions and the build_antennas method is responsible for actually placing antennas at the generated positions. Once antennas are placed, the class can be directly iterated over to iterate over the antennas (as if it were just a list of antennas itself).

```
test_antenna_positions = True
```

```
set_positions(*args, **kwargs)
```

Not implemented. Should generate positions for the antennas based on the given arguments and assign those positions to the antenna_positions attribute.

```
build_antennas(*args, **kwargs)
```

Sets up antenna objects at the positions stored in the class. By default takes an antenna class and passes a position to the 'position' argument, followed by any other arguments to be passed to this class.

```
triggered(*args, **kwargs)
```

Test for whether the detector is triggered based on the current state of the antennas.

```
clear(
```

Convenience method for clearing all antennas in the detector.

4.2.4 pyrex.ice model module

Module containing ice models. Ice model classes contains static and class methods for convenience. IceModel class is set to the preferred ice model.

```
class pyrex.ice_model.AntarcticIce
    Bases: object
```

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice. Index of refraction goes as n(z)=n0-k*exp(az).

```
k = 0.438
a = 0.0132
n0 = 1.758
thickness = 2850
classmethod gradient (z)
    Returns the gradient of the index of refraction at depth z (m).
classmethod index (z)
```

Returns the medium's index of refraction, n, at depth z (m). Supports passing a numpy array of depths.

classmethod depth_with_index (n)

Returns the depth z (m) at which the medium has the given index of refraction (inverse of index function, assumes index function is monotonic so only one solution exists). Supports passing a numpy array of indices.

static temperature (z)

Returns the temperature (K) of the ice at depth z (m). Supports passing a numpy array of depths.

classmethod attenuation_length (z, f)

Returns the attenuation length at depth z (m) and frequency f (Hz). Supports passing a numpy array of depths and/or frequencies. If both are passed as arrays, a 2-D array is returned where each row is a single depth and each column is a single frequency.

class pyrex.ice_model.NewcombIce

```
Bases: pyrex.ice_model.AntarcticIce
```

Class inheriting from AntarcticIce, with new attenuation_length function based on Matt Newcomb's fit (DOESN'T CURRENTLY WORK).

classmethod attenuation_length (z, f)

Returns the attenuation length at depth z (m) and frequency f (MHz) by Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE BOGORODSKY).

```
class pyrex.ice_model.ArasimIce
```

```
Bases: pyrex.ice_model.AntarcticIce
```

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice. Ice model index is the same as used in the ARA collaboration's arasim package.

```
k = 0.43
```

a = 0.0132

n0 = 1.78

```
pyrex.ice_model.IceModel
```

alias of ArasimIce

4.2.5 pyrex.earth_model module

Module containing earth model. Uses PREM for density as a function of radius and a simple integrator for calculation of the slant depth as a function of nadir angle.

```
pyrex.earth_model.prem_density(r)
```

Returns the earth's density (g/cm^3) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

```
pyrex.earth_model.slant_depth (angle, depth, step=5000)
```

Returns the material thickness (g/cm²) for a chord cutting through earth at Nadir angle and starting at depth (m).

4.2.6 pyrex.particle module

Module for particles (namely neutrinos) and neutrino interactions in the ice. Interactions include Earth shadowing (absorption) effect.

```
class pyrex.particle.NeutrinoInteraction (c, p) Bases: object
```

Class for neutrino interaction attributes.

```
cross section(E)
```

Return the cross section (cm²) at a given energy E (GeV).

$interaction_length(E)$

Return the interaction length (cm) in water equivalent at a given energy E (GeV).

```
class pyrex.particle.Particle(vertex, direction, energy)
```

Bases: object

Class for storing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector (automatically normalized), and an energy (GeV).

```
pyrex.particle.random_direction()
```

Generate an arbitrary 3D unit vector.

```
class pyrex.particle.ShadowGenerator(dx, dy, dz, energy_generator)
```

Bases: object

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing (sort of). energy_generator should be a function that returns a particle energy in GeV. Note that the x and y ranges are (-dx/2, dx/2) and (-dy/2, dy/2) while the z range is (-dz, 0).

```
create_particle()
```

Creates a particle with random vertex in cube with a random direction.

```
class pyrex.particle.ListGenerator(particles, loop=True)
```

Bases: object

Class to generate neutrinos by simply pulling them from a list of Particle objects. By default returns to the start of the list once the end is reached, but can optionally fail after reaching the list's end.

```
create_particle()
```

Pulls next particle from the list.

```
class pyrex.particle.FileGenerator (files)
```

Bases: object

Class to generate neutrinos by pulling their vertex, direction, and energy from a (list of) .npz file(s). Each file must have three arrays, containing the vertices, directions, and energies respectively so the first particle will have properties given by the first elements of these three arrays. Tries to smartly figure out which array is which based on their names, but if the arrays are unnamed, assumes they are in the order used above.

```
create_particle()
```

Pulls the next particle from the file(s).

4.2.7 pyrex.ray_tracing module

Module containing class for ray tracing through the ice.

```
class pyrex.ray_tracing.BasicRayTracePath (parent_tracer, launch_angle, direct)
```

```
Bases: pyrex.internal_functions.LazyMutableClass
```

Class for storing a single ray-trace solution betwen points. Calculations preformed by integrating z-steps of size dz. Most properties lazily evaluated to save on re-computation time.

z_turn_proximity

Parameter for how closely path approaches z turn. Necessary to avoid diverging integrals.

z0

Depth of the launching point.

```
z1
          Depth of the receiving point.
     n0
     rho
     phi
     beta
     z turn
     emitted_direction
     received direction
     theta (z)
          Polar angle of the ray at given depth or array of depths.
     z_integral (integrand)
          Returns the integral of the integrand (a function of z) along the path.
     path_length
     tof
     fresnel
     attenuation(f)
          Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a
          list of frequencies.
     propagate (signal)
          Applies attenuation to the signal along the path.
     coordinates
class pyrex.ray_tracing.SpecializedRayTracePath(parent_tracer, launch_angle, direct)
     Bases: pyrex.ray_tracing.BasicRayTracePath
     Class for storing a single ray-trace solution betwen points, specifically for ice model with index of refraction
     n(z) = n0 - k \exp(a z). Calculations performed using true integral evaluation (except attenuation). Ice model
     must use methods inherited from pyrex. AntarcticIce
     uniformity factor = 0.99999
     beta_tolerance = 0.005
     valid_ice_model
     z uniform
     z_integral (integrand, numerical=False, x_func=<function SpecializedRayTracePath.<lambda>>)
          Function for integrating a given integrand along the depths of the path.
     path_length
     tof
     attenuation(f)
          Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a
          list of frequencies.
     coordinates
```

```
class pyrex.ray_tracing.BasicRayTracer (from_point,
                                                                to point,
                                                                                ice model=<class
                                                'pyrex.ice_model.ArasimIce'>, dz=1)
     Bases: pyrex.internal functions.LazyMutableClass
     Class for proper ray tracing. Calculations performed by integrating z-steps with size dz. Most properties lazily
     evaluated to save on re-computation time.
     solution_class
          alias of BasicRayTracePath
     z_turn_proximity
          Parameter for how closely path approaches z_turn. Necessary to avoid diverging integrals.
     z0
          Depth of lower point. Ray tracing performed as if launching from lower point to higher point.
     z1
          Depth of higher point. Ray tracing performed as if launching from lower point to higher point.
     n0
     rho
     max angle
     peak_angle
     direct_r_max
     indirect_r_max
     exists
     expected_solutions
     solutions
     direct_angle
     indirect_angle_1
     indirect_angle_2
     static angle_search (true_r,
                                      r function,
                                                    min angle,
                                                                  max angle,
                                                                                 tolerance=1e-12,
                           max_iterations=100)
          Root-finding algorithm.
class pyrex.ray_tracing.SpecializedRayTracer (from_point,
                                                                                ice_model=<class
                                                                    to_point,
                                                       'pyrex.ice_model.ArasimIce'>, dz=1)
     Bases: pyrex.ray_tracing.BasicRayTracer
     Ray tracer specifically for ice model with index of refraction n(z) = n0 - k \exp(a z). Calculations performed
     using true integral evaluation. Ice model must use methods inherited from pyrex. Antarctic Ice
     solution class
          alias of SpecializedRayTracePath
     valid_ice_model
     z_uniform
     direct r max
     peak_angle
pyrex.ray_tracing.RayTracer
     alias of SpecializedRayTracer
```

pyrex.ray_tracing.RayTracePath

alias of SpecializedRayTracePath

class pyrex.ray_tracing.PathFinder(ice_model, from_point, to_point)

Bases: object

Class for pseudo ray tracing. Just uses straight-line paths.

exists

Boolean of whether path exists based on basic total internal reflection calculation.

emitted_ray

Direction in which ray is emitted.

received_ray

Direction from which ray is received.

path_length

Length of the path (m).

tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time_of_flight()

time_of_flight(*n_steps=100*)

Time of flight (s) for a particle along the path.

$attenuation (f, n_steps=100)$

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a list of frequencies.

propagate (signal)

Applies attenuation to the signal along the path.

class pyrex.ray_tracing.ReflectedPathFinder(ice_model, from_point, to_point, reflection_depth=0)

Bases: object

Class for pseudo ray tracing of ray reflected off ice surface. Just uses straight-line paths.

get_bounce_point (reflection_depth=0)

Calculation of point at which signal is reflected by the ice surface (z=0).

exists

Boolean of whether path exists based on whether its sub-paths exist and whether it could reflect off the ice surface.

emitted_ray

Direction in which ray is emitted.

received_ray

Direction from which ray is received.

path_length

Length of the path (m).

tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time_of_flight()

time_of_flight (n_steps=100)

Time of flight (s) for a particle along the path.

$attenuation (f, n_steps=100)$

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a list of frequencies.

```
propagate (signal)
```

Applies attenuation to the signal along the path.

4.2.8 pyrex.kernel module

Module for the simulation kernel. Includes neutrino generation, ray tracking (no raytracing yet), and hit generation.

```
class pyrex.kernel.EventKernel (generator, ice_model, antennas)
    Bases: object
```

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

```
event()
```

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

4.2.9 pyrex.internal_functions module

Helper functions for use in PyREx modules.

```
pyrex.internal_functions.normalize(vector)

Returns the normalized form of the given vector.
```

```
pyrex.internal_functions.flatten(iterator, dont_flatten=())
```

Flattens all iterable elements in the given iterator recursively and returns the resulting flat iterator. Can optionally be passed a list of classes to avoid flattening. Will not flatten strings or bytes due to recursion errors.

```
pyrex.internal_functions.mirror_func(match_func, run_func, self=None)
```

Returns a function which operates like run_func, but has all the attributes of match_func. If self argument is not None, it will be passed as the first argument to run_func.

```
pyrex.internal\_functions.lazy\_property(fn)
```

Decorator that makes a property lazily evaluated.

```
class pyrex.internal_functions.LazyMutableClass(static_attributes=None)
    Bases: object
```

Class whose properties can be lazily evaluated by using lazy_property decorator, but will re-evaluate lazy properties if any of its specified static_attributes change. By default, static_attributes is set to all attributes of the class at the time of the init call.

4.3 PyREx Custom Subpackage

Note that more modules are available as plug-ins, see *Custom Sub-Package*.

4.3.1 pyrex.custom.pyspice module

Module containing setup and wrappers for PySpice module into PyREx

```
class pyrex.custom.pyspice.NgSpiceSharedSignal(**kwargs)
     Bases: PySpice.Spice.NgSpice.Shared.NgSpiceShared
```

Helper class for bridging gap between PyREx Signal and PySpice NgSpiceShared classes

```
get_vsrc_data (voltage, time, node, ngspice_id)
```

Bases: object

Class for passing PyREx Signal object into PySpice

4.3.2 pyrex.custom.irex package

Customizations of pyrex package specific to IREX (IceCube Radio Extension)

pyrex.custom.irex.antenna module

Module containing customized antenna classes for IREX

```
class pyrex.custom.irex.antenna.IREXAntenna (position, center_frequency, bandwidth, resistance, orientation=(0, 0, 1), effective_height=None, noisy=True)
```

Bases: pyrex.antenna.Antenna

Antenna to be used in IREX. Has a position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), and polarization direction.

```
response (frequencies)
```

Butterworth filter response for the antenna's frequency range.

```
directional_gain (theta, phi)
```

Power gain of dipole antenna goes as sin(theta)^2, so electric field gain goes as sin(theta).

```
polarization_gain (polarization)
```

Polarization gain is simply the dot product of the polarization with the antenna's z-axis.

```
class pyrex.custom.irex.antenna.IREXAntennaSystem (name, position, trigger_threshold, time_over_threshold=0, orientation=(0, 0, 1), amplification=(0, 0, 1), amplification=(0, 0, 1), amplifier_clipping=(0, 0, 1), amplifier_clipping=(0, 0, 1), and (0, 0, 1), and (0, 0, 1), amplifier_clipping=(0, 0, 1), and (0, 0, 1),
```

Bases: pyrex.detector.AntennaSystem

IREX antenna system consisting of dipole antenna, low-noise amplifier, optional bandpass filter, and envelope circuit.

```
setup\_antenna (center_frequency=250000000.0, bandwidth=300000000.0, resistance=100, orientation=(0, 0, 1), effective_height=None, noisy=True)
```

Sets attributes of the antenna including center frequency (Hz), bandwidth (Hz), resistance (ohms), orientation, and effective height (m).

```
make_envelope(signal)
```

Return the signal envelope based on the antenna's envelope_method.

```
front_end(signal)
```

Apply the front-end processing of the antenna signal, including amplification, clipping, and envelope processing.

```
all waveforms
```

```
full_waveform(times)
```

trigger (signal)

pyrex.custom.irex.detector module

```
Module containing customized detector geometry classes for IREX
```

Bases: pyrex.detector.Detector

String of IREXAntennas. Sets positions of antennas on string based on the given arguments. Sets build_antennas method for setting antenna characteristics.

```
set_positions (x, y, antennas\_per\_string=2, antenna\_separation=50, lowest\_antenna=-100) Generates antenna positions along the string.
```

```
build_antennas (trigger_threshold, time_over_threshold=0, amplification=1, nam-
ing_scheme=<function IREXString.<lambda>>, orientation_scheme=<function
IREXString.<lambda>>, noisy=True, envelope_method='analytic')
```

Sets up IREXAntennaSystems at the positions stored in the class. Takes as arguments the trigger threshold, optional time over threshold, and whether to add noise to the waveforms. Other optional arguments include a naming scheme and orientation scheme which are functions taking the antenna index i and the antenna object. The naming scheme should return the name and the orientation scheme should return the orientation z-axis and x-axis of the antenna.

```
triggered (antenna_requirement=1)
```

Test whether the number of hit antennas meets the given antenna trigger requirement.

Bases: pyrex.detector.Detector

Station geometry with a number of strings evenly spaced radially around the station center. Supports any string type and passes extra keyword arguments on to the string class.

```
triggered (antenna_requirement=1, string_requirement=1)
```

Test whether the number of hit antennas meets the given antenna and string trigger requirements.

Bases: pyrex.detector.Detector

Station geometry with one string at the station center and the rest of the strings evenly spaced radially around the station center. Supports any string type and passes extra keyword arguments on to the string class.

```
set_positions (x, y, strings_per_station=4, station_diameter=50, string_type=<class 'pyrex.custom.irex.detector.IREXString'>, **string_kwargs')
Generates string positions around the station.
```

```
triggered (antenna_requirement=1, string_requirement=1)
```

Test whether the number of hit antennas meets the given antenna and string trigger requirements.

Bases: pyrex.detector.Detector

Rectangular grid of stations or strings, in a square layout if possible, separated by the given distance. Supports any station or string type and passes extra keyword arguments on to the station or string class.

```
set_positions (stations=1, station_separation=500, station_type=<class 'pyrex.custom.irex.detector.IREXString'>, **station_kwargs')
Generates rectangular grid of stations.
```

```
triggered (station_requirement=1, **station_trigger_kwargs)
```

Test whether the number of hit stations meets the given station trigger requirement.

pyrex.custom.irex.frontends module

Module containing IREX front-end circuit models

```
pyrex.custom.irex.frontends.basic_envelope_model (signal, cap=2e-11, res=500)

Model of a basic diode-capacitor-resistor envelope circuit. Takes a signal object as the input voltage and returns the output voltage signal object.
```

```
pyrex.custom.irex.frontends.bridge_rectifier_envelope_model(signal, cap=2e-11, res=500)
```

Model of a diode bridge rectifier envelope circuit. Takes a signal object as the input voltage and returns the output voltage signal object.

pyrex.custom.irex.reconstruction module

Module containing reconstruction methods for IREX

```
pyrex.custom.irex.reconstruction.quick_vertex_reconstruction(detector,
                                                                                thresh-
                                                                      old=None,
                                                                      get waveform=<function
                                                                      <lambda>>)
pyrex.custom.irex.reconstruction.full_vertex_reconstruction(detector,
                                                                                thresh-
                                                                     old=None,
                                                                     get_waveform=<function</pre>
                                                                     <lambda>>)
pyrex.custom.irex.reconstruction.get_xcorr_times (waveforms)
pyrex.custom.irex.reconstruction.minimizer_vertex_reconstruction (positions,
                                                                           times,
                                                                           guess=None)
pyrex.custom.irex.reconstruction.least_squares(vertex,
                                                                  positions,
                                                                                 times,
                                                      method='trace')
pyrex.custom.irex.reconstruction.bancroft_vertex (positions,
                                                                                 veloc-
                                                                      times.
                                                        ity=170940170.94017094)
pyrex.custom.irex.reconstruction.bancroft_scan_vertex(positions,
                                                                                 veloc-
                                                              ity=170940170.94017094)
```

CHAPTER

FIVE

VERSION HISTORY

5.1 Version 1.5.0

Changes

- Changed structure of Detector class so a detector can be built up from strings to stations to the full detector.
- Detector.antennas attribute changed to Detector.subsets, which contains the pieces which make up the detector (e.g. antennas on a string, strings in a station).
- Iterating the Detector class directly retains its effect of iterating each antenna in the detector directly.

New Features

- Added triggered() and clear() method to Detector class.
- Added two new neutrino generators ListGenerator and FileGenerator designed to pull pre-generated Particle objects.

Bug Fixes

• Preserve value_type of Signal objects passed to IREXAntennaSystem.front_end()

5.2 Version 1.4.2

Performance Improvements

• Improved performance of FastAskaryanSignal by reducing the size of the convolution.

Changes

• Adjusted time step of signals generated by kernel slightly (2000 steps instead of 2048).

5.3 Version 1.4.1

Changes

- Improved ray tracing and defaulted to the almost completely analytical SpecializedRayTracer and SpecializedRayTracePath classes as RayTracer and RayTracePath.
- Added ray tracer into EventKernel to replace PathFinder completely.

5.4 Version 1.4.0

New Features

• Implemented full ray tracing in the RayTracer and RayTracePath classes.

5.5 Version 1.3.1

New Features

- Added diode bridge rectifier envelope circuit analytic model to irex.frontends and made it the default analytic envelope model in IREXAntennaSystem.
- Added allow_reflection attribute to EventKernel class to determine whether ReflectedPathFinder solutions should be allowed.

Changes

• Changed neutrino interaction model to include all neutrino and anti-neutrino interactions rather than only charged-current neutrino (relevant for ShadowGenerator class).

5.6 Version 1.3.0

New Features

 Added and implemented ReflectedPathFinder class for rays which undergo total internal reflection and subsequently reach an antenna.

Changes

• Change AksaryanSignal angle to always be positive and remove < 90 degree restriction (Alvarez-Muniz, Romero-Wolf, & Zas paper suggests the algorithm should work for all angles).

Performance Improvements

• Improve performance of ice index calculated at many depths.

5.3. Version 1.4.1 37

5.7 Version 1.2.1

New Features

Added set_orientation function to Antenna class for setting the z_axis and x_axis attributes appropriately.

Bug Fixes

• Fixed bug where Antenna._convert_to_antenna_coordinates function was returning coordinates relative to (0,0,0) rather than the antenna's position.

5.8 Version 1.2.0

Changes

- Changed custom module to a package containing irex module.
- custom package leverages "Implicit Namespace Package" structure to allow plug-in style additions to the package in either the user's ~/.pyrex-custom/directory or the ./pyrex-custom directory.

5.9 Version 1.1.2

New Features

- Added with_times method to Signal class for interpolation/extrapolation of signals to different times.
- Added full_waveform and is_hit_during methods to Antenna class for calculation of waveform over arbitrary time array and whether said waveform triggers the antenna, respectively.
- Added front_end_processing method to IREXAntenna for processing envelope, amplifying signal, and downsampling result (downsampling currently inactive).

Changes

- Change Antenna.make_noise to use a single master noise object and use with_times to calculate noise at different times.
 - To ensure noise is not obviously periodic (for <100 signals), uses 100 times the recommended number of frequencies, which results in longer computation time for noise waveforms.

5.10 Version 1.1.1

Changes

• Moved ValueTypes inside Signal class. Now access as Signal.ValueTypes.voltage, etc.

5.7. Version 1.2.1 38

Changed signal envelope calculation in custom IREXAntenna from hilbert transform to a basic model. Spice
model also available, but slower.

5.11 Version 1.1.0

New Features

- Added directional_gain and polarization_gain methods to base Antenna.
 - receive method should no longer be overwritten in most cases.
 - Antenna now has orientation defined by z_axis and x_axis.
 - antenna_factor and efficiency attributes added to Antenna for more flexibility.
- Added value_type attribute to Signal class and derived classes.
 - Current value types are ValueTypes.undefined, ValueTypes.voltage, ValueTypes. field, and ValueTypes.power.
 - Signal objects now must have the same value_type to be added (though those with ValueTypes. undefined can be coerced).

Changes

- Made units consistent across PyREx.
- · Added ability to define Antenna noise by RMS voltage rather than temperature and resistance if desired.
- Allow DipoleAntenna to guess at effective_height if not specified.

Performance Improvements

• Increase speed of IceModel.__atten_coeffs method, resulting in increased speed of attenuation length calculations.

5.12 Version 1.0.3

New Features

Added custom module to contain classes and functions specific to the IREX project.

5.13 Version 1.0.2

New Features

• Added Antenna.make_noise() method so custom antennas can use their own noise functions.

5.11. Version 1.1.0 39

Changes

- Allow passing of numpy arrays of depths and frequencies into most IceModel methods.
 - IceModel.gradient () must still be calculated at individual depths.
- Added ability to specify RMS voltage of ThermalNoise without providing temperature and resistance.
- Removed (deprecated) Antenna.isHit().

Performance Improvements

- Allowing for IceModel to calculate many attenuation lengths at once improves speed of PathFinder. propagate().
- Improved speed of PathFinder.time_of_flight() and PathFinder.attenuation() (and improved accuracy to boot).

5.14 Version 1.0.1

Changes

• Changed Antenna not require a temperature and frequency range if no noise is produced.

Bug Fixes

- Fixed bugs in AskaryanSignal that caused the convolution to fail.
- Fixed bugs resulting from converting IceModel.temperature() from Celsius to Kelvin.

5.15 Version 1.0.0

- Created PyREx package based on original notebook.
- Added all signal classes to produce full-waveform Askaryan pulses and thermal noise.
- Changed Antenna class to DipoleAntenna to allow Antenna to be a base class.
- Changed Antenna.isHit() method to Antenna.is_hit property.
- Introduced IceModel alias for AntarcticIce (or any future preferred ice model).
- Moved AntarcticIce.attenuationLengthMN to its own NewcombIce class inheriting from AntarcticIce.
- Added PathFinder.propagate() to propagate a Signal object in a customizable way.
- Changed naming conventions to be more consistent, verbose, and "pythonic":
 - AntarcticIce.attenuationLength() becomes AntarcticIce.
 attenuation length().
 - In pyrex.earth_model, RE becomes EARTH_RADIUS.
 - In pyrex.particle, neutrino_interaction becomes NeutrinoInteraction.

5.14. Version 1.0.1 40

- In pyrex.particle, NA becomes AVOGADRO_NUMBER.
- particle class becomes Particle namedtuple.
 - * Particle.vtx becomes Particle.vertex.
 - * Particle.dir becomes Particle.direction.
 - * Particle. E becomes Particle. energy.
- In pyrex.particle, next_direction() becomes random_direction().
- shadow_generator becomes ShadowGenerator.
- PathFinder methods become properties where reasonable:
 - * PathFinder.exists() becomes PathFinder.exists.
 - * PathFinder.getEmittedRay() becomes PathFinder.emitted_ray.
 - * PathFinder.getPathLength() becomes PathFinder.path_length.
- PathFinder.propagateRay() split into PathFinder.time_of_flight() (with corresponding PathFinder.tof property) and PathFinder.attenuation().

5.16 Version 0.0.0

Original PyREx python notebook written by Kael Hanson:

https://gist.github.com/physkael/898a64e6fbf5f0917584c6d31edf7940

5.16. Version 0.0.0 41

CHAPTER

SIX

GITHUB README

6.1 PyREx - (Python package for an IceCube Radio Extension)

PyREx (**Py**thon package for an IceCube **R**adio **Ex**tension) is, as its name suggests, a Python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas (e.g. the ARA and ARIANA collaborations).

6.1.1 Useful Links

- Source (GitHub): https://github.com/bhokansonfasig/pyrex
- Documentation: https://bhokansonfasig.github.io/pyrex/
- Release notes: https://bhokansonfasig.github.io/pyrex/build/html/versions.html

6.1.2 Getting Started

Requirements

PyREx requires python version 3.6+ as well as numpy version 1.13+ and scipy version 0.19+. After installing python from https://www.python.org/downloads/, numpy and scipy can be installed with pip as follows, or by simply installing pyrex as specified in the next section.

```
pip install numpy>=1.14
pip install scipy>=0.19
```

Installing

The easiest way to get the PyREx package is using pip as follows:

```
pip install git+https://github.com/bhokansonfasig/pyrex#egg=pyrex
```

Note that since PyREx is not currently available on PyPI, a simple pip install pyrex will not have the intended effect.

6.1.3 Examples

For examples of how to use PyREx, see the examples page in the documentation, or the PyREx Demo notebook.

6.1.4 Authors

• Ben Hokanson-Fasig

6.1.5 License

MIT License

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