# **PyREx Documentation**

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**CHAPTER** 

ONE

# INTRODUCTION TO PYREX

PyREx (**Py**thon package for an IceCube **R**adio **Ex**tension) is, as its name suggests, a Python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas (e.g. the ARA and ARIANA collaborations).

# 1.1 Installation

The easiest way to get the PyREx package is using pip as follows:

```
pip install git+https://github.com/bhokansonfasig/pyrex#egg=pyrex
```

Alternatively, you can download the code from https://github.com/bhokansonfasig/pyrex and then either include the pyrex directory (the one containing the python modules) in your PYTHON\_PATH, or just copy the pyrex directory into your working directory. PyREx is not currently available on PyPI, so a simple pip install pyrex will not have the intended effect.

# 1.2 Code Example

The most basic simulation can be produced as follows:

First, import the package:

```
import pryex
```

Then, create a particle generator object that will produce random particles in a cube of 1 km on each side with a fixed energy of 100 PeV:

An array of antennas that represent the detector is also needed. The base Antenna class provides a basic antenna with a flat frequency response and no trigger condition. Here we make a single vertical "string" of four antennas with no noise:

```
antenna_array = []
for z in [-100, -150, -200, -250]:
   antenna_array.append(
        pyrex.Antenna(position=(0,0,z), noisy=False)
   )
```

Finally, we want to pass these into the EventKernel and produce an event:

Now the signals received by each antenna can be accessed by their waveforms parameter:

```
import matplotlib.pyplot as plt
for ant in kernel.ant_array:
    for wave in ant.waveforms:
        plt.figure()
        plt.plot(wave.times, wave.values)
        plt.show()
```

# 1.3 Units

For ease of use, PyREx tries to use consistent units in all classes and functions. The units used are mostly SI with a few exceptions listed in bold below:

Metric	Unit
time	seconds (s)
frequency	hertz (Hz)
distance	meters (m)
density	grams per cubic centimeter (g/cm^3)
material thickness	grams per square centimeter (g/cm^2)
temperature	kelvin (K)
energy	gigaelectronvolts (GeV)
resistance	ohms $(\Omega)$
voltage	volts (V)
electric field	volts per meter (V/m)

**CHAPTER** 

**TWO** 

# CODE EXAMPLES

The following code examples assume these imports:

```
import numpy as np
import matplotlib.pyplot as plt
import scipy.fftpack
import pyrex
```

All of the following examples can also be found (and quickly run) in the Code Examples python notebook.

# 2.1 Working with Signal Objects

The base Signal class is simply an array of times and an array of signal values, and is instantiated with these two arrays. The times array is assumed to be in units of seconds, but there are no general units for the values array. It is worth noting that the Singal object stores shallow copies of the passed arrays, so changing the original arrays will not affect the Signal object.

```
time_array = np.linspace(0, 10)
value_array = np.sin(time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)
```

Plotting the Signal object is as simple as plotting the times vs the values:

```
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

While there are no specified units for a Signal.values, there is the option to specify the value\_type of the values. This is done using the Signal.ValueTypes enum. By default, a Signal object has value\_type=ValueTypes.unknown. However, if the signal represents a voltage, electric field, or electric power; value\_type can be set to Signal.ValueTypes.voltage, Signal.ValueTypes.field, or Signal.ValueTypes.power respectively:

Signal objects can be added as long as they have the same time array and value\_type. Signal objects also support the python sum function:

```
time_array = np.linspace(0, 10)
values1 = np.sin(time_array)
values2 = np.cos(time_array)
signal1 = pyrex.Signal(time_array, values1)
```

```
plt.plot(signal1.times, signal1.values, label="signal1 = sin(t)")
signal2 = pyrex.Signal(time_array, values2)
plt.plot(signal2.times, signal2.values, label="signal2 = cos(t)")
signal3 = signal1 + signal2
plt.plot(signal3.times, signal3.values, label="signal3 = sin(t)+cos(t)")
all_signals = [signal1, signal2, signal3]
signal4 = sum(all_signals)
plt.plot(signal4.times, signal4.values, label="signal4 = 2*(sin(t)+cos(t))")
plt.legend()
plt.show()
```

The Signal class provides many convenience attributes for dealing with signals:

The Signal class also provides functions for manipulating the signal. The resample function will resample the times and values arrays to the given number of points (with the same endpoints):

```
my_signal.resample(1001)
len(my_signal.times) == len(my_signal.values) == 1001
my_signal.times[0] == 0
my_signal.times[-1] == 10
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

The with\_times function will interpolate/extrapolate the signal's values onto a new times array:

```
new_times = np.linspace(-5, 15)
new_signal = my_signal.with_times(new_times)
plt.plot(new_signal.times, new_signal.values, label="new signal")
plt.plot(my_signal.times, my_signal.values, label="original signal")
plt.legend()
plt.show()
```

The filter\_frequencies function will apply a frequency-domain filter to the values array based on the passed frequency response function:

```
def lowpass_filter(frequency):
    if frequency < 1:
        return 1
    else:
        return 0

time_array = np.linspace(0, 10, 1001)
value_array = np.sin(0.1*2*np.pi*time_array) + np.sin(2*2*np.pi*time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)

plt.plot(my_signal.times, my_signal.values)
my_signal.filter_frequencies(lowpass_filter)
plt.plot(my_signal.times, my_signal.values)
plt.show()</pre>
```

A number of classes which inherit from the Signal class are included in PyREx: EmptySignal,

FunctionSignal, AskaryanSignal, and ThermalNoise. EmptySignal is simply a signal whose values are all zero:

```
time_array = np.linspace(0,10)
empty = pyrex.EmptySignal(times=time_array)
plt.plot(empty.times, empty.values)
plt.show()
```

FunctionSignal takes a function of time and creates a signal based on that function:

```
time_array = np.linspace(0, 10, num=101)
def square_wave(time):
    if int(time)%2==0:
        return 1
    else:
        return -1
square_signal = pyrex.FunctionSignal(times=time_array, function=square_wave)
plt.plot(square_signal.times, square_signal.values)
plt.show()
```

Additionally, FunctionSignal leverages its knowledge of the function to more accurately interpolate and extrapolate values for the with times function:

```
new_times = np.linspace(0, 20, num=201)
long_square_signal = square_signal.with_times(new_times)
plt.plot(long_square_signal.times, long_square_signal.values, label="new signal")
plt.plot(square_signal.times, square_signal.values, label="original signal")
plt.legend()
plt.show()
```

AskaryanSignal produces an Askaryan pulse (in V/m) on a time array due to a neutrino of given energy observed at a given angle from the shower axis:

ThermalNoise produces Rayleigh noise (in V) at a given temperature and resistance which has been passed through a bandpass filter of the given frequency range:

Note that since ThermalNoise inherits from FunctionSignal, it can be extrapolated nicely to new times. It may be highly periodic outside of its original time range however, unless a large number of frequencies is requested

on initialization.

# 2.2 Antenna Class and Subclasses

The base Antenna class provided by PyREx is designed to be inherited from to match the needs of each project. At its core, an Antenna object is initialized with a position, a temperature, and a frequency range, as well as optionally a resistance for noise calculations and a boolean dictating whether or not noise should be added to the antenna's signals (note that if noise is to be added, a resistance must be specified).

The basic properties of an Antenna object are is\_hit and waveforms. is\_hit specifies whether or not the antenna has been triggered by an event. waveforms is a list of all the waveforms which have triggered the antenna. The antenna also defines signals, which is a list of all signals the antenna has received, and all\_waveforms which is a list of all waveforms (signal plus noise) the antenna has received including those which didn't trigger.

```
basic_antenna.is_hit == False
basic_antenna.waveforms == []
```

The Antenna class contains two attributes and three methods which represent characteristics of the antenna as they relate to signal processing. The attributes are efficiency and antenna\_factor, and the methods are response, directional\_gain, and polarization\_gain. The attributes are to be set and the methods overwritten in order to custmoize the way the antenna responds to incoming signals. efficiency is simply a scalar which multiplies the signal the antenna receives (default value is 1). antenna\_factor is a factor used in converting received electric fields into voltages (antenna\_factor = E / V; default value is 1). response takes a frequency or list of frequencies (in Hz) and returns the frequency response of the antenna at each frequency given (default always returns 1). directional\_gain takes angles theta and phi in the antenna's coordinates and returns the antenna's gain for a signal coming from that direction (default always returns 1). Finally, polarization\_gain takes a polarization vector and returns the antenna's gain for a signal with that polarization (default always returns 1).

```
basic_antenna.efficiency == 1
basic_antenna.antenna_factor == 1
freqs = [1, 2, 3, 4, 5]
basic_antenna.response(freqs) == [1, 1, 1, 1, 1]
basic_antenna.directional_gain(theta=np.pi/2, phi=0) == 1
basic_antenna.polarization_gain([0,0,1]) == 1
```

The Antenna class defines a trigger method which is also expected to be overwritten. trigger takes a Signal object as an argument and returns a boolean of whether or not the antenna would trigger on that signal (default always returns True).

```
basic_antenna.trigger(pyrex.Signal([0],[0])) == True
```

The Antenna class also defines a receive method which takes a Signal object and processes the signal according to the antenna's attributes (efficiency, antenna\_factor, response, directional\_gain, and polarization\_gain as described above). To use the receive function, simply pass it the Signal object the antenna sees, and the Antenna class will handle the rest. You can also optionally specify the origin point of the signal (used in directional\_gain calculation) and the polarization direction of the signal (used in polarization\_gain calculation). If either of these is unspecified, the corresponding gain will simply be set to 1.

Beyond Antenna.waveforms, the Antenna object also provides methods for checking the waveform and trigger status for arbitrary times: full\_waveform and is\_hit\_during. Both of these methods take a time array as an argument and return the waveform Signal object for those times and whether said waveform triggered the antenna, respectively.

```
total_waveform = basic_antenna.full_waveform(np.linspace(0,20))
plt.plot(total_waveform.times, total_waveform.values, label="Total Waveform")
plt.plot(incoming_singal_1.times, incoming_singal_1.values, label="Pure Signals")
plt.plot(incoming_signal_2.times, incoming_signal_2.values, color="C1")
plt.legend()
plt.show()
basic_antenna.is_hit_during(np.linspace(0, 200e-9)) == True
```

Finally, the Antenna class defines a clear method which will reset the antenna to a state of having received no signals:

```
basic_antenna.clear()
basic_antenna.is_hit == False
len(basic_antenna.waveforms) == 0
```

To create a custom antenna, simply inherit from the Antenna class:

```
class NoiselessThresholdAntenna(pyrex.Antenna):
    def __init__(self, position, threshold):
        super().__init__(position=position, noisy=False)
        self.threshold = threshold

def trigger(self, signal):
```

```
if max(np.abs(signal.values)) > self.threshold:
    return True
else:
    return False
```

Our custom NoiselessThresholdAntenna should only trigger when the amplitude of a signal exceeds its threshold value:

```
my_antenna = NoiselessThresholdAntenna(position=(0, 0, 0), threshold=2)
incoming_singal = pyrex.FunctionSignal(np.linspace(0,10), np.sin,
                                       value_type=pyrex.Signal.ValueTypes.voltage)
my_antenna.receive(incoming_singal)
my_antenna.is_hit == False
len(my_antenna.waveforms) == 0
len(my_antenna.all_waveforms) == 1
incoming_singal = pyrex.Signal(incoming_singal.times,
                               5*incoming_singal.values,
                               incoming_singal.value_type)
my_antenna.receive(incoming_singal)
my_antenna.is_hit == True
len (my_antenna.waveforms) == 1
len(my_antenna.all_waveforms) == 2
for wave in my_antenna.waveforms:
   plt.figure()
   plt.plot(wave.times, wave.values)
   plt.show()
```

For more on customizing PyREx, see the Custom Sub-Package section.

PyREx defines DipoleAntenna which as a subclass of Antenna, which provides a basic threshold trigger, a basic bandpass filter frequency response, a sine-function directional gain, and a typical dot-product polarization effect. A DipoleAntenna object is created as follows:

# 2.3 Ice and Earth Models

PyREx provides a class IceModel, which is an alias for whichever south pole ice model class is the preferred (currently just the basic AntarcticIce). The IceModel class provides class methods for calculating characteristics

of the ice at different depths and frequencies outlined below:

```
depth = -1000 # m
pyrex.IceModel.temperature(depth)
pyrex.IceModel.index(depth)
pyrex.IceModel.gradient(depth)
frequency = 1e8 # Hz
pyrex.IceModel.attenuation_length(depth, frequency)
```

PyREx also provides two functions realted to its earth model: prem\_density and slant\_depth. prem\_density calculates the density in grams per cubic centimeter of the earth at a given radius:

```
radius = 6360000 # m
pyrex.prem_density(radius)
```

slant\_depth calculates the material thickness in grams per square centimeter of a chord cutting through the earth at a given nadir angle, starting from a given depth:

```
nadir_angle = 60 * np.pi/180 # radians
depth = 1000 # m
pyrex.slant_depth(nadir_angle, depth)
```

# 2.4 Particle Generation

PyREx includes Particle as a container for information about neutrinos which are generated to produce Askaryan pulses. Particle contains three attributes: vertex, direction, and energy:

PyREx also includes a ShadowGenerator class for generating random neutrinos, taking into account some Earth shadowing. The neutrinos are generated in a box of given size, and with an energy given by an energy generation function:

# 2.5 Ray Tracing

While PyREx does not currently support full ray tracing, it does provide a PathFinder class which implements some basic ray analysis by Snell's law. PathFinder takes an ice model and two points as arguments and provides a number of properties and methods regarding the path between the points.

PathFinder.exists is a boolean value of whether or not the path between the points is traversable according to the indices of refraction. PathFinder.emitted\_ray is a unit vector giving the direction from from\_point to to\_point. PathFinder.path\_length is the length in meters of the straight line path between the two points.

```
my_path.exists
my_path.emitted_ray
my_path.path_length
```

PathFinder.time\_of\_flight() calculates the time it takes for light to traverse the path, with an optional parameter n\_steps defining the precision used. PathFinder.tof is a convenience property set to the time of flight using the default value of n\_steps.

```
my_path.time_of_flight(n_steps=100)
my_path.time_of_flight() == my_path.tof
```

PathFinder.attenuation() calculates the attenuation factor along the path for a signal of given frequency. Here again there is an optional parameter n\_steps defining the precision used.

```
frequency = 1e9 # Hz
my_path.attenuation(f=frequency, n_steps=100)
```

Finally, PathFinder.propagate() propagates a Signal object from from\_point to to\_point by applying a 1/PathFinder.path\_length factor, applying the frequency attenuation of PathFinder.attenuation(), and shifting the signal times by PathFinder.tof:

# 2.6 Full Simulation

PyREx provides the EventKernel class to control a basic simulation including the creation of neutrinos, the propagation of their pulses to the antennas, and the triggering of the antennas:

```
kernel = pyrex.EventKernel(generator=particle_generator,
                           ice_model=pyrex.IceModel,
                           antennas=detector)
triggered = False
while not triggered:
   kernel.event()
   for antenna in detector:
        if antenna.is_hit:
            triggered = True
            break
for antenna in detector:
    for i, wave in enumerate(antenna.waveforms):
        plt.plot(wave.times * 1e9, wave.values)
        plt.xlabel("Time (ns)")
        plt.ylabel("Voltage (V)")
        plt.title(antenna.name + " - waveform "+str(i))
```

# 2.7 More Examples

For more code examples, see the PyREx Demo python notebook.

**CHAPTER** 

THREE

# **CUSTOM SUB-PACKAGE**

While the PyREx package provides a basis for simulation, the real benefits come in customizing the analysis for different purposes. To this end the custom sub-package allows for plug-in style modules to be distributed for different collaborations.

By default PyREx comes with a custom module for IREX (IceCube Radio Extension) accessible at pyrex.custom. irex. This module includes a more thorough IREXAntenna class inheriting from the Antenna class which adds a front-end for amplifying the signal, processing signal envelopes, and downsampling the result. It also includes an IREXDetector class designed to easily produce different geometries of IREXAntenna objects.

Other institutions and research groups are encouraged to create their own custom modules to integrate with PyREx. These modules have full access to PyREx as if they were a native part of the package. When PyREx is loaded it automatically scans for these custom modules in certain parts of the filesystem and includes any modules that it can find. The first place searched is the custom directory in the PyREx package itself. Next, if a .pyrex-custom directory exists in the user's home directory (note the leading .), its subdirectories are searched for custom directories and any modules in these directories are included. Finally, if a pyrex-custom directory exists in the current working directory (this time without the leading .), its subdirectories are similarly scanned for modules inside custom directories. Note that if any name-clashing occurs, the first result found takes precedence (without warning). Additionally, none of these custom directories should contain an \_\_init\_\_.py file, or else the plug-in system may not work (For more information on the implementation, see PEP 420 and/or David Beazley's 2015 PyCon talk on Modules and Packages at https://youtu.be/0oTh1CXRaQ0?t=1h25m45s).

As an example, in the following filesystem layout available custom modules are pyrex.custom. pyspice, pyrex.custom.irex, pyrex.custom.ara, pyrex.custom.ariana, and pyrex.custom.my\_analysis:

```
/path/to/site-packages/pyrex/
|-- __init__.py
|-- signals.py
|-- antenna.py
|-- ...
|-- custom/
| |-- pyspice.py
| |-- irex/
| |-- antenna.py
 | |-- ...
/path/to/home_dir/.pyrex-custom/
|-- ara/
| |-- custom/
| |-- ara/
| | | |-- antenna.py
| | | |-- ...
|-- ariana/
| |-- custom/
| | |-- ariana.py
/path/to/cwd/pyrex-custom/
|-- my_analysis_module/
| |-- custom/
| |-- my_analysis.py
```

# **FOUR**

# **PYREX API**

# 4.1 Package contents

A Python package for simulation of Askaryan pulses and radio antennas in ice.

PyREx (Python package for an IceCube Radio Extension) is, as its name suggests, a Python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas (e.g. the ARA and ARIANA collaborations).

```
class pyrex.Signal (times, values, value_type=<ValueTypes.undefined: 0>)
```

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

#### class ValueTypes

Enum containing possible types (units) for signal values.

```
undefined = 0
voltage = 1
field = 2
power = 3
```

dt

Returns the spacing of the time array, or None if invalid.

#### envelope

Calculates envelope of the signal by Hilbert transform.

### resample(n)

Resamples the signal into n points in the same time range.

#### with times (new times)

Returns a signal object representing this signal with a different times array. Uses numpy iterp on values by default.

### spectrum

Returns the FFT spectrum of the signal.

#### frequencies

Returns the FFT frequencies of the signal.

#### filter\_frequencies (freq\_response)

Applies the given frequency response function to the signal.

```
class pyrex.EmptySignal (times, value_type=<ValueTypes.undefined: 0>)
```

Bases: pyrex.signals.Signal

Class for signal with no amplitude (all values = 0)

```
with_times (new_times)
```

Returns a signal object representing this signal with a different times array. Returns EmptySignal for new times

```
class pyrex.FunctionSignal (times, function, value_type=<ValueTypes.undefined: 0>)
```

```
Bases: pyrex.signals.Signal
```

Class for signals generated by a function

```
with times (new times)
```

Returns a signal object representing this signal with a different times array. Leverages knowledge of the function to properly interpolate and extrapolate.

#### pyrex.AskaryanSignal

alias of FastAskaryanSignal

```
class pyrex.signals.FastAskaryanSignal (times, energy, theta, n=1.78, t0=0)
```

```
Bases: pyrex.signals.Signal
```

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

#### vector\_potential

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

#### RAC (time)

Calculates R \* vector potential (A) at the Cherenkov angle in Vs at the given time (s).

```
charge_profile (z, density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

```
max_length (density=0.92, crit_energy=0.0786, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (GeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
class pyrex. ThermalNoise (times, f_band, f_amplitude=1, rms_voltage=None, temperature=None, resistance=None, n_break=0)
```

```
Bases: pyrex.signals.FunctionSignal
```

Thermal Rayleigh noise in the frequency band f\_band=[f\_min,f\_max] (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are f\_amplitude (default 1) which can be a number or a function designating the amplitudes at each frequency, and n\_freqs which is the number of frequencies to use (in f\_band) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

#### is hit

Test for whether the antenna has been triggered.

#### is\_hit\_during(times)

Test for whether the antenna has been triggered during the given times array.

#### clear()

Reset the antenna to a state of having received no signals.

#### waveforms

Signal + noise (if noisy) at each triggered antenna hit.

#### all\_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

#### full\_waveform(times)

Signal + noise (if noisy) for the given times array.

#### make\_noise(times)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

#### trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

#### directional gain (theta, phi)

Function to calculate the directive electric field gain of the antenna at given angles theta (polar) and phi (azimuthal) relative to the antenna's orientation.

#### polarization\_gain (polarization)

Function to calculate the electric field gain due to polarization for a given polarization direction.

#### response (frequencies)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

#### receive (signal, origin=None, polarization=None)

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should end with super().receive(signal).

### **class** pyrex.**DipoleAntenna** (name, position, center\_frequency, bandwidth, resistance, orientation=[0, 0,

1], trigger threshold=0, effective height=None, noisy=True)

Bases: pyrex.antenna.Antenna

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

#### trigger (signal)

Trigger on the signal if the maximum signal value is above the given threshold.

#### response (frequencies)

Butterworth filter response for the antenna's frequency range.

### directional\_gain (theta, phi)

Power gain of dipole antenna goes as sin(theta)^2, so electric field gain goes as sin(theta).

#### polarization\_gain (polarization)

Polarization gain is simply the dot product of the polarization with the antenna's z-axis.

#### pyrex.IceModel

alias of AntarcticIce

#### class pyrex.ice\_model.AntarcticIce

Bases: object

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice.

k = 0.438

a = 0.0132

n0 = 1.32

thickness = 2850

#### classmethod gradient (z)

Returns the gradient of the index of refraction at depth z (m).

#### classmethod index (z)

Returns the medium's index of refraction, n, at depth z (m). Supports passing a numpy array of depths.

#### static temperature (z)

Returns the temperature (K) of the ice at depth z (m). Supports passing a numpy array of depths.

#### classmethod attenuation\_length (z, f)

Returns the attenuation length at depth z (m) and frequency f (Hz). Supports passing a numpy array of depths and/or frequencies. If both are passed as arrays, a 2-D array is returned where each row is a single depth and each column is a single frequency.

#### pyrex.prem\_density(r)

Returns the earth's density (g/cm<sup>3</sup>) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

#### pyrex.slant\_depth (angle, depth, step=5000)

Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth (m).

#### class pyrex.Particle (vertex, direction, energy)

Class for storing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector (automatically normalized), and an energy (GeV).

#### **class** pyrex. **ShadowGenerator** (*dx*, *dy*, *dz*, *energy\_generator*)

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing (sort of). energy\_generator should be a function that returns a particle energy in GeV.

### create\_particle()

Creates a particle with random vertex in cube and random direction.

#### class pyrex.PathFinder(ice model, from point, to point)

Class for ray tracking.

#### exists

Boolean of whether path exists.

### emitted\_ray

Direction in which ray is emitted.

#### path\_length

Length of the path (m).

#### tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time\_of\_flight()

#### time\_of\_flight (n\_steps=100)

Time of flight (s) for a particle along the path.

```
attenuation (f, n\_steps=100)
```

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a list of frequencies.

```
propagate (signal)
```

Applies attenuation to the signal along the path.

```
class pyrex.EventKernel (generator, ice_model, antennas)
```

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

```
event()
```

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

# 4.2 Submodules

# 4.2.1 pyrex.signals module

Module containing classes for digital signal processing

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

# class ValueTypes

Bases: enum. Enum

Enum containing possible types (units) for signal values.

```
undefined = 0
voltage = 1
field = 2
power = 3
```

dt

Returns the spacing of the time array, or None if invalid.

#### envelope

Calculates envelope of the signal by Hilbert transform.

#### resample(n)

Resamples the signal into n points in the same time range.

```
with_times (new_times)
```

Returns a signal object representing this signal with a different times array. Uses numpy iterp on values by default.

#### spectrum

Returns the FFT spectrum of the signal.

#### frequencies

Returns the FFT frequencies of the signal.

#### filter\_frequencies (freq\_response)

Applies the given frequency response function to the signal.

4.2. Submodules

class pyrex.signals.EmptySignal (times, value\_type=<ValueTypes.undefined: 0>)

Bases: pyrex.signals.Signal

Class for signal with no amplitude (all values = 0)

with times (new times)

Returns a signal object representing this signal with a different times array. Returns EmptySignal for new times.

class pyrex.signals.FunctionSignal (times, function, value\_type=<ValueTypes.undefined: 0>)

Bases: pyrex.signals.Signal

Class for signals generated by a function

```
with times (new times)
```

Returns a signal object representing this signal with a different times array. Leverages knowledge of the function to properly interpolate and extrapolate.

class pyrex.signals.SlowAskaryanSignal (times, energy, theta, n=1.78, t0=0)

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

RAC (time)

Calculates R \* vector potential at the Cherenkov angle in Vs at the given time (s).

charge\_profile (z, density=0.92, crit\_energy=0.0786, rad\_length=36.08)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

max\_length (density=0.92, crit\_energy=0.0786, rad\_length=36.08)

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (GeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

**class** pyrex.signals.**FastAskaryanSignal** (*times*, *energy*, *theta*, *n*=1.78, *t*0=0)

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

#### vector\_potential

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

RAC (time)

Calculates R \* vector potential (A) at the Cherenkov angle in Vs at the given time (s).

charge\_profile (z, density=0.92, crit\_energy=0.0786, rad\_length=36.08)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm<sup>3</sup>), critical energy (GeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

max\_length (density=0.92, crit\_energy=0.0786, rad\_length=36.08)

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (GeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
pyrex.signals.AskaryanSignal
```

alias of FastAskaryanSignal

#### class pyrex.signals.GaussianNoise(times, sigma)

Bases: pyrex.signals.Signal

Gaussian noise signal with standard deviation sigma

class pyrex.signals.ThermalNoise(times, f\_band, f\_amplitude=1, rms\_voltage=None, temperature=None, resistance=None, n freqs=0)

Bases: pyrex.signals.FunctionSignal

Thermal Rayleigh noise in the frequency band f\_band=[f\_min,f\_max] (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are f\_amplitude (default 1) which can be a number or a function designating the amplitudes at each frequency, and n\_freqs which is the number of frequencies to use (in f\_band) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

# 4.2.2 pyrex.antenna module

Module containing antenna class capable of receiving signals

```
class pyrex.antenna.Antenna (position, z_axis=[0, 0, 1], x_axis=[1, 0, 0], antenna_factor=1, effi-
ciency=1, freq_range=None, noise_rms=None, temperature=None, re-
sistance=None, noisy=True)
```

Bases: object

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

#### is hit

Test for whether the antenna has been triggered.

#### is\_hit\_during(times)

Test for whether the antenna has been triggered during the given times array.

#### clear()

Reset the antenna to a state of having received no signals.

#### waveforms

Signal + noise (if noisy) at each triggered antenna hit.

#### all\_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

#### full\_waveform(times)

Signal + noise (if noisy) for the given times array.

### make\_noise (times)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

#### trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

### directional\_gain (theta, phi)

Function to calculate the directive electric field gain of the antenna at given angles theta (polar) and phi (azimuthal) relative to the antenna's orientation.

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#### polarization\_gain (polarization)

Function to calculate the electric field gain due to polarization for a given polarization direction.

```
response (frequencies)
```

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

```
receive (signal, origin=None, polarization=None)
```

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should end with super().receive(signal).

class pyrex.antenna.DipoleAntenna (name, position, center\_frequency, bandwidth, resistance, orientation=[0, 0, 1], trigger\_threshold=0, effective\_height=None,
noisy=True)

Bases: pyrex.antenna.Antenna

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

```
trigger (signal)
```

Trigger on the signal if the maximum signal value is above the given threshold.

```
response (frequencies)
```

Butterworth filter response for the antenna's frequency range.

```
directional_gain (theta, phi)
```

Power gain of dipole antenna goes as sin(theta)^2, so electric field gain goes as sin(theta).

```
polarization_gain (polarization)
```

Polarization gain is simply the dot product of the polarization with the antenna's z-axis.

### 4.2.3 pyrex.ice model module

Module containing ice model. AntarcticIce class contains static and class methods for easy swapping of models. IceModel class is set to the preferred ice model.

```
class pyrex.ice_model.AntarcticIce
    Bases: object
```

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice.

k = 0.438

a = 0.0132

n0 = 1.32

thickness = 2850

#### classmethod gradient (z)

Returns the gradient of the index of refraction at depth z (m).

#### classmethod index (z)

Returns the medium's index of refraction, n, at depth z (m). Supports passing a numpy array of depths.

#### static temperature (z)

Returns the temperature (K) of the ice at depth z (m). Supports passing a numpy array of depths.

#### classmethod attenuation length (z, f)

Returns the attenuation length at depth z (m) and frequency f (Hz). Supports passing a numpy array of

depths and/or frequencies. If both are passed as arrays, a 2-D array is returned where each row is a single depth and each column is a single frequency.

```
class pyrex.ice_model.Newcomblce
```

```
Bases: pyrex.ice_model.AntarcticIce
```

Class inheriting from AntarcticIce, with new attenuation\_length function based on Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE ANTARCTICICE).

```
classmethod attenuation_length (z, f)
```

Returns the attenuation length at depth z (m) and frequency f (MHz) by Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE BOGORODSKY).

```
pyrex.ice_model.IceModel
    alias of AntarcticIce
```

# 4.2.4 pyrex.earth\_model module

Module containing earth model. Uses PREM for density as a function of radius and a simple integrator for calculation of the slant depth as a function of nadir angle.

```
pyrex.earth_model.prem_density(r)
```

Returns the earth's density (g/cm<sup>3</sup>) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

```
pyrex.earth_model.slant_depth (angle, depth, step=5000)
```

Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth (m).

### 4.2.5 pyrex.particle module

Module for particles (namely neutrinos) and neutrino interactions in the ice. Interactions include Earth shadowing (absorption) effect.

```
class pyrex.particle.NeutrinoInteraction (c, p)
Bases: object
```

Class for neutrino interaction attributes.

```
{\tt cross\_section}\,(E)
```

Return the cross section at a given energy E (GeV).

```
interaction length (E)
```

Return the interaction length at a given energy E (GeV).

```
class pyrex.particle.Particle(vertex, direction, energy)
    Bases: object
```

Class for storing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector (automatically normalized), and an energy (GeV).

```
pyrex.particle.random_direction()
```

Generate an arbitrary 3D unit vector.

```
{\bf class} \; {\tt pyrex.particle.ShadowGenerator} \; (\textit{dx}, \textit{dy}, \textit{dz}, \textit{energy\_generator})
```

Bases: object

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing (sort of). energy\_generator should be a function that returns a particle energy in GeV.

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```
create_particle()
```

Creates a particle with random vertex in cube and random direction.

# 4.2.6 pyrex.ray\_tracing module

Module containing class for ray tracking through the ice. Ray tracing not yet implemented.

```
{\bf class}~{\tt pyrex.ray\_tracing.PathFinder}~(\it ice\_model, from\_point, to\_point)
```

Bases: object

Class for ray tracking.

#### exists

Boolean of whether path exists.

#### emitted\_ray

Direction in which ray is emitted.

#### path\_length

Length of the path (m).

tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time\_of\_flight()

```
time_of_flight (n_steps=100)
```

Time of flight (s) for a particle along the path.

```
attenuation (f, n \ steps=100)
```

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path. Supports passing a list of frequencies.

```
propagate (signal)
```

Applies attenuation to the signal along the path.

# 4.2.7 pyrex.kernel module

Module for the simulation kernel. Includes neutrino generation, ray tracking (no raytracing yet), and hit generation.

```
class pyrex.kernel.EventKernel (generator, ice_model, antennas)
    Bases: object
```

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

```
event()
```

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

# 4.3 PyREx Custom Subpackage

More modules available as plug-ins, see Custom Sub-Package.

# 4.3.1 pyrex.custom.irex module

Customizations of pyrex package specific to IREX (IceCube Radio Extension)

**CHAPTER** 

**FIVE** 

# **VERSION HISTORY**

# 5.1 Version 1.2.0

- Changed custom module to a package containing irex module.
- custom package leverages "Implicit Namespace Package" structure to allow plug-in style additions to the package in either the user's ~/.pyrex-custom/directory or the ./pyrex-custom directory.

### 5.2 Version 1.1.2

- Added with\_times method to Signal class for interpolation/extrapolation of signals to different times.
- Change Antenna.make\_noise to use a single master noise object and use with\_times to calculate noise at different times.
  - To ensure noise is not obviously periodic (for <100 signals), uses 100 times the recommended number of frequencies, which results in longer computation time for noise waveforms.
- Add full\_waveform and is\_hit\_during methods to Antenna class for calculation of waveform over arbitrary time array and whether said waveform triggers the antenna, respectively.
- Added front\_end\_processing method to IREXAntenna for processing envelope, amplifying signal, and downsampling result (downsampling currently inactive).

# 5.3 Version 1.1.1

- Moved ValueTypes inside Signal class. Now access as Signal.ValueTypes.voltage, etc.
- Changed signal envelope calculation in custom IREXAntenna from hilbert transform to a basic model. Spice model also available, but slower.

# 5.4 Version 1.1.0

- Made units consistent across PyREx.
- Added directional\_gain and polarization\_gain methods to base Antenna.
  - receive method should no longer be overwritten in most cases.
  - Antenna now has orientation defined by z\_axis and x\_axis.

- antenna\_factor and efficiency attributes added to Antenna for more flexibility.
- Added ability to define Antenna noise by RMS voltage rather than temperature and resistance if desired.
- Added value\_type attribute to Signal class and derived classes.
  - Current value types are ValueTypes.undefined, ValueTypes.voltage, ValueTypes. field, and ValueTypes.power.
  - Signal objects now must have the same value\_type to be added (though those with ValueTypes. undefined can be coerced).
- Allow DipoleAntenna to guess at effective\_height if not specified.
- Increase speed of IceModel.\_\_atten\_coeffs method, resulting in increased speed of attenuation length calculations.

# 5.5 Version 1.0.3

• Added custom module to contain classes and functions specific to the IREX project.

# 5.6 Version 1.0.2

- Allow passing of numpy arrays of depths and frequencies into most IceModel methods.
  - IceModel.gradient () must still be calculated at individual depths.
- Added ability to specify RMS voltage of ThermalNoise without providing temperature and resistance.
- Removed (deprecated) Antenna.isHit().
- Added Antenna.make\_noise() method so custom antennas can use their own noise functions.
- Performance improvements:
  - Allowing for IceModel to calculate many attenuation lengths at once improves speed of PathFinder.
     propagate().
  - Improved speed of PathFinder.time\_of\_flight() and PathFinder.attenuation() (and improved accuracy to boot).

# 5.7 Version 1.0.1

- Fixed bugs in AskaryanSignal that caused the convolution to fail.
- Changed Antenna not require a temperature and frequency range if no noise is produced.
- Fixed bugs resulting from converting IceModel.temperature() from Celsius to Kelvin.

#### 5.8 Version 1.0.0

- Created PyREx package based on original notebook.
- Added all signal classes to produce full-waveform Askaryan pulses and thermal noise.
- Changed Antenna class to DipoleAntenna to allow Antenna to be a base class.

- Changed Antenna.isHit() method to Antenna.is\_hit property.
- Introduced IceModel alias for AntarcticIce (or any future preferred ice model).
- Moved AntarcticIce.attenuationLengthMN to its own NewcombIce class inheriting from AntarcticIce.
- Added PathFinder.propagate() to propagate a Signal object in a customizable way.
- Changed naming conventions to be more consistent, verbose, and "pythonic":
  - AntarcticIce.attenuationLength() becomes AntarcticIce. attenuation\_length().
  - In pyrex.earth\_model, RE becomes EARTH\_RADIUS.
  - In pyrex.particle, neutrino\_interaction becomes NeutrinoInteraction.
  - In pyrex.particle, NA becomes AVOGADRO\_NUMBER.
  - particle class becomes Particle namedtuple.
    - \* Particle.vtx becomes Particle.vertex.
    - \* Particle.dir becomes Particle.direction.
    - \* Particle.E becomes Particle.energy.
  - In pyrex.particle, next\_direction() becomes random\_direction().
  - shadow\_generator becomes ShadowGenerator.
  - PathFinder methods become properties where reasonable:
    - \* PathFinder.exists() becomes PathFinder.exists.
    - \* PathFinder.getEmittedRay() becomes PathFinder.emitted\_ray.
    - \* PathFinder.getPathLength() becomes PathFinder.path\_length.
  - PathFinder.propagateRay() split into PathFinder.time\_of\_flight() (with corresponding PathFinder.tof property) and PathFinder.attenuation().

# 5.9 Version 0.0.0

Original PyREx python notebook written by Kael Hanson:

https://gist.github.com/physkael/898a64e6fbf5f0917584c6d31edf7940

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