# **PyREx Documentation**

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**CHAPTER** 

ONE

## **PYREX API**

## 1.1 Package contents

```
class pyrex.Signal (times, values)
```

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

dt

Returns the spacing of the time array, or None if invalid.

## envelope

Calculates envelope of the signal by Hilbert transform.

### resample(n)

Resamples the signal into n points in the same time range.

#### spectrum

Returns the FFT spectrum of the signal.

## frequencies

Returns the FFT frequencies of the signal.

## filter\_frequencies (freq\_response)

Applies the given frequency response function to the signal.

```
class pyrex.EmptySignal (times)
```

Bases: pyrex.signals.Signal

Class for signal with no amplitude (all values = 0)

## class pyrex.FunctionSignal (times, function)

Bases: pyrex.signals.Signal

Class for signals generated by a function

## pyrex.AskaryanSignal

alias of FastAskaryanSignal

```
class pyrex.signals.FastAskaryanSignal (times, energy, theta, n=1.78, t0=0)
```

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

#### vector potential

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

## RAC (time)

Calculates R \* vector potential (A) at the Cherenkov angle in Vs at the given time (s).

```
charge profile (z, density=0.92, crit\ energy=7.86e-05, rad\ length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm<sup>3</sup>), critical energy (TeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
max_length (density=0.92, crit_energy=7.86e-05, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (TeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

 ${f class}$  pyrex. ThermalNoise (times, temperature, resistance, f\_band, f\_amplitude=1, n\_freqs=0)

```
Bases: pyrex.signals.Signal
```

Thermal Rayleigh noise at a given temperature (K) and resistance (ohms) in the frequency band  $f_{min,f_{max}}$  (Hz). Optional parameters are  $f_{min,f_{max}}$  (Hz). Optional parameters are  $f_{min,f_{max}}$  (Hz) which can be a number or a function designating the amplitudes at each frequency, and  $f_{min,f_{max}}$  (default is based on the FFT bin size of given times array). Returned signal values are voltages (V).

## class pyrex.Antenna (position, temperature, freq\_range, resistance=None, noisy=True)

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

### is hit

Test for whether the antenna has received a signal.

## isHit()

Deprecated. Replaced by is\_hit property.

#### clear(

Reset the antenna to a state of having received no signals.

#### waveforms

Signal + noise (if noisy) at each triggered antenna hit.

## all\_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

## trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

#### response (frequencies)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

## receive (signal, polarization=[0, 0, 1])

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should end with super().receive(signal).

**class** pyrex.**DipoleAntenna** (name, position, center\_frequency, bandwidth, resistance, effective\_height, polarization=[0, 0, 1], trigger\_threshold=0, noisy=True)

```
Bases: pyrex.antenna. Āntenna
```

Antenna with a given name, position (m), center frequency (MHz), bandwidth (MHz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

```
trigger (signal)
           Trigger on the signal if the maximum signal value is above the given threshold.
     response (frequencies)
           Butterworth filter response for the antenna's frequency range.
     receive (signal, polarization=[0, 0, 1])
           Apply polarization effect to signal, then proceed with usual antenna reception.
pyrex.IceModel
     alias of AntarcticIce
class pyrex.ice_model.AntarcticIce
     Bases: object
     Class containing characteristics of ice at the south pole.
     k = 0.438
     a = 0.0132
     n0 = 1.32
     thickness = 2850
     classmethod gradient (z)
           Returns the gradient of the index of refraction at depth z (m).
     classmethod index (z)
           Returns the medium's index of refraction, n, at depth z (m).
     static temperature (z)
           Returns the temperature (K) of the ice at depth z (m)
     classmethod attenuation_length (z, f)
           Returns the attenuation length at depth z (m) and frequency f (MHz).
pyrex.prem_density(r)
     Returns the earth's density (g/cm<sup>3</sup>) for a given radius r (m). Calculated by the Preliminary Earth Model
     (PREM).
pyrex.slant_depth (angle, depth, step=5000)
     Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth
     (m).
class pyrex.Particle
     Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy
     (GeV).
     direction
     energy
     vertex
class pyrex. ShadowGenerator (dx, dy, dz, energy_generator)
     Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing
     (sort of). energy_generator should be a function that returns a particle energy in GeV.
```

create\_particle()

Class for ray tracking.

Creates a particle with random vertex in cube and random direction.

class pyrex.PathFinder(ice model, from point, to point)

#### exists

Boolean of whether path exists.

## emitted\_ray

Direction in which ray is emitted.

## path\_length

Length of the path (m).

#### tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time\_of\_flight()

## time\_of\_flight (n\_steps=10)

Time of flight (s) for a particle along the path.

```
attenuation (f, n\_steps=10)
```

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path.

## propagate (signal)

Applies attenuation to the signal along the path.

## class pyrex.EventKernel (generator, ice model, antennas)

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

#### event()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

## 1.2 Submodules

## 1.2.1 pyrex.signals module

Module containing classes for digital signal processing

```
class pyrex.signals.Signal (times, values)
     Bases: object
```

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

### dt

Returns the spacing of the time array, or None if invalid.

## envelope

Calculates envelope of the signal by Hilbert transform.

## resample(n)

Resamples the signal into n points in the same time range.

## spectrum

Returns the FFT spectrum of the signal.

#### frequencies

Returns the FFT frequencies of the signal.

## filter\_frequencies (freq\_response)

Applies the given frequency response function to the signal.

```
class pyrex.signals.EmptySignal (times)
    Bases: pyrex.signals.Signal
    Class for signal with no amplitude (all values = 0)

class pyrex.signals.FunctionSignal (times, function)
    Bases: pyrex.signals.Signal
    Class for signals generated by a function
```

 $\textbf{class} \ \texttt{pyrex.signals.SlowAskaryanSignal} \ (\textit{times, energy, theta}, n=1.78, t0=0)$ 

Bases: pyrex.signals.Signal

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

RAC (time)

Calculates R \* vector potential at the Cherenkov angle in Vs at the given time (s).

```
charge_profile (z, density=0.92, crit_energy=7.86e-05, rad_length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (TeV), and electron radiation length (g/cm^2) in ice.

```
max_length (density=0.92, crit_energy=7.86e-05, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (TeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
class pyrex.signals.FastAskaryanSignal (times, energy, theta, n=1.78, t0=0)
Bases: pyrex.signals.Signal
```

Askaryan pulse binned to times from neutrino with given energy (TeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

## vector\_potential

Recover the vector\_potential from the electric field. Mostly just for testing purposes.

RAC (time)

Calculates R \* vector potential (A) at the Cherenkov angle in Vs at the given time (s).

```
charge profile (z, density=0.92, crit\ energy=7.86e-05, rad\ length=36.08)
```

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm<sup>3</sup>), critical energy (TeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
max_length (density=0.92, crit_energy=7.86e-05, rad_length=36.08)
```

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm<sup>3</sup>), critical energy (TeV), and electron radiation length (g/cm<sup>2</sup>) in ice.

```
pyrex.signals.AskaryanSignal
    alias of FastAskaryanSignal

class pyrex.signals.GaussianNoise(times, sigma)
    Bases: pyrex.signals.FunctionSignal
```

Gaussian noise signal with standard deviation sigma

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```
class pyrex.signals.ThermalNoise (times, temperature, resistance, f\_band, f\_amplitude=1, n\_freqs=0)
```

Bases: pyrex.signals.Signal

Thermal Rayleigh noise at a given temperature (K) and resistance (ohms) in the frequency band f\_band=[f\_min,f\_max] (Hz). Optional parameters are f\_amplitude (default 1) which can be a number or a function designating the amplitudes at each frequency, and n\_freqs which is the number of frequencies to use (in f\_band) for the calculation (default is based on the FFT bin size of given times array). Returned signal values are voltages (V).

## 1.2.2 pyrex.antenna module

Module containing antenna class capable of receiving signals

```
class pyrex.antenna.Antenna (position, temperature, freq_range, resistance=None, noisy=True)
    Bases: object
```

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

### is hit

Test for whether the antenna has received a signal.

#### isHit()

Deprecated. Replaced by is\_hit property.

#### clear()

Reset the antenna to a state of having received no signals.

### waveforms

Signal + noise (if noisy) at each triggered antenna hit.

#### all\_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

## trigger (signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

```
response (frequencies)
```

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

```
receive (signal, polarization=[0, 0, 1])
```

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this fuction, but should end with super().receive(signal).

Bases: pyrex.antenna.Antenna

Antenna with a given name, position (m), center frequency (MHz), bandwidth (MHz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

## trigger (signal)

Trigger on the signal if the maximum signal value is above the given threshold.

```
response (frequencies)
```

Butterworth filter response for the antenna's frequency range.

```
receive (signal, polarization=[0, 0, 1])
```

Apply polarization effect to signal, then proceed with usual antenna reception.

## 1.2.3 pyrex.ice model module

Module containing ice model. AntarcticIce class contains static and class methods for easy swapping of models. IceModel class is set to the preferred ice model.

```
class pyrex.ice_model.AntarcticIce
    Bases: object
    Class containing characteristics of ice at the south pole.
    k = 0.438
    a = 0.0132
    n0 = 1.32
    thickness = 2850
    classmethod gradient (z)
        Returns the gradient of the index of refraction at depth z (m).
    classmethod index (z)
```

Returns the medium's index of refraction, n, at depth z (m).

```
static temperature (z)
```

Returns the temperature (K) of the ice at depth z (m)

```
classmethod attenuation_length (z, f)
```

Returns the attenuation length at depth z (m) and frequency f (MHz).

```
class pyrex.ice_model.NewcombIce
    Bases: pyrex.ice_model.AntarcticIce
```

Class inheriting from AntarcticIce, with new attenuation\_length function based on Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE ANTARCTICICE).

```
classmethod attenuation_length (z, f)
```

Returns the attenuation length at depth z (m) and frequency f (MHz) by Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE BOGORODSKY).

```
pyrex.ice_model.IceModel
    alias of AntarcticIce
```

## 1.2.4 pyrex.earth\_model module

Module containing earth model. Uses PREM for density as a function of radius and a simple integrator for calculation of the slant depth as a function of nadir angle.

```
pyrex.earth_model.prem_density(r)
```

Returns the earth's density (g/cm<sup>3</sup>) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

```
pyrex.earth_model.slant_depth (angle, depth, step=5000)
```

Returns the material thickness (g/cm<sup>2</sup>) for a chord cutting through earth at Nadir angle and starting at depth (m).

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## 1.2.5 pyrex.particle module

Module for particles (namely neutrinos) and neutrino interactions in the ice. Interactions include Earth shadowing (absorption) effect.

```
class pyrex.particle.NeutrinoInteraction (c, p)
     Bases: object
     Class for neutrino interaction attributes.
     cross\_section(E)
          Return the cross section at a given energy E (GeV).
     interaction length (E)
          Return the interaction length at a given energy E (GeV).
class pyrex.particle.Particle
     Bases: tuple
     Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy
     direction
     energy
     vertex
pyrex.particle.random_direction()
     Generate an arbitrary 3D unit vector.
class pyrex.particle.ShadowGenerator(dx, dy, dz, energy_generator)
     Bases: object
     Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into accout Earth shadowing
     (sort of). energy_generator should be a function that returns a particle energy in GeV.
     create_particle()
```

## 1.2.6 pyrex.ray\_tracing module

Module containing class for ray tracking through the ice. Ray tracing not yet implemented.

Creates a particle with random vertex in cube and random direction.

```
class pyrex.ray_tracing.PathFinder (ice_model, from_point, to_point)
    Bases: object
    Class for ray tracking.
    exists
        Boolean of whether path exists.

emitted_ray
        Direction in which ray is emitted.

path_length
        Length of the path (m).

tof
        Time of flight (s) for a particle along the path. Calculated using default values of self.time_of_flight()
        time_of_flight (n_steps=10)
        Time of flight (s) for a particle along the path.
```

```
attenuation (f, n\_steps=10)
```

Returns the attenuation factor for a signal of frequency f (Hz) traveling along the path.

```
propagate (signal)
```

Applies attenuation to the signal along the path.

## 1.2.7 pyrex.kernel module

Module for the simulation kernel. Includes neutrino generation, ray tracking (no raytracing yet), and hit generation.

```
{\bf class}~{\tt pyrex.kernel.EventKernel}~({\it generator}, ice\_{\it model}, {\it antennas})
```

Bases: object

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

event()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

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