
PyREx Documentation

Release 1.1.0

Ben Hokanson-Fasig

Oct 06, 2017

CONTENTS:

1	Introduction to PyREx	1
1.1	Installation	1
1.2	Code Example	1
1.3	Units	2
2	Code Examples	3
2.1	Working with Signal Objects	3
2.2	Antenna Class and Subclasses	5
2.3	Ice and Earth Models	7
2.4	Particle Generation	8
2.5	Ray Tracing	8
2.6	Full Simulation	9
2.7	More Examples	10
3	PyREx API	11
3.1	Package contents	11
3.2	Submodules	14
3.2.1	pyrex.signals module	14
3.2.2	pyrex.antenna module	16
3.2.3	pyrex.ice_model module	17
3.2.4	pyrex.earth_model module	18
3.2.5	pyrex.particle module	18
3.2.6	pyrex.ray_tracing module	18
3.2.7	pyrex.kernel module	19
3.2.8	pyrex.custom module	19
4	Version History	21
4.1	Version 1.1.0	21
4.2	Version 1.0.3	21
4.3	Version 1.0.2	21
4.4	Version 1.0.1	21
4.5	Version 1.0.0	22
4.6	Version 0.0.0	22
	Python Module Index	23
	Index	25

INTRODUCTION TO PYREX

PyREx (**P**ython package for an IceCube **R**adio **E**xtension) is, as its name suggests, a python package designed to simulate the measurement of Askaryan pulses via a radio antenna array around the IceCube South Pole Neutrino Observatory. The code is designed to be modular so that it can also be applied to other askaryan radio antennas, as in the ARA and ARIANA collaborations.

1.1 Installation

To use the PyREx package, download the code from <https://github.com/bhokansonfasig/pyrex> and then either include the `pyrex` directory (the one containing the python modules) in your `PYTHON_PATH`, or just copy the `pyrex` directory into your working directory. In the future, PyREx may be installable via `pip`, but it is not currently available there.

1.2 Code Example

The most basic simulation can be produced as follows:

First, import the package:

```
import pyrex
```

Then, create a particle generator object that will produce random particles in a cube of 1 km on each side with a fixed energy of 100 PeV:

```
particle_generator = pyrex.ShadowGenerator(dx=1000, dy=1000, dz=1000,  
                                           energy_generator=lambda: 1e8)
```

An array of antennas that represent the detector is also needed. The base `Antenna` class provides a basic antenna with a flat frequency response and no trigger condition. Here we make a single vertical “string” of four antennas with no noise:

```
antenna_array = []  
for z in [-100, -150, -200, -250]:  
    antenna_array.append(  
        pyrex.Antenna(position=(0,0,z), noisy=False)  
    )
```

Finally, we want to pass these into the `EventKernel` and produce an event:

```
kernel = pyrex.EventKernel(generator=particle_generator,
                           ice_model=pyrex.IceModel, antennas=antenna_array)
kernel.event()
```

Now the signals received by each antenna can be accessed by their `waveforms` parameter:

```
import matplotlib.pyplot as plt
for ant in kernel.ant_array:
    for wave in ant.waveforms:
        plt.figure()
        plt.plot(wave.times, wave.values)
        plt.show()
```

1.3 Units

For ease of use, PyREx tries to use consistent units in all classes and functions. The units used are mostly SI with a few exceptions listed in bold below:

Metric	Unit
time	seconds (s)
frequency	hertz (Hz)
distance	meters (m)
density	grams per cubic centimeter (g/cm³)
material thickness	grams per square centimeter (g/cm²)
temperature	kelvin (K)
energy	gigaelectronvolts (GeV)
resistance	ohms (Ω)
voltage	volts (V)
electric field	volts per meter (V/m)

CODE EXAMPLES

The following code examples assume these imports:

```
import numpy as np
import matplotlib.pyplot as plt
import scipy.fftpack
import pyrex
```

All of the following examples can also be found (and quickly run) in the Code Examples python notebook.

2.1 Working with Signal Objects

The base `Signal` class is simply an array of times and an array of signal values, and is instantiated with these two arrays. The `times` array is assumed to be in units of seconds, but there are no general units for the `values` array (though it is commonly assumed to be in volts or volts per meter). It is worth noting that the `Signal` object stores shallow copies of the passed arrays, so changing the original arrays will not affect the `Signal` object.

```
time_array = np.linspace(0, 10)
value_array = np.sin(time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)
```

Plotting the `Signal` object is as simple as plotting the times vs the values:

```
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

`Signal` objects can be added as long as they have the same time array, and also support the python `sum` function:

```
time_array = np.linspace(0, 10)
values1 = np.sin(time_array)
values2 = np.cos(time_array)
signal1 = pyrex.Signal(time_array, values1)
plt.plot(signal1.times, signal1.values, label="signal1")
signal2 = pyrex.Signal(time_array, values2)
plt.plot(signal2.times, signal2.values, label="signal2")
signal3 = signal1 + signal2
plt.plot(signal3.times, signal3.values, label="signal3")
all_signals = [signal1, signal2, signal3]
signal4 = sum(all_signals)
plt.plot(signal4.times, signal4.values, label="signal4")
plt.legend()
plt.show()
```

The `Signal` class provides many convenience attributes for dealing with signals:

```
my_signal.dt == my_signal.times[1] - my_signal.times[0]
my_signal.spectrum == scipy.fftpack.fft(my_signal.values)
my_signal.frequencies == scipy.fftpack.fftfreq(n=len(my_signal.values),
                                              d=my_signal.dt)
my_signal.envelope == np.abs(scipy.signal.hilbert(my_signal.values))
```

The `Signal` class also provides functions for manipulating the signal. The `resample` function will resample the times and values arrays to the given number of points (with the same endpoints):

```
my_signal.resample(1001)
len(my_signal.times) == len(my_signal.values) == 1001
my_signal.times[0] == 0
my_signal.times[-1] == 10
```

The `filter_frequencies` function will apply a frequency-domain filter to the values array based on the passed frequency response function:

```
def lowpass_filter(frequency):
    if frequency < 1:
        return 1
    else:
        return 0

time_array = np.linspace(0, 10, 1001)
value_array = np.sin(0.1*2*np.pi*time_array) + np.sin(2*2*np.pi*time_array)
my_signal = pyrex.Signal(times=time_array, values=value_array)

plt.plot(my_signal.times, my_signal.values)
my_signal.filter_frequencies(lowpass_filter)
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

A number of classes which inherit from the `Signal` class are included in PyREx: `EmptySignal`, `FunctionSignal`, `AskaryanSignal`, and `ThermalNoise`. `EmptySignal` is simply a signal whose values are all zero:

```
time_array = np.linspace(0,10)
empty = pyrex.EmptySignal(times=time_array)
plt.plot(empty.times, empty.values)
plt.show()
```

`FunctionSignal` takes a function of time and creates a signal based on that function:

```
time_array = np.linspace(0,10)
def square_wave(time):
    if int(time)%2==0:
        return 1
    else:
        return -1
square_signal = pyrex.FunctionSignal(times=time_array, function=square_wave)
plt.plot(square_signal.times, square_signal.values)
plt.show()
```

`AskaryanSignal` produces an Askaryan pulse on a time array due to a neutrino of given energy observed at a given angle from the shower axis:


```
time_array = np.linspace(-10e-9, 40e-9, 1001)
neutrino_energy = 1e8 # GeV
observation_angle = 45 * np.pi/180 # radians
askaryan = pyrex.AskaryanSignal(times=time_array, energy=neutrino_energy,
                                theta=observation_angle)
plt.plot(askaryan.times, askaryan.values)
plt.show()
```

ThermalNoise produces Rayleigh noise at a given temperature and resistance which has been passed through a bandpass filter of the given frequency range:

```
time_array = np.linspace(-10e-9, 40e-9, 1001)
noise_temp = 300 # K
system_resistance = 1000 # ohm
frequency_range = (550e6, 750e6) # Hz
noise = pyrex.ThermalNoise(times=time_array, temperature=noise_temp,
                           resistance=system_resistance,
                           f_band=frequency_range)
plt.plot(noise.times, noise.values)
plt.show()
```

2.2 Antenna Class and Subclasses

The base Antenna class provided by PyREx is designed to be inherited from to match the needs of each project. At its core, an Antenna object is initialized with a position, a temperature, and a frequency range, as well as optionally a resistance for noise calculations and a boolean dictating whether or not noise should be added to the antenna's signals (note that if noise is to be added, a resistance must be specified).

```
position = (0, 0, -100) # m
temperature = 300 # K
resistance = 1 # ohm
frequency_range = (0, 1e3) # Hz
basic_antenna = pyrex.Antenna(position=position, temperature=temperature,
                              resistance=resistance,
                              freq_range=frequency_range)
noiseless_antenna = pyrex.Antenna(position=position, noisy=False)
```

The basic properties of an Antenna object are `is_hit` and `waveforms`. `is_hit` specifies whether or not the antenna has been triggered by an event. `waveforms` is a list of all the waveforms which have triggered the antenna. The antenna also defines `signals`, which is a list of all signals the antenna has received, and `all_waveforms` which is a list of all waveforms (signal plus noise) the antenna has received including those which didn't trigger.

```
basic_antenna.is_hit == False
basic_antenna.waveforms == []
```

The Antenna class defines three methods which are expected to be overwritten: `trigger`, `response`, and `receive`. `trigger` takes a Signal object as an argument and returns a boolean of whether or not the antenna would trigger on that signal (default always returns True). `response` takes a frequency or list of frequencies (in Hz) and returns the frequency response of the antenna at each frequency given (default always returns 1).

```
basic_antenna.trigger(pyrex.Signal([0],[0])) == True
freqs = [1, 2, 3, 4, 5]
basic_antenna.response(freqs) == [1, 1, 1, 1, 1]
```

The receive method is a bit different in that it contains some default functionality:

```
def receive(self, signal):
    copy = Signal(signal.times, signal.values)
    copy.filter_frequencies(self.response)
    self.signals.append(copy)
```

In this sense, the receive function is intended to be extended instead of overwritten. In derived classes, it is recommended that a newly defined receive function call `super().receive(signal)`. For example, if a polarization is to be applied, the following receive function could be implemented:

```
def receive(self, signal, signal_polarization):
    polarization_factor = np.vdot(self.polarization, signal_polarization)
    polarized_signal = Signal(signal.times,
                             signal.values * polarization_factor)
    super().receive(polarized_signal)
```

To use the receive function, simply pass it the Signal object the antenna sees, and the Antenna class will handle the rest:

```
incoming_signal = pyrex.FunctionSignal(np.linspace(0,10), np.sin)
basic_antenna.receive(incoming_signal)
basic_antenna.is_hit == True
for wave in basic_antenna.waveforms:
    plt.figure()
    plt.plot(wave.times, wave.values)
    plt.show()
for pure_signal in basic_antenna.signals:
    plt.figure()
    plt.plot(pure_signal.times, pure_signal.values)
    plt.show()
```

The Antenna class also defines a clear method which will reset the antenna to a state of having received no signals:

```
basic_antenna.clear()
basic_antenna.is_hit == False
len(basic_antenna.waveforms) == 0
```

To create a custom antenna, simply inherit from the Antenna class:

```
class NoiselessThresholdAntenna(pyrex.Antenna):
    def __init__(self, position, threshold):
        super().__init__(position=position, noisy=False)
        self.threshold = threshold

    def trigger(self, signal):
        if max(np.abs(signal.values)) > self.threshold:
            return True
        else:
            return False
```

Our custom NoiselessThresholdAntenna should only trigger when the amplitude of a signal exceeds its threshold value:

```
my_antenna = NoiselessThresholdAntenna(position=(0, 0, 0), threshold=2)

incoming_signal = pyrex.FunctionSignal(np.linspace(0,10), np.sin)
my_antenna.receive(incoming_signal)
```

```

my_antenna.is_hit == False
len(my_antenna.waveforms) == 0
len(my_antenna.all_waveforms) == 1

incoming_singal = pyrex.Signal(incoming_singal.times,
                               5*incoming_singal.values)
my_antenna.receive(incoming_singal)
my_antenna.is_hit == True
len(my_antenna.waveforms) == 1
len(my_antenna.all_waveforms) == 2

for wave in my_antenna.waveforms:
    plt.figure()
    plt.plot(wave.times, wave.values)
    plt.show()

```

PyREx defines `DipoleAntenna` which as a subclass of `Antenna`, which provides a basic threshold trigger, a basic bandpass filter, and a polarization effect on the reception of a signal. A `DipoleAntenna` object is created as follows:

```

antenna_identifier = "antenna 1"
position = (0, 0, -100)
center_frequency = 250e6 # Hz
bandwidth = 300e6 # Hz
resistance = 100 # ohm
antenna_length = 3e8/center_frequency/2 # m
polarization_direction = (0, 0, 1)
trigger_threshold = 1e-5 # V
dipole = pyrex.DipoleAntenna(name=antenna_identifier, position=position,
                             center_frequency=center_frequency,
                             bandwidth=bandwidth, resistance=resistance,
                             effective_height=antenna_length,
                             polarization=polarization_direction,
                             trigger_threshold=trigger_threshold)

```

2.3 Ice and Earth Models

PyREx provides a class `IceModel`, which is an alias for whichever south pole ice model class is the preferred (currently just the basic `AntarcticIce`). The `IceModel` class provides class methods for calculating characteristics of the ice at different depths and frequencies outlined below:

```

depth = -1000 # m
pyrex.IceModel.temperature(depth)
pyrex.IceModel.index(depth)
pyrex.IceModel.gradient(depth)
frequency = 1e8 # Hz
pyrex.IceModel.attenuation_length(depth, frequency)

```

PyREx also provides two functions related to its earth model: `prem_density` and `slant_depth`. `prem_density` calculates the density in grams per cubic centimeter of the earth at a given radius:

```

radius = 6360000 # m
pyrex.prem_density(radius)

```

`slant_depth` calculates the material thickness in grams per square centimeter of a chord cutting through the earth at a given nadir angle, starting from a given depth:

```
nadir_angle = 60 * np.pi/180 # radians
depth = 1000 # m
pyrex.slant_depth(nadir_angle, depth)
```

2.4 Particle Generation

PyREx includes `Particle` as a container for information about neutrinos which are generated to produce Askaryan pulses. `Particle` contains three attributes: `vertex`, `direction`, and `energy`:

```
initial_position = (0,0,0) # m
direction_vector = (0,0,-1)
particle_energy = 1e8 # GeV
pyrex.Particle(vertex=initial_position, direction=direction_vector,
               energy=particle_energy)
```

PyREx also includes a `ShadowGenerator` class for generating random neutrinos, taking into account some Earth shadowing. The neutrinos are generated in a box of given size, and with an energy given by an energy generation function:

```
box_width = 1000 # m
box_depth = 500 # m
const_energy_generator = lambda: 1e8 # GeV
my_generator = pyrex.ShadowGenerator(dx=box_width, dy=box_width,
                                     dz=box_depth,
                                     energy_generator=const_energy_generator)
my_generator.create_particle()
```

2.5 Ray Tracing

While PyREx does not currently support full ray tracing, it does provide a `PathFinder` class which implements some basic ray analysis by Snell's law. `PathFinder` takes an ice model and two points as arguments and provides a number of properties and methods regarding the path between the points.

```
start = (0, 0, -100) # m
finish = (0, 0, -250) # m
my_path = pyrex.PathFinder(ice_model=pyrex.IceModel,
                          from_point=start, to_point=finish)
```

`PathFinder.exists` is a boolean value of whether or not the path between the points is traversable according to the indices of refraction. `PathFinder.emitted_ray` is a unit vector giving the direction from `from_point` to `to_point`. `PathFinder.path_length` is the length in meters of the straight line path between the two points.

```
my_path.exists
my_path.emitted_ray
my_path.path_length
```

`PathFinder.time_of_flight()` calculates the time it takes for light to traverse the path, with an optional parameter `n_steps` defining the precision used. `PathFinder.tof` is a convenience property set to the time of flight using the default value of `n_steps`.

```
my_path.time_of_flight(n_steps=100)
my_path.time_of_flight() == my_path.tof
```

`PathFinder.attenuation()` calculates the attenuation factor along the path for a signal of given frequency. Here again there is an optional parameter `n_steps` defining the precision used.

```
frequency = 1e9 # Hz
my_path.attenuation(f=frequency, n_steps=100)
```

Finally, `PathFinder.propagate()` propagates a `Signal` object from `from_point` to `to_point` by applying a `1/PathFinder.path_length` factor, applying the frequency attenuation of `PathFinder.attenuation()`, and shifting the signal times by `PathFinder.tof`:

```
time_array = np.linspace(0, 5e-9, 1001)
my_signal = (pyrex.FunctionSignal(time_array, lambda t: np.sin(1e9*2*np.pi*t))
            + pyrex.FunctionSignal(time_array, lambda t: np.sin(1e10*2*np.pi*t)))
plt.plot(my_signal.times, my_signal.values)
plt.show()

my_path.propagate(my_signal)
plt.plot(my_signal.times, my_signal.values)
plt.show()
```

2.6 Full Simulation

PyREx provides the `EventKernel` class to control a basic simulation including the creation of neutrinos, the propagation of their pulses to the antennas, and the triggering of the antennas:

```
particle_generator = pyrex.ShadowGenerator(dx=1000, dy=1000, dz=500,
                                           energy_generator=lambda: 1e8)

detector = []
for i, z in enumerate([-100, -150, -200, -250]):
    detector.append(
        pyrex.DipoleAntenna(name="antenna_"+str(i), position=(0, 0, z),
                           center_frequency=250e6, bandwidth=300e6,
                           resistance=0, effective_height=0.6,
                           trigger_threshold=0, noisy=False)
    )
kernel = pyrex.EventKernel(generator=particle_generator,
                           ice_model=pyrex.IceModel,
                           antennas=detector)

triggered = False
while not triggered:
    kernel.event()
    for antenna in detector:
        if antenna.is_hit:
            triggered = True
            break

for antenna in detector:
    for i, wave in enumerate(antenna.waveforms):
        plt.plot(wave.times * 1e9, wave.values)
        plt.xlabel("Time (ns)")
        plt.ylabel("Voltage (V)")
        plt.title(antenna.name + " - waveform " + str(i))
```

2.7 More Examples

For more code examples, see the PyREx Demo python notebook.

3.1 Package contents

class `pyrex.Signal` (*times, values*)

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

dt

Returns the spacing of the time array, or None if invalid.

envelope

Calculates envelope of the signal by Hilbert transform.

resample (*n*)

Resamples the signal into n points in the same time range.

spectrum

Returns the FFT spectrum of the signal.

frequencies

Returns the FFT frequencies of the signal.

filter_frequencies (*freq_response*)

Applies the given frequency response function to the signal.

class `pyrex.EmptySignal` (*times*)

Bases: `pyrex.signals.Signal`

Class for signal with no amplitude (all values = 0)

class `pyrex.FunctionSignal` (*times, function*)

Bases: `pyrex.signals.Signal`

Class for signals generated by a function

`pyrex.AskaryanSignal`

alias of `FastAskaryanSignal`

class `pyrex.signals.FastAskaryanSignal` (*times, energy, theta, n=1.78, t0=0*)

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

vector_potential

Recover the vector_potential from the electric field. Mostly just for testing purposes.

RAC (*time*)

Calculates $R * \text{vector potential (A)}$ at the Cherenkov angle in Vs at the given time (s).

charge_profile (*z, density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

max_length (*density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm^3), critical energy (GeV), and electron radiation length (g/cm^2) in ice.

class `pyrex.ThermalNoise` (*times, f_band, f_amplitude=1, rms_voltage=None, temperature=None, resistance=None, n_freqs=0*)

Bases: `pyrex.signals.Signal`

Thermal Rayleigh noise in the frequency band $f_band=[f_min, f_max]$ (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are $f_amplitude$ (default 1) which can be a number or a function designating the amplitudes at each frequency, and n_freqs which is the number of frequencies to use (in f_band) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

class `pyrex.Antenna` (*position, freq_range=None, temperature=None, resistance=None, noisy=True*)

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

is_hit

Test for whether the antenna has received a signal.

clear ()

Reset the antenna to a state of having received no signals.

waveforms

Signal + noise (if noisy) at each triggered antenna hit.

all_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

make_noise (*times*)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

trigger (*signal*)

Function to determine whether or not the antenna is triggered by the given Signal object.

response (*frequencies*)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

receive (*signal, polarization=[0, 0, 1]*)

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this function, but should end with `super().receive(signal)`.

class `pyrex.DipoleAntenna` (*name, position, center_frequency, bandwidth, resistance, effective_height, polarization=[0, 0, 1], trigger_threshold=0, noisy=True*)

Bases: `pyrex.antenna.Antenna`

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

trigger (*signal*)

Trigger on the signal if the maximum signal value is above the given threshold.

response (*frequencies*)

Butterworth filter response for the antenna's frequency range.

receive (*signal, polarization=[0, 0, 1]*)

Apply polarization effect to signal, then proceed with usual antenna reception.

`pyrex.IceModel`

alias of `AntarcticIce`

class `pyrex.ice_model.AntarcticIce`

Bases: `object`

Class containing characteristics of ice at the south pole. In all cases, depth z is given with negative values in the ice and positive values above the ice.

k = 0.438

a = 0.0132

n0 = 1.32

thickness = 2850

classmethod `gradient` (z)

Returns the gradient of the index of refraction at depth z (m).

classmethod `index` (z)

Returns the medium's index of refraction, n , at depth z (m). Supports passing a numpy array of depths.

static `temperature` (z)

Returns the temperature (K) of the ice at depth z (m). Supports passing a numpy array of depths.

classmethod `attenuation_length` (z, f)

Returns the attenuation length at depth z (m) and frequency f (Hz). Supports passing a numpy array of depths and/or frequencies. If both are passed as arrays, a 2-D array is returned where each row is a single depth and each column is a single frequency.

`pyrex.prem_density` (r)

Returns the earth's density (g/cm^3) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

`pyrex.slant_depth` (*angle, depth, step=5000*)

Returns the material thickness (g/cm^2) for a chord cutting through earth at Nadir angle and starting at depth (m).

class `pyrex.Particle`

Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy (GeV).

direction

energy

vertex

class `pyrex.ShadowGenerator` ($dx, dy, dz, \text{energy_generator}$)

Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into account Earth shadowing (sort of). `energy_generator` should be a function that returns a particle energy in GeV.

create_particle()

Creates a particle with random vertex in cube and random direction.

class pyrex.PathFinder (*ice_model, from_point, to_point*)

Class for ray tracking.

exists

Boolean of whether path exists.

emitted_ray

Direction in which ray is emitted.

path_length

Length of the path (m).

tof

Time of flight (s) for a particle along the path. Calculated using default values of self.time_of_flight()

time_of_flight (*n_steps=100*)

Time of flight (s) for a particle along the path.

attenuation (*f, n_steps=100*)

Returns the attenuation factor for a signal of frequency *f* (Hz) traveling along the path. Supports passing a list of frequencies.

propagate (*signal*)

Applies attenuation to the signal along the path.

class pyrex.EventKernel (*generator, ice_model, antennas*)

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

event ()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

3.2 Submodules

3.2.1 pyrex.signals module

Module containing classes for digital signal processing

class pyrex.signals.Signal (*times, values*)

Bases: object

Base class for signals. Takes arrays of times and values (values array forced to size of times array by zero padding or slicing). Supports adding between signals with the same time values, resampling the signal, and calculating the signal's envelope.

dt

Returns the spacing of the time array, or None if invalid.

envelope

Calculates envelope of the signal by Hilbert transform.

resample (*n*)

Resamples the signal into *n* points in the same time range.

spectrum

Returns the FFT spectrum of the signal.

frequencies

Returns the FFT frequencies of the signal.

filter_frequencies (*freq_response*)

Applies the given frequency response function to the signal.

class `pyrex.signals.EmptySignal` (*times*)

Bases: `pyrex.signals.Signal`

Class for signal with no amplitude (all values = 0)

class `pyrex.signals.FunctionSignal` (*times, function*)

Bases: `pyrex.signals.Signal`

Class for signals generated by a function

class `pyrex.signals.SlowAskaryanSignal` (*times, energy, theta, n=1.78, t0=0*)

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

RAC (*time*)

Calculates $R * \text{vector potential}$ at the Cherenkov angle in Vs at the given time (s).

charge_profile (*z, density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

max_length (*density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

class `pyrex.signals.FastAskaryanSignal` (*times, energy, theta, n=1.78, t0=0*)

Bases: `pyrex.signals.Signal`

Askaryan pulse binned to times from neutrino with given energy (GeV) observed at angle theta (radians). Optional parameters are the index of refraction n, and pulse offset to start time t0 (s). Returned signal values are electric fields (V/m).

Note that the amplitude of the pulse goes as 1/R, where R is the distance from source to observer. R is assumed to be 1 meter so that dividing by a different value produces the proper result.

vector_potential

Recover the vector_potential from the electric field. Mostly just for testing purposes.

RAC (*time*)

Calculates $R * \text{vector potential}$ (A) at the Cherenkov angle in Vs at the given time (s).

charge_profile (*z, density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the longitudinal charge profile in the EM shower at distance z (m) with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

max_length (*density=0.92, crit_energy=0.0786, rad_length=36.08*)

Calculates the maximum length (m) of an EM shower with parameters for the density (g/cm³), critical energy (GeV), and electron radiation length (g/cm²) in ice.

`pyrex.signals.AskaryanSignal`

alias of `FastAskaryanSignal`

```
class pyrex.signals.GaussianNoise(times, sigma)
```

Bases: `pyrex.signals.FunctionSignal`

Gaussian noise signal with standard deviation sigma

```
class pyrex.signals.ThermalNoise(times, f_band, f_amplitude=1, rms_voltage=None, temperature=None, resistance=None, n_freqs=0)
```

Bases: `pyrex.signals.Signal`

Thermal Rayleigh noise in the frequency band `f_band=[f_min,f_max]` (Hz) at a given temperature (K) and resistance (ohms) or with a given RMS voltage (V). Optional parameters are `f_amplitude` (default 1) which can be a number or a function designating the amplitudes at each frequency, and `n_freqs` which is the number of frequencies to use (in `f_band`) for the calculation (default is based on the FFT bin size of the given times array). Returned signal values are voltages (V).

3.2.2 pyrex.antenna module

Module containing antenna class capable of receiving signals

```
class pyrex.antenna.Antenna(position, freq_range=None, temperature=None, resistance=None, noisy=True)
```

Bases: `object`

Base class for an antenna with a given position (m), temperature (K), allowable frequency range (Hz), total resistance (ohm) used for Johnson noise, and whether or not to include noise in the antenna's waveforms. Defines default trigger, frequency response, and signal reception functions that can be overwritten in base classes to customize the antenna.

is_hit

Test for whether the antenna has received a signal.

clear()

Reset the antenna to a state of having received no signals.

waveforms

Signal + noise (if noisy) at each triggered antenna hit.

all_waveforms

Signal + noise (if noisy) at all antenna hits, even those that didn't trigger.

make_noise(times)

Returns the noise signal generated by the antenna over the given array of times. Used to add noise to signal for production of the antenna's waveforms.

trigger(signal)

Function to determine whether or not the antenna is triggered by the given Signal object.

response(frequencies)

Function to return the frequency response of the antenna at the given frequencies (Hz). This function should return the response as imaginary numbers, where the real part is the amplitude response and the imaginary part is the phase response.

receive(signal, polarization=[0, 0, 1])

Process incoming signal according to the filter function and store it to the signals list. Subclasses may extend this function, but should end with `super().receive(signal)`.

```
class pyrex.antenna.DipoleAntenna(name, position, center_frequency, bandwidth, resistance, effective_height, polarization=[0, 0, 1], trigger_threshold=0, noisy=True)
```

Bases: `pyrex.antenna.Antenna`

Antenna with a given name, position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), polarization direction, and trigger threshold (V).

trigger (*signal*)

Trigger on the signal if the maximum signal value is above the given threshold.

response (*frequencies*)

Butterworth filter response for the antenna's frequency range.

receive (*signal, polarization=[0, 0, 1]*)

Apply polarization effect to signal, then proceed with usual antenna reception.

3.2.3 pyrex.ice_model module

Module containing ice model. AntarcticIce class contains static and class methods for easy swapping of models. IceModel class is set to the preferred ice model.

class `pyrex.ice_model.AntarcticIce`

Bases: `object`

Class containing characteristics of ice at the south pole. In all cases, depth *z* is given with negative values in the ice and positive values above the ice.

k = 0.438

a = 0.0132

n0 = 1.32

thickness = 2850

classmethod `gradient` (*z*)

Returns the gradient of the index of refraction at depth *z* (m).

classmethod `index` (*z*)

Returns the medium's index of refraction, *n*, at depth *z* (m). Supports passing a numpy array of depths.

static `temperature` (*z*)

Returns the temperature (K) of the ice at depth *z* (m). Supports passing a numpy array of depths.

classmethod `attenuation_length` (*z, f*)

Returns the attenuation length at depth *z* (m) and frequency *f* (Hz). Supports passing a numpy array of depths and/or frequencies. If both are passed as arrays, a 2-D array is returned where each row is a single depth and each column is a single frequency.

class `pyrex.ice_model.NewcombIce`

Bases: `pyrex.ice_model.AntarcticIce`

Class inheriting from AntarcticIce, with new `attenuation_length` function based on Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE ANTARCTICICE).

classmethod `attenuation_length` (*z, f*)

Returns the attenuation length at depth *z* (m) and frequency *f* (MHz) by Matt Newcomb's fit (DOESN'T CURRENTLY WORK - USE BOGORODSKY).

`pyrex.ice_model.IceModel`

alias of `AntarcticIce`

3.2.4 pyrex.earth_model module

Module containing earth model. Uses PREM for density as a function of radius and a simple integrator for calculation of the slant depth as a function of nadir angle.

```
pyrex.earth_model.prem_density(r)
    Returns the earth's density (g/cm3) for a given radius r (m). Calculated by the Preliminary Earth Model (PREM).

pyrex.earth_model.slant_depth(angle, depth, step=5000)
    Returns the material thickness (g/cm2) for a chord cutting through earth at Nadir angle and starting at depth (m).
```

3.2.5 pyrex.particle module

Module for particles (namely neutrinos) and neutrino interactions in the ice. Interactions include Earth shadowing (absorption) effect.

```
class pyrex.particle.NeutrinoInteraction(c, p)
    Bases: object

    Class for neutrino interaction attributes.

    cross_section(E)
        Return the cross section at a given energy E (GeV).

    interaction_length(E)
        Return the interaction length at a given energy E (GeV).

class pyrex.particle.Particle
    Bases: tuple

    Named tuple for containing particle attributes. Consists of a 3-D vertex (m), 3-D direction vector, and an energy (GeV).

    direction
    energy
    vertex

pyrex.particle.random_direction()
    Generate an arbitrary 3D unit vector.

class pyrex.particle.ShadowGenerator(dx, dy, dz, energy_generator)
    Bases: object

    Class to generate UHE neutrino vertices in (relatively) shallow detectors. Takes into account Earth shadowing (sort of). energy_generator should be a function that returns a particle energy in GeV.

    create_particle()
        Creates a particle with random vertex in cube and random direction.
```

3.2.6 pyrex.ray_tracing module

Module containing class for ray tracking through the ice. Ray tracing not yet implemented.

```
class pyrex.ray_tracing.PathFinder(ice_model, from_point, to_point)
    Bases: object

    Class for ray tracking.
```

exists

Boolean of whether path exists.

emitted_ray

Direction in which ray is emitted.

path_length

Length of the path (m).

tof

Time of flight (s) for a particle along the path. Calculated using default values of `self.time_of_flight()`

time_of_flight (*n_steps=100*)

Time of flight (s) for a particle along the path.

attenuation (*f, n_steps=100*)

Returns the attenuation factor for a signal of frequency *f* (Hz) traveling along the path. Supports passing a list of frequencies.

propagate (*signal*)

Applies attenuation to the signal along the path.

3.2.7 pyrex.kernel module

Module for the simulation kernel. Includes neutrino generation, ray tracking (no raytracing yet), and hit generation.

class `pyrex.kernel.EventKernel` (*generator, ice_model, antennas*)

Bases: `object`

Kernel for generation of events with a given particle generator, ice model, and list of antennas.

event ()

Generate particle, propagate signal through ice to antennas, process signal at antennas, and return the original particle.

3.2.8 pyrex.custom module

Module containing customized classes for IREX

class `pyrex.custom.IREXBaseAntenna` (*position, center_frequency, bandwidth, resistance, effective_height, polarization=(0, 0, 1), noisy=True*)

Bases: `pyrex.antenna.Antenna`

Antenna to be used in IREXAntenna class. Has a position (m), center frequency (Hz), bandwidth (Hz), resistance (ohm), effective height (m), and polarization direction.

response (*frequencies*)

Butterworth filter response for the antenna's frequency range.

receive (*signal, polarization=[0, 0, 1]*)

Apply polarization effect to signal, then proceed with usual antenna reception.

class `pyrex.custom.IREXAntenna` (*name, position, trigger_threshold, time_over_threshold=0, polarization=(0, 0, 1), noisy=True*)

Bases: `object`

IREX antenna system consisting of dipole antenna, low-noise amplifier, optional bandpass filter, and envelope circuit.

change_antenna (*center_frequency=250000000.0, bandwidth=300000000.0, resistance=100, polarization=(0, 0, 1), noisy=True*)

Changes attributes of the antenna including center frequency (Hz), bandwidth (Hz), and resistance (ohms).

is_hit

signals

waveforms

all_waveforms

receive (*signal, polarization=[0, 0, 1]*)

clear ()

trigger (*signal*)

class pyrex.custom.**IREXDetector** (*number_of_stations, station_separation, antennas_per_string, antenna_separation, lowest_antenna, geometry='grid', strings_per_station=1, string_separation=100*)

Bases: object

Class for automatically generating antenna positions based on geometry criteria. Takes as arguments the number of stations, the distance between stations, the number of antennas per string, the separation (in z) of the antennas on the string, the position of the lowest antenna, and the name of the geometry to use. Optional parameters (depending on the geometry) are the number of strings per station and the distance from station to string. The `build_antennas` method is responsible for actually placing antennas at the generated positions, after which the class can be directly iterated to iterate over the antennas.

build_antennas (*trigger_threshold, time_over_threshold=0, naming_scheme=<function IREXDetector.<lambda>>, polarization_scheme=<function IREXDetector.<lambda>>, noisy=True*)

Sets up IREXAntennas at the positions stored in the class. Takes as arguments the trigger threshold, optional time over threshold, and whether to add noise to the waveforms. Other optional arguments include a naming scheme and polarization scheme which are functions taking the antenna index *i* and the antenna object and should return the name and polarization of the antenna, respectively.

VERSION HISTORY

4.1 Version 1.1.0

- Made units consistent across PyREx

4.2 Version 1.0.3

- Added `custom` module to contain classes and functions specific to the IREX project.

4.3 Version 1.0.2

- Allow passing of numpy arrays of depths and frequencies into most `IceModel` methods.
 - `IceModel.gradient()` must still be calculated at individual depths.
- Added ability to specify RMS voltage of `ThermalNoise` without providing temperature and resistance.
- Removed (deprecated) `Antenna.isHit()`.
- Added `Antenna.make_noise()` method so custom antennas can use their own noise functions.
- Performance improvements:
 - Allowing for `IceModel` to calculate many attenuation lengths at once improves speed of `PathFinder.propagate()`.
 - Improved speed of `PathFinder.time_of_flight()` and `PathFinder.attenuation()` (and improved accuracy to boot).

4.4 Version 1.0.1

- Fixed bugs in `AskaryanSignal` that caused the convolution to fail.
- Changed `Antenna` not require a temperature and frequency range if no noise is produced.
- Fixed bugs resulting from converting `IceModel.temperature()` from Celsius to Kelvin.

4.5 Version 1.0.0

- Created PyREx package based on original notebook.
- Added all signal classes to produce full-waveform Askaryan pulses and thermal noise.
- Changed `Antenna` class to `DipoleAntenna` to allow `Antenna` to be a base class.
- Changed `Antenna.isHit()` method to `Antenna.is_hit` property.
- Introduced `IceModel` alias for `AntarcticIce` (or any future preferred ice model).
- Moved `AntarcticIce.attenuationLengthMN` to its own `NewcombIce` class inheriting from `AntarcticIce`.
- Added `PathFinder.propagate()` to propagate a `Signal` object in a customizable way.
- Changed naming conventions to be more consistent, verbose, and “pythonic”:
 - `AntarcticIce.attenuationLength()` becomes `AntarcticIce.attenuation_length()`.
 - In `pyrex.earth_model`, `RE` becomes `EARTH_RADIUS`.
 - In `pyrex.particle`, `neutrino_interaction` becomes `NeutrinoInteraction`.
 - In `pyrex.particle`, `NA` becomes `AVOGADRO_NUMBER`.
 - `particle` class becomes `Particle` namedtuple.
 - * `Particle.vtx` becomes `Particle.vertex`.
 - * `Particle.dir` becomes `Particle.direction`.
 - * `Particle.E` becomes `Particle.energy`.
 - In `pyrex.particle`, `next_direction()` becomes `random_direction()`.
 - `shadow_generator` becomes `ShadowGenerator`.
 - `PathFinder` methods become properties where reasonable:
 - * `PathFinder.exists()` becomes `PathFinder.exists`.
 - * `PathFinder.getEmittedRay()` becomes `PathFinder.emitted_ray`.
 - * `PathFinder.getPathLength()` becomes `PathFinder.path_length`.
 - `PathFinder.propagateRay()` split into `PathFinder.time_of_flight()` (with corresponding `PathFinder.tof` property) and `PathFinder.attenuation()`.

4.6 Version 0.0.0

Original PyREx python notebook written by Kael Hanson:

<https://gist.github.com/physkael/898a64e6fbf5f0917584c6d31edf7940>

PYTHON MODULE INDEX

p

- `pyrex`, [11](#)
- `pyrex.antenna`, [16](#)
- `pyrex.custom`, [19](#)
- `pyrex.earth_model`, [18](#)
- `pyrex.ice_model`, [17](#)
- `pyrex.kernel`, [19](#)
- `pyrex.particle`, [18](#)
- `pyrex.ray_tracing`, [18](#)
- `pyrex.signals`, [14](#)

A

a (pyrex.ice_model.AntarcticIce attribute), 13, 17
 all_waveforms (pyrex.Antenna attribute), 12
 all_waveforms (pyrex.antenna.Antenna attribute), 16
 all_waveforms (pyrex.custom.IREXAntenna attribute), 20
 AntarcticIce (class in pyrex.ice_model), 13, 17
 Antenna (class in pyrex), 12
 Antenna (class in pyrex.antenna), 16
 AskaryanSignal (in module pyrex), 11
 AskaryanSignal (in module pyrex.signals), 15
 attenuation() (pyrex.PathFinder method), 14
 attenuation() (pyrex.ray_tracing.PathFinder method), 19
 attenuation_length() (pyrex.ice_model.AntarcticIce class method), 13, 17
 attenuation_length() (pyrex.ice_model.NewcombIce class method), 17

B

build_antennas() (pyrex.custom.IREXDetector method), 20

C

change_antenna() (pyrex.custom.IREXAntenna method), 19
 charge_profile() (pyrex.signals.FastAskaryanSignal method), 12, 15
 charge_profile() (pyrex.signals.SlowAskaryanSignal method), 15
 clear() (pyrex.Antenna method), 12
 clear() (pyrex.antenna.Antenna method), 16
 clear() (pyrex.custom.IREXAntenna method), 20
 create_particle() (pyrex.particle.ShadowGenerator method), 18
 create_particle() (pyrex.ShadowGenerator method), 13
 cross_section() (pyrex.particle.NeutrinoInteraction method), 18

D

DipoleAntenna (class in pyrex), 12
 DipoleAntenna (class in pyrex.antenna), 16
 direction (pyrex.Particle attribute), 13

direction (pyrex.particle.Particle attribute), 18
 dt (pyrex.Signal attribute), 11
 dt (pyrex.signals.Signal attribute), 14

E

emitted_ray (pyrex.PathFinder attribute), 14
 emitted_ray (pyrex.ray_tracing.PathFinder attribute), 19
 EmptySignal (class in pyrex), 11
 EmptySignal (class in pyrex.signals), 15
 energy (pyrex.Particle attribute), 13
 energy (pyrex.particle.Particle attribute), 18
 envelope (pyrex.Signal attribute), 11
 envelope (pyrex.signals.Signal attribute), 14
 event() (pyrex.EventKernel method), 14
 event() (pyrex.kernel.EventKernel method), 19
 EventKernel (class in pyrex), 14
 EventKernel (class in pyrex.kernel), 19
 exists (pyrex.PathFinder attribute), 14
 exists (pyrex.ray_tracing.PathFinder attribute), 18

F

FastAskaryanSignal (class in pyrex.signals), 11, 15
 filter_frequencies() (pyrex.Signal method), 11
 filter_frequencies() (pyrex.signals.Signal method), 15
 frequencies (pyrex.Signal attribute), 11
 frequencies (pyrex.signals.Signal attribute), 14
 FunctionSignal (class in pyrex), 11
 FunctionSignal (class in pyrex.signals), 15

G

GaussianNoise (class in pyrex.signals), 15
 gradient() (pyrex.ice_model.AntarcticIce class method), 13, 17

I

IceModel (in module pyrex), 13
 IceModel (in module pyrex.ice_model), 17
 index() (pyrex.ice_model.AntarcticIce class method), 13, 17
 interaction_length() (pyrex.particle.NeutrinoInteraction method), 18
 IREXAntenna (class in pyrex.custom), 19

IREXBaseAntenna (class in pyrex.custom), 19
IREXDetector (class in pyrex.custom), 20
is_hit (pyrex.Antenna attribute), 12
is_hit (pyrex.antenna.Antenna attribute), 16
is_hit (pyrex.custom.IREXAntenna attribute), 20

K

k (pyrex.ice_model.AntarcticIce attribute), 13, 17

M

make_noise() (pyrex.Antenna method), 12
make_noise() (pyrex.antenna.Antenna method), 16
max_length() (pyrex.signals.FastAskaryanSignal method), 12, 15
max_length() (pyrex.signals.SlowAskaryanSignal method), 15

N

n0 (pyrex.ice_model.AntarcticIce attribute), 13, 17
NeutrinoInteraction (class in pyrex.particle), 18
NewcombIce (class in pyrex.ice_model), 17

P

Particle (class in pyrex), 13
Particle (class in pyrex.particle), 18
path_length (pyrex.PathFinder attribute), 14
path_length (pyrex.ray_tracing.PathFinder attribute), 19
PathFinder (class in pyrex), 14
PathFinder (class in pyrex.ray_tracing), 18
prem_density() (in module pyrex), 13
prem_density() (in module pyrex.earth_model), 18
propagate() (pyrex.PathFinder method), 14
propagate() (pyrex.ray_tracing.PathFinder method), 19
pyrex (module), 11
pyrex.antenna (module), 16
pyrex.custom (module), 19
pyrex.earth_model (module), 18
pyrex.ice_model (module), 17
pyrex.kernel (module), 19
pyrex.particle (module), 18
pyrex.ray_tracing (module), 18
pyrex.signals (module), 14

R

RAC() (pyrex.signals.FastAskaryanSignal method), 12, 15
RAC() (pyrex.signals.SlowAskaryanSignal method), 15
random_direction() (in module pyrex.particle), 18
receive() (pyrex.Antenna method), 12
receive() (pyrex.antenna.Antenna method), 16
receive() (pyrex.antenna.DipoleAntenna method), 17
receive() (pyrex.custom.IREXAntenna method), 20
receive() (pyrex.custom.IREXBaseAntenna method), 19

receive() (pyrex.DipoleAntenna method), 13
resample() (pyrex.Signal method), 11
resample() (pyrex.signals.Signal method), 14
response() (pyrex.Antenna method), 12
response() (pyrex.antenna.Antenna method), 16
response() (pyrex.antenna.DipoleAntenna method), 17
response() (pyrex.custom.IREXBaseAntenna method), 19
response() (pyrex.DipoleAntenna method), 13

S

ShadowGenerator (class in pyrex), 13
ShadowGenerator (class in pyrex.particle), 18
Signal (class in pyrex), 11
Signal (class in pyrex.signals), 14
signals (pyrex.custom.IREXAntenna attribute), 20
slant_depth() (in module pyrex), 13
slant_depth() (in module pyrex.earth_model), 18
SlowAskaryanSignal (class in pyrex.signals), 15
spectrum (pyrex.Signal attribute), 11
spectrum (pyrex.signals.Signal attribute), 14

T

temperature() (pyrex.ice_model.AntarcticIce static method), 13, 17
ThermalNoise (class in pyrex), 12
ThermalNoise (class in pyrex.signals), 16
thickness (pyrex.ice_model.AntarcticIce attribute), 13, 17
time_of_flight() (pyrex.PathFinder method), 14
time_of_flight() (pyrex.ray_tracing.PathFinder method), 19
tof (pyrex.PathFinder attribute), 14
tof (pyrex.ray_tracing.PathFinder attribute), 19
trigger() (pyrex.Antenna method), 12
trigger() (pyrex.antenna.Antenna method), 16
trigger() (pyrex.antenna.DipoleAntenna method), 17
trigger() (pyrex.custom.IREXAntenna method), 20
trigger() (pyrex.DipoleAntenna method), 13

V

vector_potential (pyrex.signals.FastAskaryanSignal attribute), 11, 15
vertex (pyrex.Particle attribute), 13
vertex (pyrex.particle.Particle attribute), 18

W

waveforms (pyrex.Antenna attribute), 12
waveforms (pyrex.antenna.Antenna attribute), 16
waveforms (pyrex.custom.IREXAntenna attribute), 20