

Table 1: Results for the 40 p -median test problems using the Greedy algorithm

| Test Problem | n | p | Edges | Optimal Solution | Computational Time (seconds) | | | | Gap to Optimal (%) | | | |
|--------------|-----|-----|-------|------------------|------------------------------|-----|-----|---------|--------------------|------|-------|---------|
| | | | | | Mean | Min | Max | Std Dev | Mean | Best | Worst | Std Dev |
| 1 | 5 | 100 | 198 | 5819 | 0 | 0 | 0.1 | 0.01 | 1.2 | 1.2 | 1.2 | 0 |
| 2 | 10 | 100 | 193 | 4093 | 0 | 0 | 0 | 0.01 | 0.6 | 0.6 | 0.6 | 0 |
| 3 | 10 | 100 | 198 | 4250 | 0 | 0 | 0.1 | 0.01 | 3.5 | 3.5 | 3.5 | 0 |
| 4 | 20 | 100 | 196 | 3034 | 0 | 0 | 0.1 | 0.01 | 2 | 1.8 | 2.2 | 0.2 |
| 5 | 33 | 100 | 196 | 1355 | 0 | 0 | 0.1 | 0.01 | 2.6 | 1.7 | 4.4 | 0.69 |
| 6 | 5 | 200 | 786 | 7824 | 0 | 0 | 0.1 | 0.02 | 2.6 | 2.6 | 2.6 | 0 |
| 7 | 10 | 200 | 779 | 5631 | 0 | 0 | 0.1 | 0.02 | 0.3 | 0.3 | 0.3 | 0 |
| 8 | 20 | 200 | 792 | 4445 | 0 | 0 | 0.1 | 0.02 | 1.6 | 1.5 | 2.3 | 0.16 |
| 9 | 40 | 200 | 785 | 2734 | 0.1 | 0 | 0.1 | 0.02 | 4.9 | 4.1 | 5.2 | 0.48 |
| 10 | 67 | 200 | 786 | 1255 | 0.1 | 0.1 | 0.2 | 0.02 | 5.5 | 3.6 | 7.8 | 1.6 |
| 11 | 5 | 300 | 1772 | 7696 | 0 | 0 | 0.1 | 0.02 | 0.3 | 0.3 | 0.3 | 0 |
| 12 | 10 | 300 | 1758 | 6634 | 0.1 | 0 | 0.1 | 0.03 | 0.3 | 0.3 | 0.3 | 0 |
| 13 | 30 | 300 | 1760 | 4374 | 0.2 | 0.1 | 0.2 | 0.03 | 2.3 | 2.3 | 2.3 | 0 |
| 14 | 60 | 300 | 1771 | 2968 | 0.3 | 0.2 | 0.4 | 0.03 | 2.5 | 2.1 | 3.1 | 0.26 |
| 15 | 100 | 300 | 1754 | 1729 | 0.5 | 0.4 | 0.6 | 0.04 | 6.2 | 4.5 | 7.9 | 0.83 |
| 16 | 5 | 400 | 3153 | 8162 | 0.1 | 0 | 0.1 | 0.03 | 0.9 | 0.9 | 0.9 | 0 |
| 17 | 10 | 400 | 3142 | 6999 | 0.1 | 0.1 | 0.2 | 0.04 | 0.3 | 0.3 | 0.3 | 0 |
| 18 | 40 | 400 | 3134 | 4809 | 0.4 | 0.3 | 0.6 | 0.07 | 1.4 | 1.3 | 1.5 | 0.07 |
| 19 | 80 | 400 | 3134 | 2845 | 0.8 | 0.6 | 0.9 | 0.06 | 3.9 | 3.6 | 4.3 | 0.19 |
| 20 | 133 | 400 | 3144 | 1789 | 1.4 | 1.3 | 1.6 | 0.07 | 7.6 | 5.8 | 8.9 | 0.69 |
| 21 | 5 | 500 | 4909 | 9138 | 0.1 | 0 | 0.2 | 0.04 | 0 | 0 | 0 | 0 |
| 22 | 10 | 500 | 4896 | 8579 | 0.2 | 0.1 | 0.2 | 0.04 | 1.1 | 1.1 | 1.1 | 0 |
| 23 | 50 | 500 | 4903 | 4619 | 0.7 | 0.5 | 0.8 | 0.05 | 1.6 | 1.5 | 1.8 | 0.11 |
| 24 | 100 | 500 | 4914 | 2961 | 1.9 | 1.4 | 2.5 | 0.36 | 2.2 | 1.8 | 2.5 | 0.16 |
| 25 | 167 | 500 | 4894 | 1828 | 2.8 | 2.6 | 3.2 | 0.12 | 7.9 | 6.6 | 9.6 | 0.65 |
| 26 | 5 | 600 | 7069 | 9917 | 0.1 | 0.1 | 0.2 | 0.03 | 1.8 | 1.8 | 1.8 | 0 |
| 27 | 10 | 600 | 7072 | 8307 | 0.2 | 0.2 | 0.3 | 0.04 | 0.8 | 0.8 | 0.8 | 0 |
| 28 | 60 | 600 | 7054 | 4498 | 1.5 | 1.2 | 1.7 | 0.1 | 1.8 | 1.7 | 2.2 | 0.12 |
| 29 | 120 | 600 | 7042 | 3033 | 3 | 2.7 | 3.5 | 0.17 | 3.5 | 2.5 | 4.5 | 0.53 |
| 30 | 200 | 600 | 7042 | 1989 | 5.2 | 4.9 | 5.8 | 0.22 | 9.1 | 7.1 | 10.1 | 0.55 |
| 31 | 5 | 700 | 9601 | 10086 | 0.1 | 0.1 | 0.2 | 0.03 | 0 | 0 | 0 | 0 |
| 32 | 10 | 700 | 9584 | 9297 | 0.2 | 0.1 | 0.3 | 0.04 | 0.4 | 0.4 | 0.4 | 0 |
| 33 | 70 | 700 | 9616 | 4700 | 1.8 | 1.6 | 2 | 0.1 | 2.1 | 2 | 2.3 | 0.11 |
| 34 | 140 | 700 | 9585 | 3013 | 3.7 | 3.5 | 4.1 | 0.13 | 2.9 | 2 | 3.8 | 0.56 |
| 35 | 5 | 800 | 12548 | 10400 | 0.2 | 0.1 | 0.4 | 0.06 | 0.1 | 0.1 | 0.1 | 0 |
| 36 | 10 | 800 | 12560 | 9934 | 0.6 | 0.5 | 0.7 | 0.03 | 0.2 | 0.2 | 0.2 | 0 |
| 37 | 80 | 800 | 12564 | 5057 | 2.8 | 2.4 | 3.9 | 0.25 | 1.5 | 1.2 | 1.9 | 0.2 |
| 38 | 5 | 900 | 15898 | 11060 | 0.3 | 0.3 | 0.4 | 0.02 | 0.8 | 0.8 | 0.8 | 0 |
| 39 | 10 | 900 | 15896 | 9423 | 0.6 | 0.5 | 0.7 | 0.04 | 0.3 | 0.3 | 0.3 | 0 |
| 40 | 90 | 900 | 15879 | 5128 | 3.6 | 3.2 | 4.1 | 0.22 | 1.8 | 1.3 | 2 | 0.18 |

Table 2: Results for the 40 p -median test problems using the Fast Greedy algorithm

| Test Problem | n | p | Edges | Optimal Solution | Computational Time (seconds) | | | | Gap to Optimal (%) | | | |
|--------------|-----|-----|-------|------------------|------------------------------|-----|-----|---------|--------------------|-------|-------|---------|
| | | | | | Mean | Min | Max | Std Dev | Mean | Best | Worst | Std Dev |
| 1 | 5 | 100 | 198 | 5819 | 0 | 0 | 0.1 | 0.01 | 20.3 | 20.3 | 20.3 | 0 |
| 2 | 10 | 100 | 193 | 4093 | 0 | 0 | 0.1 | 0.01 | 66.3 | 66.3 | 66.3 | 0 |
| 3 | 10 | 100 | 198 | 4250 | 0 | 0 | 0.1 | 0.01 | 64.9 | 64.9 | 64.9 | 0 |
| 4 | 20 | 100 | 196 | 3034 | 0.1 | 0.1 | 0.1 | 0.01 | 178.3 | 178.3 | 178.3 | 0 |
| 5 | 33 | 100 | 196 | 1355 | 0.1 | 0.1 | 0.1 | 0.01 | 376.4 | 376.4 | 376.4 | 0 |
| 6 | 5 | 200 | 786 | 7824 | 0 | 0 | 0.1 | 0.01 | 10.1 | 10.1 | 10.1 | 0 |
| 7 | 10 | 200 | 779 | 5631 | 0 | 0 | 0.1 | 0.01 | 41.8 | 41.8 | 41.8 | 0 |
| 8 | 20 | 200 | 792 | 4445 | 0.1 | 0.1 | 0.1 | 0.01 | 108.4 | 108.4 | 108.4 | 0 |
| 9 | 40 | 200 | 785 | 2734 | 0.1 | 0.1 | 0.2 | 0.01 | 221.2 | 221.2 | 221.2 | 0 |
| 10 | 67 | 200 | 786 | 1255 | 0.2 | 0.2 | 0.3 | 0.02 | 457.9 | 457.9 | 457.9 | 0 |
| 11 | 5 | 300 | 1772 | 7696 | 0 | 0 | 0.1 | 0.01 | 11.1 | 11.1 | 11.1 | 0 |
| 12 | 10 | 300 | 1758 | 6634 | 0.1 | 0 | 0.1 | 0.02 | 36.2 | 36.2 | 36.2 | 0 |
| 13 | 30 | 300 | 1760 | 4374 | 0.1 | 0.1 | 0.2 | 0.02 | 110.1 | 110.1 | 110.1 | 0 |
| 14 | 60 | 300 | 1771 | 2968 | 0.2 | 0.2 | 0.3 | 0.02 | 262.5 | 262.5 | 262.5 | 0 |
| 15 | 100 | 300 | 1754 | 1729 | 0.4 | 0.3 | 0.5 | 0.03 | 417.7 | 417.4 | 418.2 | 0.4 |
| 16 | 5 | 400 | 3153 | 8162 | 0.1 | 0 | 0.1 | 0.03 | 6.8 | 6.8 | 6.8 | 0 |
| 17 | 10 | 400 | 3142 | 6999 | 0.1 | 0 | 0.1 | 0.03 | 37.1 | 37.1 | 37.1 | 0 |
| 18 | 40 | 400 | 3134 | 4809 | 0.2 | 0.1 | 0.2 | 0.03 | 122.7 | 122.7 | 122.7 | 0 |
| 19 | 80 | 400 | 3134 | 2845 | 0.3 | 0.3 | 0.4 | 0.03 | 262.5 | 262.5 | 262.5 | 0 |
| 20 | 133 | 400 | 3144 | 1789 | 0.5 | 0.5 | 0.7 | 0.05 | 547 | 547 | 547 | 0 |
| 21 | 5 | 500 | 4909 | 9138 | 0.1 | 0 | 0.2 | 0.04 | 7.6 | 7.6 | 7.6 | 0 |
| 22 | 10 | 500 | 4896 | 8579 | 0.1 | 0.1 | 0.2 | 0.02 | 24.9 | 24.8 | 24.9 | 0.06 |
| 23 | 50 | 500 | 4903 | 4619 | 0.3 | 0.2 | 0.3 | 0.03 | 142.3 | 142.3 | 142.3 | 0 |
| 24 | 100 | 500 | 4914 | 2961 | 0.5 | 0.4 | 0.8 | 0.08 | 286.1 | 285.9 | 286.3 | 0.2 |
| 25 | 167 | 500 | 4894 | 1828 | 0.6 | 0.6 | 0.8 | 0.04 | 499 | 499 | 499 | 0 |
| 26 | 5 | 600 | 7069 | 9917 | 0.1 | 0.1 | 0.2 | 0.04 | 5.4 | 5.4 | 5.4 | 0 |
| 27 | 10 | 600 | 7072 | 8307 | 0.1 | 0.1 | 0.2 | 0.02 | 24.1 | 24.1 | 24.1 | 0 |
| 28 | 60 | 600 | 7054 | 4498 | 0.3 | 0.3 | 0.4 | 0.04 | 132.7 | 132.2 | 133.3 | 0.55 |
| 29 | 120 | 600 | 7042 | 3033 | 0.5 | 0.5 | 0.6 | 0.04 | 279.7 | 279.7 | 279.7 | 0 |
| 30 | 200 | 600 | 7042 | 1989 | 0.8 | 0.7 | 0.9 | 0.04 | 542.6 | 542.6 | 542.6 | 0 |
| 31 | 5 | 700 | 9601 | 10086 | 0.2 | 0.1 | 0.2 | 0.03 | 7.4 | 7.4 | 7.4 | 0 |
| 32 | 10 | 700 | 9584 | 9297 | 0.2 | 0.1 | 0.2 | 0.03 | 28.5 | 28.5 | 28.5 | 0 |
| 33 | 70 | 700 | 9616 | 4700 | 0.4 | 0.3 | 0.5 | 0.04 | 167.8 | 167.8 | 167.8 | 0 |
| 34 | 140 | 700 | 9585 | 3013 | 0.6 | 0.6 | 0.9 | 0.05 | 302.9 | 302.9 | 302.9 | 0 |
| 35 | 5 | 800 | 12548 | 10400 | 0.2 | 0.1 | 0.3 | 0.04 | 4.3 | 4.3 | 4.3 | 0 |
| 36 | 10 | 800 | 12560 | 9934 | 0.2 | 0.2 | 0.3 | 0.04 | 26.4 | 26.4 | 26.4 | 0 |
| 37 | 80 | 800 | 12564 | 5057 | 0.5 | 0.4 | 0.5 | 0.03 | 172.2 | 172.2 | 172.2 | 0.02 |
| 38 | 5 | 900 | 15898 | 11060 | 0.2 | 0.2 | 0.3 | 0.03 | 5.9 | 5.9 | 5.9 | 0 |
| 39 | 10 | 900 | 15896 | 9423 | 0.2 | 0.2 | 0.3 | 0.03 | 23.3 | 23.3 | 23.3 | 0 |
| 40 | 90 | 900 | 15879 | 5128 | 0.6 | 0.5 | 0.7 | 0.04 | 167.6 | 167.6 | 167.6 | 0 |

Table 3: Results for the 40 p -median test problems using the Stingy algorithm

| Test Problem | n | p | Edges | Optimal Solution | Computational Time (seconds) | | | | Gap to Optimal (%) | | | |
|--------------|-----|-----|-------|------------------|------------------------------|-------|-------|---------|--------------------|-------|-------|---------|
| | | | | | Mean | Min | Max | Std Dev | Mean | Best | Worst | Std Dev |
| 1 | 5 | 100 | 198 | 5819 | 3.3 | 3.2 | 4.2 | 0.16 | 116.1 | 116.1 | 116.1 | 0 |
| 2 | 10 | 100 | 193 | 4093 | 3.3 | 3.2 | 3.6 | 0.11 | 131.9 | 126.3 | 138.1 | 3.4 |
| 3 | 10 | 100 | 198 | 4250 | 3.3 | 3.2 | 3.6 | 0.11 | 130.6 | 130.4 | 131 | 0.29 |
| 4 | 20 | 100 | 196 | 3034 | 3.1 | 3 | 3.7 | 0.12 | 108.5 | 106.7 | 110.2 | 1.78 |
| 5 | 33 | 100 | 196 | 1355 | 2.9 | 2.8 | 3.4 | 0.15 | 145 | 138.5 | 155.6 | 8.07 |
| 6 | 5 | 200 | 786 | 7824 | 28.2 | 27.8 | 30.2 | 0.47 | 99.2 | 99.2 | 99.2 | 0 |
| 7 | 10 | 200 | 779 | 5631 | 28.1 | 27.6 | 28.7 | 0.36 | 125.3 | 124.5 | 126.1 | 0.81 |
| 8 | 20 | 200 | 792 | 4445 | 27.8 | 27.4 | 28.4 | 0.34 | 131.3 | 128.7 | 133 | 2.1 |
| 9 | 40 | 200 | 785 | 2734 | 26.9 | 26.5 | 27.5 | 0.37 | 135.3 | 132.2 | 137.1 | 2.34 |
| 10 | 67 | 200 | 786 | 1255 | 25 | 24.4 | 28.5 | 0.77 | 173.2 | 173.2 | 173.2 | 0 |
| 11 | 5 | 300 | 1772 | 7696 | 131.8 | 131.5 | 132.3 | 0.38 | 154.2 | 148.2 | 172.4 | 12.12 |
| 12 | 10 | 300 | 1758 | 6634 | 131.4 | 131.1 | 131.6 | 0.23 | 163 | 163 | 163 | 0 |
| 13 | 30 | 300 | 1760 | 4374 | 130.1 | 129.7 | 130.7 | 0.44 | 149.6 | 149.6 | 149.6 | 0 |
| 14 | 60 | 300 | 1771 | 2968 | 125.5 | 125.2 | 125.9 | 0.26 | 138.7 | 137 | 140.6 | 1.97 |
| 15 | 100 | 300 | 1754 | 1729 | 116.4 | 115.8 | 117.4 | 0.38 | 125.8 | 123.7 | 127.3 | 1.03 |
| 16 | 5 | 400 | 3153 | 8162 | 406.3 | 406.1 | 406.5 | 0.17 | 149.7 | 149.7 | 149.7 | 0 |
| 17 | 10 | 400 | 3142 | 6999 | 406.8 | 405.4 | 408.1 | 1.41 | 136.8 | 135.4 | 141 | 2.79 |
| 18 | 40 | 400 | 3134 | 4809 | 402.4 | 400.1 | 408.2 | 3.86 | 135.7 | 134.2 | 136.9 | 1.26 |
| 19 | 80 | 400 | 3134 | 2845 | 389.6 | 388.9 | 390.5 | 0.69 | 124.3 | 124 | 124.7 | 0.33 |
| 20 | 133 | 400 | 3144 | 1789 | 359 | 358.8 | 359.2 | 0.19 | 128.2 | 128.2 | 128.2 | 0 |