Q1 * Intuitively WTW = I would minimize the low here

(a) For min \frac{1}{2} || W T W x - x || 2 W G IR Man men

Let WWx = 7

min $\frac{1}{2} || \tilde{x} - x ||^2$ would be achieved when $\tilde{x} - x = 0$

W is a Wide Matrix. Water Feature dimension V Encoding

We want & to be as close as to x after the Encode - pecode proces

: Information (important features from x) sets preserved

(b) $\begin{array}{c}
|R| \\
|R| \\$

(C) VWL = VWL/PATHS + VWL/PATH2

 - TWL= WX (WTWX-X) - W(WTWX-X)XT

|RMXN |RNX| |R|XN |R|XN |R|XN |R|XN

LHS: IR MXM

RHU: IR MXM

dim Matched

(a)
$$IR^{m\times m}$$
 $IR^{m\times m}$ $IR^{m\times m}$

(b)
$$\frac{\partial \mathcal{L}_{1}}{\partial K} = \frac{\partial H}{\partial K} \frac{\partial \mathcal{L}_{1}}{\partial H}$$

$$= \frac{\partial \log (\det (KI))}{\partial K} \cdot (-\frac{N_{2}}{2})$$

$$= (K^{T})^{-1} \cdot (-\frac{N_{2}}{2}) = -\frac{D}{2} (K^{T})^{-1}$$

Cookbook #57

$$\frac{\partial \mathcal{L}_{i}}{\partial X^{T}} = \mathcal{N}^{T} \frac{\partial \mathcal{L}_{i}}{\partial \mathcal{M}}$$

$$= \mathcal{N}^{T} \cdot -\frac{\mathcal{D}}{2} \cdot (k^{T})^{-1}$$

$$= -\frac{\mathcal{D}}{2} \cdot (d \cdot X)^{T} \cdot (k^{T})^{-1}$$

$$= -\frac{d\mathcal{D}}{2} \cdot X^{T} \cdot (k^{T})^{-1}$$

$$= R^{nxm} \cdot R^{mxm}$$

*
$$\frac{\partial \mathcal{L}_{1}}{\partial x} | part = \left(-\frac{dp}{2} x^{T} (K^{T})^{-1} \right)^{T}$$

= $-\frac{dp}{2} K^{-1} X$

$$\frac{\partial \mathcal{L}_{1}}{\partial \mathcal{N}} = \frac{\partial \mathcal{L}_{1}}{\partial \mathcal{M}} \cdot (\chi^{\mathsf{T}})^{\mathsf{T}}$$
$$= -\frac{p}{2} (k^{\mathsf{T}})^{-1} \chi$$

*
$$\frac{\partial \mathcal{L}}{\partial x} | PATH_2 = \mathcal{L} \cdot \frac{\partial \mathcal{L}_1}{\partial N}$$

= $-\frac{\partial \mathcal{D}}{2} (K^T)^T x$

$$\frac{\partial \mathcal{L}_{1}}{\partial X} = \frac{\partial \mathcal{L}_{1}}{\partial X} \Big|_{MATH 1} + \frac{\partial \mathcal{L}_{1}}{\partial X} \Big|_{MATH 2}$$

$$= -\frac{\partial \mathcal{D}}{\partial X} \left(X^{T} \left(K^{T} \right)^{-1} + \left(K^{T} \right)^{-1} X \right)$$

$$\frac{\partial \mathcal{L}_{1}}{\partial P} = \frac{\partial \mathcal{L}_{2}}{\partial R} \cdot Q^{T}$$

$$= -\frac{1}{2} \cdot \underbrace{1 \cdot Q^{T}}_{Q^{T}} \cdot Q^{T}$$

$$= -\frac{1}{2} \cdot (\Upsilon \Upsilon^{T})^{T}$$

$$\frac{\partial d_{1}}{\partial k} = -k^{-T} \frac{\partial L_{2}}{\partial k^{-1}} k^{-T}$$

$$= -k^{-T} \frac{\partial d_{2}}{\partial \rho} k^{-T}$$

$$= -k^{-T} \cdot (+\frac{1}{2}\gamma\gamma^{T}) \cdot k^{-T}$$

$$+ k^{-T} \cdot (+\frac{1}{2}\gamma\gamma^{T}) \cdot k^{-T}$$

$$\frac{\partial L_2}{\partial M} = \frac{\partial J_2}{\partial K}$$

$$\frac{\partial L_2}{\partial M} = \frac{\partial J_2}{\partial K}$$

$$= \frac{\partial L_2}{\partial K}$$

$$= \frac{\partial L_2}{\partial K}$$

$$\frac{3L_{2}}{3X} | p_{0}\tilde{l}H_{2} = \frac{2}{2} (x^{T} k^{-T} \gamma \gamma^{T} k^{-T})^{T}$$

$$= \frac{2}{2} (k^{-1} \gamma \gamma^{T} k^{-1} \chi)$$

$$\frac{3L_{2}}{3X} | p_{0}\tilde{l}H_{1} = \frac{3L_{2}}{3N} (x^{T})^{T}$$

$$= 2 (k^{-T} \cdot (\frac{1}{2} \gamma \gamma^{T}) \cdot k^{-T} \cdot \chi)$$

$$= \frac{2}{2} k^{-T} \gamma \gamma^{T} k^{-T} \chi$$

$$\frac{\partial L_2}{\partial X} = \frac{\partial L_2}{\partial x} \Big| p_{37H1} + \frac{\partial L_1}{\partial x} \Big| p_{37H2}$$

$$= \frac{d}{2} \left(K^{-1} \Upsilon \Upsilon^{T} K^{-1} X + K^{-7} \Upsilon \Upsilon^{T} K^{-7} X \right)$$

(6)
$$\frac{3X}{3\xi} = \frac{3\xi_1}{3\xi_1} + \frac{3\xi_2}{3\xi_2}$$

(c)
$$\frac{\partial \mathcal{L}}{\partial z_{2}} = \frac{\partial \mathcal{L}}{\partial b_{2}} = \frac{\partial \mathcal{L}}{\partial z_{2}'}$$
 (Pau Grad)

($\mathcal{L}(\mathcal{L})$

$$\frac{\partial \mathcal{L}}{\partial h_{1}} = \frac{\partial \mathcal{L}_{2}'}{\partial h_{1}} \frac{\partial \mathcal{L}}{\partial \partial \mathcal{L}_{2}'}$$

$$= W_{2}^{T} \frac{\partial \mathcal{L}}{\partial b_{2}}$$

$$= W_{2}^{T} \frac{\partial \mathcal{L}}{\partial b_{2}} \in \mathbb{R}^{H \times C \times C} = \mathbb{R}^{H}$$

$$(W_{2} h_{1} = \mathcal{L}_{2}')$$

(3)
$$h_1 = \text{Swish}(z_1)$$

$$h_{1,i} = \overline{z}_{l,i} \delta(\overline{z}_{l,i})$$

$$\begin{bmatrix} \overline{z}_{l,i} \\ \overline{z}_{l,i} \\ \overline{z}_{l,H} \end{bmatrix} \rightarrow \underbrace{\begin{bmatrix} h_{l,i} \\ h_{l,i} \\ h_{l,H} \end{bmatrix}}$$

$$\frac{\partial h_{i,i}}{\partial z_{i,i}} = \frac{\partial (z_{i,i})}{\partial z_{i,i}} + \frac{\partial \partial (z_{i,i})}{\partial z_{i,i}}$$

$$= \frac{\partial (z_{i,i})}{\partial z_{i,i}} + \frac{\partial \partial (z_{i,i})}{\partial z_{i,i}} \left(1 - \partial (z_{i,i})\right)$$
Thus, we should define the state of the stat

$$\frac{\partial h_{i}}{\partial z_{i}} \in \mathbb{R}^{H \times H} ; \left[\frac{\partial h_{i}}{\partial z_{i}} \right]_{i,j} = \frac{\partial h_{i,i}}{\partial z_{i,j}} = \begin{cases} \partial(z_{i}, i) \in \mathcal{Z}_{i,i} \cup (1-\delta(z_{i,i})) \\ 0 \end{cases}$$

(("")

$$\frac{\partial \mathcal{L}}{\partial z_{1}} = \frac{\partial h_{1}}{\partial z_{1}} \frac{\partial \mathcal{L}}{\partial h_{1}}$$

$$= \operatorname{diag} \left(\underbrace{\delta(z_{1}, i)} + \underbrace{Z_{1}, i \delta(z_{1}, i)} \left(\underbrace{1 - \delta(z_{1}, i)} \right) \cdot \underbrace{W_{2} T} \frac{\partial \mathcal{L}}{\partial h_{2}} \right)$$

$$= \left(\underbrace{\delta(z_{1})} + \underbrace{h_{1}} \underbrace{O(1 - \delta(z_{1}))} \underbrace{OW_{2} T} \frac{\partial \mathcal{L}}{\partial h_{2}} \right)$$

$$\uparrow_{|R|} \downarrow_{|R|} \downarrow_{|R|}$$

$$\frac{\partial \mathcal{L}}{\partial \mathcal{L}} = \frac{\partial \mathcal{L}}{\partial \mathcal{L}}$$

$$\frac{\partial \mathcal{L}}{\partial X} = W_1^T \frac{\partial \mathcal{L}}{\partial z_1'}$$

$$\uparrow \qquad \qquad \uparrow \qquad \qquad \downarrow \\ |R^P| \qquad \downarrow \\ |R^{WK-1}| \qquad \qquad \downarrow \\ |R^{WK-1}| \qquad \qquad \downarrow \\ |R^H| \qquad \qquad \downarrow \\ |R^$$

$$\frac{\partial \mathcal{L}}{\partial W_{1}} = \frac{\partial \mathcal{L}}{\partial \mathcal{Z}_{1}} X^{T}$$

$$\uparrow \qquad \uparrow$$

$$\downarrow R^{HND} = \left(\delta(\mathcal{Z}_{1}) + h, O(1 - \delta(\mathcal{Z}_{1})) O W_{2}^{T} \frac{\partial \mathcal{L}}{\partial b_{2}} X^{T}\right)$$

$$\downarrow \qquad \uparrow$$

$$\downarrow R^{HNI} \qquad \qquad \downarrow R^{HNI}$$

NEURAL_NET.PY

```
import numpy as np
import matplotlib.pyplot as plt
class TwoLayerNet(object):
  11 11 11
  A two-layer fully-connected neural network. The net has an input dimension of
  {\it D}, a hidden layer dimension of {\it H}, and performs classification over {\it C} classes.
  We train the network with a softmax loss function and L2 regularization on the
  weight matrices. The network uses a ReLU nonlinearity after the first fully
  connected layer.
  In other words, the network has the following architecture:
  input - fully connected layer - ReLU - fully connected layer - softmax
  The outputs of the second fully-connected layer are the scores for each class.
  def __init__(self, input_size, hidden_size, output_size, std=1e-4):
    Initialize the model. Weights are initialized to small random values and
    biases are initialized to zero. Weights and biases are stored in the
    variable self.params, which is a dictionary with the following keys:
    W1: First layer weights; has shape (H, D)
    b1: First layer biases; has shape (H,)
    W2: Second layer weights; has shape (C, H)
    b2: Second layer biases; has shape (C,)
    Inputs:
    - input_size: The dimension D of the input data.
    - hidden_size: The number of neurons H in the hidden layer.
    - output_size: The number of classes C.
    self.params = {}
    self.params['W1'] = std * np.random.randn(hidden_size, input_size)
   self.params['b1'] = np.zeros(hidden_size)
    self.params['W2'] = std * np.random.randn(output_size, hidden_size)
    self.params['b2'] = np.zeros(output_size)
  def loss(self, X, y=None, reg=0.0):
    Compute the loss and gradients for a two layer fully connected neural
```

network.

```
Inputs:
- X: Input data of shape (N, D). Each X[i] is a training sample.
- y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
 an integer in the range 0 \le y[i] \le C. This parameter is optional; if it
 is not passed then we only return scores, and if it is passed then we
 instead return the loss and gradients.
- reg: Regularization strength.
Returns:
If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
the score for class c on input X[i].
If y is not None, instead return a tuple of:
- loss: Loss (data loss and regularization loss) for this batch of training
 samples.
- grads: Dictionary mapping parameter names to gradients of those parameters
 with respect to the loss function; has the same keys as self.params.
# Unpack variables from the params dictionary
# Compute the forward pass
scores = None
# ------ #
# YOUR CODE HERE:
# Calculate the output scores of the neural network. The result
  should be (N, C). As stated in the description for this class,
# there should not be a ReLU layer after the second FC layer.
# The output of the second FC layer is the output scores. Do not
# use a for loop in your implementation.
# ------ #
W1, b1 = self.params['W1'], self.params['b1']
W2, b2 = self.params['W2'], self.params['b2']
layer1 = np.matmul(W1, X.T).T+b1
ReLU_act = np.where(layer1.T>0, layer1.T, 0)
scores = np.matmul(W2, ReLU_act).T+b2
# ----- #
# END YOUR CODE HERE
# ------ #
# If the targets are not given then jump out, we're done
```

```
if y is None:
 return scores
# Compute the loss
loss = None
# ----- #
# YOUR CODE HERE:
# Calculate the loss of the neural network. This includes the
# softmax loss and the L2 regularization for W1 and W2. Store the
# total loss in the variable loss. Multiply the regularization
# loss by 0.5 (in addition to the factor reg).
# ------ #
# scores is num_examples by num_classes
batch_size = X.shape[0]
true_index = np.vstack([np.arange(X.shape[0]), y]).T # index map (N,2)
row_indices, col_indices = true_index[:, 0], true_index[:, 1]
true_scores = scores[row_indices, col_indices] # y_i's for imgs (N,1)
all_score = np.log(np.sum(np.exp(scores), axis=1))-true_scores
# softmax loss and the L2 regularization (F-norm) for W1 and W2.
loss = np.sum(all_score, axis=0)/batch_size + \
     0.5*reg*(np.linalg.norm(W1)**2 + np.linalg.norm(W2)**2)
# ------ #
# END YOUR CODE HERE
grads = {}
# ----- #
# YOUR CODE HERE:
  Implement the backward pass. Compute the derivatives of the
# weights and the biases. Store the results in the grads
  dictionary. e.g., grads['W1'] should store the gradient for
# W1, and be of the same size as W1.
# ----- #
# Use a indicator(mask) matrix (N, C); X (N, D)
# each row marks correct class as 1 and remaining entries 0
# use this to vectorize the extra term -X[i] if j==y[i]
num_class = b2.shape[0]
grad_softmax = np.zeros([batch_size, num_class])
```

```
for i in range(batch_size):
   for j in range(num_class):
     if j==y[i]:
       grad_softmax[i,j] += np.exp(scores[i, y[i]])/np.sum(np.exp(scores[i]))-1
       grad_softmax[i,j] += np.exp(scores[i, j])/np.sum(np.exp(scores[i]))
 grad_softmax = grad_softmax/batch_size
 grad_W1_reg = 0.5*reg*2*W1
 grad_W2_reg = 0.5*reg*2*W2
 grad_b2 = np.sum(grad_softmax, axis=0)
 grad_W2_loss = np.matmul(grad_softmax.T, ReLU_act.T)
 grad_ReLU = np.matmul(W2.T, grad_softmax.T)
 grad_layer1_T = np.multiply(np.where(layer1.T>0, 1, 0), grad_ReLU)
 grad_b1 = grad_layer1_T.T
 grad_W1_loss = np.matmul(grad_b1.T, X)
 grad_b1 = np.sum(grad_b1, axis=0)
 grad_W1 = grad_W1_loss + grad_W1_reg
 grad_W2 = grad_W2_loss + grad_W2_reg
 grads['W1'] = grad_W1
 grads['W2'] = grad_W2
 grads['b1'] = grad_b1
 grads['b2'] = grad_b2
  # ----- #
  # END YOUR CODE HERE
 return loss, grads
def train(self, X, y, X_val, y_val,
         learning_rate=1e-3, learning_rate_decay=0.95,
         reg=1e-5, num_iters=100,
         batch_size=200, verbose=False):
  Train this neural network using stochastic gradient descent.
  Inputs:
  - X: A numpy array of shape (N, D) giving training data.
```

```
- y: A numpy array f shape (N,) giving training labels; y[i] = c means that
 X[i] has label c, where 0 <= c < C.
- X_val: A numpy array of shape (N_val, D) giving validation data.
- y_val: A numpy array of shape (N_val,) giving validation labels.
- learning_rate: Scalar giving learning rate for optimization.
- learning_rate_decay: Scalar giving factor used to decay the learning rate
 after each epoch.
- req: Scalar giving regularization strength.
- num_iters: Number of steps to take when optimizing.
- batch_size: Number of training examples to use per step.
- verbose: boolean; if true print progress during optimization.
num_train = X.shape[0]
iterations_per_epoch = max(num_train / batch_size, 1)
# Use SGD to optimize the parameters in self.model
loss_history = []
train_acc_history = []
val_acc_history = []
for it in np.arange(num_iters):
 X_batch = None
 y_batch = None
 # ============ #
 # YOUR CODE HERE:
 # Create a minibatch by sampling batch_size samples randomly.
 # =========== #
 sel_n = np.random.choice(np.arange(num_train), batch_size, replace=True)
 X_batch = X[sel_n]
 y_batch = y[sel_n]
 # ----- #
 # END YOUR CODE HERE
 # Compute loss and gradients using the current minibatch
 loss, grads = self.loss(X_batch, y=y_batch, reg=reg)
 loss_history.append(loss)
 # YOUR CODE HERE:
 # Perform a gradient descent step using the minibatch to update
 # all parameters (i.e., W1, W2, b1, and b2).
 # ============== #
```

```
self.params['W1'] = self.params['W1'] - learning_rate*grads['W1']
   self.params['W2'] = self.params['W2'] - learning_rate*grads['W2']
   self.params['b1'] = self.params['b1'] - learning_rate*grads['b1']
   self.params['b2'] = self.params['b2'] - learning_rate*grads['b2']
   # END YOUR CODE HERE
   if verbose and it % 100 == 0:
     print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
   # Every epoch, check train and val accuracy and decay learning rate.
   if it % iterations_per_epoch == 0:
     # Check accuracy
     train_acc = (self.predict(X_batch) == y_batch).mean()
     val_acc = (self.predict(X_val) == y_val).mean()
     train_acc_history.append(train_acc)
     val_acc_history.append(val_acc)
     # Decay learning rate
     learning_rate *= learning_rate_decay
 return {
   'loss_history': loss_history,
   'train_acc_history': train_acc_history,
   'val_acc_history': val_acc_history,
def predict(self, X):
 Use the trained weights of this two-layer network to predict labels for
  data points. For each data point we predict scores for each of the C
 classes, and assign each data point to the class with the highest score.
 Inputs:
  - X: A numpy array of shape (N, D) giving N D-dimensional data points to
   classify.
 Returns:
  - y_pred: A numpy array of shape (N,) giving predicted labels for each of
   the elements of X. For all i, y_pred[i] = c means that X[i] is predicted
   to have class c, where 0 \le c \le C.
 y_pred = None
```

return y_pred

two_layer_nn

February 9, 2024

0.1 This is the 2-layer neural network notebook for ECE C147/C247 Homework #3

Please follow the notebook linearly to implement a two layer neural network.

Please print out the notebook entirely when completed.

The goal of this notebook is to give you experience with training a two layer neural network.

```
[10]: import random
  import numpy as np
  from utils.data_utils import load_CIFAR10
  import matplotlib.pyplot as plt

%matplotlib inline
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

0.2 Toy example

Before loading CIFAR-10, there will be a toy example to test your implementation of the forward and backward pass. Make sure to read the description of TwoLayerNet class in neural_net.py file , understand the architecture and initializations

```
[11]: from nndl.neural_net import TwoLayerNet

[12]: # Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.

input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5
```

```
def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

net = init_toy_model()
X, y = init_toy_data()
```

0.2.1 Compute forward pass scores

```
[13]: ## Implement the forward pass of the neural network.
      ## See the loss() method in TwoLayerNet class for the same
      # Note, there is a statement if y is None: return scores, which is why
      # the following call will calculate the scores.
      scores = net.loss(X)
      print('Your scores:')
      print(scores)
      print()
      print('correct scores:')
      correct_scores = np.asarray([
          [-1.07260209, 0.05083871, -0.87253915],
          [-2.02778743, -0.10832494, -1.52641362],
          [-0.74225908, 0.15259725, -0.39578548],
          [-0.38172726, 0.10835902, -0.17328274],
          [-0.64417314, -0.18886813, -0.41106892]])
      print(correct_scores)
      print()
      # The difference should be very small. We get < 1e-7
      print('Difference between your scores and correct scores:')
      print(np.sum(np.abs(scores - correct_scores)))
     Your scores:
     [[-1.07260209 0.05083871 -0.87253915]
      [-2.02778743 -0.10832494 -1.52641362]
      [-0.74225908  0.15259725  -0.39578548]
      [-0.38172726 0.10835902 -0.17328274]
      [-0.64417314 -0.18886813 -0.41106892]]
     correct scores:
     [[-1.07260209 0.05083871 -0.87253915]
```

```
[-2.02778743 -0.10832494 -1.52641362]

[-0.74225908  0.15259725 -0.39578548]

[-0.38172726  0.10835902 -0.17328274]

[-0.64417314 -0.18886813 -0.41106892]]

Difference between your scores and correct scores:

3.381231222787662e-08
```

0.2.2 Forward pass loss

```
[14]: loss, _ = net.loss(X, y, reg=0.05)
    correct_loss = 1.071696123862817

# should be very small, we get < 1e-12
    print("Loss:",loss)
    print('Difference between your loss and correct loss:')
    print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Loss: 1.071696123862817 Difference between your loss and correct loss: 0.0

0.2.3 Backward pass

Implements the backwards pass of the neural network. Check your gradients with the gradient check utilities provided.

```
W1 max relative error: 1.2832896562471202e-09
W2 max relative error: 2.9632250794530335e-10
b1 max relative error: 3.1726809611748053e-09
b2 max relative error: 1.8391748601536041e-10
```

0.2.4 Training the network

Implement neural_net.train() to train the network via stochastic gradient descent, much like the softmax and SVM.

Final training loss: 0.014497864587766035



0.3 Classify CIFAR-10

Do classification on the CIFAR-10 dataset.

```
[17]: from utils.data_utils import load_CIFAR10
      def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
          Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
          it for the two-layer neural net classifier.
          # Load the raw CIFAR-10 data
          cifar10 dir = 'C:/Users/User/Desktop/EE247/HW3 Code/data/
       ⇔cifar-10-batches-py' # remember to use correct path
          X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
          # Subsample the data
          mask = list(range(num_training, num_training + num_validation))
          X_val = X_train[mask]
          y_val = y_train[mask]
          mask = list(range(num training))
          X_train = X_train[mask]
          y_train = y_train[mask]
          mask = list(range(num_test))
          X_test = X_test[mask]
          y_test = y_test[mask]
          # Normalize the data: subtract the mean image
          mean_image = np.mean(X_train, axis=0)
          X_train -= mean_image
          X_val -= mean_image
          X_test -= mean_image
          # Reshape data to rows
          X_train = X_train.reshape(num_training, -1)
          X val = X val.reshape(num validation, -1)
          X_test = X_test.reshape(num_test, -1)
          return X_train, y_train, X_val, y_val, X_test, y_test
      # Invoke the above function to get our data.
      X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
      print('Train data shape: ', X_train.shape)
      print('Train labels shape: ', y_train.shape)
      print('Validation data shape: ', X_val.shape)
      print('Validation labels shape: ', y_val.shape)
      print('Test data shape: ', X_test.shape)
      print('Test labels shape: ', y_test.shape)
```

Train data shape: (49000, 3072) Train labels shape: (49000,)

```
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

0.3.1 Running SGD

If your implementation is correct, you should see a validation accuracy of around 28-29%.

```
iteration 0 / 1000: loss 2.302757518613176
iteration 100 / 1000: loss 2.302120159207236
iteration 200 / 1000: loss 2.2956136007408703
iteration 300 / 1000: loss 2.251825904316413
iteration 400 / 1000: loss 2.188995235046776
iteration 500 / 1000: loss 2.1162527791897747
iteration 600 / 1000: loss 2.064670827698217
iteration 700 / 1000: loss 1.9901688623083942
iteration 800 / 1000: loss 2.002827640124685
iteration 900 / 1000: loss 1.9465176817856495
Validation accuracy: 0.283
```

0.4 Questions:

The training accuracy isn't great.

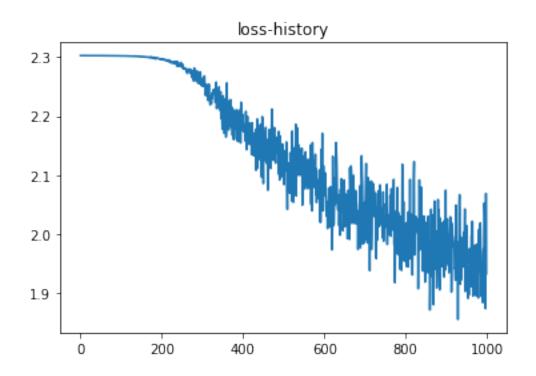
- (1) What are some of the reasons why this is the case? Take the following cell to do some analyses and then report your answers in the cell following the one below.
- (2) How should you fix the problems you identified in (1)?

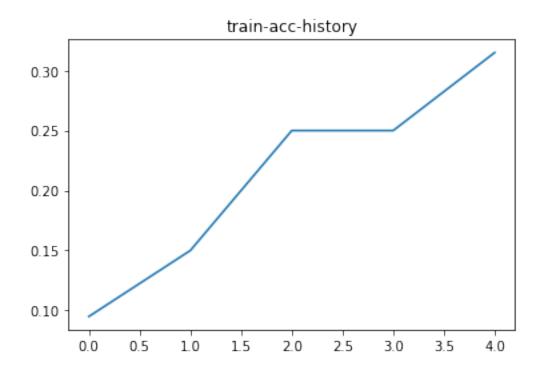
```
[19]: stats['train_acc_history']
```

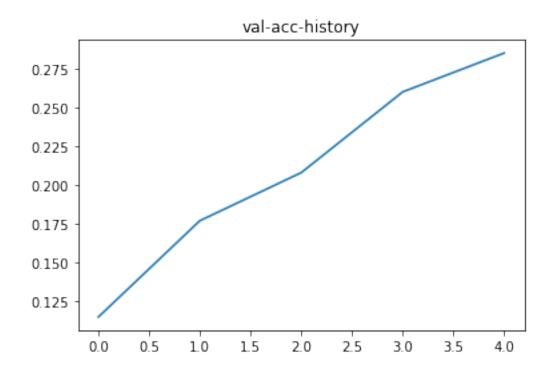
[19]: [0.095, 0.15, 0.25, 0.25, 0.315]

```
[20]: | # =========== #
    # YOUR CODE HERE:
     Do some debugging to gain some insight into why the optimization
      isn't great.
    # ----- #
   # Plot the loss function and train / validation accuracies
   plt.figure()
   plt.plot(stats['loss_history'])
   plt.title('loss-history')
   plt.figure()
   plt.plot(stats['train_acc_history'])
   plt.title('train-acc-history')
   plt.figure()
   plt.plot(stats['val_acc_history'])
   plt.title('val-acc-history')
   # ----- #
    # END YOUR CODE HERE
```

[20]: Text(0.5, 1.0, 'val-acc-history')







0.5 Answers:

- (1) Loss function fluctuates a lot and hasn't decayed enough. It can decay lower with more training iterations and the fluctuation can be ameliorated by taking a larger batch size.
- (2) Larger training epoch (decay further), larger batch size (smoother decay). I'll also try with a larger lr such that the loss function decays faster. I don't need to worry too much of the overshoot since there exists lr decay

0.6 Optimize the neural network

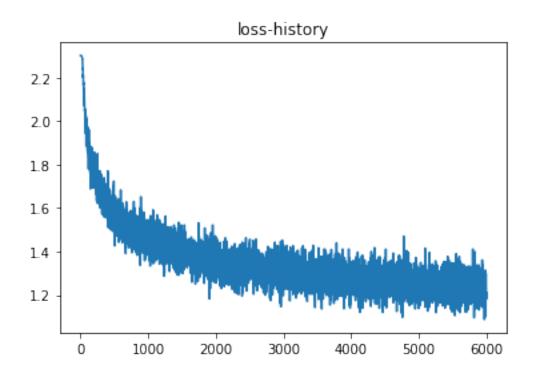
Use the following part of the Jupyter notebook to optimize your hyperparameters on the validation set. Store your nets as best_net.

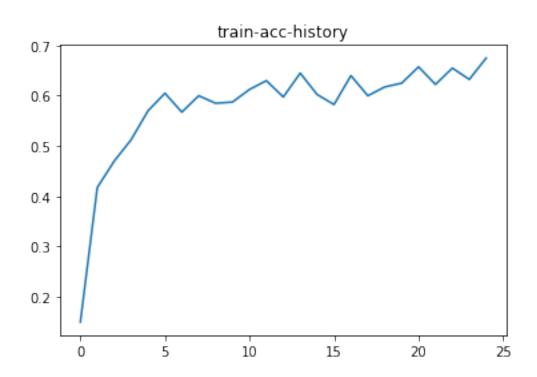
```
[21]: best_net = None # store the best model into this
     # ----- #
     # YOUR CODE HERE:
         Optimize over your hyperparameters to arrive at the best neural
         network. You should be able to get over 50% validation accuracy.
     #
        For this part of the notebook, we will give credit based on the
         accuracy you get. Your score on this question will be multiplied by:
     #
           min(floor((X - 28\%)) / \%22, 1)
         where if you get 50% or higher validation accuracy, you get full
     #
     #
         points.
        Note, you need to use the same network structure (keep hidden size = 50)!
       ______#
     input_size = 32 * 32 * 3
     hidden size = 50
     num classes = 10
     lr = 1e-3
     iters = 6000
     batch = 400
     # Train the network
     net_mod = TwoLayerNet(input_size, hidden_size, num_classes)
     stats = net_mod.train(X_train, y_train, X_val, y_val,
                         num_iters=iters, batch_size=batch_,
                         learning_rate=lr, learning_rate_decay=0.95,
                         reg=0.25, verbose=True)
     # Predict on the validation set
     val acc = (net mod.predict(X val) == y val).mean()
     print('Validation accuracy: ', val_acc)
     best_net = net_mod
```

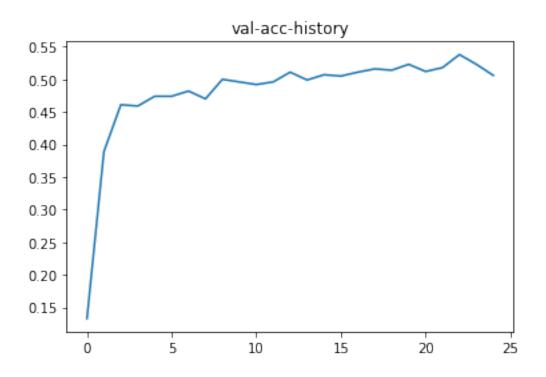
```
iteration 0 / 6000: loss 2.302762288641366
iteration 100 / 6000: loss 1.8852494717090207
iteration 200 / 6000: loss 1.7962950741320023
iteration 300 / 6000: loss 1.651165686686989
iteration 400 / 6000: loss 1.6158751938485285
iteration 500 / 6000: loss 1.5436437449755958
iteration 600 / 6000: loss 1.5725534690119538
iteration 700 / 6000: loss 1.4688592803155993
iteration 800 / 6000: loss 1.4318646060349418
iteration 900 / 6000: loss 1.425127627408014
iteration 1000 / 6000: loss 1.4491556160774328
iteration 1100 / 6000: loss 1.4416939947721261
iteration 1200 / 6000: loss 1.3501226822248382
iteration 1300 / 6000: loss 1.4160920700014503
iteration 1400 / 6000: loss 1.3467830104383287
iteration 1500 / 6000: loss 1.3448662238097877
iteration 1600 / 6000: loss 1.4197755381492512
iteration 1700 / 6000: loss 1.4254237589032333
iteration 1800 / 6000: loss 1.3665506908102778
iteration 1900 / 6000: loss 1.4197004214241231
iteration 2000 / 6000: loss 1.4548570177254125
iteration 2100 / 6000: loss 1.3189692623050142
iteration 2200 / 6000: loss 1.2776628135568069
iteration 2300 / 6000: loss 1.3306031739525246
iteration 2400 / 6000: loss 1.3491076189751257
iteration 2500 / 6000: loss 1.2966604984705528
iteration 2600 / 6000: loss 1.2850170687114508
iteration 2700 / 6000: loss 1.2658133126519933
iteration 2800 / 6000: loss 1.2988766410541497
iteration 2900 / 6000: loss 1.3563244925067393
iteration 3000 / 6000: loss 1.3430040434621786
iteration 3100 / 6000: loss 1.2524709986808067
iteration 3200 / 6000: loss 1.2098087597851526
iteration 3300 / 6000: loss 1.2426177323739365
iteration 3400 / 6000: loss 1.2041518548643582
iteration 3500 / 6000: loss 1.2870236868526028
iteration 3600 / 6000: loss 1.3337298296588673
iteration 3700 / 6000: loss 1.2326630138088914
iteration 3800 / 6000: loss 1.2197263909241798
iteration 3900 / 6000: loss 1.3132900512960841
iteration 4000 / 6000: loss 1.2893353950558646
iteration 4100 / 6000: loss 1.1909370240669899
```

```
iteration 4200 / 6000: loss 1.3609445669501865
     iteration 4300 / 6000: loss 1.323173460967407
     iteration 4400 / 6000: loss 1.3292380287552292
     iteration 4500 / 6000: loss 1.2113067128676147
     iteration 4600 / 6000: loss 1.3017226327665503
     iteration 4700 / 6000: loss 1.2511323082378984
     iteration 4800 / 6000: loss 1.2774189627552273
     iteration 4900 / 6000: loss 1.1859844162827398
     iteration 5000 / 6000: loss 1.2521712836823535
     iteration 5100 / 6000: loss 1.273840223428511
     iteration 5200 / 6000: loss 1.3424765883720597
     iteration 5300 / 6000: loss 1.2019292948586433
     iteration 5400 / 6000: loss 1.2778041897301633
     iteration 5500 / 6000: loss 1.2617993210097684
     iteration 5600 / 6000: loss 1.193282549252632
     iteration 5700 / 6000: loss 1.1985767781210055
     iteration 5800 / 6000: loss 1.256850464874166
     iteration 5900 / 6000: loss 1.234138882780408
     Validation accuracy: 0.521
     Validation accuracy: 0.521
[22]: plt.figure()
     plt.plot(stats['loss_history'])
      plt.title('loss-history')
      plt.figure()
      plt.plot(stats['train_acc_history'])
      plt.title('train-acc-history')
      plt.figure()
      plt.plot(stats['val_acc_history'])
      plt.title('val-acc-history')
```

[22]: Text(0.5, 1.0, 'val-acc-history')





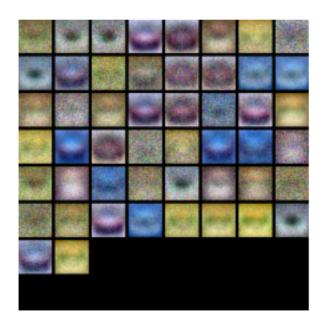


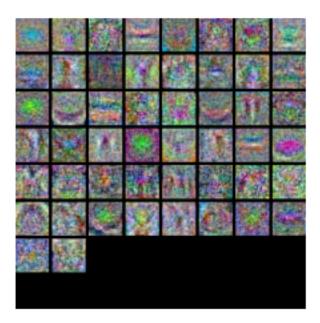
```
[23]: from utils.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
    W1 = net.params['W1']
    W1 = W1.T.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
    plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
    plt.gca().axis('off')
    plt.show()

show_net_weights(subopt_net)
show_net_weights(best_net)
```





0.7 Question:

(1) What differences do you see in the weights between the suboptimal net and the best net you arrived at?

0.8 Answer:

(1) I got more variantions and details in the best net weights. For the suboptimal net, most of its weights are templates resembling cars. For the best net weights, it's generating templates of different classes and each template has more high frequency compenents (details), which would benefit classification.

0.9 Evaluate on test set

```
[25]: test_acc = (best_net.predict(X_test) == y_test).mean()
    print('Test accuracy: ', test_acc)

Test accuracy: 0.517
[]:
```

LAYERS.PY

```
import numpy as np
import pdb
def affine_forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d_1 * ... * d_k, and
 then transform it to an output vector of dimension M.
 Inputs:
 -x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 11 11 11
 # YOUR CODE HERE:
 # Calculate the output of the forward pass. Notice the dimensions
 \# of w are D x M, which is the transpose of what we did in earlier
     assignments.
 # ============ #
 num_train = x.shape[0]
 out = np.matmul(x.reshape(num_train, np.product(x.shape[1::])), w) \
      + b.reshape([1, b.shape[0]])
 # ========== #
 # END YOUR CODE HERE
 cache = (x, w, b)
 return out, cache
```

```
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: Input data, of shape (N, d_1, \ldots, d_k)
   - w: Weights, of shape (D, M)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
 - dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 x, w, b = cache
 dx, dw, db = None, None, None
 # YOUR CODE HERE:
 # Calculate the gradients for the backward pass.
 # ----- #
 # dout is N x M
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which
 # dw should be D x M; it relates to dout through multiplication with x, which is N x D af
 # db should be M; it is just the sum over dout examples
 db = np.sum(dout, axis=0)
 dw = np.matmul(x.reshape(x.shape[0], np.product(x.shape[1::])).T, dout)
 dx_br = np.matmul(dout, w.T)
 dx = dx_br.reshape(x.shape)
 # END YOUR CODE HERE
 # ------ #
 return dx, dw, db
def relu_forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
```

```
Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ----- #
 # YOUR CODE HERE:
  Implement the ReLU forward pass.
 out = np.where(x>=0, x, 0)
 # END YOUR CODE HERE
 cache = x
 return out, cache
def relu_backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
 # ========== #
 # YOUR CODE HERE:
  Implement the ReLU backward pass
 # ------ #
 # ReLU directs linearly to those > 0
 dx = np.multiply(np.where(x>=0, 1, 0), dout)
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 return dx
```

```
def softmax_loss(x, y):
  Computes the loss and gradient for softmax classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
    for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 \le y[i] < C
 Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  n|n|n
 probs = np.exp(x - np.max(x, axis=1, keepdims=True))
 probs /= np.sum(probs, axis=1, keepdims=True)
 N = x.shape[0]
 loss = -np.sum(np.log(probs[np.arange(N), y])) / N
 dx = probs.copy()
 dx[np.arange(N), y] = 1
 dx /= N
 return loss, dx
```

FC_NET.PY

```
import numpy as np
from .layers import *
from .layer_utils import *
class TwoLayerNet(object):
 A two-layer fully-connected neural network with ReLU nonlinearity and
  softmax loss that uses a modular layer design. We assume an input dimension
  of D, a hidden dimension of H, and perform classification over C classes.
  The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
  optimization.
  The learnable parameters of the model are stored in the dictionary
  self.params that maps parameter names to numpy arrays.
 def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
              dropout=0, weight_scale=1e-3, reg=0.0):
    Initialize a new network.
   Inputs:
    - input_dim: An integer giving the size of the input
    - hidden_dims: An integer giving the size of the hidden layer
    - num_classes: An integer giving the number of classes to classify
    - dropout: Scalar between 0 and 1 giving dropout strength.
    - weight_scale: Scalar giving the standard deviation for random
     initialization of the weights.
    - reg: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
    # YOUR CODE HERE:
      Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
    \# self.params['W2'], self.params['b1'] and self.params['b2']. The
    # biases are initialized to zero and the weights are initialized
```

```
# so that each parameter has mean O and standard deviation weight_scale.
 # The dimensions of W1 should be (input_dim, hidden_dim) and the
 # dimensions of W2 should be (hidden_dims, num_classes)
 # ----- #
 std = weight_scale
 self.params['W1'] = std * np.random.randn(input_dim, hidden_dims)
 self.params['b1'] = np.zeros(hidden_dims)
 self.params['W2'] = std * np.random.randn(hidden_dims, num_classes)
 self.params['b2'] = np.zeros(num_classes)
 # =========== #
 # END YOUR CODE HERE
 def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Inputs:
 - X: Array of input data of shape (N, d_1, \ldots, d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
   scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
  names to gradients of the loss with respect to those parameters.
 scores = None
 # ------ #
 # YOUR CODE HERE:
 # Implement the forward pass of the two-layer neural network. Store
 # the class scores as the variable 'scores'. Be sure to use the layers
 # you prior implemented.
 W1, b1 = self.params['W1'], self.params['b1']
 W2, b2 = self.params['W2'], self.params['b2']
```

```
layer1, layer1_cache = affine_forward(X, W1, b1)
ReLU_act, ReLU_act_cache = relu_forward(layer1)
scores, layer2_cache = affine_forward(ReLU_act, W2, b2)
# ----- #
# END YOUR CODE HERE
# ----- #
# If y is None then we are in test mode so just return scores
if y is None:
 return scores
loss, grads = 0, {}
# ----- #
# YOUR CODE HERE:
   Implement the backward pass of the two-layer neural net. Store
   the loss as the variable 'loss' and store the gradients in the
   'qrads' dictionary. For the grads dictionary, grads['W1'] holds
  the gradient for W1, grads['b1'] holds the gradient for b1, etc.
   i.e., grads[k] holds the gradient for self.params[k].
  Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
   for each W. Be sure to include the 0.5 multiplying factor to
#
  match our implementation.
  And be sure to use the layers you prior implemented.
sf_loss, grad_softmax = softmax_loss(scores, y)
reg_loss = 0.5*self.reg*(np.linalg.norm(W1)**2 + np.linalg.norm(W2)**2)
loss = sf_loss + reg_loss
""" forward pass:
layer1, layer1_cache = affine_forward(X, W1, b1)
ReLU_act, ReLU_act_cache = relu_forward(layer1)
scores, layer2_cache = affine_forward(ReLU_act, W2, b2)
grad_ReLU, grad_W2, grad_b2 = affine_backward(grad_softmax, layer2_cache)
grad_layer1 = relu_backward(grad_ReLU, ReLU_act_cache)
_, grad_W1, grad_b1 = affine_backward(grad_layer1, layer1_cache)
grad_W1_reg = 0.5*self.reg*2*W1
grad_W2_reg = 0.5*self.reg*2*W2
grads['W2'] = grad_W2 + grad_W2_reg
```

```
grads['b2'] = grad_b2
   grads['W1'] = grad_W1 + grad_W1_reg
   grads['b1'] = grad_b1
    # ----- #
    # END YOUR CODE HERE
    # ----- #
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
 ReLU nonlinearities, and a softmax loss function. This will also implement
  dropout and batch normalization as options. For a network with L layers,
  the architecture will be
  \{affine - [batch norm] - relu - [dropout]\} x (L - 1) - affine - softmax
  where batch normalization and dropout are optional, and the {...} block is
  repeated L - 1 times.
  Similar to the TwoLayerNet above, learnable parameters are stored in the
  self.params dictionary and will be learned using the Solver class.
 def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
              dropout=0, use_batchnorm=False, reg=0.0,
              weight_scale=1e-2, dtype=np.float32, seed=None):
   Initialize a new FullyConnectedNet.
   Inputs:
    - hidden_dims: A list of integers giving the size of each hidden layer.
    - input_dim: An integer giving the size of the input.
   - num_classes: An integer giving the number of classes to classify.
    - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
     the network should not use dropout at all.
   - use_batchnorm: Whether or not the network should use batch normalization.
    - reg: Scalar giving L2 regularization strength.
    - weight_scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - dtype: A numpy datatype object; all computations will be performed using
     this datatype. float32 is faster but less accurate, so you should use
```

float64 for numeric gradient checking.

```
- seed: If not None, then pass this random seed to the dropout layers. This
 will make the dropout layers deteriminstic so we can gradient check the
 model.
self.use_batchnorm = use_batchnorm
self.use_dropout = dropout > 0
self.reg = reg
self.num_layers = 1 + len(hidden_dims)
self.dtype = dtype
self.params = {}
# ----- #
# YOUR CODE HERE:
# Initialize all parameters of the network in the self.params dictionary.
# The weights and biases of layer 1 are W1 and b1; and in general the
# weights and biases of layer i are Wi and bi. The
# biases are initialized to zero and the weights are initialized
# so that each parameter has mean O and standard deviation weight_scale.
# ----- #
dim_list = np.hstack([input_dim, hidden_dims, num_classes])
std = weight_scale
for i in range(self.num_layers):
   key_W = "W" + str(i+1)
   key_b = "b" + str(i+1)
   self.params[key_W] = std * np.random.randn(dim_list[i], dim_list[i+1])
   self.params[key_b] = np.zeros(dim_list[i+1])
# ----- #
# END YOUR CODE HERE
# When using dropout we need to pass a dropout_param dictionary to each
# dropout layer so that the layer knows the dropout probability and the mode
# (train / test). You can pass the same dropout_param to each dropout layer.
self.dropout_param = {}
if self.use_dropout:
 self.dropout_param = {'mode': 'train', 'p': dropout}
 if seed is not None:
   self.dropout_param['seed'] = seed
# With batch normalization we need to keep track of running means and
# variances, so we need to pass a special bn_param object to each batch
```

```
# normalization layer. You should pass self.bn_params[0] to the forward pass
  # of the first batch normalization layer, self.bn_params[1] to the forward
  # pass of the second batch normalization layer, etc.
 self.bn_params = []
 if self.use_batchnorm:
   self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]
  # Cast all parameters to the correct datatype
 for k, v in self.params.items():
   self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
 Compute loss and gradient for the fully-connected net.
  Input / output: Same as TwoLayerNet above.
 X = X.astype(self.dtype)
 mode = 'test' if y is None else 'train'
 # Set train/test mode for batchnorm params and dropout param since they
 # behave differently during training and testing.
 if self.dropout_param is not None:
   self.dropout_param['mode'] = mode
 if self.use_batchnorm:
   for bn_param in self.bn_params:
     bn_param[mode] = mode
 scores = None
  # ------ #
  # YOUR CODE HERE:
 # Implement the forward pass of the FC net and store the output
  # scores as the variable "scores".
  # ----- #
 cache_ls = []
 in_{-} = X
  """ FORWARD
  layer1, layer1_cache = affine_forward(X, W1, b1)
  cache_ls2.append(layer1_cache)
 ReLU_act, ReLU_act_cache = relu_forward(layer1)
  cache_ls2.append(ReLU_act_cache)
```

```
layer2, layer2_cache = affine_forward(ReLU_act, W2, b2)
cache_ls2.append(layer2_cache)
ReLU_act2, ReLU_act_cache2 = relu_forward(layer2)
cache_ls2.append(ReLU_act2)
scores, layer3_cache = affine_forward(ReLU_act2, W3, b3)
cache_ls2.append(layer3_cache)
for i in range(self.num_layers):
   key_W = "W" + str(i+1)
   key_b = "b" + str(i+1)
   W_i, b_i = self.params[key_W], self.params[key_b]
   layer_out, layer_cache = affine_forward(in_, W_i, b_i)
   cache_ls.append(layer_cache)
   if i < self.num_layers-1:</pre>
      ReLU_act, ReLU_act_cache = relu_forward(layer_out)
      cache_ls.append(ReLU_act_cache)
      in_ = ReLU_act
   #output layer
   else:
      scores = layer_out
# ------ #
# END YOUR CODE HERE
# ----- #
# If test mode return early
if mode == 'test':
 return scores
loss, grads = 0.0, {}
# ----- #
# YOUR CODE HERE:
# Implement the backwards pass of the FC net and store the gradients
# in the grads dict, so that grads[k] is the gradient of self.params[k]
# Be sure your L2 regularization includes a 0.5 factor.
# ------ #
```

```
sf_loss, grad_softmax = softmax_loss(scores, y)
reg_loss = 0.0
for i in range(self.num_layers):
   kev_W = W'' + str(i+1)
   W_i = self.params[key_W]
   reg_loss += 0.5*self.reg*(np.linalg.norm(W_i)**2)
loss = sf_loss + reg_loss
"""BACKWARD
grad_ReLU2, grad_W3, grad_b3 = affine_backward(grad_softmax, layer_cache[4]) #i==5
grad\_layer2 = relu\_backward(grad\_ReLU2, layer\_cache[3]) #i==4
grad_ReLU1, grad_W2, grad_b2 = affine_backward(grad_layer2, layer_cache[2])
                                                                        #i==3
grad_layer1 = relu_backward(grad_ReLU1, layer_cache[1]) #i==2
\_, grad_W1, grad_b1 = affine_backward(grad_layer1, layer_cache[0]) #i==1
# len(cache_ls) is guaranteed to be an odd num due to sandwitching
# (no activation @ output layer)
grad_backnode, grad_W_i, grad_b_i = affine_backward(grad_softmax, cache_ls[-1])
key_W = "W" + str(self.num_layers)
key_b = "b" + str(self.num_layers)
grad_Wi_reg = 0.5*self.reg*2*self.params[key_W]
grads[key_W] = grad_W_i+grad_Wi_reg
grads[key_b] = grad_b_i
for i in range(len(cache_ls)-1, 1, -2):
   grad_layer = relu_backward(grad_backnode, cache_ls[i-1])
   grad_backnode, grad_W_i, grad_b_i = affine_backward(grad_layer, cache_ls[i-2])
   key_W = "W" + str(i//2)
   key_b = "b" + str(i//2)
   grad_Wi_reg = 0.5*self.reg*2*self.params[key_W]
   grads[key_W] = grad_W_i + grad_Wi_reg
   grads[key_b] = grad_b_i
# ----- #
# END YOUR CODE HERE
# ----- #
return loss, grads
```

FC nets

February 9, 2024

1 Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

1.1 Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

def layer forward(x, w):

```
""" Receive inputs x and weights w """
# Do some computations ...
z = # ... some intermediate value
# Do some more computations ...
out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
       Receive derivative of loss with respect to outputs and cache,
       and compute derivative with respect to inputs.
       11 11 11
       # Unpack cache values
       x, w, z, out = cache
       # Use values in cache to compute derivatives
       dx = # Derivative of loss with respect to x
       dw = # Derivative of loss with respect to w
       return dx, dw
[20]: ## Import and setups
      import time
      import numpy as np
      import matplotlib.pyplot as plt
      from nndl.fc_net import *
      from utils.data_utils import get_CIFAR10_data
      from utils.gradient_check import eval_numerical_gradient,_

eval_numerical_gradient_array
      from utils.solver import Solver
      %matplotlib inline
      plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
      plt.rcParams['image.interpolation'] = 'nearest'
      plt.rcParams['image.cmap'] = 'gray'
      # for auto-reloading external modules
      # see http://stackoverflow.com/questions/1907993/
       \rightarrow autoreload-of-modules-in-ipython
      %load ext autoreload
      %autoreload 2
      def rel_error(x, y):
        """ returns relative error """
        return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
     The autoreload extension is already loaded. To reload it, use:
       %reload_ext autoreload
[21]: # Load the (preprocessed) CIFAR10 data.
      # you may find an error here, this is may be because you forgot to use correct_
       ⇒path in get_CIFAR10_data()
      data = get_CIFAR10_data()
      for k in data.keys():
```

```
print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

1.2 Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine_forward in nndl/layers.py and the backward pass is affine_backward.

After you have implemented these, test your implementation by running the cell below.

1.2.1 Affine layer forward pass

Implement affine_forward and then test your code by running the following cell.

```
[22]: # Test the affine_forward function
      num_inputs = 2
      input\_shape = (4, 5, 6)
      output_dim = 3
      input_size = num_inputs * np.prod(input_shape)
      weight_size = output_dim * np.prod(input_shape)
      x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs, *input shape)
      w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape),_
       →output dim)
      b = np.linspace(-0.3, 0.1, num=output_dim)
      out, _ = affine_forward(x, w, b)
      correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                              [ 3.25553199, 3.5141327, 3.77273342]])
      # Compare your output with ours. The error should be around 1e-9.
      print('Testing affine_forward function:')
      print('difference: {}'.format(rel_error(out, correct_out)))
```

Testing affine_forward function: difference: 9.769849468192957e-10

1.2.2 Affine layer backward pass

Implement affine backward and then test your code by running the following cell.

```
[23]: # Test the affine backward function
      x = np.random.randn(10, 2, 3)
      w = np.random.randn(6, 5)
      b = np.random.randn(5)
      dout = np.random.randn(10, 5)
      dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x,_
      dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w,__
       ⇔dout)
      db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0], b,_
       -dout)
      _, cache = affine_forward(x, w, b)
      dx, dw, db = affine_backward(dout, cache)
      # The error should be around 1e-10
      print('Testing affine_backward function:')
      print('dx error: {}'.format(rel_error(dx_num, dx)))
      print('dw error: {}'.format(rel_error(dw_num, dw)))
      print('db error: {}'.format(rel_error(db_num, db)))
```

Testing affine_backward function: dx error: 1.554353357560498e-10

dw error: 2.3511429449233634e-09 db error: 2.6764309756641935e-11

1.3 Activation layers

In this section you'll implement the ReLU activation.

1.3.1 ReLU forward pass

Implement the relu_forward function in nndl/layers.py and then test your code by running the following cell.

```
print('difference: {}'.format(rel_error(out, correct_out)))
```

Testing relu_forward function: difference: 4.999999798022158e-08

1.3.2 ReLU backward pass

Implement the relu_backward function in nndl/layers.py and then test your code by running the following cell.

```
[25]: x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be around 1e-12
print('Testing relu_backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing relu_backward function: dx error: 3.275621371969467e-12

1.4 Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in nndl/layer_utils.py.

1.4.1 Affine-ReLU layers

We've implemented affine_relu_forward() and affine_relu_backward in nndl/layer_utils.py. Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

Testing affine relu forward and affine relu backward:

dx error: 6.615955056119943e-11
dw error: 6.104731962774415e-09
db error: 1.2376859507070784e-10

1.5 Softmax loss

You've already implemented it, so we have written it in layers.py. The following code will ensure they are working correctly.

```
[27]: num_classes, num_inputs = 10, 50
    x = 0.001 * np.random.randn(num_inputs, num_classes)
    y = np.random.randint(num_classes, size=num_inputs)

dx_num = eval_numerical_gradient(lambda x: softmax_loss(x, y)[0], x,u
    overbose=False)
    loss, dx = softmax_loss(x, y)

# Test softmax_loss function. Loss should be 2.3 and dx error should be 1e-8
    print('\nTesting softmax_loss:')
    print('loss: {}'.format(loss))
    print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing softmax_loss: loss: 2.3025509558316175 dx error: 8.257249984553402e-09

1.6 Implementation of a two-layer NN

In nndl/fc_net.py, implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

```
[28]: N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)
```

```
std = 1e-2
model = TwoLayerNet(input_dim=D, hidden_dims=H, num_classes=C, weight_scale=std)
print('Testing initialization ... ')
W1_std = abs(model.params['W1'].std() - std)
b1 = model.params['b1']
W2_std = abs(model.params['W2'].std() - std)
b2 = model.params['b2']
assert W1_std < std / 10, 'First layer weights do not seem right'
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'
assert np.all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct_scores = np.asarray(
 [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.
→33206765, 16.09215096],
   [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.
→49994135, 16.18839143],
   [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
→66781506, 16.2846319 ]])
scores_diff = np.abs(scores - correct_scores).sum()
assert scores_diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct_loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'</pre>
model.reg = 1.0
loss, grads = model.loss(X, y)
correct_loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'
for reg in [0.0, 0.7]:
 print('Running numeric gradient check with reg = {}'.format(reg))
 model.reg = reg
 loss, grads = model.loss(X, y)
 for name in sorted(grads):
```

```
f = lambda _: model.loss(X, y)[0]
grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
print('{} relative error: {}'.format(name, rel_error(grad_num,
grads[name])))
```

```
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.8336562786695002e-08
W2 relative error: 3.201560569143183e-10
b1 relative error: 9.828315204644842e-09
b2 relative error: 4.329134954569865e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 2.5279152310200606e-07
W2 relative error: 7.976652806155026e-08
b1 relative error: 1.564679947504764e-08
b2 relative error: 9.089617896905665e-10
```

1.7 Solver

We will now use the utils Solver class to train these networks. Familiarize yourself with the API in utils/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 50%.

```
[29]: model = TwoLayerNet()
     solver = None
     # ----- #
     # YOUR CODE HERE:
       Declare an instance of a TwoLayerNet and then train
        it with the Solver. Choose hyperparameters so that your validation
       accuracy is at least 50%. We won't have you optimize this further
         since you did it in the previous notebook.
     model as TwoLayerNet()
     data as CIFAR-10 data
     11 11 11
     solver = Solver(model, data,
                   update_rule='sgd',
                    optim_config={
                      'learning_rate': 1e-3,
                    lr_decay=0.95,
```

```
num_epochs=15, batch_size=100,
                print_every=100)
solver.train()
# END YOUR CODE HERE
# ----- #
(Iteration 1 / 7350) loss: 2.298564
(Epoch 0 / 15) train acc: 0.142000; val_acc: 0.156000
(Iteration 101 / 7350) loss: 1.858356
(Iteration 201 / 7350) loss: 1.817273
(Iteration 301 / 7350) loss: 1.685811
(Iteration 401 / 7350) loss: 1.421284
(Epoch 1 / 15) train acc: 0.417000; val_acc: 0.452000
(Iteration 501 / 7350) loss: 1.597581
(Iteration 601 / 7350) loss: 1.572142
(Iteration 701 / 7350) loss: 1.475473
(Iteration 801 / 7350) loss: 1.498437
(Iteration 901 / 7350) loss: 1.397053
(Epoch 2 / 15) train acc: 0.510000; val_acc: 0.489000
(Iteration 1001 / 7350) loss: 1.551160
(Iteration 1101 / 7350) loss: 1.445567
(Iteration 1201 / 7350) loss: 1.408582
(Iteration 1301 / 7350) loss: 1.432239
(Iteration 1401 / 7350) loss: 1.340010
(Epoch 3 / 15) train acc: 0.548000; val_acc: 0.503000
(Iteration 1501 / 7350) loss: 1.246971
(Iteration 1601 / 7350) loss: 1.353292
(Iteration 1701 / 7350) loss: 1.483650
(Iteration 1801 / 7350) loss: 1.327398
(Iteration 1901 / 7350) loss: 1.290622
(Epoch 4 / 15) train acc: 0.538000; val acc: 0.494000
(Iteration 2001 / 7350) loss: 1.245361
(Iteration 2101 / 7350) loss: 1.430901
(Iteration 2201 / 7350) loss: 1.360906
(Iteration 2301 / 7350) loss: 1.431490
(Iteration 2401 / 7350) loss: 1.398528
(Epoch 5 / 15) train acc: 0.539000; val acc: 0.514000
(Iteration 2501 / 7350) loss: 1.287843
(Iteration 2601 / 7350) loss: 1.131582
(Iteration 2701 / 7350) loss: 1.284818
(Iteration 2801 / 7350) loss: 1.215222
(Iteration 2901 / 7350) loss: 1.368394
(Epoch 6 / 15) train acc: 0.568000; val_acc: 0.498000
(Iteration 3001 / 7350) loss: 0.992158
(Iteration 3101 / 7350) loss: 1.145389
```

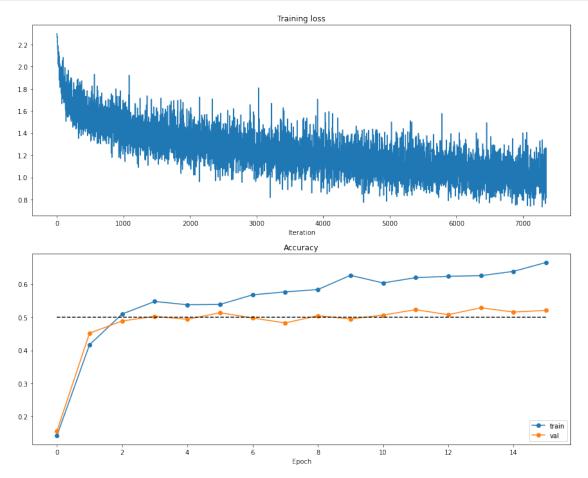
```
(Iteration 3201 / 7350) loss: 1.314393
(Iteration 3301 / 7350) loss: 1.081020
(Iteration 3401 / 7350) loss: 1.329748
(Epoch 7 / 15) train acc: 0.577000; val acc: 0.483000
(Iteration 3501 / 7350) loss: 1.109539
(Iteration 3601 / 7350) loss: 1.061484
(Iteration 3701 / 7350) loss: 1.244280
(Iteration 3801 / 7350) loss: 1.166834
(Iteration 3901 / 7350) loss: 1.199950
(Epoch 8 / 15) train acc: 0.584000; val_acc: 0.505000
(Iteration 4001 / 7350) loss: 1.344948
(Iteration 4101 / 7350) loss: 1.057932
(Iteration 4201 / 7350) loss: 0.982783
(Iteration 4301 / 7350) loss: 1.169271
(Iteration 4401 / 7350) loss: 1.075300
(Epoch 9 / 15) train acc: 0.627000; val_acc: 0.495000
(Iteration 4501 / 7350) loss: 1.123154
(Iteration 4601 / 7350) loss: 1.277694
(Iteration 4701 / 7350) loss: 1.065818
(Iteration 4801 / 7350) loss: 1.106089
(Epoch 10 / 15) train acc: 0.604000; val acc: 0.507000
(Iteration 4901 / 7350) loss: 1.106192
(Iteration 5001 / 7350) loss: 1.267657
(Iteration 5101 / 7350) loss: 0.986157
(Iteration 5201 / 7350) loss: 1.134579
(Iteration 5301 / 7350) loss: 1.405458
(Epoch 11 / 15) train acc: 0.620000; val_acc: 0.523000
(Iteration 5401 / 7350) loss: 1.359432
(Iteration 5501 / 7350) loss: 1.163835
(Iteration 5601 / 7350) loss: 0.932364
(Iteration 5701 / 7350) loss: 1.126674
(Iteration 5801 / 7350) loss: 1.192106
(Epoch 12 / 15) train acc: 0.624000; val_acc: 0.508000
(Iteration 5901 / 7350) loss: 1.042706
(Iteration 6001 / 7350) loss: 0.969401
(Iteration 6101 / 7350) loss: 1.028092
(Iteration 6201 / 7350) loss: 1.022832
(Iteration 6301 / 7350) loss: 1.401650
(Epoch 13 / 15) train acc: 0.626000; val_acc: 0.529000
(Iteration 6401 / 7350) loss: 1.043180
(Iteration 6501 / 7350) loss: 0.769892
(Iteration 6601 / 7350) loss: 0.982982
(Iteration 6701 / 7350) loss: 0.992465
(Iteration 6801 / 7350) loss: 0.927957
(Epoch 14 / 15) train acc: 0.639000; val_acc: 0.516000
(Iteration 6901 / 7350) loss: 0.953537
(Iteration 7001 / 7350) loss: 1.171512
(Iteration 7101 / 7350) loss: 0.979305
```

```
(Iteration 7201 / 7350) loss: 1.272414
(Iteration 7301 / 7350) loss: 0.901373
(Epoch 15 / 15) train acc: 0.666000; val_acc: 0.521000
```

```
[30]: # Run this cell to visualize training loss and train / val accuracy

plt.subplot(2, 1, 1)
plt.title('Training loss')
plt.plot(solver.loss_history, '-')
plt.xlabel('Iteration')

plt.subplot(2, 1, 2)
plt.title('Accuracy')
plt.plot(solver.train_acc_history, '-o', label='train')
plt.plot(solver.val_acc_history, '-o', label='val')
plt.plot([0.5] * len(solver.val_acc_history), 'k--')
plt.xlabel('Epoch')
plt.legend(loc='lower right')
plt.gcf().set_size_inches(15, 12)
plt.show()
```



1.8 Multilayer Neural Network

Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc_net.py.

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in HW #4.

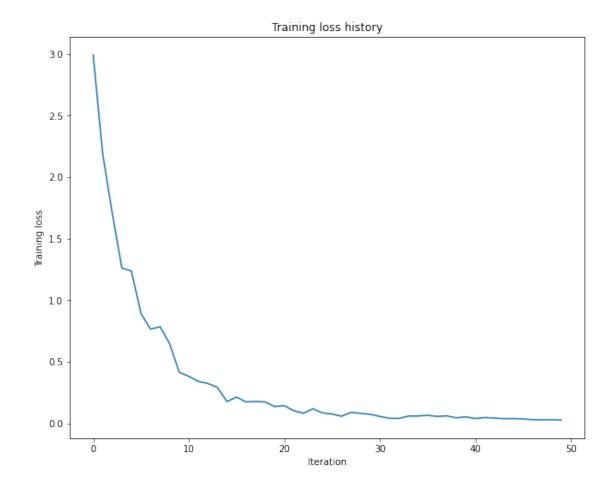
```
[36]: N, D, H1, H2, C = 2, 15, 20, 30, 10
      X = np.random.randn(N, D)
      y = np.random.randint(C, size=(N,))
      for reg in [0, 3.14]:
        print('Running check with reg = {}'.format(reg))
        model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                                  reg=reg, weight_scale=5e-2, dtype=np.float64)
        loss, grads = model.loss(X, y)
        print('Initial loss: {}'.format(loss))
        for name in sorted(grads):
          f = lambda : model.loss(X, y)[0]
          grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,_
       \rightarrowh=1e-5)
          print('{} relative error: {}'.format(name, rel_error(grad_num,_
       ⇒grads[name])))
     Running check with reg = 0
     Initial loss: 2.3033682473448396
     W1 relative error: 8.101915100584249e-07
     W2 relative error: 8.994324030155071e-07
     W3 relative error: 3.907310666524492e-07
     b1 relative error: 2.5729337488534124e-07
     b2 relative error: 1.2817524795895165e-09
     b3 relative error: 1.3733992957550199e-10
```

```
b1 relative error: 2.5729337488534124e-07
b2 relative error: 1.2817524795895165e-09
b3 relative error: 1.3733992957550199e-10
Running check with reg = 3.14
Initial loss: 7.1787664422529005
W1 relative error: 1.0041290373018651e-08
W2 relative error: 5.936333665923039e-08
W3 relative error: 3.752034433265848e-08
b1 relative error: 7.248406624655567e-09
b2 relative error: 1.1011066930384422e-08
b3 relative error: 1.8355020685404189e-10
```

[43]: # Use the three layer neural network to overfit a small dataset.

```
num_train = 50
small_data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X_val': data['X_val'],
  'y_val': data['y_val'],
}
#### !!!!!!
# Play around with the weight scale and learning rate so that you can overfit all
 ⇔small dataset.
# Your training accuracy should be 1.0 to receive full credit on this part.
weight_scale = 2e-2
learning_rate = 4e-3
model = FullyConnectedNet([100, 100],
              weight_scale=weight_scale, dtype=np.float64)
solver = Solver(model, small data,
                print_every=10, num_epochs=50, batch_size=50,
                update rule='sgd',
                optim_config={
                  'learning_rate': learning_rate,
solver.train()
plt.plot(solver.loss_history, '-')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()
(Iteration 1 / 50) loss: 2.993091
(Epoch 1 / 50) train acc: 0.300000; val_acc: 0.149000
(Epoch 2 / 50) train acc: 0.380000; val_acc: 0.099000
(Epoch 3 / 50) train acc: 0.700000; val_acc: 0.160000
(Epoch 4 / 50) train acc: 0.660000; val_acc: 0.146000
(Epoch 5 / 50) train acc: 0.760000; val_acc: 0.167000
(Epoch 6 / 50) train acc: 0.840000; val_acc: 0.170000
(Epoch 7 / 50) train acc: 0.860000; val_acc: 0.177000
(Epoch 8 / 50) train acc: 0.940000; val_acc: 0.161000
(Epoch 9 / 50) train acc: 0.940000; val_acc: 0.165000
(Epoch 10 / 50) train acc: 0.980000; val acc: 0.159000
(Iteration 11 / 50) loss: 0.380591
(Epoch 11 / 50) train acc: 0.980000; val acc: 0.163000
(Epoch 12 / 50) train acc: 0.980000; val_acc: 0.169000
(Epoch 13 / 50) train acc: 0.980000; val_acc: 0.172000
```

```
(Epoch 14 / 50) train acc: 0.980000; val_acc: 0.178000
(Epoch 15 / 50) train acc: 0.980000; val_acc: 0.166000
(Epoch 16 / 50) train acc: 1.000000; val_acc: 0.161000
(Epoch 17 / 50) train acc: 0.980000; val_acc: 0.167000
(Epoch 18 / 50) train acc: 1.000000; val acc: 0.162000
(Epoch 19 / 50) train acc: 1.000000; val_acc: 0.174000
(Epoch 20 / 50) train acc: 1.000000; val acc: 0.169000
(Iteration 21 / 50) loss: 0.141857
(Epoch 21 / 50) train acc: 1.000000; val_acc: 0.168000
(Epoch 22 / 50) train acc: 1.000000; val_acc: 0.169000
(Epoch 23 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 24 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 25 / 50) train acc: 1.000000; val_acc: 0.171000
(Epoch 26 / 50) train acc: 1.000000; val_acc: 0.168000
(Epoch 27 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 28 / 50) train acc: 1.000000; val_acc: 0.171000
(Epoch 29 / 50) train acc: 1.000000; val_acc: 0.177000
(Epoch 30 / 50) train acc: 1.000000; val_acc: 0.166000
(Iteration 31 / 50) loss: 0.054953
(Epoch 31 / 50) train acc: 1.000000; val acc: 0.163000
(Epoch 32 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 33 / 50) train acc: 1.000000; val acc: 0.164000
(Epoch 34 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 35 / 50) train acc: 1.000000; val_acc: 0.163000
(Epoch 36 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 37 / 50) train acc: 1.000000; val_acc: 0.164000
(Epoch 38 / 50) train acc: 1.000000; val_acc: 0.165000
(Epoch 39 / 50) train acc: 1.000000; val_acc: 0.171000
(Epoch 40 / 50) train acc: 1.000000; val_acc: 0.171000
(Iteration 41 / 50) loss: 0.037822
(Epoch 41 / 50) train acc: 1.000000; val_acc: 0.168000
(Epoch 42 / 50) train acc: 1.000000; val_acc: 0.168000
(Epoch 43 / 50) train acc: 1.000000; val_acc: 0.171000
(Epoch 44 / 50) train acc: 1.000000; val_acc: 0.172000
(Epoch 45 / 50) train acc: 1.000000; val acc: 0.171000
(Epoch 46 / 50) train acc: 1.000000; val acc: 0.168000
(Epoch 47 / 50) train acc: 1.000000; val acc: 0.168000
(Epoch 48 / 50) train acc: 1.000000; val_acc: 0.169000
(Epoch 49 / 50) train acc: 1.000000; val_acc: 0.168000
(Epoch 50 / 50) train acc: 1.000000; val_acc: 0.169000
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