

$$\boxed{A1} + \boxed{A2} + \boxed{A3}$$

Essendo l'urto di tipo elastico, si conserva l'energia cinetica. Quindi nessuna variazione né di velocità né di E. cinetica né di quantità di moto.

$$\boxed{A4} \quad p = m \cdot v = 1 \cdot 3 = \boxed{3 \text{ Kg } \frac{\text{m}}{\text{s}}}$$

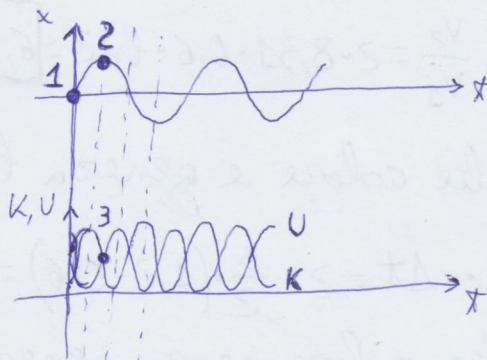
$$\boxed{A5} \quad p = F \cdot \Delta t$$

$$F = \frac{p}{\Delta t} = \frac{3}{0,03} = \boxed{100 \text{ N}}$$

$$\boxed{B1} \quad \omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{4}{1}} = \boxed{2 \text{ rad/s}}$$

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{2} = \boxed{\pi \text{ s}}$$

$$f = \frac{1}{T} = \boxed{\frac{1}{\pi} \text{ Hz}}$$



- 1: a riposo
- 2: massima elongazione
- 3: punto di equilibrio

$$\boxed{B2} + \boxed{B3} + \boxed{B4} + \boxed{B5} + \boxed{B6}$$

Caso 1:

$$x(t) = 2 \sin(2t)$$

$$v(t) = 4 \cos(2t)$$

$$a(t) = -8 \sin(2t)$$

$$U = \frac{1}{2} k x^2 = \frac{1}{2} (4 \sin(2t))^2 = 8 \sin^2(2t)$$

$$K = \frac{1}{2} m v^2 = \frac{1}{2} (4 \cos(2t))^2 = 8 \cos^2(2t)$$

Caso 2:

$$x(t) = 2 \cos(2t)$$

$$v(t) = -4 \sin(2t)$$

$$a(t) = -8 \cos(2t)$$

$$U = \frac{1}{2} k x^2 = \frac{1}{2} (2 \cos(2t))^2 = 8 \cos^2(2t)$$

$$K = \frac{1}{2} m v^2 = \frac{1}{2} (-4 \sin(2t))^2 = 8 \sin^2(2t)$$

Caso 3:

$$\frac{1}{2} m v^2 = \frac{1}{2} k x^2$$

$$\frac{k}{m} = \frac{v^2}{x^2} \Rightarrow \frac{v}{x} = \sqrt{\frac{k}{m}}$$

$$\frac{4 \cos(2t + \varphi)}{2 \sin(2t + \varphi)} = \sqrt{\frac{4}{1}}$$

$$2 \cotan(2t + \varphi) = 2$$

$$\cotan(2t + \varphi) = 1$$

$$2t + \varphi = \arccot(1)$$

$$2t + \varphi = \frac{\pi}{2}$$

$$\varphi = \frac{\pi}{2}$$

Si applicano le formule del caso 1 con l'aggiunta della fase $\frac{\pi}{2}$

C1

$$P_1 = 5 \text{ N/m}^2$$

$$V_1 = 2 \text{ m}^3$$

$$T_1 = \frac{P_1 V_1}{nR} = \frac{5 \cdot 2}{2 \cdot 8,31} = 0,6 \text{ K}$$

$$P_2 = \frac{nRT_2}{V_2} = \frac{2 \cdot 8,31 \cdot 0,6}{4} = 2,49 \text{ N/m}^2$$

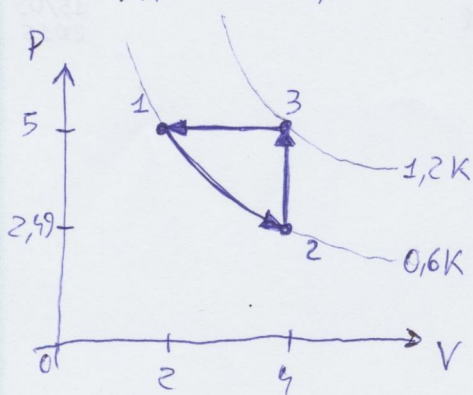
$$V_2 = 4 \text{ m}^3$$

$$T_2 = 0,6 \text{ K}$$

$$P_3 = 5 \text{ N/m}^2$$

$$V_3 = 4 \text{ m}^3$$

$$T_3 = \frac{P_3 V_3}{nR} = \frac{5 \cdot 4}{2 \cdot 8,31} = 1,2 \text{ K}$$



C2 + C3 + C4

$$L_{12} = Q_{12} = nRT \ln \frac{V_2}{V_1} = 2 \cdot 8,31 \cdot 0,6 \cdot \ln 2 = 6,91 \text{ J}$$

(Isoterma. Assorbe calore e genera lavoro)

$$L_{23} = 0 \quad Q = ncv \Delta T = 2 \cdot \frac{3}{2} \cdot 8,31 \cdot (1,2 - 0,6) = 3 \cdot 8,31 \cdot 0,6 = 14,96 \text{ J}$$

(Isocora. Assorbe calore senza generare lavoro)

$$L_{31} = P \cdot \Delta V = 5 \cdot (-2) = -10 \text{ J} \quad Q = ncp \Delta T = 2 \cdot \frac{5}{2} \cdot 8,31 \cdot (0,6 - 1,2) = 5 \cdot 8,31 \cdot (-0,6) = -24,93 \text{ J}$$

(Isobara. Rilascia calore e subisce lavoro)

$$L_T = 6,91 + 0 - 10 = -3,09 \text{ J} \quad [\text{Subisce lavoro}]$$

$$Q_T = 6,91 + 14,96 - 24,93 = -3,06 \text{ J} \quad [\text{Rilascia calore}]$$