



**LOUISIANA STATE UNIVERSITY**  
**College of Agriculture**  
**School of Plant, Environmental, and Soil Sciences**  
**AGRO 7075 Prediction-based Breeding**



**G x E**

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## Basic concepts

- **Environment** - all not genetic features affecting the plant development
  - *edaphoclimatic conditions, harvest, year, management, diseases...*
- Agriculture has evolved into greater environmental control
  - *fertilizers, pest and disease control, irrigation, **GMOs**...*
- One cultivar can be extremely productive in one environment but not in another
- **Genotype x Environment**: differential performance of genotypes as a function of environment variations
- $P = G + E + GE$

# Main causes of GxE

- **Predictable factors**

- Agricultural practices
- Soil physical composition
- Sowing method
- Photoperiod
- Soil fertility
- Aluminum toxicity

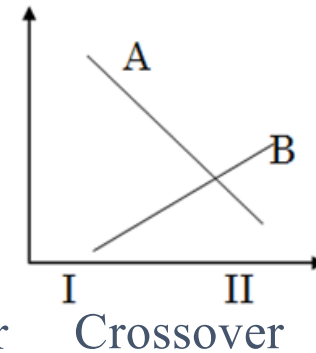
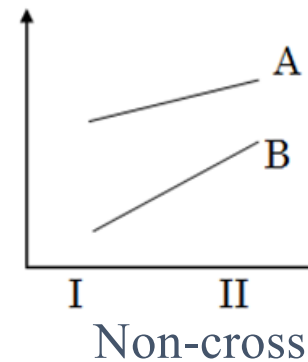
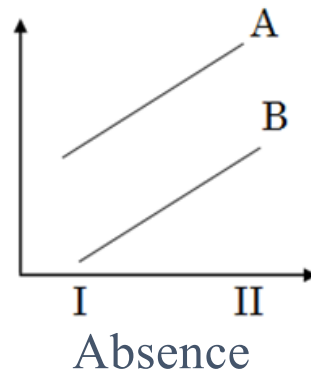
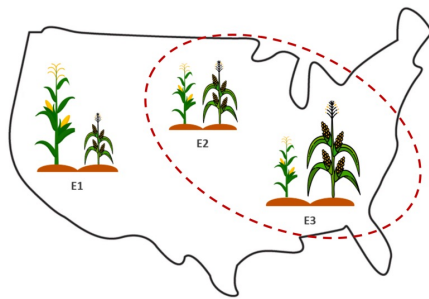
- **Unpredictable factors**

- Relative humidity of the air
- Rainfall distribution
- Atmospheric and soil temperature
- Pathogens
- Insects
- Diseases

**Genetic composition**  
**E.g., Hybrids vs Inbreds**

**Improvement for biotic and  
abiotic stress conditions**

# Genotype x Environment types

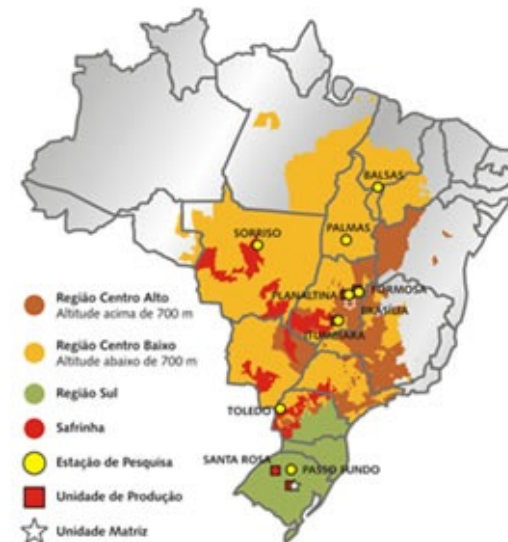


- **Which is the most common one?**
- It depends on the crops and trait
- **What is the desirable type?**
- It depends on the target trait (*productivity vs. diseases vs. flowering*)
- the objective (*specific or mega environments*),
- And the seed market

# GxE implications

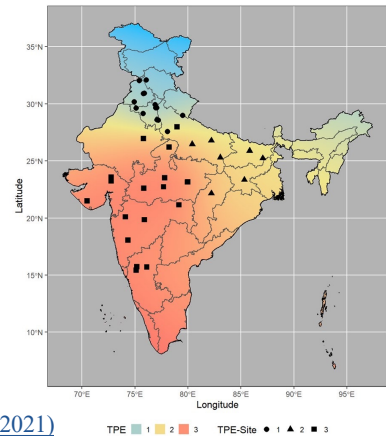
- A material recommended for one location, is not for another
- An improvement program at each location - **high cost**
- It makes it **difficult** to obtain cultivars of **wide adaptability**
- Preserves genetic variability - prevents only one genotype in large areas - **genetic vulnerability**

The more advanced the breeding program and the market, the greater the tendency to capitalize on GxE



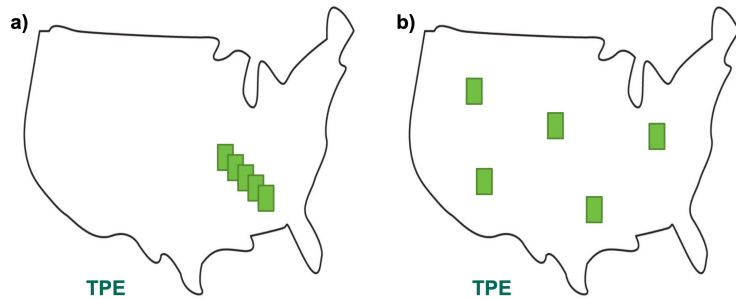
# Target Population of Environments (TPE)

- The set of **farms** and future **seasons** in which the **varieties** released by a breeding program **will be grown**
- Environment (**predictable and non-predictable ones**)
- Socio-economic factors
- Management / Production system (**DRS or transplanted; available technology; hybrids, lines, clones; use of fertilizer and plant protection**)
- Market preferences (**type of grain, color, composition, ...**)
- Frontiers (**transit and trade are not allowed**)
- **What is the difference between mega-environment and TPE?**
- *Clusters that minimize GxE intra ME, then combine the other layers*



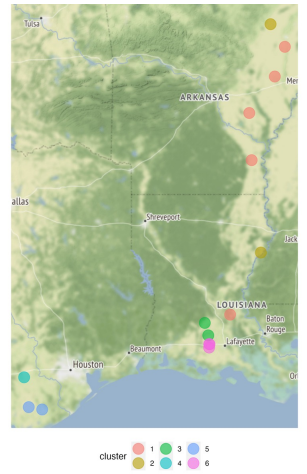
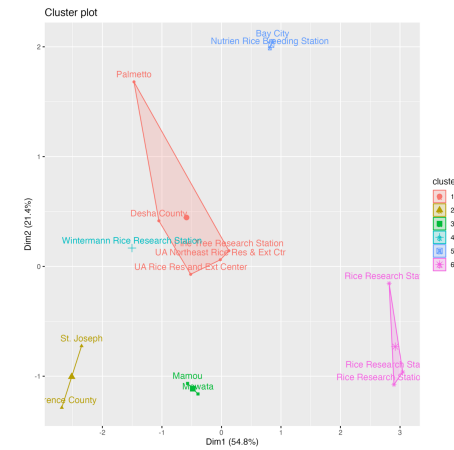
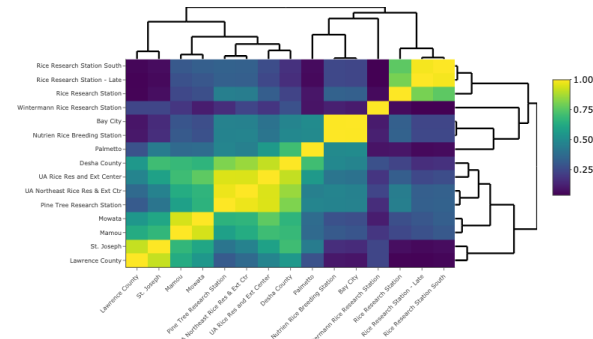
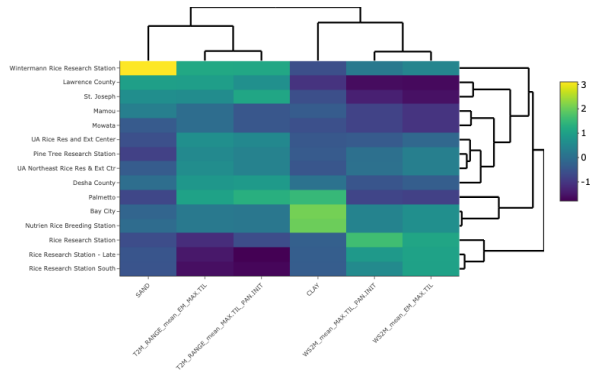
[Crespo-Herrera et al \(2021\)](#)

# Number of locations vs. number of environments



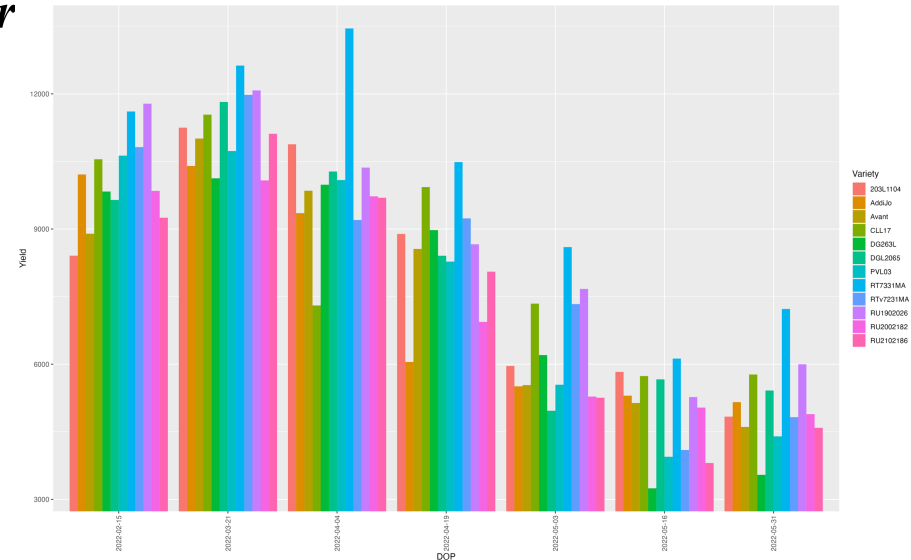
## Overall trend:

- Minimize the number of **replicates** and maximize the number of **“unique” locations**
- Sparse designs (**later...**)



# Choosing locations for MET

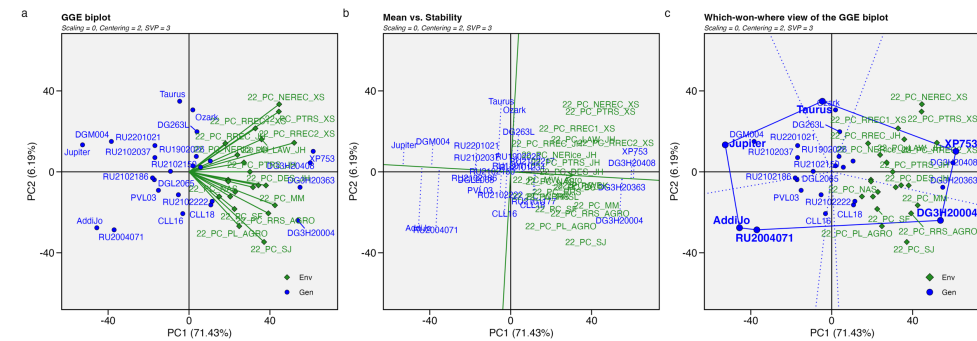
- The ideal environment should:
  - a) promote the expression of the *genotype's performances*
  - b) maximize the *genetic variance*
  - c) *minimize* the variance of environment and *GxE* interaction
  - d) have *consistent* characteristics from year to year
  - e) *represent* the actual farming environment
  - f) Be *accessible*
  - g) represent the actual *market*





# Environmental stratification - mega-environments

- **Tests:** the costliest phase
- **Mega-environment:** minimum GxE variance within group and maximum between
- **Optimize:** trials, replicates, and allocation
- **KPI:** broad-sense heritability (repeatability)



Observed phenotype

$$y_{ijk} = \mu + g_i + t_j + gt_{jk} + e_{ijk}$$

Surrogate of genetic value (estimate we select on)

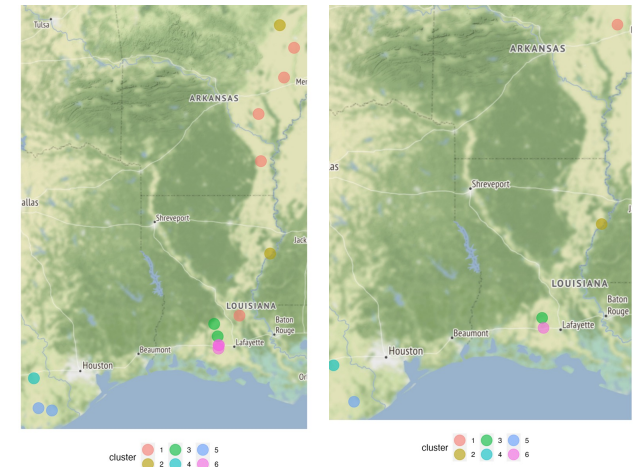
Confounding factors

Random error (what we want to reduce)

Systematic confounding factors

- Correct for the environmental effect
- Correct for (and use) GxE interaction effect

$$H^2 = \frac{\sigma_g^2}{\sigma_p^2} = \frac{\sigma_g^2}{\sigma_g^2 + \frac{\sigma_{gxe}^2}{nEnv} + \frac{\sigma_e^2}{nEnv * nRep}}$$



## Estimating GxE

- At least two genotypes and two environments

Yield	Env 1	Env 2	Total (Ti.)	SV	DF	E(MS)	F
Genotype A	10	09	19	Blocks:Env	(b-1)a	Ve + gVb	
Genotype B	08	12	20	Enviroments (A)	a-1	Ve + gVb + gbVa	MSA / MSB
Total (Y.j)	18	21	39 (Y.)	Genotypes (G)	g-1	Ve + ba*Vga + baVg	MSG / MSGA
				G x A	(a-1)(g-1)	Ve + ba*Vga	MSGA / MSR
				Residual	(a-1)(b-1)a	Ve	

$$C = \frac{Y_{..}^2}{N} \quad SQA = \frac{\sum Y_{.j}^2}{I} - C \quad SQG = \frac{\sum Y_{i.}^2}{J} - C$$

$$SQTotal = \sum Y_{ij}^2 - C \quad SQ_{GxA} = SQtotal - SQA - SQG$$

- The principle is the same for DOP, year, location, N, etc.
- What happens when we have a 100% crossover GxE?
- Genotypes, environments and GxE interaction - fixed or random?

## Decompose GxE into simple and complex

- $MS_{G \times E} = \text{simple} + \text{complex}$

$$MS_{G \times E} = 1.72$$

- *Simple*

$$S = \frac{1}{2}(\sqrt{Q_1} - \sqrt{Q_2})^2$$

$$S = 0.01 = 0.06\%$$

- *Complex*

$$C_1 = (1 - r)\sqrt{Q_1 \cdot Q_2}$$

$$C = 1.71 = 99.4\%$$

- *Example:*

SV	DF	MS	
		ENV 1	ENV 2
Genotypes	255	5.73	4.96
Residual	224	1.47	1.53

$$(r = 0.68)$$

SV	DF	MS
Environments	1	113.30
Genotypes	255	5.09
G x E	255	6.52
Residual	450	1.50

# Effects on Response to Selection

- You can increase the decrease in gains with the selection

$$RS = i \cdot h \cdot \sigma_a \quad \sigma_{G(i1)}^2 = \sigma_{Gi}^2 + \sigma_{GE(i1)}^2$$

- Selection and response in the same environment - capitalizes on GxE

$$\sigma_{G(i1)}^2 = \sigma_{Gi}^2 + \sigma_{GE(i1)}^2 \quad \sigma_{G(i2)}^2 = ? \quad COV(Y_{ij}; Y_{ij}') = \sigma_G^2 - \sigma_{GE}^2 \quad r_g = \frac{\hat{\sigma}_g^2 - \hat{\sigma}_{ge}^2}{\sqrt{\hat{\sigma}_{g1}^2 \cdot \hat{\sigma}_{g2}^2}}$$

- Selection in one and response in another contrasting environment

Average environments – minimize GxE

$$H^2 = \frac{\sigma_g^2}{\sigma_p^2} = \frac{\sigma_g^2}{\sigma_g^2 + \frac{\sigma_{gxe}^2}{nEnv} + \frac{\sigma_e^2}{nEnv * nRep}}$$

Specific environment – capitalize GxE

$$V_{(y)} = Vg + Ve/r$$



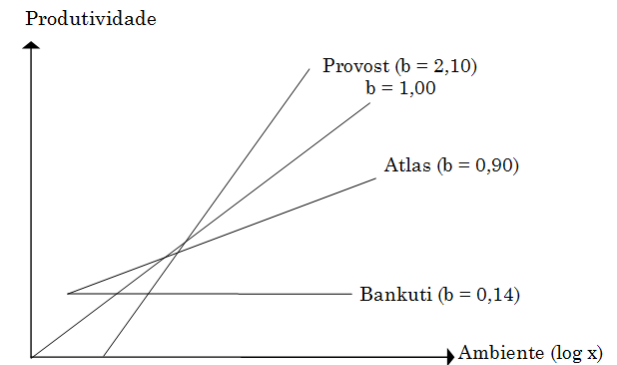
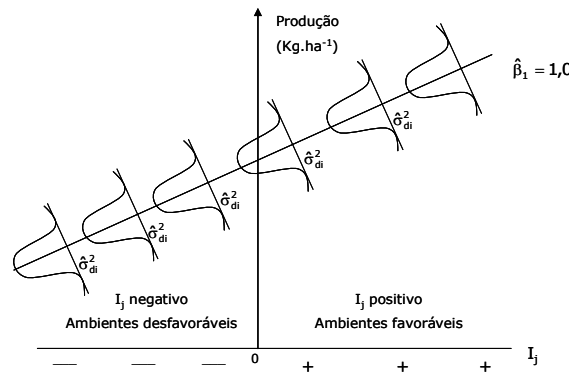
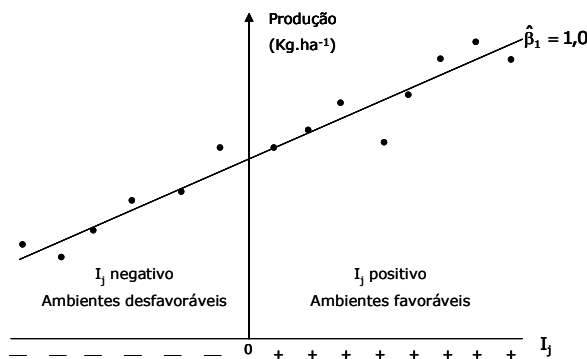
$$Vg = Vg + Vg * year + Vg * loc + Vg * season + Vg * M...$$

# Adaptability and stability – Regression methods

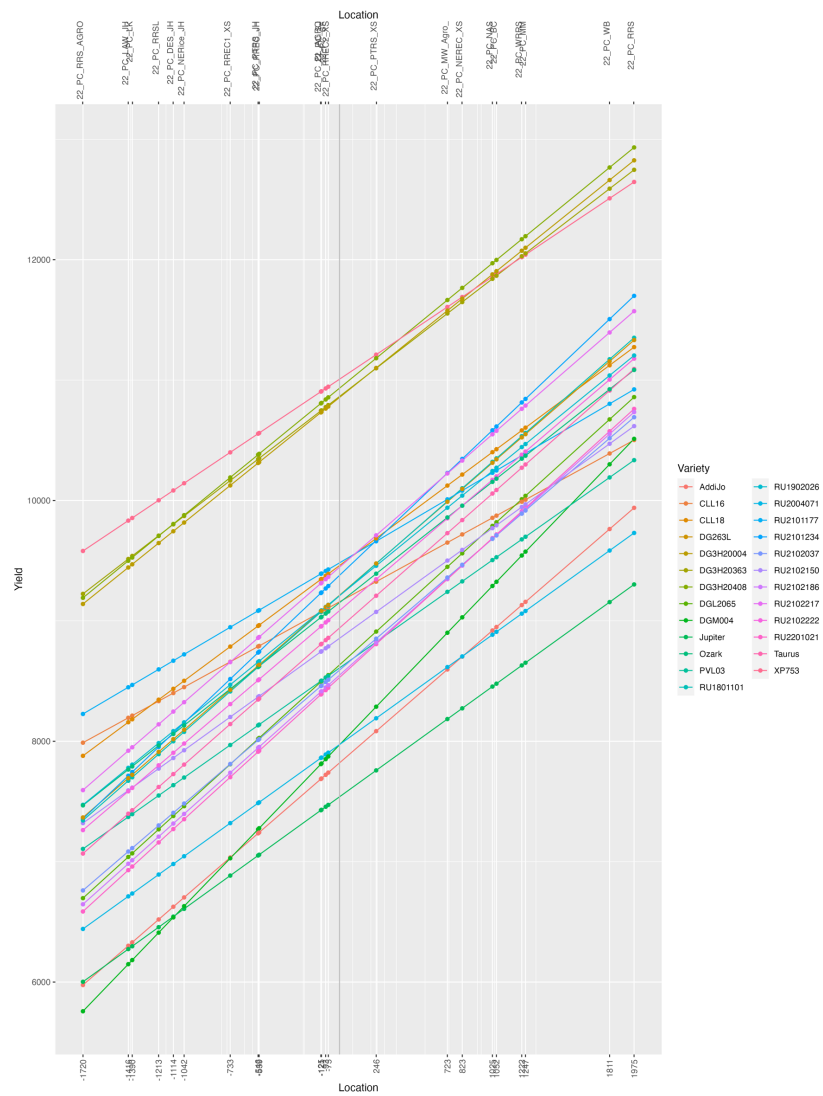
- **Adaptability:** ability to take advantage of environmental variations
- **Stability:** predictable behavior in the face of variations in the environment
- **Finlay K, Wilkinson G (1963):** Linear regression coefficient and the variance of the regression deviations

$$I_j = \bar{I}_{..j} - \bar{Y}_{..}$$

$$Y_{ij} = m_i + b_i I_j + d_{ij}$$



- $d_{ij}$ : regression deviations predictability (*stability*)
- *What would be the ideal cultivar?*
- $Y_{ij}$ : high overall performance
- $b_i = 1.0$
- $d_{ij} = 0$



# HMRPGV

- Harmonic Mean of Relative Performance of Genotypic Values - *Linn & Binns (1988)* via Mixed Models (*Resende, 2007*)
- First, estimate the genotypic values for each individual in each environment
- **Then, estimate the harmonic average (*HMRPGV*):**

$$H = \frac{n}{\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} + \dots + \frac{1}{x_n}} \quad HMRPGV_i = \frac{E}{\sum_{j=1}^E \frac{1}{Gv_{ij}/\mu_j}}$$

- Select individuals with a **good baseline performance** and **minimum variation**
- Also good for many levels of stress conditions

## Multiplicative models: GGE-Biplot

- **GGE** stands for genotype main effect (G) + the interaction (GE), which is the only source of variation relevant to cultivar evaluation
- Mathematically, GGE is the genotype by environment data matrix **after the environment means are subtracted**
- The biplot is constructed by the first two symmetrically scaled principal components (**PC1 and PC2**) derived from singular value decomposition (**SVD**) of environment-centered MET data
- **SVD creates three matrices**: the singular value matrix, the entry eigenvector matrix, and the tester eigenvector matrix
- A biplot graphically displays the **interrelationship** among the entries (e.g., genotypes), testers (e.g., environments), **and the interaction** between them



# Multiplicative models - GGE-Biplot

- The mean yield of genotype  $i$  in environment  $j$  is commonly described by a general linear model:

$$\hat{y}_{ij} = \mu + \alpha_i + \beta_j + \phi_{ij}$$

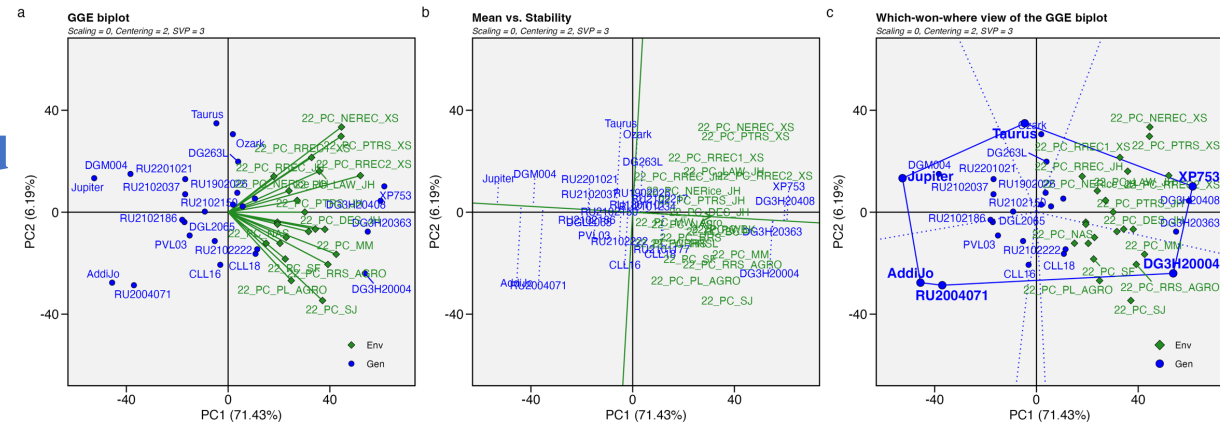
- Environment means are subtracted**

$$\phi_{ij} = \hat{y}_{ij} - \mu - \beta_j = \sum_{k=1}^p \xi_{ik}^* \eta_{jk}^*$$

- Apply SVD**

where  $\xi_{ik}^* = \lambda_k^\alpha \xi_{ik}$ ;  $\eta_{jk}^* = \lambda_k^{1-\alpha} \eta_{jk}$  being  $\lambda_k$  the  $k$ th eigenvalue from the SVD ( $k = 1, \dots, p$ ), with  $p \leq \min(e, g)$ ;  $\alpha$  is the singular value partition factor for the Principal Component (PC)  $k$ ;  $\xi_{ik}^*$  and  $\eta_{jk}^*$  are the PC scores for genotype  $i$  and environment  $j$ , respectively.

**Always use phenotypes in analyses!!!**



# Sparse-Testing

- **Experimental designs:** understand and control the effect of the environment (year x location combination) on the phenotype
- **Replications within environments, row and column:** control micro-environmental spatial variation within locations. Estimate the blocks, spatial trends, and residual effects.
- **Trials are replications across locations and years:** control macro-environmental spatial and seasonal variation. Estimate the effects of years, locations, and GxE interaction effects.
- When is it possible? From which breeding stage?
- **Sparse designs:** alleles are replicated across locations, not individuals
- **Sparse + GS + W:** a way to select for GxE in the early stages

