

Sept. 3/19

Mechatronics Lab: (CB-1034)

No tutorial this week.

→ Matlab used for assignments (15%)

↳ 5 assignments total

→ 3 lab sessions

↳ 1 lab report

↳ Wang using course website on Flash, not D2L

Chapter 1 - Introduction

(1.1) - overview

→ Signal process: to extract representative features for advanced analysis

→ pattern classification (diagnostics)

→ modeling (forecasting)

→ control

(1.2) - maintenance strategies

→ run-to-break

→ preventative maintenance ($\geq 25\%$)

↳ periodically shut down machine for maintenance

↳ unnecessary downtimes

→ predictive maintenance (research state)

↳ condition monitoring → recognize defects

↳ predict the remaining useful life of the faulty component

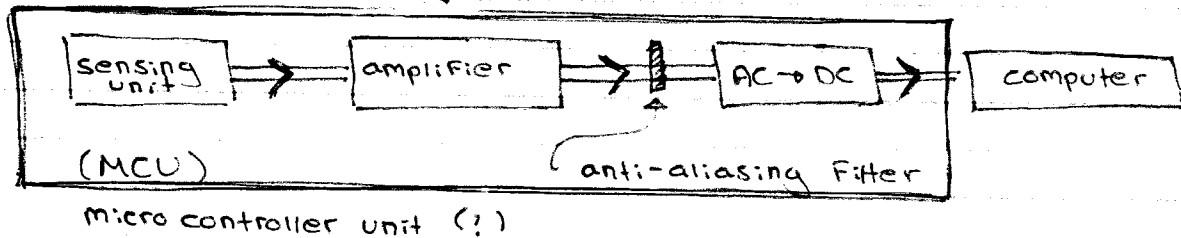
↳ schedule maintenance operations

- literature review, discuss the maintenance strategies

Condition monitoring

- recognize the defects at its earliest stage
- Prevent machinery performance degradation, malfunction, failure.

Smart Sensors



(1.3) - approaches to Fault detection

① classical approaches ~ biological sense

- looking
- listening
- touching
- Smelling

② Automatic diagnosis

- Analytical model

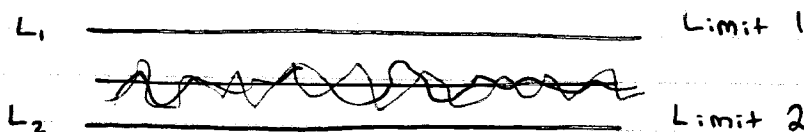


diff. equations

- Signal Processing - based

③ Monitoring

- limit checking
- index

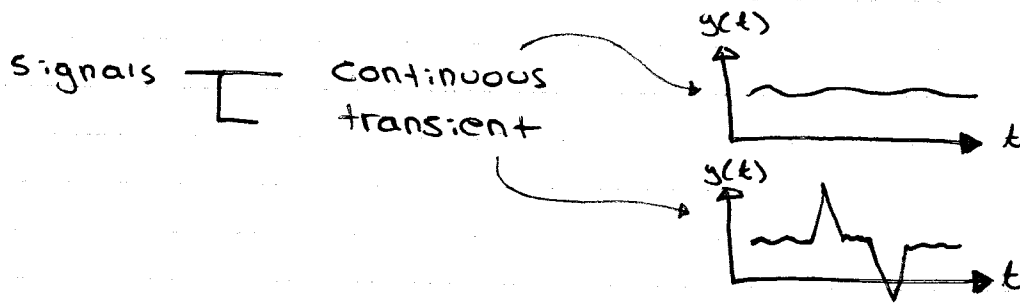


Chapter 2 - Introduction to Signals & Systems

(2.1) - Signal Classification

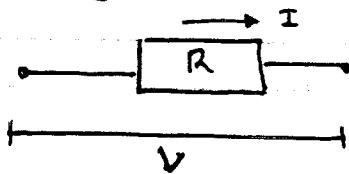
< deterministic (inputs, outputs)
 Random (statistical quantities, mean, std.)

e.g. $y(t) = 28^{32(t)}$



Signals $\begin{cases} \text{stationary} & (\text{statistical quantities don't change w/time}) \\ \text{non-stationary} & (\text{change w.r.t. time}) \end{cases}$

Enough power



$$\text{Energy} = I^2 R^1 = \frac{V^2}{R=1}$$

(if $R=1$, then) $= I^2 = V^2$

$$\text{Energy} = \int x^2(t) dt$$

I^2
 V^2



Sep. 5/19

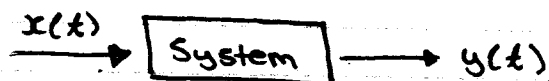
(2.2) - System Properties

1) Causality

@ any time t , $y(t) \sim x(t)$

$$x(t) \longleftrightarrow y(t)$$

$$t \leq t_1$$

Output $y(t_1)$ depends on $x(t) | t \leq t_1$.Not depending on its future input
 $x(t) | t > t_1$.System \rightarrow Causal

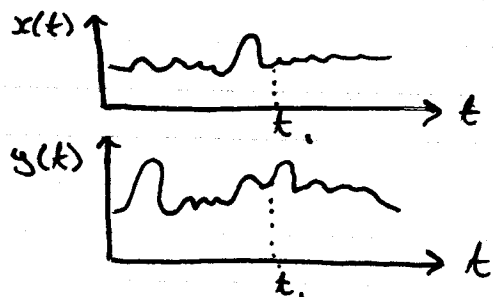
Real systems are causal

- Assume no initial energy

$$y(t) = x^2(t) + \underbrace{1}_{\text{initial energy}}$$

$$\text{When } x(t) = 0, y(t) = 0$$

$$y(t) = x^2(t)$$



EX1

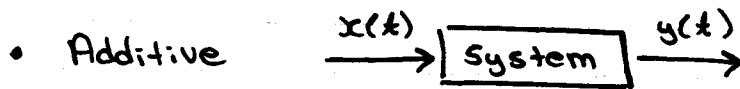
$$y(t) = 3x(t+1)$$

$$t = 1$$

$$y(t) |_{t=1} = 3x(t+1)$$

 \hookrightarrow non-causal
offline processing
diagnostics

2) Linearity:



Input	Output
$x_1(t)$	$y_1(t)$
$x_2(t)$	$y_2(t)$

Additive: $x_1 + x_2$

$y_1 + y_2$

→ If the output is a sum, the system can be considered additive

• Homogeneous

Input	Output
$x_1(t)$	$y_1(t)$
homogeneous: $a x_1(t)$	$a y_1(t)$

→ output is ... scaled by same amount as input

• Linear ~ additive + homogeneous

Input	Output
linear: $a x_1(t) + b x_2(t)$	$a y_1 + b y_2$

EX2

$$y(t) = t x(t)$$

Input	Output
$x_1(t) = u$	$y_1 = t u$
$x_2 = 3u$	$3 y_2 = 3 t u$
$x_3 = x_1 + x_2$	$y_3 = 4 t u$
$= 4u$	

$$y_3 = 4 t u = y_1 + y_2 = \underline{\text{linear}} \quad \rightarrow \quad (y_1 + y_2 = y_3)$$

EX3

$$y(t) = x^2(t)$$

Input	Output
$x_1 = u$	$y_1 = u^2$
$x_2 = 3u$	$y_2 = 9u^2$
$x_3 = 4u$	$y_3 = 16u^2$

$$y_1 + y_2 = 10u^2 \neq y_3 \quad \underline{\text{non-linear}}$$

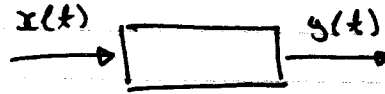
Linear System

↳ Superposition depends on this

3) Time Invariance

Input
 $x(t)$

Output
 $y(t)$



Shifted input $x(t-t_1)$, $y(t-t_1)$

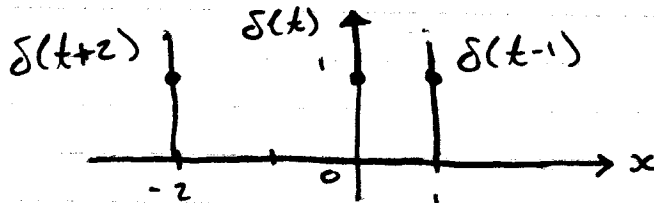
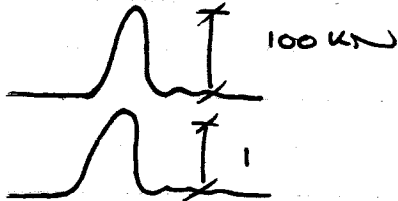
$t_1 = \text{number}$

time invariant

- System properties don't change with time

impulse
 $\delta(t)$

$$\delta(t) = \begin{cases} 1, & t = 0 \\ 0, & \text{otherwise} \end{cases}$$



basically, input has shift, output has corresponding shift.

$$\begin{aligned} t_1 &= 1 > 0 \\ \text{then } \delta(t-t_1) &= \delta(t-1) \\ t_1 &= -2 < 0 \\ \text{then } \delta(t-t_1) &= \delta(t+2) \end{aligned}$$

Ex4

$$y(t) = x^2(t) + 3$$

Input

$$x_1(t) = x(t)$$

$$x_2(t) = x(t-t_1)$$

Time Invariant

Output

$$y_1 = x^2(t)$$

$$y_2 = x^2(t-t_1)$$

EX5

$$y(t) = t x(t)$$

Input

$$x_1(t) = x(t)$$

$$x_2 = x(t - t_1)$$

Output

$$y_1 = t x(t)$$

$$y_2 = t x(t - t_1)$$

#

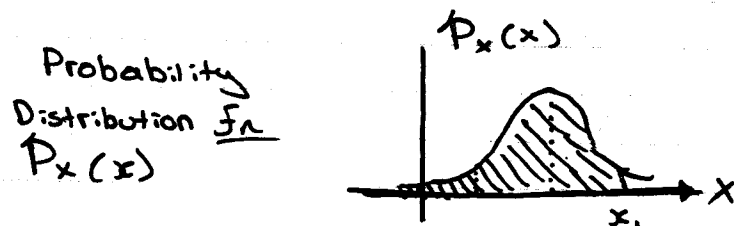
$$y_3(t) | t = t - t_1$$

$$= y(t - t_1) = (t - t_1) x(t - t_1)$$

In signal processing,

Assume: casual, linear, time invariant

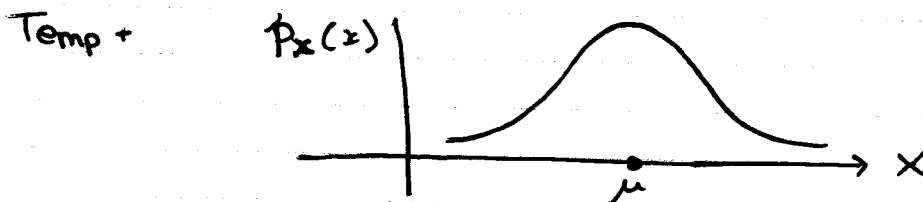
(2.3) - Review of Statistical Quantities

① Probability f_n Random variable X Probability of $P_x = \text{Prob}(x \leq x_1)$

$$P_x = \int_{-\infty}^{x_1} p_x(x) dx$$

$$p_x(x) \geq 0$$

$$\int_{-\infty}^{\infty} p_x(x) dx = 1$$



Gaussian probability density function (PDF)

$$p_x = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

 μ = mean σ = st. d σ^2 = variance