

OCT. 31/18

Fick's Laws (where $T = \text{const.}$)

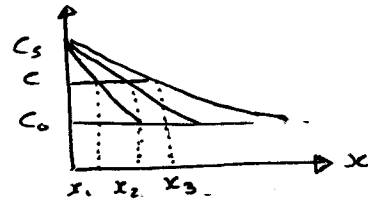
$$\frac{C(x_i, t_i) - C_0}{C_s - C_0} = 1 - \text{erf}\left(\frac{x_i}{2\sqrt{Dt_i}}\right)$$

$$\text{erf}\left(\frac{x_i}{2\sqrt{Dt_i}}\right) = \text{const.}$$

$$\frac{x_i}{2\sqrt{Dt_i}} = \text{const.}$$

$$\text{If } T \text{ is constant, } \frac{x_1}{\sqrt{D_1 t_1}} = \frac{x_2}{\sqrt{D_2 t_2}}$$

$$\hookrightarrow D \text{ is constant} \rightarrow \frac{x_1}{\sqrt{t_1}} = \frac{x_2}{\sqrt{t_2}} \rightarrow \frac{x_1^2}{t_1} = \frac{x_2^2}{t_2}$$

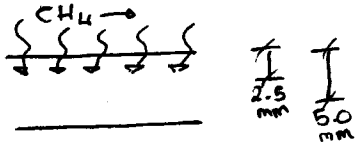


$$C(x_1, t_1) = C(x_2, t_2) = C(x_3, t_3) = C(x_i, t_i)$$

Example

$$@ x = 2.5 \text{ mm}, t = 10 \text{ hrs}, C(x, t) = 0.45 \text{ wt.}\%$$

$$@ x = 5.0 \text{ mm}, t = ?, C(x, t) = 0.45 \text{ wt.}\%$$

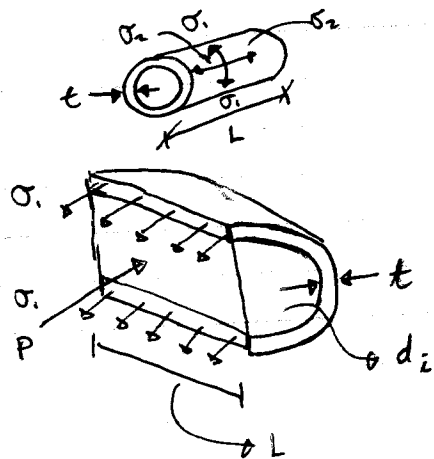


$$\frac{x_1}{\sqrt{D_1 t_1}} = \frac{x_2}{\sqrt{D_2 t_2}} ; \frac{x_1}{x_2} = \frac{\sqrt{t_1}}{\sqrt{t_2}}$$

$$\therefore t_2 = 40 \text{ hours}$$

→ need to use error packing function, interpolation
 ↳ basically, assignment questions.

Example A



σ_1 : Circumferential stress - makes the diameter bigger (hoop stress)

σ_2 : longitudinal stress - makes the length bigger

where $\sigma_1 = 2\sigma_2$

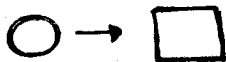
$$\sigma_1 = \frac{Pr_i}{2t}$$

$$\sigma_1 = \sigma_w = \frac{\sigma_y}{N} = \frac{r_i \Delta P}{t}$$

$$\sigma_y = \frac{Nr_i \Delta P}{t} = 4 \times 50 \times 10^{-3} \text{ m} \times (20 - 0.5) \times \frac{101 \times 10^3 \text{ N/m}^2}{1 \text{ atm}}$$

$$\sigma_y = 1907 \text{ MPa, (steel, copper, brass, titanium)}$$

→ Lecture 9: Example



$$\sigma_{fs} = \frac{F_s L}{\pi R^3} \Rightarrow \frac{(950 \text{ N})(50 \times 10^{-3} \text{ m})}{\pi (3.5 \times 10^{-3} \text{ m})^3} = 352 \times 10^6 \text{ N/m}^2$$

$$\sigma_{fs} = \frac{3F_s L}{2bd^2} \Rightarrow F_s = \frac{2d^2 \sigma_{fs}}{3L} = \frac{2 \times (12 \times 10^{-3} \text{ m})^3 \times (352 \times 10^6 \text{ N/m}^2)}{3 \times (40 \times 10^{-3} \text{ m})} = 10138 \text{ N}$$