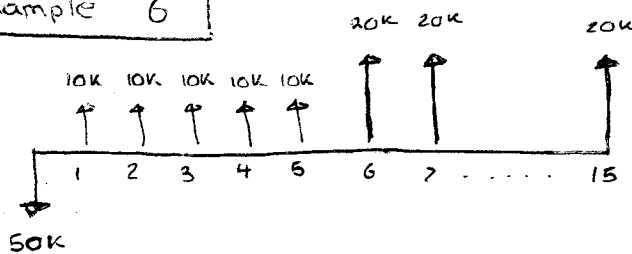


## Example 6



MARR = 9%

AE = ?

$$PW(9\%) = -5000 + 10000(P/A, 9\%, 5) + 20000(P/A, 9\%, 10)(P/F, 9\%, 5)$$

$$= 73318$$

$$AE(9\%) = PW(A/P, 9\%, 15)$$

$$= 73318(A/P, 9\%, 15)$$

$$\hookrightarrow = 9096$$

AE > 0 (accept or recommend)

## Example 7

First cycle ⚡ MARR = 12% (not given in question)

$$\rightarrow PW(12\%) = -1000000 + 800000(P/A, 12\%, 4) - 100000(P/G, 12\%, 4)$$

$$= 1017150$$

$$\rightarrow AE(12\%) = PW(A/P, 12\%, 4)$$

$$= 1017150(A/P, 12\%, 4)$$

$$= 334880$$

Two cycles

$$\rightarrow PW(12\%) = -1000000 - 1000000(P/F, 12\%, 4) \dots$$

$$\dots + 800000(P/A, 12\%, 8) - 100000(P/G, 12\%, 4) \dots$$

$$\dots - 100000(P/G, 12\%, 4)(P/F, 12\%, 4)$$

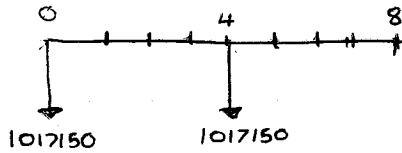
$$PW(12\%) = 1663560$$

$$\rightarrow AE(12\%) = 1663560(A/P, 12\%, 8)$$

$$= 334880 \text{ (same as one cycle)}$$

Simplify:

→ 2 cycles



### Example 8

Capital cost

$$\begin{aligned} CR(10\%) &= (P - S)(A/P, 10\%, 5) + 5i \\ &= (20000 - 4000)(A/P, 10\%, 5) + (4000)(0.10) \\ &= 4620.76 \end{aligned}$$

$$\begin{aligned} \text{Total Annual Cost} &= \text{Cap. cost} + \text{Oper. cost} \\ &= 4620.76 + 500 \\ &= 5120.76 \end{aligned}$$

→ Compare to 5000 per year

### Example 9

$$PW(15\%) = 3553$$

$$\begin{aligned} AW(15\%) &= 3553(A/P, 15\%, 3) \\ &= 1556 \end{aligned}$$

Savings per machine hour

$$\Rightarrow \frac{1556}{2000} = 0.78/\text{hr}$$

## START CLASS NOTES 6

Break-even interest rate :  $i^*$

Simple investments change sign once

### Example 3

$$PW(i^*) = -1250000 + 731500(P/A, i^*, 15) + 80000(P/F, i^*, 15) = 0$$

$$i^* = 58.71\% \quad (\text{from software})$$

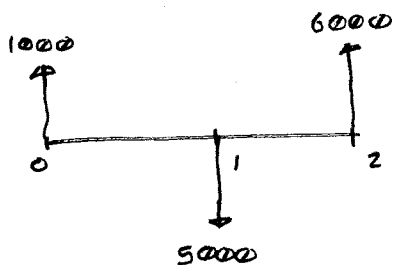
$$MARR = 18\%$$

$$IRR > MARR \quad (\text{accept or recommend})$$

$$PW(18\%) = -1250000 + 731500(P/A, 18\%, 15) + 80000(P/F, 18\%, 15)$$

$$\rightarrow > 0; \quad \text{so} \quad IRR > MARR$$

### Example 5



$$MARR = 25\%$$

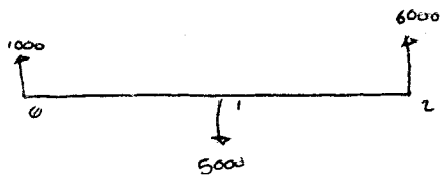
Non-simple inv.

ERR

### Example 5

→ Exact ERR

End of year 1 :



non-simple, more than one sign change, apply ERR  
(otherwise use IRR)

$$FW = 1000(F/P, 25\%, 1) - 5000 = -3750$$

End of year 2

$$FW = -3750(F/P, ERR, 1) + 6000 = 0$$

(Somehow) → Trial and error,  $ERR = 60\%$

$ERR > MARR$  (accept or recommend)

→ Approximate ERR

$$FW(\text{rec}) = 1000(F/P, 25\%, 2) + 6000$$

$$FW(\text{dist}) = 5000(F/P, ERR, 1)$$

$$FW(\text{rec}) = FW(\text{dist})$$

$$1000(F/P, 25\%, 2) + 6000 = 5000(F/P, ERR, 1)$$

$$\text{app ERR} = 61.25\%$$

app ERR > MARR (accept or recommend)

→ BEGIN CLASS NOTES 7

### Example 1

(M.)  $PW(12\%) = -209000 + 55000(P/A, 12\%, 5) + 80000(P/F, 12\%, 5)$   
 $PW(12\%) = 34657$

$M_2$ 

$$PW(12\%) = -294600 + 74000(P/A, 12\%, 5) + 120000(P/F, 12\%, 5)$$

$$PW(12\%) = 40245$$

 $M_3$ 

$$PW(12\%) = -294600 + 58000(P/A, 13\%, 12\%, 5) \dots$$

$$\dots + 120000(P/F, 12\%, 5)$$

$$PW(12\%) = 37085$$

$\therefore M_2$  is the recommended machine

### Example 2

→  $B_2 - B_1$

0	-9000
1	2850
2	4425
3	4830

Simple

IRR

$$PW(IRR) = -9000 + (2850)(P/F, IRR, 1) + (4425)(P/F, IRR, 2) \dots$$

$$\dots + (4830)(P/F, IRR, 3) = 0$$

→  $IRR = 15\%$

$$IRR > MARR$$

15

10

→ The invest is good

$B_2$  is best

### Example 4

Analysis period = 2 years

MARR = 15%

→ Model A

$$\begin{aligned} PW(15\%) &= -300000 - 80000(P/A, 15\%, 2) + 90000(P/F, 15\%, 2) \\ &= -362000 \end{aligned}$$

→ Model B

$$\begin{aligned} PW(15\%) &= -480000 - 45000(P/A, 15\%, 2) + 250000(P/F, 15\%, 2) \\ &= -364000 \end{aligned}$$

→ Model A > Model B, recommend Model A

### Example 5

$$\begin{aligned} PW(15\%) &= -12500 - (5000)(P/A, 15\%, 5) - (10000)(P/A, 15\%, 2)(P/F, 15\%, 3) \\ &\quad \dots + (2000)(P/F, 15\%, 3) = -34359 \end{aligned}$$

Model A

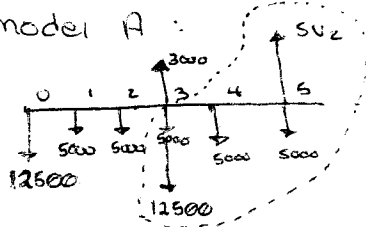
$$\begin{aligned} PW(15\%) &= -15000 - 4000(P/A, 15\%, 4) - (5000 + 11000)(P/F, 15\%, 5) \\ &\quad \dots + (1500)(P/F, 15\%, 4) = -31031 \end{aligned}$$

Model B

→ Model B > Model A, recommend Model B

### Second approach

Model A:



Model B:

