

MARCH 4/19

$$A_A = a\alpha_2 (\underbrace{j\cos\theta_2 + j^2\sin\theta_2}_{A_A^t}) - a\omega_2^2 (\underbrace{\cos\theta_2 + j\sin\theta_2}_{A_A^c})$$

**Example** (Ch. 7, Slide 21)

$$A = 8 \sin 16.5^\circ = 2.271$$

$$B = 6 \sin(-53.1^\circ) = -4.8$$

$$C = 10(-10) \sin(45^\circ) + 10(-5) \cos(45^\circ) + 6(-4.2 \times 3)^2 \cos(-53.1^\circ) \dots \\ \dots - (8)(-6.6)^2 \cos(16.5^\circ) = -163.29$$

$$D = 8 \cos(16.5^\circ) = 7.671$$

$$E = 6 \cos(-53.1^\circ) = 3.6$$

$$F = 10(-10) \cos(45^\circ) - 10(-5)^2 \sin(45^\circ) - 6(-4.243)^2 \sin(53.1^\circ) \dots \\ \dots + 8(6.6)^2 \sin(16.5^\circ) = 62.145$$

$$\alpha_3 = \frac{(-163.29)(7.671) - (2.271)(-62.145)}{(2.271)(3.6) - (-4.8)(7.671)} = -24.7 \text{ rad/s}^2 \text{ (cw)}$$

$$\alpha_4 = \frac{(-163.29)(3.6) - (-4.8)(-62.145)}{(2.271)(3.6) - (-4.8)(7.671)} = -19.7 \text{ rad/s}^2 \text{ (cw)}$$

$$\hat{A}_S = \hat{A}_S^t + \hat{A}_S^c = jS\alpha_2 e^{j(\theta_2 + \delta_2)} - S\omega_2^2 e^{j(\theta_2 + \delta_2)}$$

$$\hat{A}_P = \hat{A}_A + \hat{A}_{PA} = \hat{A}_A^t + \hat{A}_A^c + \hat{A}_{PA}^t + \hat{A}_{PA}^c$$

$$\hat{A}_A^t = ja\alpha_2 e^{j\theta_2} = j10(-10) \cos 45^\circ - 10(-10) \sin(45^\circ) = -j70.7 + 70.7$$

$$\hat{A}_A^c = -a\omega_2^2 e^{j\theta_2} = -10(-5)^2 \cos 45^\circ - j10(-5)^2 \sin(45^\circ) = 176.75 - j176.75$$

$$\hat{A}_{PA}^t = jP\alpha_3 e^{j(\theta_3 + \delta_3)} = j10(-24.7) \cos(-53.1 + 80^\circ) - 10(-24.7) \sin(-53.1 + 80^\circ)$$

$$\hat{A}_{PA}^c = -P\omega_3^2 e^{j(\theta_3 + \delta_3)} = \dots \quad \omega_3 = -j220.3 + 111.75 \\ = (-10)(-4.243)^2 \cos(-53.1^\circ + 80^\circ) - j(-10)(-4.243)^2 \sin(-53.1^\circ + 80^\circ) = -160.6 - j81.45$$

$$\hat{A}_P = -154.9 - j549.2 \text{ cm/s}^2 \quad \swarrow \quad \searrow \quad \text{this is the angle we're finding}$$

$$|\hat{A}_P| = 570.6 \text{ cm/s}^2 \quad \swarrow \quad \searrow \quad \text{(because it's in the third quadrant)}$$

$$\theta = \tan^{-1}\left(\frac{549.2}{-154.9}\right) = 180^\circ + 74.2^\circ = 254.2^\circ$$

Given : a, b, c,  $\theta_2$ ,  $\omega_2$ ,  $\alpha_2$  (slide 24)

Position analysis :  $\theta_3$ , d

Velocity analysis :  $\omega_3$ ,  $\dot{d}$

$$\hat{A}_A = \hat{A}_B + \hat{A}_{AB} = \hat{A}_B + \hat{A}_{BA}^t + \hat{A}_{BA}^n$$

$$\alpha_3 = \frac{2(5) \cos(60^\circ) - (2)(-2)^2 \sin(60^\circ) + 6(0.542)^2 \sin(127.9^\circ)}{6 \cos(127.9^\circ)}$$

$$= 0.146 \text{ rad/s}^2 \text{ (ccw)}$$

$$\ddot{d} = -2(5) \sin(60^\circ) - 2(-2)^2 \cos(60^\circ) + 6(0.146) \sin(127.9^\circ) + 6(0.542)^2 \cos(127.9^\circ) = -13.05 \text{ cm/s}^2$$

Coriolis Acceleration : (slide 26)

$$\hat{A}_p = \ddot{p} e^{i\theta_2}$$

$$\hat{V}_p = \frac{d\hat{R}_p}{dt} = \frac{dp}{dt} e^{i\theta_2} + p \dot{\theta}_2 e^{i\theta_2}$$

$$= \dot{p} e^{i\theta_2} + i p \omega_2 e^{i\theta_2} = \hat{V}_{p, \text{slip}} + \hat{V}_{p, \text{trans}}$$

$$\hat{A}_p = \frac{d\hat{V}_p}{dt} = \ddot{p} e^{i\theta_2} + p \ddot{\theta}_2 e^{i\theta_2} + i \dot{p} \omega_2 e^{i\theta_2} + i p \alpha_2 e^{i\theta_2} + i p \omega_2 \dot{\omega}_2 e^{i\theta_2}$$

$$= \ddot{p} e^{i\theta_2} + 2i \dot{p} \omega_2 e^{i\theta_2} + i p \alpha_2 e^{i\theta_2} - p \omega_2^2 e^{i\theta_2}$$

$$= \hat{A}_{p, \text{slip}} + \hat{A}_{p, \text{coriolis}} + \hat{A}_p^t + \hat{A}_p^n$$

$$\hat{A}_{p, \text{slip}} = \ddot{p} e^{i\theta_2}$$

$$\hat{A}_{p, \text{coriolis}} = 2i \dot{p} \omega_2 e^{i\theta_2} = 2\dot{p} \omega_2 e^{i(\theta_2 + 90^\circ)}$$

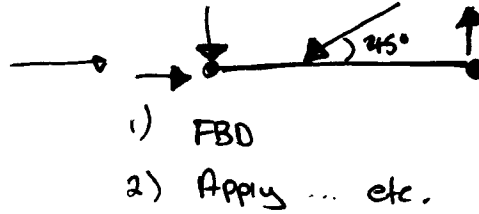
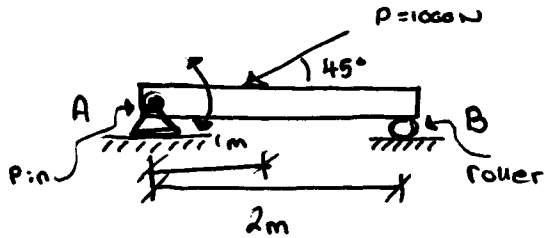
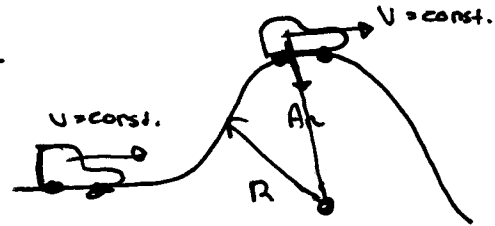
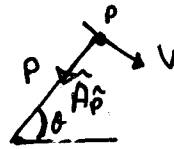
Project :

1st input : from table

2nd input : from table (in degrees)

$$\hat{A}_p^* = -P \left(\frac{V}{P}\right)^2 e^{i\theta}$$

$$\begin{aligned}\hat{A}_p &= \hat{A}_p^* + A_p^* \\ &= 3P\alpha e^{i\theta} - P\omega^2 e^{i\theta}\end{aligned}$$



(Statics review material)

2 Objects { Particles (no size) - a point bodies

$$\begin{cases} \sum F = ma \\ \sum M = I_G \alpha \end{cases}$$

Special cases:

Translational motion:

$$\sum F = ma$$

$$\sum M_G = 0$$

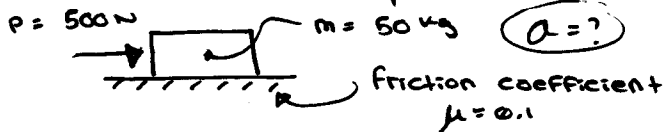


Pure rotation:

$$\sum F = ma_G$$

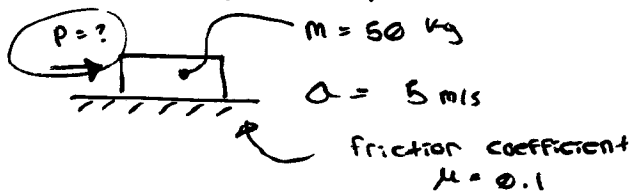
$$\sum M_G = I_G \alpha$$

Forward dynamic problem:



(kinetostatic problem)

Inverse dynamic problem:



$$\textcircled{1} : a = \frac{P-f}{m}$$

$$a = 9.02 \text{ m/s}^2$$

$$\textcircled{2} \quad N = W$$

$$f = \mu N = 9.02 \text{ m/s}^2$$

Centre of gravity of Composite bodies :

$$\bar{X} = \frac{m_A \bar{X}_A + m_B \bar{X}_B}{m_A + m_B}$$

$$\bar{Y} = \frac{m_A \bar{Y}_A + m_B \bar{Y}_B}{m_A + m_B}$$