

JAN. 7 / 20

- Attendance will be done through the Top Hat app.
- Most classes are 1hr. / 5 min. break / 1hr.

Engineering Economics: The science that deals with techniques of quantitative analysis, used for selecting a preferred alternative from technically viable ones.

- Engineering economic analysis are decisions based upon established facts.

Proprietorship: a business owned by 1 individual.

Partnership: a business with 1 or more owner.

Corporation: a legal entity created under provincial or federal law, entity separate from owners & managers

Equipment + process selection: Selecting best alternative

Equipment Replacement: Consider replacement expenditure

New Product + Product Expansion: Decisions for increasing revenue

Cost Reduction: lower firms operating costs

Improvement of Quality Design: continuously improve quality of product

Engineers must estimate:

1. Required investment in a project
2. Product demand
3. Selling Price
4. Manufacturing cost
5. Product life

Principles  
of  
Engineering  
Economics

Principle 1 : nearby penny is worth a distant dollar

Principle 2 : all that counts are the differences among alt's

Principle 3 : marginal revenue must exceed marginal cost

Principle 4 : additional risk is not taken without the expected additional return.

- in this course we're only considering compound interest

Market Interest Rate : Interest rate quoted by financial institutions (the cost of money to the borrowers).

Earning Power : money earns more over time.

Purchasing Power : loss of value due to inflation.

Time value : A dollar today is worth more than a dollar in the future.

Principal : Initial money.

Interest Rate : cost, expressed as percent per unit time.

Interest period : length of time, often a year (how frequently interest is calculated).

Number of Interest Periods : length of time of transaction.

Plan for Receipts (or payments) : particular cash flow over specified time.

Future amount of money : cumulative effects of the interest rate over a number of interest periods.

Jan. 9/20

→ Exam on March 2nd (?)

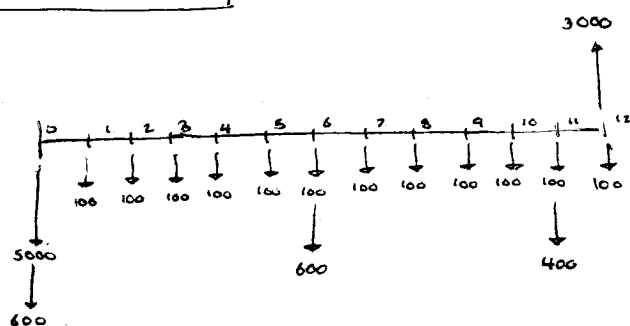
Cash Flow diagram: graphical summary of the timing and magnitude of a set of cash flows.

↳ Upward arrows represent positive flow

Downward arrows represent negative flow

end of period convention: placing all cash-flow transactions at the end of an interest period.

### Example 1



Simple interest: interest rate charged to initial sum

Compound interest: interest rate charged to initial sum + uncollected interest

(\*)  
General  
compound  
interest  
equation

$$F = P(1+i)^N$$

where  $N$  is number of periods  
 $i$  is interest rate  
 $P$  is principal amount

Economic equivalence: exists between individual cash flows and/or patterns of cash flows that have the same economic effect (in the end).

Principle 1: Equivalence calculations made to compare alternatives need the same timescale

Principle 2: Equivalence depends on interest rate

Principle 3: Equivalence calculations ...

Principle 4: ...

Five types of cash flows :

Single cash flow

Equal series

Linear gradient series

Geometric gradient series

Irregular series

Compound amount factor :  $F = P(1+i)^N = P(F/P, i, N)$

Example

$$P = 20000$$

$$i = 12\%$$

$$N = 15 \text{ years}$$

$$F = ?$$

$$F = P(F/P, i, N)$$

$$F = P(F/P, 12\%, 15)$$

By equation :

$$F = 20000 (1 + 0.12)^{15}$$

$$F = 109472$$

By tables :

$$F = P(F/P, 12\%, 15)$$

$$= 5.4736 \quad (\text{compound amount factor})$$

$$= 20000 (5.4736)$$

$$= 109472$$

Present worth factor :  $P = F / (1+i)^N = F(P/F, i, N)$

Example 2

$$F = 1000$$

$$i = 12\%$$

$$N = 5$$

$$P = ?$$

$$P = F(P/F, 12\%, 5)$$

$$= 0.5674$$

$$= 1000 (0.5674)$$

$$= 567.40$$

## Example 3

$$P = 10$$

$$F = 20$$

$$N = 5$$

$$i = ?$$

$$F = P(F/P, i, N)$$

$$20 = 10(1+i)^5$$

$$\rightarrow i = 14.87\%$$

## Example 4

$$P = 6000$$

$$F = 12000$$

$$i = 20\%$$

$$N = ?$$

$$F = P(F/P, i, N)$$

$$12000 = 6000(1+0.2)^N$$

$$\rightarrow N = 3.8 \text{ years}$$

## Example 5

$$P = 25000(P/F, 10\%, 1)$$

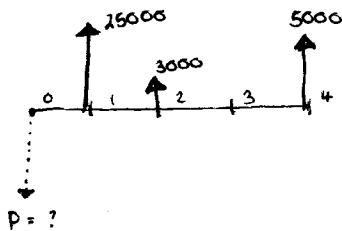
$$+ 3000(P/F, 10\%, 2)$$

$$+ 5000(P/F, 10\%, 4)$$

$$P = 25000(0.9091) + 3000(0.8264) + 5000(0.6830)$$

$$P = 28622$$

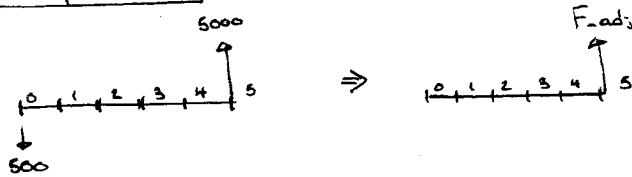
here's  
the  
question...



The Sinking Fund Factor (A)

$$A = F \left[ \frac{i}{(1+i)^N - 1} \right] = F(A/F, i, N)$$

### Example 6



Step 1:  $F_{adj} = 5000 - 500(F/P, 7\%, 5)$   
 $\approx 4299$

Step 2:  $A = F_{adj}(A/F, 7\%, 5)$   
 $= 4299 \left[ \frac{0.07}{(1+0.07)^5 - 1} \right]$   
 $= 4299[0.1739]$   
 $= 747.55$

### Example 7

$$A = 30000$$

$$i = 7\%$$

$$N = 10$$

$$F = ?$$

$$F = A(F/A, 7\%, 10)$$

$$= 30000 \left[ \frac{(1+0.07)^{10} - 1}{0.07} \right]$$

$$\approx 41449$$

Capital recovery factor  $A = P \left[ \frac{i(1+i)^N}{(1+i)^N - 1} \right] = P(A/P, i, N)$

{ P is always 1 period before first period. }

{ F is always last period. }