

Devin Gendron

Hw sec 2.1, #'s: 5, 10, (25-31), 52, 54

5. Indicate which of the following sentences are statements.

a. 1,024 is the smallest four-digit number that is a perfect square.

**Ans: A) is a statement because it is a true proposition.**

b. She is a mathematics major.

**Ans: B) is not a statement because the pronoun is not clear without preceding information.**

c.  $128=26$

**Ans: C) is a statement even though it is false.**

d.  $x=26$

**Ans: D) is a statement because the value for x will not change.**

10. Let p be the statement "DATAENDFLAG is off," q the statement "ERROR equals 0," and r the statement "SUM is less than 1,000." Express the following sentences in symbolic notation.

a. DATAENDFLAG is off, ERROR equals 0, and SUM is less than 1,000.

**Ans:  $p \wedge q \wedge r$**

b. DATAENDFLAG is off but ERROR is not equal to 0.

**Ans:  $p \wedge \sim q$**

c. DATAENDFLAG is off; however, ERROR is not 0 or SUM is greater than or equal to 1,000.

**Ans:  $p \wedge (\sim q \vee \sim r)$**

d. DATAENDFLAG is on and ERROR equals 0 but SUM is greater than or equal to 1,000.

**Ans:  $\sim p \wedge q \wedge \sim r$**

e. Either DATAENDFLAG is on or it is the case that both ERROR equals 0 and SUM is less than 1,000.

**Ans:  $\sim p \vee (q \wedge r)$**

Use De Morgan's laws to write negations for the statements in 25–31.

**Using:**  $\sim(p \wedge q) \equiv \sim p \vee \sim q$    &    $\sim(p \vee q) \equiv \sim p \wedge \sim q$

25. Hal is a math major and Hal's sister is a computer science major.

**Ans: Hal is not a math major or Hal's sister is not a computer science major.**

26. Sam is an orange belt and Kate is a red belt.

**Ans: Sam is not an orange belt or Kate is not a red belt.**

27. The connector is loose or the machine is unplugged.

**Ans: The connector is not loose and the machine is not unplugged.**

28. The units digit of 467 is 4 or it is 6.

**Ans: The units digit of 467 is not 4 and it is not 6.**

29. This computer program has a logical error in the first ten lines or it is being run with an incomplete data set.

**Ans: This computer program does not have a logical error in the first ten lines and it is not being run with an incomplete data set.**

30. The dollar is at an all-time high and the stock market is at a record low.

**Ans: The dollar is not at an all-time high or the stock market is not at a record low.**

31. The train is late or my watch is fast.

**Ans: The train is not late and my watch is not fast.**

Use Theorem 2.1.1 to verify the logical equivalences in 50–54. Supply a reason for each step.

52.  $\sim(p \vee \sim q) \vee (\sim p \wedge \sim q) \equiv \sim p$

$\sim(p \vee \sim q) \vee (\sim p \wedge \sim q) \equiv (\sim p \wedge \sim(\sim q)) \vee (\sim p \wedge \sim q)$    **by De Morgan's Laws**

$\equiv (\sim p \wedge q) \vee (\sim p \wedge \sim q)$    **by the double negative law**

$\equiv \sim p \wedge (q \vee \sim q)$    **by the distributive law**

$\equiv \sim p \wedge t$    **by the negation law**

$\equiv \sim p$    **by the identity law**

$$54. (p \wedge (\sim(\sim p \vee q))) \vee (p \wedge q) \equiv p$$

$$(p \wedge (\sim(\sim p \vee q))) \vee (p \wedge q) \equiv (p \wedge (\sim(\sim p) \wedge \sim q)) \vee (p \wedge q)$$

by De Morgan's Laws

$$\equiv (p \wedge (p \wedge \sim q)) \vee (p \wedge q)$$

by the double negative law

$$\equiv (p \wedge p) \wedge (p \wedge \sim q) \vee (p \wedge q)$$

by the distributive law

$$\equiv p \wedge (p \wedge \sim q) \vee (p \wedge q)$$

by the idempotent law

$$\equiv p \wedge (p \wedge (\sim q \vee q))$$

by the distributive law

$$\equiv p \wedge (p \wedge t)$$

by the negation law

$$\equiv p \wedge p$$

by the identity law

$$\equiv p$$

by the idempotent law