

Devin Gendron

Reading : pp. 290-291, 304-307

Set 5.6 : 2 , 4 & Set 5.7: 4, 6, 7

Find the first four terms (questions 2 & 4).

$$\begin{aligned} 2. \quad & b_k = b_{k-1} + 3k, \text{ for all integers } k \geq 2 \\ & b_1 = 1 \end{aligned}$$

$$b_1 = 1$$

$$b_2 = b_1 + 3(2) = 7$$

$$b_3 = b_2 + 3(3) = 16$$

$$b_4 = b_3 + 3(4) = 28$$

$$\begin{aligned} 4. \quad & d_k = k(d_{k-1})^2, \text{ for all integers } k \geq 1 \\ & d_0 = 3 \end{aligned}$$

$$d_0 = 3$$

$$d_1 = 1(d_0)^2 = 9$$

$$d_2 = 2(d_1)^2 = 162$$

$$d_3 = 3(d_2)^2 = 78,732$$

A sequence is defined recursively. Use iteration to guess an explicit formula for the sequence. Use the formulas from Section 5.2 to simplify your answers wherever possible.

$$\begin{aligned} 4. \quad & b_k = \frac{b_{k-1}}{1 + b_{k-1}}, \text{ for all integers } k \geq 1 \\ & b_0 = 1 \end{aligned}$$

$$b_0 = 1$$

$$b_1 = b_0 / (1 + b_0) = 1 / (1 + 1)$$

$$= 2^{-1}$$

$$b_2 = b_1 / (1 + b_1) = 1 / (1 + (1 / (1 + 1)))$$

$$= 2(2^{-1})$$

$$b_3 = b_2 / (1 + b_2) = 1 / (1 + (1 / (1 + (1 / (1 + 1)))))$$

$$= 2(2(2^{-1}))$$

$$b_4 = b_3 / (1 + b_3) = 1 / (1 + (1 / (1 + (1 / (1 + (1 / (1 + 1)))))))$$

$$= 2(2(2(2^{-1})))$$

Guess: n^{-1}

H 6. $d_k = 2d_{k-1} + 3$, for all integers $k \geq 2$
 $d_1 = 2$

$$d_1 = 2$$

$$d_2 = 2(d_1) + 3 = 2 \cdot 2 + 3 = 2^2 + 2 + 1$$

$$d_3 = 2(d_2) + 3 = 2 \cdot (2 \cdot 2 + 3) + 3 = 2^3 + 3(2+1)$$

$$d_4 = 2(d_3) + 3 = 2 \cdot (2 \cdot (2 \cdot 2 + 3) + 3) + 3 = 2^4 + 3(2^2 + 2 + 1)$$

$$d_k = 2^n + 3(2^{n-2} + 2^{n-3} + \dots + 2^0)$$

$$2^n + 3((2^{n-1} - 1)/(2 - 1))$$

$$= 2^n + 3(2^{n-1} - 1)$$

$$\text{Guess: } 2^n + 3(2^{n-1} - 1)$$

7. $e_k = 4e_{k-1} + 5$, for all integers $k \geq 1$
 $e_0 = 2$

$$e_0 = 2$$

$$e_1 = 4(e_0) + 5$$

$$e_2 = 4(e_1) + 5 = 4^2(e_0) + 4(5) + 5$$

$$e_3 = 4(e_2) + 5 = 4^3(e_0) + 4^2(5) + 4^1(5) = 4^3(e_0) + 5(1 + 4^1 + 4^2 + 4^3)$$

$$\text{Guess: } e_k = 4^k(e_0) + (5(4^k - 1))/3$$