

CS261 Data Structures

Hash Tables

Buckets/Chaining

Hash Tables: Resolving Collisions

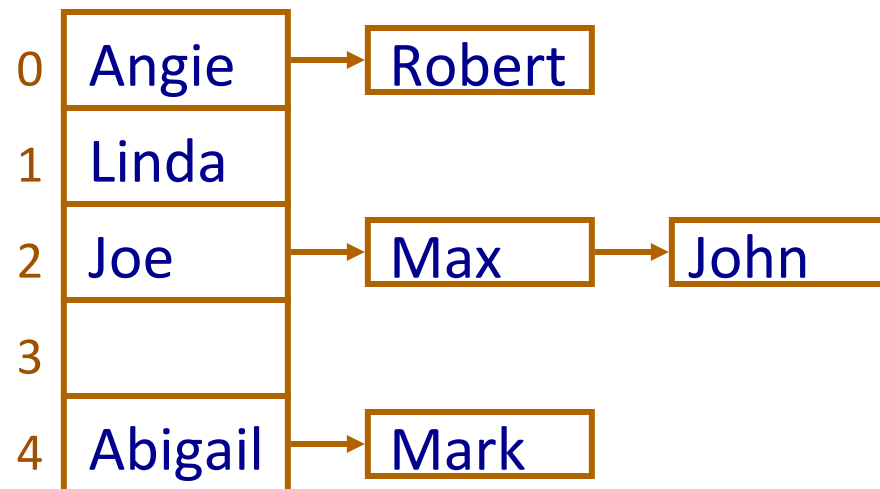
There are two general approaches to resolving collisions:

1. Open address hashing: if a spot is full, probe for next empty spot
2. Chaining (or buckets): keep a collection at each table entry

Resolving Collisions: Chaining / Buckets

Maintain a collection (i.e., a Bag ADT) at each table entry:

Each collection is called a 'bucket' or a 'chain'



Hash Table Implementation: Initialization

```
struct HashTable {  
    struct Linked List **table; /* Hash table → Array of Lists. */  
    int cnt;  
    int size;  
}
```

```
void initHashTable(struct HashTable *ht, int size) {  
    int i;  
  
    ht->size = size;  
    ht->cnt = 0;  
    ht->table = malloc(size * sizeof(struct LinkedList *));  
    assert(ht->table != 0);  
    for(i = 0; i < size; i++) ht->table[i] = newList();  
}
```

Hash Table Implementation: Add

```
void addHashTable(struct HashTable *ht, TYPE val) {  
    /* Compute hash table bucket index. */  
    int idx = hash(val) % ht->size;  
    if (idx < 0) idx += ht->size;  
  
    /* Add to bucket. */  
    addList(ht->table[idx], val);  
    ht->cnt++;  
  
    /* Next step: Reorganize if load factor to large. */  
}
```

Hash Table: Contains & Remove

- Contains: find correct bucket, then checks to see if element is there
- Remove: if element is in the table, remove it and decrement the count

Hash Table Size

- Load factor:

The diagram shows the formula $\lambda = n / m$ in blue. Three orange dotted arrows point from the formula to its components: one from λ to the text 'Load factor', one from n to the text '# of elements', and one from m to the text 'Size of table'.

$$\lambda = n / m$$

- Load factor represents average number of elements in each bucket
- **For chaining, load factor can be greater than 1**
- As in open address hashing: if load factor becomes larger than some fixed limit (say, 8) → double table size

Hash Tables: Algorithmic Complexity

- Assuming:
 - Time to compute hash function is constant
 - Chaining uses a linked list
 - Worst case analysis \rightarrow All values hash to same position
 - Best case analysis \rightarrow Hash function uniformly distributes the values
- Contains operation:
 - Worst case for open addressing $\rightarrow O(n)$
 - Worst case for chaining $\rightarrow O(n)$
 - Best case for open addressing $\rightarrow O(1)$
 - Best case for chaining $\rightarrow O(1)$

Hash Tables With Chaining: Average Case

- Assume hash function distributes elements uniformly (a BIG if)
- Average case for all operations: $O(\lambda)$
- Want to keep the load factor relatively small
- Resize table (doubling its size) if load factor is larger than some fixed limit (e.g., 8)
 - Only improves things *IF* hash function distributes values uniformly
 - How do we handle a resize?

Design Decisions

- Implement the Map interface to store values with keys (ie. implement a dictionary)
- Rather than store linked lists, build the linked lists directly
 - `Link **hashTable;`

- Worksheet 38: Hash Tables using Buckets